

THREE-DIMENSIONAL FINITE ELEMENT
MODELING OF POLLUTANT
TRANSPORT IN AQUIFERS

By

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CHAPTER I

INTRODUCTION

The use of aquifers as a source of freshwater to supply public need has increased. Requirements of the Environmental Impact Analysis and Statement have focused public attention on the quality of water for domestic use. Factors which affect the groundwater quality include: (a) leakage from ponds and lagoons, (b) sanitary landfills, (c) deep injection wells, (d) road salt, pesticides and fertilizers, (e) sanitary landfills, (f) sea water intrusion, (g) mine drainage and oil-field brines, (h) cesspools and septic tanks, (i) leakage from oil pipeline oil storage tanks and sewage pipelines, (j) animal feed lots, and (k) industrial waste water. Numerical modeling seems to be the best tool for understanding, preventing, and predicting the groundwater problems.

Research Problem

In this study, Galerkin's finite element method is used to analyze the transport of a pollutant in a three-dimensional aquifer system. The collection of water quality data is expensive and gathering information on migration of contaminant plumes under field conditions is a lengthy process; therefore, a properly calibrated and validated numerical

model used with field data is an excellent tool with which to predict the future migration of a plume in saturated aquifers.

Objectives

(1) To develop Galerkin's finite element method for solving the three-dimensional solute transport in a saturated aquifer;

(2) To validate the model using the existing analytical solutions of the dispersion equation in two and three dimensions;

(3) To validate the model with available numerical models in two dimensions.

Procedures

Galerkin's finite element method is modeled with the solute transport equation. The model requires that the continuous variables be replaced with discrete variables as elements. Each discrete subregion is modeled by the same transport equation. The concentration will be assembled at all nodes and solved on an IBM 3081K system. After the model is developed, it is validated against existing analytical solutions.

CHAPTER II

LITERATURE REVIEW

Ground water represents more than 95 percent of all available freshwater in the world. Total groundwater withdrawal of 89 bgpd provides 20 percent of the water used in the United States. Approximately 34 percent of the public water supply and 79 percent of the water for rural domestic use are derived from potable groundwater sources. Groundwater is an important natural resource that can become increasingly valuable throughout the country. The increased use of groundwater as a source of potable water will depend on controlling its contamination. Mathematical modeling can be used as an effective tool in the development of methods for abating groundwater pollution.

The development of advanced computer techniques have enabled engineers to use a discrete process for approximating complex problems. The partial differential equations are divided into a set of discrete equations, which in turn are reduced to a system of algebraic equations. Two major techniques have been used in the groundwater field. One is the finite difference method and the other one is the finite element method. In recent years, several textbooks have been published that are excellent for studying these two

methods. They are: Remson, Hornberger, and Molz (1971), Segerlind (1976), Pinder and Gray (1977), Rao (1982), and Zienkiewicz and Morgan (1983). In this chapter, a detailed discussion of these two methods will be given.

Finite Difference Method (FDM)

The finite difference method (FDM) is a discrete technique in which the domain of interest is represented by a set of points or nodes, and information between these points is commonly obtained using Taylor's series expansions. Richardson (1910) introduced the finite difference method to calculate the approximate solution of partial differential equations.

Solving the solute transport problem, one calculates the groundwater flow velocities. Prickett (1975) summarized the numerical and analog models in his reports. Douglas, Peaceman, and Rachford (1959) used an Alternating Direction Implicit (ADI) technique to solve a two dimensional, two phase, incompressible flow model. Peaceman and Rachford (1962) used a similar method to solve the problem of miscible displacement in porous media. Bresler (1973) and Marino (1974) used the Crank-Nicholson technique to obtain solutions solving the mass transport problems. The finite difference method of solving the mass transport equations may introduce numerical dispersion. Numerical smearing and artificial dispersion of a sharp concentration front were shown to be at least of the same order of magnitude as the

actual dispersion. This artificial dispersion limits the applicability of the solutions. Lantz (1971) and Chaudhari (1971) provide guidelines for a high order finite difference scheme that eliminates most of the numerical dispersion.

Garder, Peaceman, and Pozzi (1964) used the method of characteristics (MOC) to solve a one dimensional dispersion equation. Reddell and Sunada (1970) used the method to solve the problem of saltwater intrusion. Pinder and Cooper (1970) used the ADI procedure to solve the flow equation and the MOC to solve the solute transport equation. Konikow and Bredehoeft (1978) developed a MOC model to study changes in dissolved solid concentration in a stream-aquifer system. Numerical solutions of the dispersion equation for different adsorption equilibrium were provided by Lai and Jurinak (1972) using the explicit finite-difference scheme. Douglas and Jones (1963) developed a technique called the Predictor-Corrector Finite Difference Method. The method uses two finite approximate differences, each advancing the solution by one-half increment in the time domain. The predictor equation is a modification of the implicit finite-difference approximation, and the corrector equation is a modification of the Crank-Nicholson approximation (Remson et al. 1971). Tagamets and Sternberg (1974) used the method for solving the one dimensional convection-dispersion equation for adsorption in porous media. Trescott, Pinder, and Larson (1975) solved the two-dimensional flow problem by the Line

Successive Over Relaxation (LSOR) method and compared it with the ADI method.

The explicit approximation is sometimes referred to as a "Forward Difference," and the implicit approximation is referred to as a "Backward Difference." Pinder and Gray (1976) described the explicit method as requiring a minimum of computational effort, but usually conditionally stable. The implicit method is usually unconditionally stable yet it requires an additional computational effort when a variable time step is used. The Crank-Nicholson method is second order accurate and usually stable.

Finite Element Method (FEM)

The finite element method is numerical method that can be used to solve complex engineering problems.

Clough (1960) appears to be the first to use the term "finite element." Today, the finite element method is a powerful tool for the approximate solution of differential equations governing diverse physical phenomena. The method can be seen as a discretization procedure of continuum problems presented by mathematically defined statements. High speed electronic digital computers have enabled engineers to employ various numerical discretization techniques for approximating solutions of complex problems. The finite element method was originally developed as a tool for structural analysis, but the theory and formulation have been progressively refined and generalized so that the method can

be applied successfully to other fields such as heat flow, seepage, etc.

The two major approaches are (a) the Variational Approach and (b) the Weighted Residual Approach.

Variational Approach (Raleigh-Ritz Method)

The variational approach applies the calculus of variations. Variational calculus states that the minimization of the functional requires that the differential equation, with the boundary conditions, be satisfied. The variational approach can be used with most physical and engineering problems.

Weighted Residual Approach

In the weighted residual approach, the finite element matrices are derived directly from the governing differential equation. These equations satisfy both the homogeneous and certain specific boundary conditions. In several investigations, the method has been used to solve the groundwater flow and quality problems.

In the method of weighted residuals, the function C is replaced by trial function \bar{C} . \bar{C} is a set of approximation close to C ,

$$C \cong \bar{C} \cong \sum_{i=0}^n C_i W_i \quad i = 0, 1, 2, \dots, n \quad (2.1)$$

where C is a linear independent function, W_i is the weighting function defined over both the time and space

domain. C_i indicates undetermined coefficients. The approximate function \bar{C} is substituted into the governing equation, resulting in an error called the residual.

$$L(C) = L(\bar{C}) = R \quad (2.2)$$

This method chooses the undetermined coefficients such that the error can be minimized to zero, thus making the trial solution equal to the exact solution.

The function $L(R)$ is chosen so that $L(R) = 0$ when $R = 0$, W_j is the weighting function, $j = 1, 2, \dots, n$ and the integration is over the domain of the problem. The equation can be shown as:

$$\int_t \int_v L(R) W_j dV dt = 0 \quad (2.3)$$

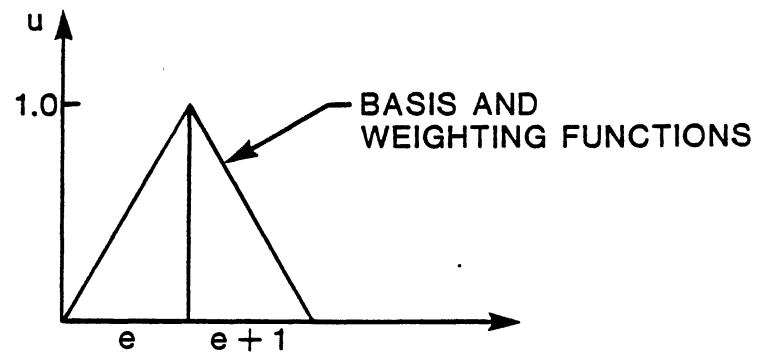
Three different weighted residual methods are described as follows (Figure 1).

(a) Galerkin's Method:

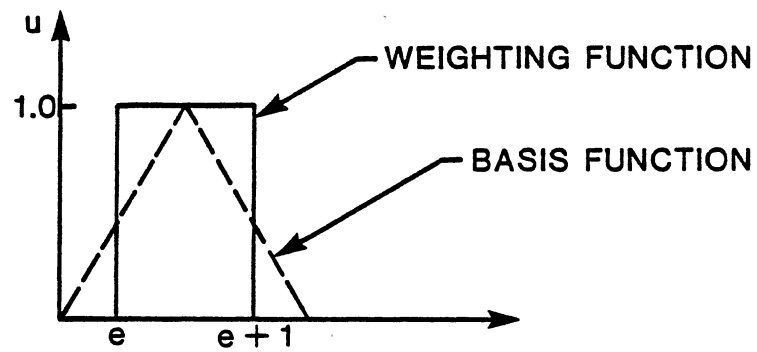
The Galerkin's method chooses the basis function to be the same as the weighting function yielding

$$\int_v R W_j dV = 0 \quad j = 1, 2, \dots, n \quad (2.4)$$

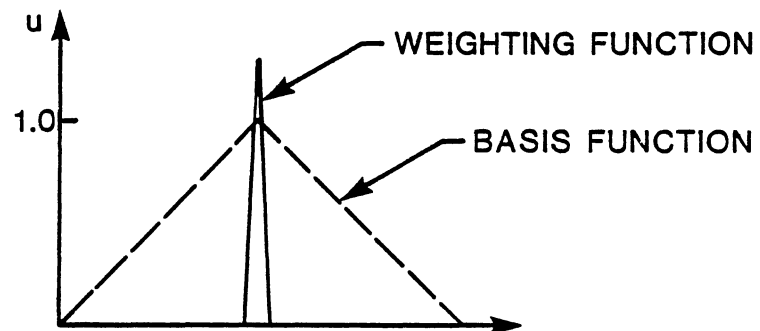
The requirement of this method is that the continuous function must be zero if it is orthogonal to every member of the complete set.



(a) GALERKIN METHOD



(b) SUBDOMAIN METHOD



(c) COLLOCATION METHOD

Figure 1. The Three Weighted Residual Methods

(b) Subdomain Method:

In the subdomain method, the domain V is first divided into finite subdomains. Unity is chosen as the weighting function in the subregion V_i and zero is used elsewhere so that

$$\int_V R W_j dV = 0 \quad (2.5)$$

where $W_j = 1$ if (x,y,z) in domain V_i otherwise $W_j = 0$.

(c) Collocation Method:

In the collocation method, Dirac delta is chosen as the weighting function W_j .

$$W_j = \delta(x-x_i)\delta(y-y_i)\delta(z-z_i) \quad (2.6)$$

The method approaches the exact solution by setting the residue equal to zero at n points in domain V ,

$$\int_V R\delta_i(x,y,z) dV = 0 \quad i = 1,2,\dots,n \quad (2.7)$$

FEM-Solute Transport

The application of the finite element models to groundwater began in the 1960's (Zienkiewicz, Mayer, and Cheung, 1966). Witherspoon and Javandel (1968) applied the finite element method to transient flow in porous media by employing the variational principle. Price, Carendish, and Varga (1968) introduced a numerical method of high order accuracy for the one-dimensional diffusion-convection equation based

on Galerkin's approach. Guymon (1970) and Guymon, Scott, and Harrmann (1970) presented a variational approach to the dispersion equation in which the convective terms do not appear explicitly. Nalluswami, Logenbaugh, and Sunda (1972) expanded Guymon's work by improving the numerical techniques, taking into account the tensor properties of the dispersive coefficient. Tyagi (1971, 1973, 1975a, 1975b, 1975c) used the finite element method to predict the transition zone between fresh and salt water in coastal aquifers, the flow in saturated and unsaturated zones of aquifers, and the water quality in unsaturated flows. Bruch and Zyvoloski (1973) used a finite element weight residual solution in a one-dimensional diffusion-convection field problem. The results are compared with a finite-difference solution as well as the analytical solution. Pinder (1973) used Galerkin's finite element approach to simulate the areal movement of a saturated aquifer. Cheung and Harrison (1973) applied the finite element methods to two-dimensional field problems in isotropic media. Smith, Farraday, and O'Connor (1973) used Raleigh-Ritz and Galerkin's finite element methods to solve the two-dimensional diffusion-convection problem, taking into consideration the miscible displacement. Sykes (1975) developed a two-dimensional model for variably saturated porous media that was used to predict the transient movement of the trace radionuclide and to analyze the transport of ammonium undergoing nitrification and denitrification. He applied Galerkin's technique to the mass

conservation equation. Gupta and Tanji (1975) developed a three-dimensional flow and mass transport model. The model was applied to a complex groundwater region in Sutter Basin, California, to simulate the rising connate water through a vertical fault. In the various situations where high-speed computers can simulate complex water systems at a minimum cost, models have been developed. Wang and Cheng (1975) studied the two-dimensional convection-dispersion equation to solve the pollutant dispersion in a semi-infinite aquifer.

A two-dimensional transient model for the flow of a dissolved constituent throughout porous media was developed by Duguid and Reeves (1976). The mechanism of advective transport, hydrodynamic dispersion, chemical adsorption, and radioactive decay are included in the mathematical formulation. The model also simulates a pond seepage problem, Grove (1977) used Galerkin's finite element method to solve mass-transport equations. The technique was applied to a field problem involving an aquifer polluted with chloride, tritium, and strontium-90. The results, compared with the finite difference method and the analytical solution, showed a high degree of accuracy. Van Genuchten (1978) developed a model for predicting potential groundwater pollution by the disposal of liquid or solid waste. A hypothetical landfill located adjacent to a river provided considerable insight into the subsurface movement of landfill leachates. Gureghian, Ward, and Cleary (1980, 1981) developed a two-

dimensional model for the migration of the groundwater pollutant. A field application of the model was made to the leachate migration from the Babylon sanitary landfill in Long Island, New York. The results were compared with those of a two-dimensional analytical solution. The results were in agreement during the calibration and verification period.

The numerical model used to simulate the groundwater contamination from Price's landfill in New Jersey was presented by Gray and Hoffman (1983), and was a two-dimensional transient model using linear triangular elements. The model assumed that the species being considered was convective and nonabsorbing.

Gupta, Kincaid, Meyer, Newbill, and Cole (1982) developed a multi-dimensional finite element code for the analysis of coupled fluid, energy and solute transport. A major thrust of this program has been the study of natural aquifers as host for thermal energy storage and retrieval.

Voss (1984) developed a computer program that simulates fluid movement and the transport of either energy or dissolute substances in a subsurface environment.

Cole, Gupta, and Pinder (1984) developed a three-dimensional groundwater model for a multiaquifer system in which isoparametric element is used. The model was applied to a groundwater reservoir beneath Long Island, New York. Babu and Pinder (1984) developed a model based on an operator splitting algorithm which treats the horizontal plane using

finite elements in the first step, and the vertical dimension using finite difference in the second step. The model provides considerable saving in both computer memory requirements and computational efforts.

Comparison of FEM and FDM

(a) In finite difference approximations of a differential equation, the discrete representation of the equation is applied at a point. In the finite element method the discrete equations are applicable over a region.

(b) The numerical solution of the dispersion equation may cause numerical dispersion. The algebraic equations generated by the finite difference method are particularly susceptible to numerical errors, while finite element method solutions, in general, are more reliable (Anderson 1979).

Benefits of Using the Finite Element Method

(a) With the finite element method, the domain of interest can be divided into irregular subdivisions, as described by the physical geometry of the problem.

(b) The properties of each element can be evaluated individually. Each element can be linked to different material properties.

(c) The boundary conditions can be adjusted easily.

(d) The method is flexible and can be used to handle thermal energy, chemical loads, time dependence, and nonlinearities.

CHAPTER III

MATHEMATICAL FORMULATION

This chapter presents a basic equation of groundwater flow and solute transport in porous media. The mathematical derivation of both equations has been documented by Jacob (1940), Cooper (1966), Remson et al. (1971), Bear (1972, 1977), Ogata (1974), Grove (1978), and Mercer and Faust (1980). In this study, our interest is in the flow and solute transport in saturated zones of aquifers.

Flow Equation

An equation that describes a three-dimensional unsteady groundwater flow can be written as:

$$\frac{\partial}{\partial x} \left(k_{xx} \frac{\partial h}{\partial x} \right) + \frac{\partial}{\partial y} \left(k_{yy} \frac{\partial h}{\partial y} \right) + \frac{\partial}{\partial z} \left(k_{zz} \frac{\partial h}{\partial z} \right) + Q = S_s \frac{\partial h}{\partial t} \quad (3.1)$$

where h = hydraulic head, (L),

k_{ii} = hydraulic conductivity, $i = x, y, z$, (L/T),

Q = source of sink term, (L/T), such as irrigation, wells, and evapotranspiration,

S_s = specific storage, (L^{-1}),

t = time, (T).

For the homogeneous fluid with a saturated aquifer with thickness b (L), the transmissivity of the aquifer may be defined as $T_{ii} = k_{ii}b$, where T_{ii} is the transmissivity (L^2T^{-1}). The storage coefficient of the aquifer can be defined as $S = S_s b$, where S is the storage coefficient (dimensionless).

Assuming that the Cartesian coordinates axes x and y are aligned with the principal components of the transmissivity tensor, the three-dimensional saturated flow can be represented as:

$$\frac{\partial}{\partial x} (T_{xx} \frac{\partial h}{\partial x}) + \frac{\partial}{\partial y} (T_{yy} \frac{\partial h}{\partial y}) + \frac{\partial}{\partial z} (T_{zz} \frac{\partial h}{\partial z}) + Q_b = S_s \frac{\partial h}{\partial t} \quad (3.2)$$

where Q_b is the volume flux per unit area (LT^{-1}).

For a two-dimensional groundwater flow, the equation may be written as:

$$\frac{\partial}{\partial x} (T_{xx} \frac{\partial h}{\partial x}) + \frac{\partial}{\partial y} (T_{yy} \frac{\partial h}{\partial y}) = S_s \frac{\partial h}{\partial t} - Q_b \quad (3.3)$$

The Groundwater Flow Equation

The problem of nonsteady flow in an artesian aquifer was first analyzed by Theis (1935). Jacob (1940) applied the Theis equation with hydrologic concepts and derived a differential equation for nonsteady flow in a uniformly thick, horizontal, compressible sand. The equation stated in two dimensions is:

$$\frac{\partial^2 h}{\partial x^2} + \frac{\partial^2 h}{\partial y^2} = - \frac{S}{T} \frac{\partial h}{\partial t} \quad (3.4)$$

$$S = \rho g b (\alpha_p + \Theta \beta_p),$$

$$T = \text{transmissivity of the medium, } L^2 T^{-1},$$

$$b = \text{thickness of aquifer, } L,$$

$$S = \text{storage coefficient (dimensionless),}$$

$$\alpha_p = \text{compressibility of medium } LT,$$

$$\beta_p = \text{compressibility of liquid, } LT^2 M^{-1},$$

$$\Theta = \text{porosity of the medium.}$$

The equation can be extended to a three-dimensional saturated flow and expressed as:

$$\frac{\partial^2 h}{\partial x^2} + \frac{\partial^2 h}{\partial y^2} + \frac{\partial^2 h}{\partial z^2} = \frac{S_s}{k} \frac{\partial h}{\partial t} \quad (3.5)$$

The basic governing equation for saturated flow is

$$\frac{\partial}{\partial x} \left(k_x \frac{\partial h}{\partial x} \right) + \frac{\partial}{\partial y} \left(k_y \frac{\partial h}{\partial y} \right) + \frac{\partial}{\partial z} \left(k_z \frac{\partial h}{\partial z} \right) - Q = S \frac{\partial h}{\partial t} \quad (3.6)$$

where $Q = \text{strength of sink or source, } LT^{-1};$

$$Q = Q_w(x_i, y_i, z_i, t) \delta(x-x_i) \delta(y-y_i) \delta(z-z_i)$$

where $Q_w = \text{well discharge or recharge, } L^3 T^{-1};$

$\delta = \text{Dirac delta function.}$

There are several books that give a detailed derivation of the groundwater flow equation in saturated porous media, three of which are Bear (1972, 1979) and Remson et al. (1971).

To apply the principle of conservation of mass to a control volume (representative element volume), we first consider the y-z plane. The rate of solute into the plane at x is $CV_{x,x}^* dydz$ and the rate of solute flow out y-z face at $x+dx$ is $CV_{x+dx}^* dydz$. Similar expression is used for the other two planes (Figure 2).

The mass balance is

$$\text{INPUT} - \text{OUTPUT} = \text{ACCUMULATION} \quad (3.7)$$

$$\begin{aligned} \text{so, } & (CV_{x,x}^* - CV_{x,x+dx}^*) dydz \\ & (CV_{y,y}^* - CV_{y,y+dy}^*) dydz \\ & (CV_{z,z}^* - CV_{z,z+dz}^*) dydz \end{aligned} \quad (3.8)$$

$$dx dy dz \frac{\partial C}{\partial t} = -(\partial CV_{dx}^* dy dz) + (-\partial CV_{dy}^* dx dz) + (-\partial CV_{dz}^* dx dy) \quad (3.9)$$

Divide by $dx dy dz$:

$$\frac{\partial C}{\partial t} = \frac{\partial CV^*}{\partial x} + \frac{\partial CV^*}{\partial y} + \frac{\partial CV^*}{\partial z} \quad (3.10)$$

The rate of solute accumulation within the volume element is $\partial c / \partial t dx dy dz$. Bear (1972, 1977) gave the equation for calculating the velocities:

$$CV_i^* = CV_i + CV^0 \quad (3.11)$$

where $V_i = V^* - V_i$,

V_i^* = mass of average velocity

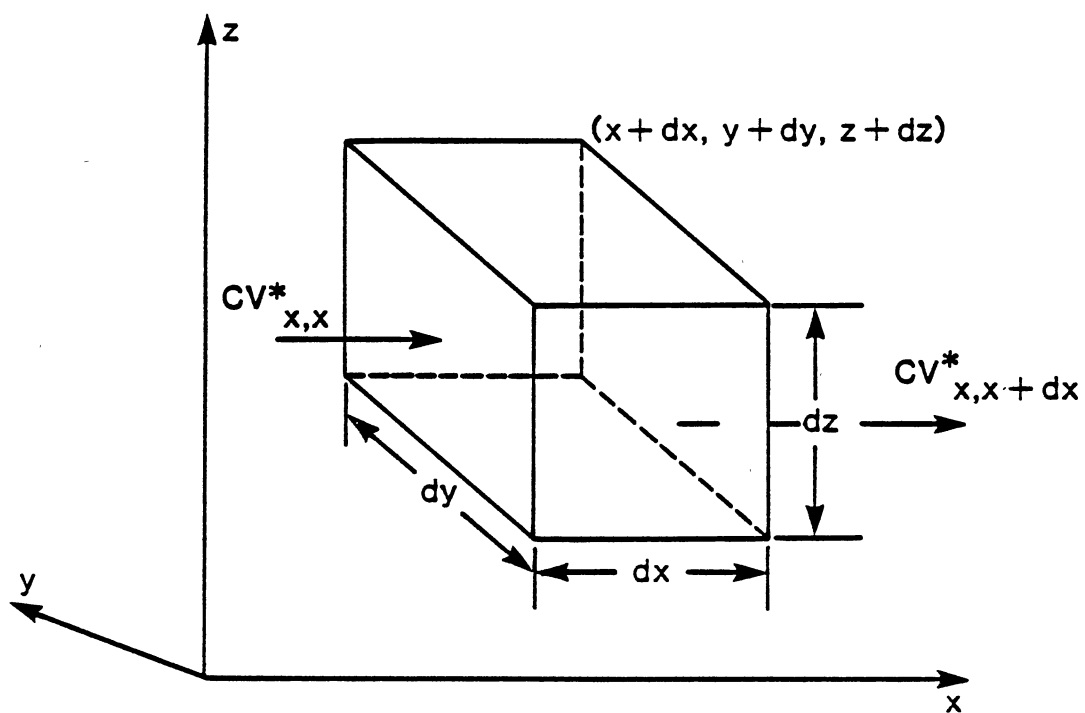


Figure 2. Control Volume (the Solute Flow Through)

- V_i = seepage velocity
 v^o = the derivation of the particles instantaneous velocity from the average one
 CV_i^* = transport by convection
 CV^o = the diffusive flux
 D_{ij} = dispersion coefficient

Where we rearrange equation (3.10), the general form of solute transport equation is obtained:

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial x_i} \left(D_{ij} \frac{\partial C}{\partial x_j} - V_i C \right) \quad (3.12)$$

Dispersivity

Scheidegger (1961) and Bear (1972, 1979) stated that the influence of the void space is represented by a_{ijklm} , the dispersivity of the porous medium, which in saturated flow is a property of the geometry of the solid matrix. It is a fourth rank tensor which has certain properties of symmetry. For an isotropic porous medium with two constants:

$$\begin{aligned} a_L &= \text{longitudinal dispersivity} \\ a_T &= \text{transverse dispersivity} \end{aligned} \quad (3.13)$$

For a three dimensional case: $i, j = 1, 2, 3$

$$\begin{aligned} a_{iiii} &= a_L \\ a_{ijjj} &= a_T \\ a_{iiij} &= a_{iiji} = a_{ijii} = a_{ijjj} = 0 \\ a_{ijij} &= a_{ijji} = 0.5(a_L - a_T) \end{aligned} \quad (3.14)$$

Several approaches are used to receive the dispersivity. One method is a trial and error adjustment of the value of the chosen longitudinal and transverse dispersivity in a solute transport model of a field situation until the simulated movement pattern closely resembles the pattern observed in the field. Grove and Boetem (1971) described a two-well injection method in which the mathematical equations used to calculate dispersivity from the test are based on the assumption of homogeneity of the geologic materials in the test area. The regional flow can be neglected during the test.

Matthess (1982) stated that the coefficient of hydrodynamic dispersion increases with increasing porosity, growing grain sizes, and growing inconformity. Finally, the hydrodynamic coefficient D depends on groundwater flow velocity.

$$D = \alpha V_w^{(a)+b} \quad (3.15)$$

where D = coefficient of hydrodynamic dispersion

V_w = average groundwater velocity

α = dispersivity coefficient

Matthess and Pekdeger (1981) found that in a laboratory study the value α was on the order of 0.1 cm to 1 m; in field experiments the values were between 0.1 to 100 m; and the values for fractured and karstic rocks were between 10 to 10000 m. The exponent (a) in the equation is close to one.

Dispersion Coefficient

The dispersion phenomenon includes two processes: mechanical dispersion and molecular diffusion. Mechanical dispersion, or spreading the solute with respect to the average flow produced by velocity variation in the pore space, is sometimes called convective diffusion. Molecular diffusion depends on time. Its effects on the overall dispersion are more significant at low flow velocities. In pollutant movement in groundwater, the contribution of molecular diffusion to the hydrodynamic dispersion term is usually negligible in comparison to mechanical dispersion. Scheidegger (1961) and Bear (1972, 1979) pointed out that the dispersion coefficient as a tensor should have 81 components for the three-dimensional case, but they were able, through the use of symmetry, to reduce this number to 32 individual components. For an isotropic medium, they reduced the number of components of the tensor to nine. For the three-dimensional case,

$$D_{ij} = \begin{vmatrix} D_{11} & D_{12} & D_{13} \\ D_{21} & D_{22} & D_{23} \\ D_{31} & D_{32} & D_{33} \end{vmatrix} \quad (3.16)$$

Bruch and Street (1967) used the following equations to measure the longitudinal and transverse dispersion coefficient.

$$\begin{aligned} D_L &= \mu(1.8)(Vd_{50}/\mu)^{1.2} \\ \text{and} \quad D_T &= \mu(0.11)(Vd_{50}/\mu)^{0.7} \end{aligned} \quad (3.17)$$

where μ = kinematic viscosity

d_{50} = mean grain size

V = velocity

$Re < 10^{-3}$

The most popular method of calculating the dispersion coefficient has been described by Scheidegger (1961). Several other investigations give more information about the equation (Bear, 1972; Grove and Boetem, 1971; and Konikow and Bredehoeft, 1978) They show the relationship between the dispersion coefficient and flow velocity as.

$$D_{ij} = a_{ijmn} \frac{V_m V_n}{|V|} \quad (3.18)$$

where V_m, V_n = a component of the flow velocity of fluid in m and n directions (LT^{-1})

V = the magnitude of the velocity vector (LT^{-1})

For the three-dimensional dispersion coefficient that equals

$$D_{11} = a_{1111} \frac{V_1 V_1}{|V|} + a_{1122} \frac{V_2 V_2}{|V|} + a_{1133} \frac{V_3 V_3}{|V|}$$

$$\begin{aligned}
D_{22} &= a_{2211} \frac{V_1 V_1}{|V|} + a_{2222} \frac{V_2 V_2}{|V|} + a_{2233} \frac{V_3 V_3}{|V|} \\
D_{33} &= a_{3311} \frac{V_1 V_1}{|V|} + a_{3322} \frac{V_2 V_2}{|V|} + a_{3333} \frac{V_3 V_3}{|V|} \\
D_{12} &= D_{21} = a_{1212} \frac{V_1 V_2}{|V|} + a_{1221} \frac{V_2 V_1}{|V|} \\
D_{13} &= D_{31} = a_{1313} \frac{V_1 V_3}{|V|} + a_{1331} \frac{V_3 V_1}{|V|} \\
D_{23} &= D_{32} = a_{2323} \frac{V_2 V_3}{|V|} + a_{2332} \frac{V_3 V_2}{|V|}
\end{aligned} \tag{3.19}$$

If we substitute the equation by using isotropic media, it becomes

$$\begin{aligned}
D_{11} &= a_L \frac{V_1 V_1}{|V|} + a_T \frac{V_2 V_2}{|V|} + a_T \frac{V_3 V_3}{|V|} \\
D_{22} &= a_T \frac{V_1 V_1}{|V|} + a_L \frac{V_2 V_2}{|V|} + a_T \frac{V_3 V_3}{|V|} \\
D_{33} &= a_T \frac{V_1 V_1}{|V|} + a_T \frac{V_2 V_2}{|V|} + a_L \frac{V_3 V_3}{|V|}
\end{aligned}$$

and

$$D_{12} = D_{21} = (a_L - a_T) \frac{V_1 V_2}{|V|}$$

$$\begin{aligned}
 D_{12} = D_{31} &= (a_L - a_T) \frac{V_1 V_3}{|V|} \\
 D_{23} = D_{32} &= (a_L - a_T) \frac{V_2 V_3}{|V|}
 \end{aligned} \tag{3.20}$$

Scheidegger (1961) and Bachmat and Bear (1964) also show that for a Cartesian coordinate system x_i in which one of the axes, say x_1 , coincides with the direction of the average velocity, then $V_1 = |V|$ and $V_2 = 0$. Substituting these relations into equations, we obtain

$$\begin{aligned}
 D_{11} &= a_L V = D_L \\
 D_{22} = D_{33} &= a_T V = D_T \\
 D_{12} = D_{13} = D_{23} &= D_{31} = D_{32} = 0
 \end{aligned} \tag{3.21}$$

Solving quotients equations for a_L and a_T results in

$$a_L = \frac{D_L}{|V|}$$

and

$$a_T = \frac{D_T}{|V|}$$

Introducing quotients produces:

$$\begin{aligned}
 D_{11} &= D_L \frac{(V_1)^2}{|V|^2} + D_T \frac{(V_2)^2}{|V|^2} + D_T \frac{(V_3)^2}{|V|^2} \\
 D_{22} &= D_T \frac{(V_1)^2}{|V|^2} + D_L \frac{(V_2)^2}{|V|^2} + D_T \frac{(V_3)^2}{|V|^2}
 \end{aligned}$$

$$\begin{aligned}
 D_{33} &= D_T \frac{(V_1)^2}{|V|^2} + D_T \frac{(V_2)^2}{|V|^2} + D_L \frac{(V_3)^2}{|V|^2} \\
 D_{12} = D_{21} &= (D_L - D_T) \frac{V_1 V_2}{|V|^2} \\
 D_{13} = D_{31} &= (D_L - D_T) \frac{V_1 V_3}{|V|^2} \\
 D_{23} = D_{32} &= (D_L - D_T) \frac{V_2 V_3}{|V|^2}
 \end{aligned} \tag{3.23}$$

where $|V|$ is equal to $(V_1^2 + V_2^2 + V_3^2)^{0.5}$.

If $x=1$, $y=2$, and $z=3$, then the dispersion coefficients for isotropic porous media are:

$$D_{ij} = \begin{vmatrix} D_{xx} & D_{xy} & D_{xz} \\ D_{yx} & D_{yy} & D_{yz} \\ D_{zx} & D_{zy} & D_{zz} \end{vmatrix} \tag{3.24}$$

Kinetic Coefficients

The changes due to the reaction of the solute with its surroundings include adsorption, desorption, biodegradation, volatilization, precipitation, and chemical transformation. K is the rate of production of the solute in different reactions.

$$K = K_a + K_b + K_t + K_v \tag{3.25}$$

K_a is the reaction constant for the solute's change in adsorption concentration. K_b is the biodegradation constant; organic compounds are decomposed by microorganisms that obtain carbon and hydrogen from these processes for cell synthesis. The energy necessary for this metabolism is supplied by the digestion of substances rich in energy into simpler compounds and finally into CO_2 and H_2O . Zoetman, Harman, Linders, Morra, and Sloof (1981) calculated the constant for toluene to be 0.3, ethylene 0.6, benzene 1, and dichloromethane 10. K_v is the volatilization constant. Highly volatile materials such as gasoline and chlorinated hydrocarbons may escape by diffusion from the soil into the atmosphere. Volatilization provides a measure of the tendency of a substance to vaporize. Tinsley (1979) and Khan (1980) give more details of factors that influence volatilization of organic chemicals in soil. K_t is the chemical transformation constant. Chemical reaction leads to an "elimination" or "disappearance" of a given chemical in the groundwater environment. K_p is the precipitation constant. This is another chemical interaction. Several other reactions are involved in the general K term such as desorption, etc.

$$\frac{\partial S}{\partial t} = KC \quad (3.26)$$

In this study, one species and first order kinetic linear-equilibrium adsorption isotherm is assumed. Several other adsorption isotherms are summarized by Pinder (1977).

If a radioactive material effects a change in its environment, then the adsorption term becomes

$$\frac{\partial S}{\partial t} = \lambda C \quad (3.27)$$

where λ is the radioactive constant and

$$\lambda = \frac{\ln 2}{T \ 1/2} \quad (3.28)$$

If the sources or sinks for the solute are different, then the reactant's concentration can be represented by Q

$$Q = Q_w \delta(x-x_1)\delta(y-y_1)\delta(z-z_1) \quad (3.29)$$

where Q = fluid sources or sinks term

Q_w = strength of fluid source or sink (L^3T^{-1})

δ = Dirac Delta function on (L^{-1})

C^* = solution concentration of the fluid source or sink
(ML^{-3})

The equation can now be written as:

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial x_i} (D_{ij} \frac{\partial C}{\partial x_j}) - \frac{\partial}{\partial x_i} (CV_i) + QC^* - \lambda C + KC$$

$$\begin{aligned}
\frac{\partial C}{\partial t} &= \frac{\partial}{\partial x} \left(D_{xx} \frac{\partial C}{\partial x} + D_{xy} \frac{\partial C}{\partial z} + D_{xz} \frac{\partial C}{\partial y} \right) \\
&+ \frac{\partial}{\partial y} \left(D_{yx} \frac{\partial C}{\partial x} + D_{yy} \frac{\partial C}{\partial y} + D_{yz} \frac{\partial C}{\partial z} \right) \\
&+ \frac{\partial}{\partial z} \left(D_{zx} \frac{\partial C}{\partial x} + D_{yz} \frac{\partial C}{\partial y} + D_{zz} \frac{\partial C}{\partial z} \right) \quad (3.30) \\
&- \frac{\partial V_x C}{\partial x} - \frac{\partial V_y C}{\partial y} - \frac{\partial V_z C}{\partial z} + Q C^* - \lambda C + K C
\end{aligned}$$

or

$$\frac{\partial C}{\partial t} = \nabla(D\nabla C) - \nabla \cdot (\vec{V}C) - \lambda C + K C + Q C^*$$

CHAPTER IV

SOLUTE TRANSPORT BY FINITE ELEMENTS

The finite element method is a powerful numerical technique for solving differential equations in different disciplines, including groundwater hydrology. The general steps for the method include:

1. The domain of interest is divided into a number of elements and described by nodal points.
2. The basic function is chosen.
3. The weighted integral of the residue is set to zero in order to obtain a set of simultaneous equations.
4. The resulting set of equations is solved to obtain the values of dependent variables at all nodes.

Galerkin's Approach

The dispersion equation is represented by

$$\begin{aligned} \frac{\partial C}{\partial t} = & \frac{\partial}{\partial x} \left(D_{xx} \frac{\partial C}{\partial x} + D_{xy} \frac{\partial C}{\partial y} + D_{xz} \frac{\partial C}{\partial z} \right) \\ & + \frac{\partial}{\partial y} \left(D_{yx} \frac{\partial C}{\partial x} + D_{yy} \frac{\partial C}{\partial y} + D_{yz} \frac{\partial C}{\partial z} \right) \\ & + \frac{\partial}{\partial z} \left(D_{zx} \frac{\partial C}{\partial x} + D_{zy} \frac{\partial C}{\partial y} + D_{zz} \frac{\partial C}{\partial z} \right) \end{aligned} \quad (4.1)$$

$$- \frac{\partial(V_x C)}{\partial x} - \frac{\partial(V_y C)}{\partial y} - \frac{\partial(V_z C)}{\partial z} + QC^* - \lambda C - KC$$

This equation can be shown by $L(C)=0$. To solve the differential equation by Galerkin's technique, the equation can be written as:

$$\begin{aligned} (L(C)) = & \frac{\partial C}{\partial t} - KC - \frac{\partial}{\partial x} \left(D_{xx} \frac{\partial C}{\partial x} + D_{xy} \frac{\partial C}{\partial z} + D_{xz} \frac{\partial C}{\partial y} \right) \\ & + \frac{\partial}{\partial y} \left(D_{yx} \frac{\partial C}{\partial x} + D_{yy} \frac{\partial C}{\partial y} + D_{yz} \frac{\partial C}{\partial z} \right) \\ & + \frac{\partial}{\partial z} \left(D_{zx} \frac{\partial C}{\partial x} + D_{yz} \frac{\partial C}{\partial y} + D_{zz} \frac{\partial C}{\partial z} \right) \\ & - \frac{\partial V_x C}{\partial x} - \frac{\partial V_y C}{\partial y} - \frac{\partial V_z C}{\partial z} - QC^* + \lambda C \end{aligned} \quad (4.2)$$

The function C can be approximated by the piecewise linear function \bar{C} .

$$C(x,y,z,t) \approx \bar{C}(x,y,z,t) = \sum_{i=1}^n C_i(t) W_i(x,y,z) \quad (4.3)$$

where $W_i(x,y,z)$ is a basic function. It is a set of linearly independent functions and satisfies the required boundary conditions. The unknown coefficient $C_i(t)$ is the discrete nodal value of the concentration as a function of time. The summation index is 'i'. The number of nodes within the solution domain is 'n'.

In order to get an exact solution, the residual error R is minimized.

$$L(C) - L(\bar{C}) = R \quad (4.4)$$

So that $L\{C(x,y,z)\}$ must be orthogonal to the shape function. According to the theory of inner product (Churchill, 1941),

$$\int_V L(\bar{C})W_k dV = 0 \quad (4.5)$$

where W_i is the weighting function in Galerkin's method.

The weighting function is equal to shape function

$$L \left\{ \sum_{i=1}^n C_i(t)W_i(x,y,z) \right\} W_k(x,y,z) dV = 0, \quad k = 1, 2, \dots, n \quad (4.6)$$

in which there are n undetermined coefficients C_i . If the set of trial functions W_k are orthogonal in the given domain,

$L(\bar{C})$ will approach the exact solution of $L(C)$:

$$L(C) - L(\bar{C}) = 0 \quad (4.7)$$

In the vector form:

$$\int_V L(\bar{C})W_k(x,y,z) dV = \int_V L \left\{ K\bar{C} + \frac{\partial \bar{C}}{\partial t} - \nabla(D \cdot \bar{C}) \right\} W_k dV$$

$$+ \nabla \cdot (V\bar{C}) - \lambda\bar{C} + QC\}W_k(x,y,z)dV \quad (4.8)$$

Equation (4.8) depends on the actual case. Some solute will not react and adsorption will not occur.

If first order linear equilibrium adsorption isotherm occurs, $S = KC = K\bar{C}$, or if radioactive decay happens, \bar{C} will remain in the equation, otherwise the term is "zero." For simplicity, $\bar{C} = C$, from the above derivation.

$$\int_V \frac{\partial C}{\partial t} - KC - \frac{\partial}{\partial x_i} (D_{ij} \frac{\partial C}{\partial x_j}) + \nabla \cdot (V\bar{C}) + \lambda C\}W_k dV - \int_V QC^*W_k dV = 0 \quad (4.9)$$

and

$$\nabla \cdot (D \cdot \nabla C) = \frac{\partial}{\partial x_i} (D_{ij} \frac{\partial C}{\partial x_j}) \quad (4.10)$$

The third term in equation (4.9) can be evaluated using Green's theory as

$$\int_V \frac{\partial}{\partial x_i} (D_{ij}) - \frac{\partial C}{\partial x_j} dV = \int_A W_k D_{ij} \frac{\partial C}{\partial x_j} dV - \int_V D_{ij} \frac{\partial W_i \partial C}{\partial x_i \partial x_j} dV \quad (4.11)$$

The last term in equation (4.11) becomes

$$\int_V \frac{\partial}{\partial x_i} (W_k D_{ij} \frac{\partial C}{\partial x_j}) dV = \int_A W_k D_{ij} \frac{\partial C}{\partial x_j} \ell_i dA \quad (4.12)$$

where ℓ_i are the direction cosines of A, and A is the boundary of the aquifer. Thus, equation (4.9) can be written as:

$$\begin{aligned}
& \int_V \left\{ \frac{\partial C}{\partial t} - KC + \lambda C + \nabla(VC) \right\} W_k dV - \int_V \frac{\partial}{\partial x_i} \left(W_k D_{ij} \frac{\partial C}{\partial x_j} \right) dV \\
& + \int_A W_k D_{ij} \frac{\partial C}{\partial x_i} l_i dA + \int_V D_{ij} \frac{\partial W_k}{\partial x_i} \frac{\partial C}{\partial x_j} dV - \int_V QC^* W_k dV = 0
\end{aligned} \tag{4.13}$$

$$\begin{aligned}
& \int_V \left(\frac{\partial C}{\partial t} - KC + \lambda C \right) W_i W_k dV + \int_V W_k V_i \frac{\partial W}{\partial x_i} dV + \int_V W_k W_i \frac{\partial V_i}{\partial x_i} dV \\
& + \int_A W_k D_{ij} \frac{\partial C}{\partial x_j} l_i dA + \int_V D_{ij} \frac{\partial W_k}{\partial x_i} \frac{\partial W_i C}{\partial x_j} dV
\end{aligned} \tag{4.14}$$

$$- \int_A W_k D_{ij} \frac{\partial C W_i}{\partial x_j} l_i dA - \int_V QC^* W_k dV = 0$$

Equation (4.14) can be represented by the following matrix equation:

$$[GN]\{C\} + [GM] \left\{ \frac{\partial C}{\partial t} \right\} + \{GF\} = 0 \tag{4.15}$$

where:

$$\begin{aligned}
[GN] = \sum_e \int_V \{ & D_{ij} \frac{\partial W_k}{\partial x_i} \frac{\partial W_i}{\partial x_j} + V_i W_k \frac{\partial W_i}{\partial x_i} + W_i W_k \frac{\partial V_i}{\partial x_i} \\
& + W_i W_k \frac{\partial V_i}{\partial x_i} + (-K + \lambda) W_i W_k \} dV
\end{aligned}$$

$$[GM] = \sum_e \int_V W_i W_k dV$$

$$[GF] = \sum_e \int_v w_k Q C^* dv - \int_A w_k D_{ij} \frac{\partial C W_i}{\partial x_j} l_i dA$$

Shape Functions

Selecting the adequate shape function usually leads to improving the accuracy and efficiency of solving the problem. Applying linear, quadratic, and cubic hexahedral elements, one can easily transform the isoparametric concept from quadrilaterals to deformed hexahedra. Isoparametric elements were first introduced by Ergatoudis et al. (1968). Since then, many papers have been published giving extensive details on how to choose the appropriate shape function for various forms of elements (Seegerlind, 1976; Zienkiewicz, 1977; Rao, 1982; and Lapidus and Pinder, 1984). The major difference between the isoparametric element and nondeformed elements is in the transformation of global coordinates to local coordinates using the Jacobian matrix. Figure 3 shows an isoparametric element in local and global coordinates.

The Jacobian matrix is given as:

$$[J] = \begin{vmatrix} \frac{\partial x}{\partial \alpha} & \frac{\partial y}{\partial \alpha} & \frac{\partial z}{\partial \alpha} \\ \frac{\partial x}{\partial \beta} & \frac{\partial y}{\partial \beta} & \frac{\partial z}{\partial \beta} \\ \frac{\partial x}{\partial r} & \frac{\partial y}{\partial r} & \frac{\partial z}{\partial r} \end{vmatrix} \quad (4.16)$$

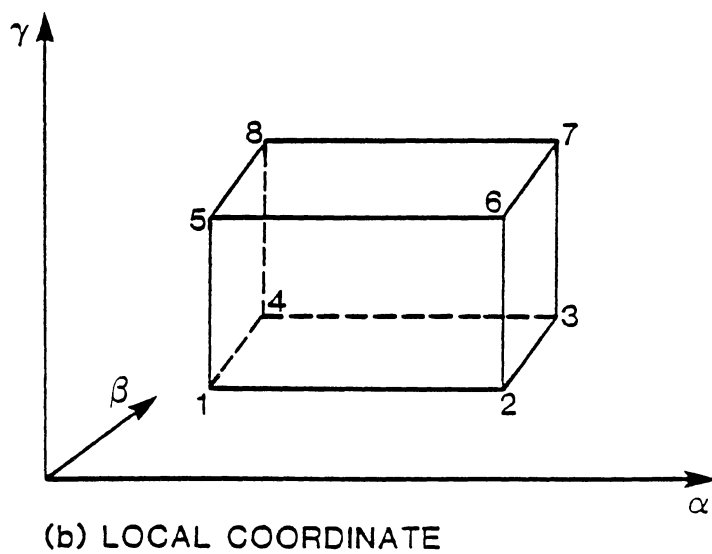
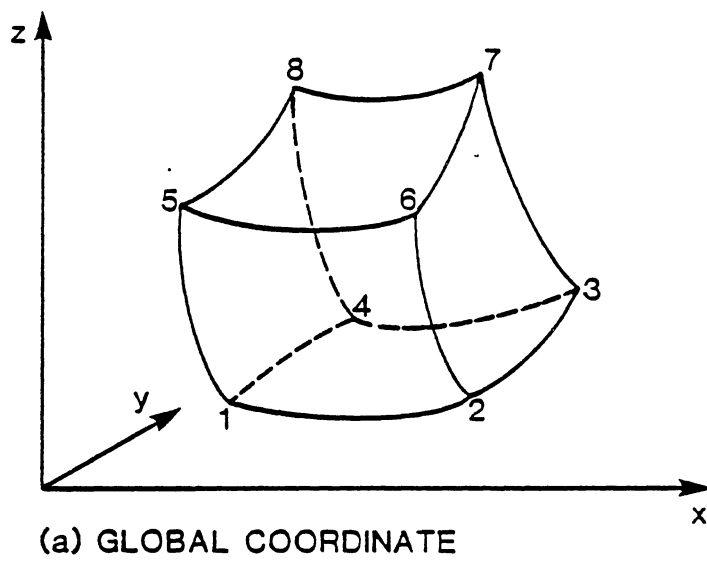


Figure 3. Isoparametric Element in Global and Local Coordinates

The relationship between global and local derivatives is given as

$$\begin{pmatrix} \frac{\partial W_i}{\partial x} \\ \frac{\partial W_i}{\partial y} \\ \frac{\partial W_i}{\partial z} \end{pmatrix} = [J]^{-1} \begin{pmatrix} \frac{\partial W_i}{\partial \alpha} \\ \frac{\partial W_i}{\partial \beta} \\ \frac{\partial W_i}{\partial r} \end{pmatrix} \quad (4.17)$$

Shape functions are given below for linear, quadratic, cubic, and mixed elements. The node numbers correspond to the nodes shown in Figure 4.

1. Linear quadrilateral element (8 nodes):

$$W_i = (1+\alpha_i)(1+\beta\beta_i)(1+rr_i)(\alpha_i+\beta\beta_i-2)/8, \quad i = 1, 2, \dots, 8$$

2. Quadratic quadrilateral element (20 nodes):

$$(i) \quad W_i = (1-\alpha_i)(1+\beta\beta_i)(1+rr_i)(\alpha_i+\beta\beta_i-2)/8$$

where $i = 1, 2, 3, 4, 5, 6, 7, 8$

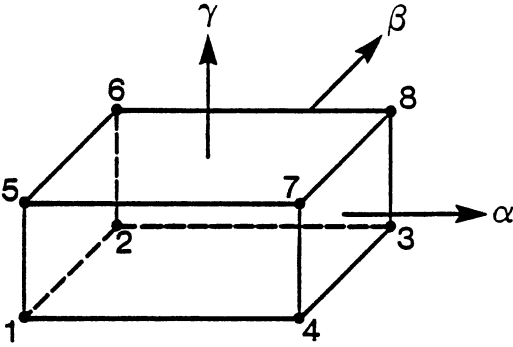
$$(ii) \quad W_i = (1-r^2)(1+\alpha_i)(1+\beta\beta_i)/4, \quad i = 9, 10, 11, 12$$

$$(iii) \quad W_i = (1-\alpha^2)(1+\beta\beta_i)(1+rr_i)/4, \quad i = 13, 14, 15, 16$$

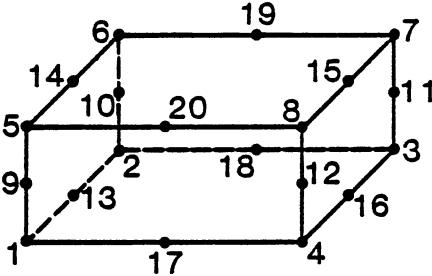
$$(iv) \quad W_i = (1-\beta^2)(1+\alpha_i)(1+rr_i)/4, \quad i = 17, 18, 19, 20$$

3. Cubic quadrilateral elements (32 nodes):

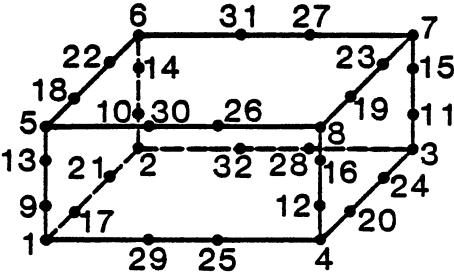
$$(i) \quad W_i = (1+\alpha_i)(1+\beta\beta_i)(1+rr_i)\{9(\alpha^2+\beta^2+r^2)-19\}/64$$



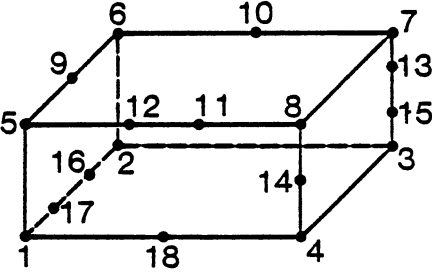
(a) LINEAR ELEMENT



(b) QUADRATIC ELEMENT



(c) CUBIC ELEMENT



(d) MIXED ELEMENT

Figure 4. Prism Elements for Three-Dimensional Model

where $i = 1, 2, 3, 4, 5, 6, 7, 8$

$$(ii) W_i = 9(1-\alpha^2)(1+9\alpha\alpha_i)(1+\beta\beta_i)(1+rr_i)/64$$

where $i = 17, 18, 19, 20, 21, 22, 23, 24$

$$(iii) W_i = 9(1-\beta^2)(1+9\beta\beta_i)(1+\alpha\alpha_i)(1+rr_i)/64$$

where $i = 25, 26, 27, 28, 29, 30, 31, 32$

$$(iv) W_i = 9(1-r^2)(1+9rr_i)(1+\alpha\alpha_i)(1+\beta\beta_i)/64$$

where $i = 9, 10, 11, 12, 13, 14, 15, 16$

4. Mixed quadrilateral elements (18 nodes):

(i) Linear side: W_i for $i = 1, 2, 3, 4, 5, 6, 7, 8$

(ii) Quadratic side: (a) W_i for $i = 10, 14$

(b) W_i for $i = 9$

(c) W_i for $i = 18$

(iii) Cubic side: (a) W_i for $i = 16, 17$

(b) W_i for $i = 11, 12$

(c) W_i for $i = 13, 15$

Seegerlind (1976) defined $\alpha_0 = \alpha\alpha_1$, $\beta_0 = \beta\beta_1$, and $r_0 = rr_1$. For the corner of the linear element:

$$\alpha_0 = \alpha\alpha_i = -\alpha, \text{ since } \alpha_i = -1 \text{ and } \beta_0 = -\beta, r_0 = -r$$

Then, W_i becomes

$$W_i = \frac{1}{8} (1 - \alpha)(1 - \beta)(1 - r)$$

For the quadratic element:

1. Corner node:

$$W_i = \frac{1}{64} (1 + \alpha_0)(1 + \beta_0)(1 + r_0)\{9(\alpha^2 + \beta^2 + r^2) - 19\}$$

2. Midside node:

$$\alpha = 0; \beta_i = +1; r = +1$$

$$W_i = \frac{1}{64} (1 - \alpha^2)(1 + 9\alpha_0)(1 + \beta_0)(1 + r_0)$$

For the cubic element:

1. Corner node:

$$W_i = \frac{1}{64} (1 + \alpha_0)(1 + \beta_0)(1 + r_0)\{9(\alpha^2 + \beta^2 + r^2) - 19\}$$

2. Midside node:

$$\alpha = +\frac{1}{3}; \beta_i = +1; r = +1$$

$$W_i = \frac{1}{64} (1 - \alpha^2)(1 + 9\alpha_0)(1 + \beta_0)(1 + r_0)$$

Numerical Integration

Gaussian quadrature integration is used in this study. The range of the integral is defined between -1 and 1. Lapidus and Pinder (1982) gave the appropriate Gaussian quadrature expression as

$$\int_{-1}^1 f(\alpha) = \sum_{i=1}^n W_i f(\alpha_i) + R_n$$

where W_i = weighting factor

α_i = Coordinate of the i^{th} integration point (Gauss point)

n = total number of integration points

$$R_n = 2^{2n+1} (n!)^2 4(2n+1)^2 (-1)^{n+1} \left\{ (2n!) \right\}^{2n-1} \frac{d^{2n} f}{d\alpha^{2n}} \Big|_{\alpha=\Theta}$$

$-1 < \Theta < 1$

A polynomial of degree $(2n-1)$ can be integrated exactly by using n integration points. The weighting coefficients and integration points are computed using Legendre polynomials. The technique is often called the Gauss-Legendre quadrature method. Zienkiewicz (1971) tabulated the integration points and weights up to 10 points, as shown in Table I. For the three-dimensional case, the formula becomes

$$\int_{-1}^1 \int_{-1}^1 \int_{-1}^1 f(\alpha, \beta, r) d\alpha d\beta dr = \sum_{k=1}^n \sum_{j=1}^n \sum_{i=1}^n W_i W_j W_k f(\alpha_i, \beta_j, r_k)$$

TABLE I
 ABSCISSAE AND WEIGHT COEFFICIENTS OF
 THE GAUSSIAN QUADRATURE FORMULA

$$\int_{-1}^1 f(x) dx = \sum_{i=1}^n W_k f(a_i)$$

n	Weighting Coefficient (W_k)	Abscissae ($+a$)
1	2.00000 00000	0.00000 00000
2	1.00000 00000	0.57735 02691
3	0.55555 55555 0.88888 88888	0.77459 66692 0.00000 00000
4	0.34785 48451 0.65214 51548	0.86113 63115 0.33998 10435
5	0.23692 68850 0.47862 86704 0.56888 88888	0.90617 98459 0.53846 93101 0.00000 00000
6	0.17132 44923 0.36076 15730 0.46791 39345	0.93246 95142 0.66120 94864 0.23861 91860
7	0.12948 49661 0.27970 53914 0.38183 00505 0.41795 91836	0.94910 79123 0.74153 11855 0.40584 51513 0.00000 00000
8	0.10122 85362 0.22238 10344 0.31370 66458 0.36268 37833	0.96028 98564 0.79666 64774 0.52553 24099 0.18343 46424
9	0.08127 43883 0.18064 81606 0.26061 06964 0.31234 70770 0.33023 93550	0.96816 02395 0.83603 11073 0.61337 14327 0.32425 34234 0.00000 00000
10	0.06667 13443 0.14945 13491 0.21908 63625 0.26926 67193 0.29552 42247	0.97390 65285 0.86506 33666 0.67940 95682 0.43339 53941 0148870 43389

Node Numbering and Assembly of Elements

Assigning a number to a node is a very important step in the finite element method. Labeling the node in a right manner saves computer storage and increases computational efficiency in obtaining a solution. Proper numbering of the nodes gives a banded matrix instead of a full matrix. A matrix is banded because zeros beyond the bandwidth need not be stored on the computer. The method of calculating the bandwidth has been defined by Segerlind (1976), Zienkiewicz (1971), and Rao (1982). They have given the equation as

$$\text{NBAND} = (D + 1) * \text{NDOF} \quad (4.18)$$

where NBAND = bandwidth

D = maximum largest difference in the node number
occurring for all elements

NDOF = number of degrees of freedom at each node

The equation shows that D has to be minimized in order to minimize the bandwidth. Cook (1981) points out that a shorter bandwidth can be obtained simply by numbering the nodes across the shortest dimension of the matrix.

After the matrices have been calculated for each element, they are assembled to form a global system. Figure 5(a) shows the domain to be divided into five elements, and Figures 5(b) and 5(c) show how they are assembled together.

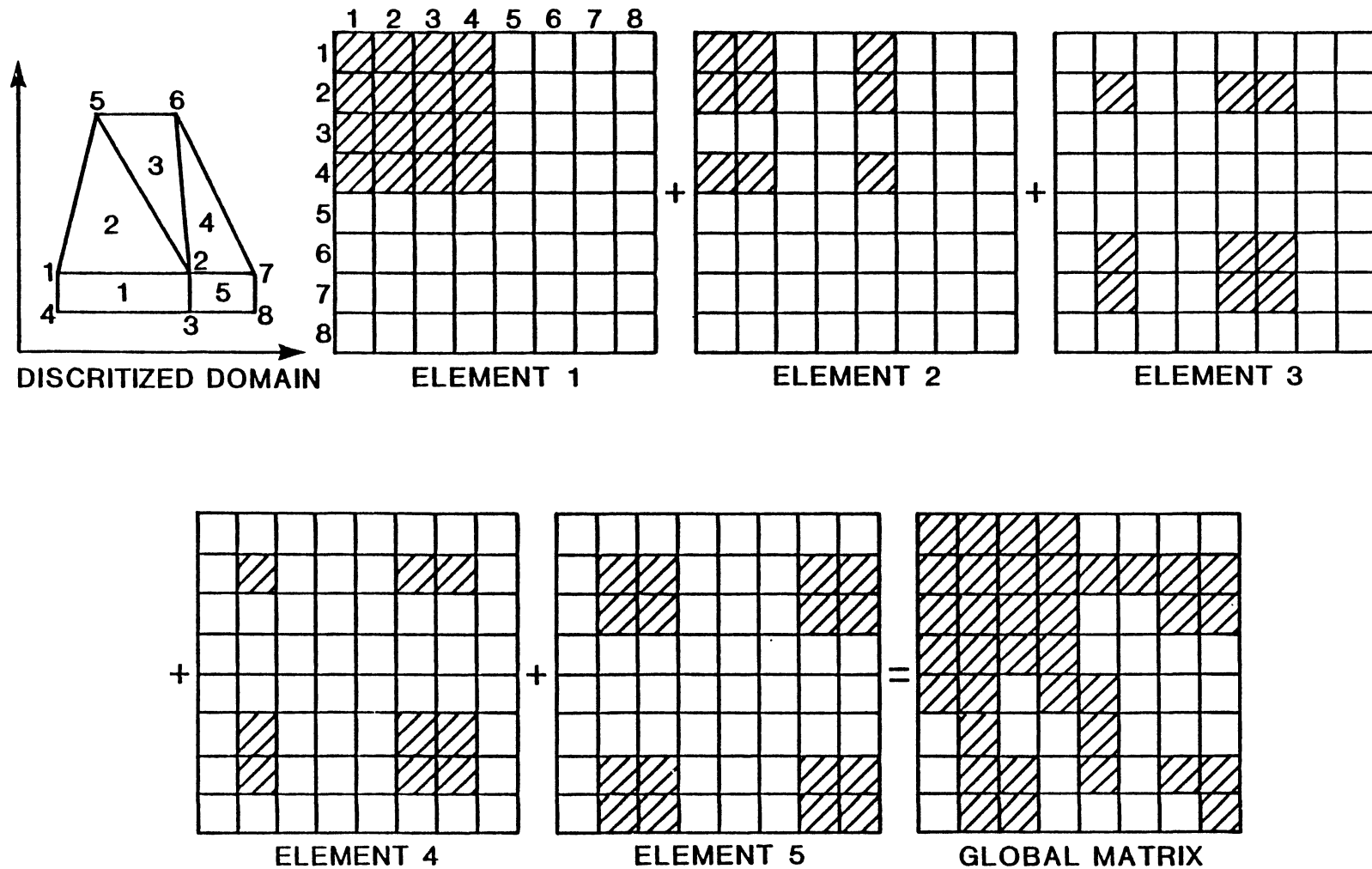


Figure 5. Illustration of Assemblage

Initial and Boundary Conditions

Before any of the partial differential equations previously derived can be solved, initial and boundary conditions must be specified. The initial condition is the value of the dependant variable at time zero over the whole domain. This could be

$$C = C_0(x,y,z,t)$$

For groundwater applications, two types of boundary are generally used: (1) specified value, and (2) specified flux. Whether the value is head, concentration, or temperature depends on the equation. The value in this study is concentration.

With the specified value type, values of concentration are specified along the boundary, which also is known as the Dirichlet Condition.

Concentration is specified along the boundary and equated to the normal derivative, also known as the Newman condition, where the flux is specified.

CHAPTER V

SOLUTION OF FINITE ELEMENT EQUATIONS

This chapter will describe how the solute transport equation developed in Chapter III can be solved.

Discretization in Time Domain

The finite element technique has been applied to the special derivative, while the time derivative has usually been approximated by using the finite difference method. The element equation developed in Chapter IV can be written as

$$[GN]\{C\} + [GM]\left\{\frac{\partial C}{\partial t}\right\} + \{GF\} = 0 \quad (5.1)$$

Remson et al. (1971), Pinder and Gray (1977), and Huykorn et al. (1983) replaced the time derivative by a weighted finite difference approximation. Therefore, the above equation becomes

$$\begin{aligned} & [GN](\Theta\{C\}_{t+\Delta t} + (1-\Theta)\{C\}_t) + \frac{1}{\Delta t}[GM](\{C\}_{t+\Delta t} - \{C\}_t) \\ & = \Theta\{GF\}_{t+\Delta t} + (1-\Theta)\{GF\}_t \quad (0 < \Theta < 1) \end{aligned} \quad (5.2)$$

where Θ dictates the reference point in the time of difference formula. For $\Theta = 0$, the scheme is known as the forward

finite difference method; with $\Theta = 1$, it becomes the backward finite difference scheme and with $\Theta = 0.5$, it is called the central finite difference scheme.

In this study, the backward finite difference scheme has been chosen for discretization of the time. When $\Theta = 1$, it is substituted into equation (5.2) and gives

$$[GN]\{C\}_{t+\Delta t} + \left(\frac{1}{\Delta t}\right)\{C\}_{t+\Delta t} - \left(\frac{1}{\Delta t}\right)[GM]\{C\}_t = \{GF\}_{t+\Delta t} \quad (5.3)$$

Stability and Convergence of Implicit Scheme

For any approximation method to be valid, it must present a solution that is close to the exact solution. If one considers a fixed point and inquires about the difference between two meshes that become finer and finer, the error goes to zero. We will say that a finite difference method is convergent. The second aspect is fixing Δx and Δt and then examining when $t \rightarrow \infty$. In doing so, one hopes that errors are not amplified. If the amplification of errors is restricted, the method is said to be stable.

Gray and Pinder (1977), Chung (1978), and Huyakorn and Pinder (1983) described the stability and convergence requirement and found that the solution to the approximating finite difference equation can be written as $C_{i,k}$, where i is the pivotal node and k is the time interval. Due to the round-off errors during algebraic manipulations, a solution

$C_{i,k}$ is obtained which will differ from the time solution by a numerical error $E_{i,k}$ such that

$$E_{i,k} = C_{i,k} - \bar{C}_{i,k} \quad (5.4)$$

A numerical scheme will be considered stable if, with increased time, $E_{i,k}$ tends to zero for all the values of i . Substitution of a finite difference approximation into the homogeneous set of equations, obtained from equation (5.1), by getting {GF} equal to zero, gives an expression

$$\{C\}_{k+1} = [GN^*]\{C\}_k \quad (5.5)$$

and

$$\{C\}_0 = \{W\} \quad (5.6)$$

where $\{C\}_0$ is the matrix of initial conditions and $[GN^*]$, a matrix called the amplification matrix. Two stability criteria are considered. The first criterion, defined by Saulyev (1964), defines the following norms, which are consistent inasmuch as they satisfy the Schwarz inequality (Westlake, 1968).

$$||\{C\}_k|| = \text{MAX}_{1 \leq i \leq n} |C_{i,k}| \quad (5.7)$$

and

$$||[GN^*]|| = \text{MAX}_{1 \leq i \leq n} \sum_{j=1}^n |GN_{i,j}| \quad (5.8)$$

Let us consider a matrix $\{\bar{W}\}$ composed of the initial conditions and slightly modified, due to rounding off of

its components using the overbar notation. The equation (5.5) becomes

$$\{\bar{C}\}_{k+1} = [GN^*]\{\bar{C}\}_k \quad (k = 1, 2, \dots, k) \quad (5.9)$$

and

$$\{\bar{C}\}_0 = \{\bar{W}\} \quad (5.10)$$

in which p is the total number of time steps considered. If the error vector is defined by

$$\{\bar{E}\}_k = \{C\}_k - \{\bar{C}\}_k \quad (5.11)$$

then

$$\{\bar{E}\}_{k+1} = [GN^*]\{\bar{E}\}_k \quad (5.12)$$

$$\text{where } \{\bar{E}\}_0 = \{W\} - \{\bar{W}\} \quad (5.13)$$

$$\text{or } \{\bar{E}\}_k = [GN^*]_k \{\bar{E}\}_0 = [GN^*]_k (\{W\} - \{\bar{W}\}) \quad (5.14)$$

for the Schwarz inequality and above equation becomes

$$||\{\bar{E}\}_k|| \leq ||[GN^*]||_k ||\{\bar{E}\}_0|| \quad (5.15)$$

It is apparent from equation (5.15) that the error $\{E\}$ in the initial data will not grow with an increase in k , and that the solution will remain stable only if

$$||[GN^*]|| \leq 1 \quad (5.16)$$

This same relationship holds true when the error is assumed at any arbitrary time level, because this level can always be considered as a new set of initial conditions.

The second criterion is the Neumann necessary condition for stability. Chung (1978) and Huyakorn and Pinder (1983) developed the same equation as (5.1), and stated that the stability of the numerical solution can be assumed if the norm of the amplification is made smaller than unity. For a symmetric $[GN^*]$, the appropriate norm to use is the special norm $||[GN^*]||_2$. Thus, the inequality becomes

$$||[GN^*]||_2 \leq 1 \quad (5.17)$$

since $||[GN^*]||_2$ is defined as

$$||[GN^*]||_2 = \max_I |\lambda_I| \quad (5.18)$$

where λ_I denotes the eigenvalue of $[GN]$, the stability criterion becomes

$$\max_I |\lambda_I| \leq 1 \quad (5.19)$$

For the explicit scheme $\Theta = 0$, substitute to equation (5.3) using $k+1$ step instead of $t+\Delta t$ time step. As the $[GF]$ is set equal to zero, the equation becomes

$$([GM]/\Delta t)\{C\}_{k+1} = ([GM]/\Delta t - [GN])\{C\}_k \quad (5.20)$$

and from equation (5.5)

$$[GN^*] = [GM]^{-1} ([GM] - \Delta t [GN]) \quad (5.21)$$

where $[I]$ is a unit matrix and

$$[I] = [GN^*] + \Delta t [GM]^{-1} [GN] \quad (5.22)$$

Taking matrix norm on both sides

$$1 \leq ||[GN^*]||_2 + \Delta t ||[GM]^{-1}||_2 ||[GN]||_2 \quad (5.23)$$

or

$$||[GN^*]||_2 \geq ||[I]||_2 - \Delta t ||[GM]^{-1}||_2 ||[GN]||_2 \quad (5.24)$$

For stability $||[GN^*]|| \leq 1$ but

$$1 - \Delta t ||[GM]^{-1}||_2 ||[GN]||_2 \leq 1 \quad (5.25)$$

It can be seen that a bound for Δt outside of the inequality is not valid, so the explicit scheme is conditionally stable. For implicit scheme, $\Theta = 1$

$$[GN^*] = ([GN]_2 + [GM]/\Delta t)^{-1} ([GM]/\Delta t) \quad (5.26)$$

It can be shown that for all values of Δt we have

$$||[GN^*]||_2 \leq ||[I]||_2 = 1 \quad (5.27)$$

Thus, we say the implicit is unconditionally stable.

The main point of this section is to prove that the implicit scheme is stable and convergent.

Initial and Boundary Conditions

The specification of initial and boundary conditions is necessary in order to obtain a solution of the solute trans-

port equation. The initial concentration can be calculated from field data or from previous simulation. From the Dirichlet condition, the concentration at certain nodes is specified, the Neumann Condition, the solute flux entering or leaving the aquifer is specified.

The Neumann condition can be used to represent an aquifer with well withdrawal or injection, and a constant concentration boundary in the model can represent parts of the aquifer where the concentration will not change with time. If the constant concentration represents a fluid source, the solute concentration in the source fluid must also be specified. If the boundary represents a fluid sink, then the concentration of the product will be the same as the concentration in the aquifer at the location of the sink.

The boundary condition is put into the program before the formation of the global equation, enabling one to solve the matrix in the model. The subprogram BOUND will handle this portion.

Segerlind (1976) described two methods for specifying the boundary condition: one is the deletion row and column, and the other is the multiplication of the diagonal terms by a very large number. The first method was chosen for this study. The equation for backward expression also can take the following form:

$$[GN]\{C\}_t + \frac{1}{\Delta t} [GM]([C]_t - \{C\}_{t-\Delta t}) + \{GF\}_t = 0 \quad (5.28)$$

Rearranging equation (5.28).

$$\left([GN] + \frac{1}{\Delta t} [GM] \right) \{C\}_t = \frac{1}{\Delta t} [GM] \{C\}_{t-\Delta t} - \{GF\} \quad (5.29)$$

The equation shows the value of concentration. On the right hand side are the knowns and on the other side are the unknowns. The first value of $C(t)$ is the known value from the equation and it becomes

$$[GL] \{C\}_t = \{GF\} \quad (5.30)$$

where $[GL] = ([GN] + [GM]/\Delta t)$, and

$$GF = ([GM]/\Delta t) \{C\} - \{GF\}$$

Equation (5.30) can be expressed as

$$\begin{vmatrix} GL_{i,j} & \dots & GL_{i,L} & \dots & GL_{i,n} \\ \vdots & & \vdots & & \vdots \\ GL_{L,j} & \dots & GL_{L,L} & \dots & GL_{L,n} \\ \vdots & & \vdots & & \vdots \\ GL_{n,j} & \dots & GL_{n,L} & \dots & GL_{n,n} \end{vmatrix} \begin{vmatrix} C_i \\ \vdots \\ C_L \\ \vdots \\ C_n \end{vmatrix} = \begin{Bmatrix} GF_i \\ \vdots \\ GF_L \\ \vdots \\ GF_n \end{Bmatrix} \quad (5.31)$$

where $i, j = 1, 2, \dots, n$

The value of C_L is specified according to the deletion row and column method. All the coefficients in the row l are set to zero except the diagonal term, which is left unchanged $GL_{L,j} = 0$, but $L \neq j$ and the L^{th} term of GF_L will be replaced by $G_{LL}C_L$.

$$\begin{vmatrix} GL_{i,j} & \dots & GL_{i,L} & \dots & GL_{i,n} \\ \vdots & & \vdots & & \vdots \\ GL_{L,j} & \dots & GL_{L,L} & \dots & GL_{L,n} \\ \vdots & & \vdots & & \vdots \\ GL_{n,j} & \dots & GL_{n,L} & \dots & GL_{n,n} \end{vmatrix} \begin{vmatrix} C_i \\ \vdots \\ C_L \\ \vdots \\ C_n \end{vmatrix} = \begin{Bmatrix} GF_i \\ \vdots \\ GF_L \\ \vdots \\ GF_n \end{Bmatrix} \quad (5.32)$$

where $i, j = 1, 2, \dots, n$

All of the remaining equations are modified by subtracting the product $GL_{i,L}C_L$ from GF_i and then setting $GL_{L,L} = 0$, $i = 1, n$ and $i \neq L$.

$$\begin{vmatrix} GL_{i,j} & \dots & GL_{i,L} & \dots & GL_{i,n} \\ \vdots & & \vdots & & \vdots \\ 0 & \dots & GL_{L,L} & \dots & 0 \\ \vdots & & \vdots & & \vdots \\ GL_{n,j} & \dots & GL_{n,L} & \dots & GL_{n,n} \end{vmatrix} \begin{vmatrix} C_i \\ \vdots \\ C_L \\ \vdots \\ C_n \end{vmatrix} = \begin{Bmatrix} GF_i - GL_{i,L} C_L \\ \vdots \\ GF_L - C_L \\ \vdots \\ GF_n - GL_{n,L} C_L \end{Bmatrix} \quad (5.33)$$

The above process continues the completion, and is applied to the solution of the matrix equation.

Matrix Solution

Each numerical approximation tends to an algebraic equation for each node point. These are combined to form a matrix equation; that is, a set of N equations with N unknowns, where N is the number of nodes. The general form of equations, written in matrix form, is as equation (5.30)

$$[GL]\{C\}_t = \{GF\} \quad (5.34)$$

Where GL is a matrix containing coefficients related to grids spacing and to aquifer properties such as dispersion

coefficient. C is a vector containing the dependent variable to be determined in our case, is concentration and GF is a vector containing all known information, such as boundary condition information.

In general, a matrix equation may be solved numerically by the direct or iterative method. In the direct method, a sequence of operations is performed once, providing a solution that is exact except for machine round-off error. The iterative method is a process of successive approximations. An initial guess at the matrix solution is made, then this guess is imposed by some iterative process until an error criterion is attained.

In this study, the direct method has been used for solving the matrix, and the Gauss elimination and back substitution has been adapted to solve the matrix. The basic objective of this method is to transform the given system into an equivalent triangular system, then the triangular system can be solved by back substitution. The method is shown below.

$$\begin{aligned}
 GL_{11}^{\circ} C_1 + GL_{12}^{\circ} C_2 + \dots + GL_{1n}^{\circ} C_n &= GF_1^{\circ} \\
 GL_{21}^{\circ} C_1 + GL_{22}^{\circ} C_2 + \dots + GL_{2n}^{\circ} C_n &= GF_2^{\circ} \\
 \dots &= \dots \\
 GL_{n1}^{\circ} C_1 + GL_{n2}^{\circ} C_2 + \dots + GL_{nn}^{\circ} C_n &= GF_n^{\circ}
 \end{aligned} \tag{5.35}$$

where the superscript 0 means the original values. By solving the first equation for C_1 , we obtain

$$C_1 = \frac{GF_1^1}{GF_{11}^1} - \frac{GL_{12}^1}{GL_{11}^1} C_2 - \frac{GL_{13}^1}{GL_{11}^1} C_3 - \dots - \frac{GL_{1n}^1}{GL_{11}^1} C_n$$

Substitution of this C into the remaining equation

(5.35) leads to

$$\begin{aligned} GL_{22}^1 C_2 + GL_{23}^1 C_3 + \dots + GL_{2n}^1 C_n &= GF_2^1 \\ GL_{32}^1 C_2 + GL_{33}^1 C_3 + \dots + GL_{3n}^1 C_n &= GF_3^1 \\ \dots &= \dots \\ \dots &= \dots \\ GL_{n2}^1 C_2 + GL_{n3}^1 C_3 + \dots + GL_{nn}^1 C_n &= GF_n^1 \end{aligned} \tag{5.36}$$

In general

$$C_k = \frac{GF_k^{k-1}}{GF_{kk}^{k-1}} - \sum_{j=k+1}^n \frac{GL_{kj}^{k-1}}{GL_{kk}^{k-1}} C_j \tag{5.37}$$

where

$$\begin{aligned} GL_{ij}^k &= GL_{ij}^{k-1} - \{(GL_{ik}^{k-1} GL_{kj}^{k-1}) / GL_{kk}^{k-1}\} \\ GF_i^k &= GF_i^{k-1} - \{(GL_{ik}^{k-1} GF_k^{k-1}) / GL_{kk}^{k-1}\} \\ i, j &= k+1, \dots, n \end{aligned}$$

After applying the same procedure $n-1$ times, the original system of equations reduces to the following single equation:

$$GL_{nn}^{n-1} C_n = GF_n^{n-1}$$

then

$$C_n = \frac{GF_n^{n-1}}{GL_{nn}^{k-1}}$$

The C_{n-1} , C_{n-2} , ... C_{n-k} value can be found in reverse order. If at any stage in the elimination process one of the pivot elements vanishes, we attempt to rearrange the remaining rows so as to obtain a nonvanishing pivot. Otherwise, the matrix GL is singular and the system has no solution. This is done in subprogram SOLVER.

CHAPTER VI

COMPUTER PROGRAM

The computer program has been written for the three-dimensional pollutant in a groundwater system. This program was written in standard FORTRAN language and run on the Oklahoma State University IBM/3081K - WATFIV system.

Main Program

The main program coordinates other subroutines; it controls input and prints output of data, dimensions the program at prescribed time increments, calls for shape function, assembles the element matrices into the global matrix, calculates the bandwidth, and solves the matrix. When maximum time has been reached, computations are determined. A flow chart for the main program and general type of finite element analysis are shown in Figures 6 and 7.

Subroutine INPUT

The subprogram reads and prints all the input data, including the specified nodes of boundary condition.

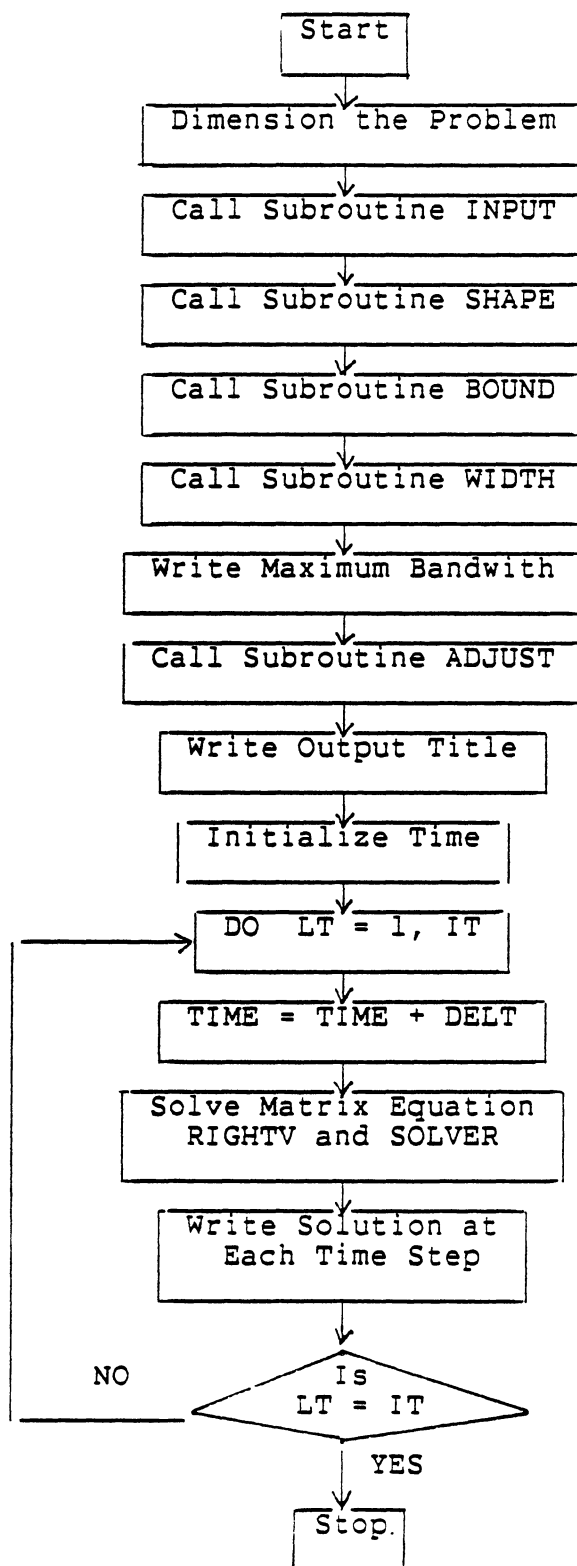


Figure 6. Flow Chart for Main Program

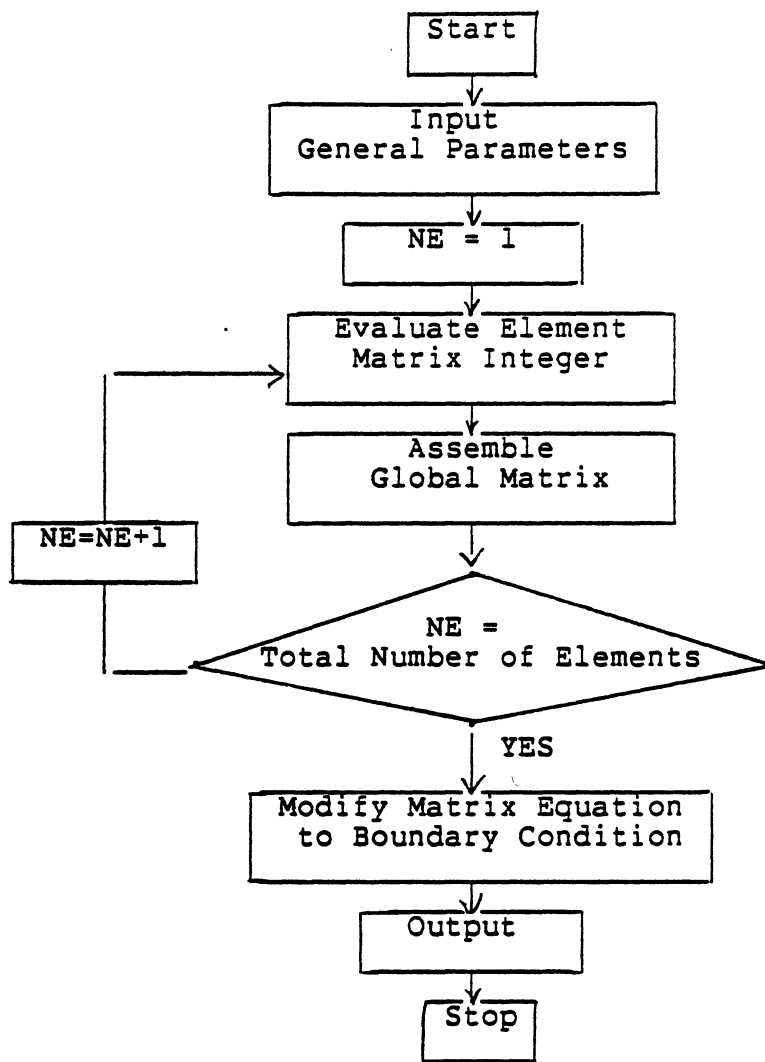


Figure 7. General Type Flow Chart for Finite Element Analysis

Subroutine SHAPE

This subprogram provides the local coordinates for each element and Gaussian Quadrature information. It does the numerical integration of the shape function for all elements. From the SHAPE subprogram, the Jacobian matrix and its determinant are obtained. Then the program calls the subprogram GLOBAL.

Subroutine GLOBAL

This subprogram assembles the element matrices into global matrix. The global matrices represent RMX (right hand side vector), STOMX, and GLOBMX.

Subroutine BOUND

This subprogram modifies the global matrix with given boundary conditions. The given known boundary conditions are ND(I). The method of deletion of rows and columns is used. The flow chart for subroutine bound is shown in Figure 8.

Subroutine WIDTH

This subprogram calculates the bandwidth. In order to minimize computer storage requirements, it is important to keep the maximum difference between any two numbers of any given element as small as possible.

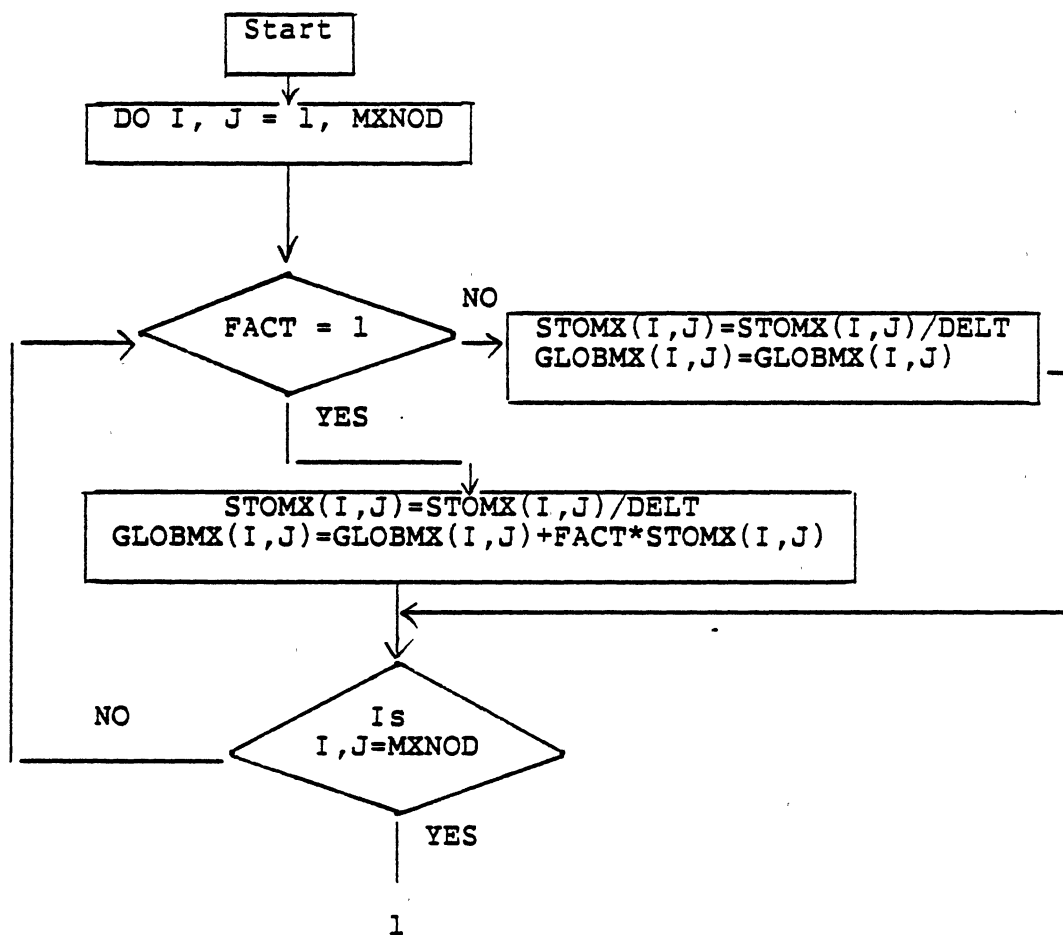


Figure 8. Flow Chart of Subroutine BOUND

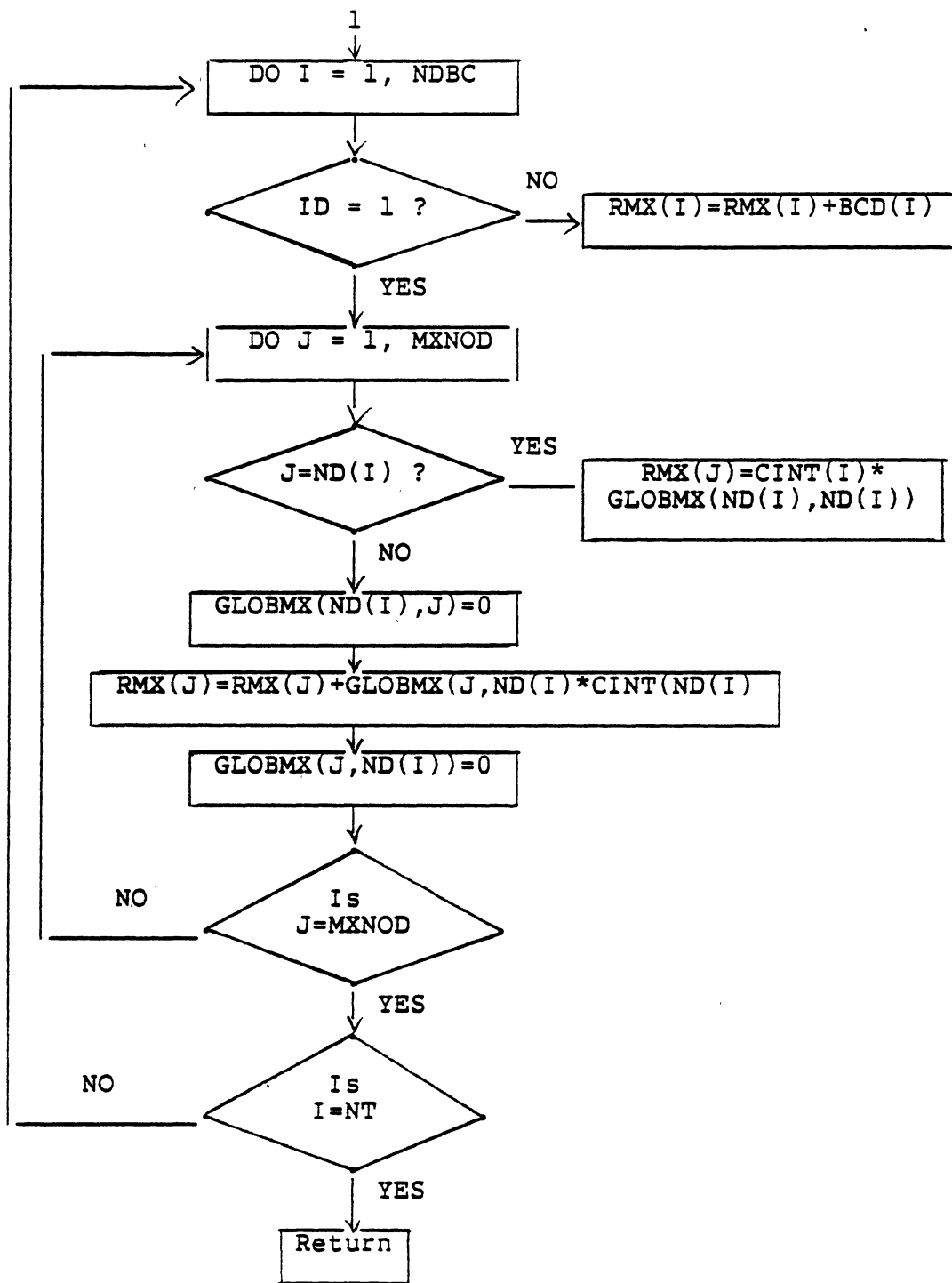


Figure 8. (Continued)

Subroutine ADJUST

This subprogram decomposes the matrix into an upper triangular matrix using the Gaussian elimination procedure.

Subroutine RIGHTV

This subprogram updates the righthand side vector, and will be called after each time step.

Subroutine SOLVER

This subprogram accepts the upper band of the matrix from subroutine ADJUST and solves the unknown in the system of equations. Using backward substitution, vector C is solved.

CHAPTER VII

ONE-DIMENSIONAL VALIDATION

Example Problem

A two-dimensional analytical solution developed by Cleary, Miller, and Pinder (1978) was used to validate the three-dimensional model. In the testing problem, the dimensions of the model are 70 by 100 feet and the thickness of the aquifer is 100 feet. Figure 9 shows the strip source with a finite width aquifer.

$$\frac{\partial C}{\partial t} + V \frac{\partial C}{\partial x} = D_x \frac{\partial^2 C}{\partial x^2} + D_y \frac{\partial^2 C}{\partial y^2} - KC \quad (7.1)$$

subject to

$$C = C_0 e^{-rt} \quad x = 0; \quad y_1 \geq y \geq y_2$$

$$C = 0 \quad x = 0; \quad \text{all other } y$$

$$\frac{\partial C}{\partial y} = 0 \quad y = 0$$

$$\frac{\partial C}{\partial y} = 0 \quad y = w$$

$$\frac{\partial C}{\partial x} = 0 \quad x \rightarrow \infty$$

$$C = 0 \quad t = 0$$

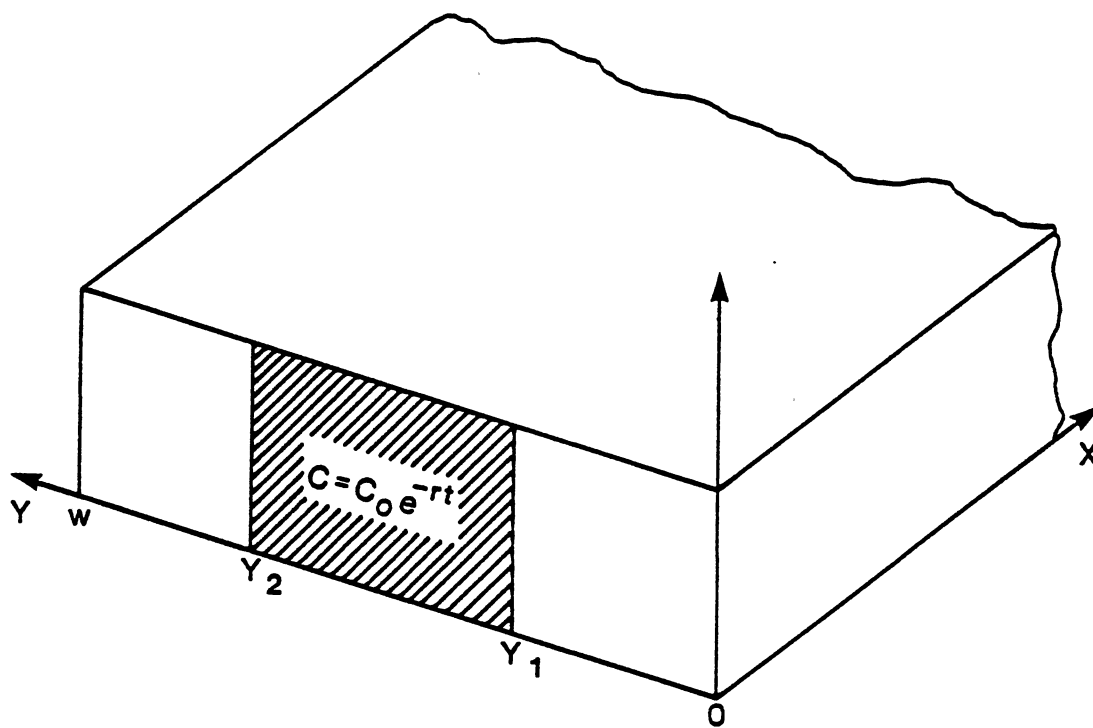


Figure 9. Strip Source with Finite Width Aquifer

In the test, the 'r' and 'K' values are set to zero. r is the first-order rate on the boundary condition and K is the first order decay constant in the system. In the y direction, velocity is 2ft/day, limits of the strip source is located between 20 to 50 feet.

Analytical Solution

The analytical solution provided by Cleary et al. (1978) is as follows:

$$\begin{aligned}
 \frac{C(x,y,t)}{C_0} &= e^{-rt} \{u(Y-Y_1) - u(Y-Y_2)\} \\
 &- \sum_{n=0}^{\infty} L_n \cos(r_n Y) \left[P_n e^{-(r_n^2 D_y + k)t} \left\{ \operatorname{Erfc}\left(\frac{V_x \sqrt{t}}{2\sqrt{D_x}} - \frac{x}{2\sqrt{D_x t}}\right) \right. \right. \\
 &- \left. \left. \exp\left(\frac{xV_x}{D_x}\right) \operatorname{Erfc}\left(\frac{r_x \sqrt{t}}{2\sqrt{D_x}} + \frac{x}{2\sqrt{D_x t}}\right) \right\} \right. \\
 &+ \left. \left\{ (k-r)P_n + D_y \frac{r_n}{W} [\sin(r_n Y_2) - \sin(r_n Y)] \right\} \frac{\exp\left(\frac{V_x x}{2D_x} - rt\right)}{(r_n^2 D_y + k - r)} \right. \\
 &\left. \left\{ \exp\left(\frac{-xV_x}{2D_x} + \exp\left[\frac{xV_x}{2D_x} - (r_n^2 D_y + k - r)t\right] \operatorname{Erfc}\left(\frac{V_x}{2} \sqrt{\frac{t}{D_x}} + \frac{x}{2\sqrt{tD_x}}\right) \right. \right. \right. \\
 &\left. \left. - \exp\left(\frac{x}{\sqrt{D_x t}} \sqrt{\frac{V_x^2}{4D_x} + r_n^2 D_y + k - r} \operatorname{Erfc}\left\{\frac{x}{2\sqrt{D_x t}} \sqrt{\frac{V_x^2}{4D_x} + r_n^2 D_y + k - r} t\right\} \right) \right\}
 \end{aligned}$$

$$- \exp\left(\frac{-x}{\sqrt{D_x}} \sqrt{\left(\frac{V_n^2}{4D_x} + r_n^2 D_y + k - r\right)} \operatorname{Erfc}\left\{\frac{x}{2\sqrt{D_x t}} \sqrt{\left(\frac{V_x^2}{4D_x} + r_n^2 D_y + k - r\right)t}\right\}\right)]$$

where

$$L = \begin{cases} 1/2 & \text{if } n=0 \\ 1 & \text{if } n>0 \end{cases} ; P_n = \begin{cases} (y_2 - y_1)/w & \text{if } n=0 \\ [\sin(r_n y_2) - \sin(r_n y_1)]/r_n w & \text{if } n>0 \end{cases}$$

$$r_n = n\pi/w; n = 0, 1, 2, 3, \dots$$

Numerical Model

The developed model can be modified to a two-dimensional problem by making the top and bottom nodes equal. The aquifer had been discretized into 20, 50, 70, and 100 elements. The total nodes are 60, 132, 176, and 242 for different discretizations. The same input data are necessary in the numerical model. Figure 10 shows the model discretized into 70 elements.

Validation

The testing result will be compared to the center of the x direction and also compared at 20 and 50 day time periods. Figures 11 and 12 show the dimensionless result at different times. We can see that the result of 100 elements will move closer to the analytical solution. Figures 13 and 14 and Tables II and III show the error percentage between the analytical solution and model solution. The error

LENGTH OF AQUIFER	$L = 100$ FT.
THICKNESS OF AQUIFER	$H = 100$ FT.
WIDTH OF AQUIFER	$w = 70$ FT.
STRIP SOURCE	$Y_1 = 20$ FT.
	$Y_2 = 50$ FT.
NUMBER OF NODES	$N = 176$
NUMBER OF ELEMENT	$E = 70$

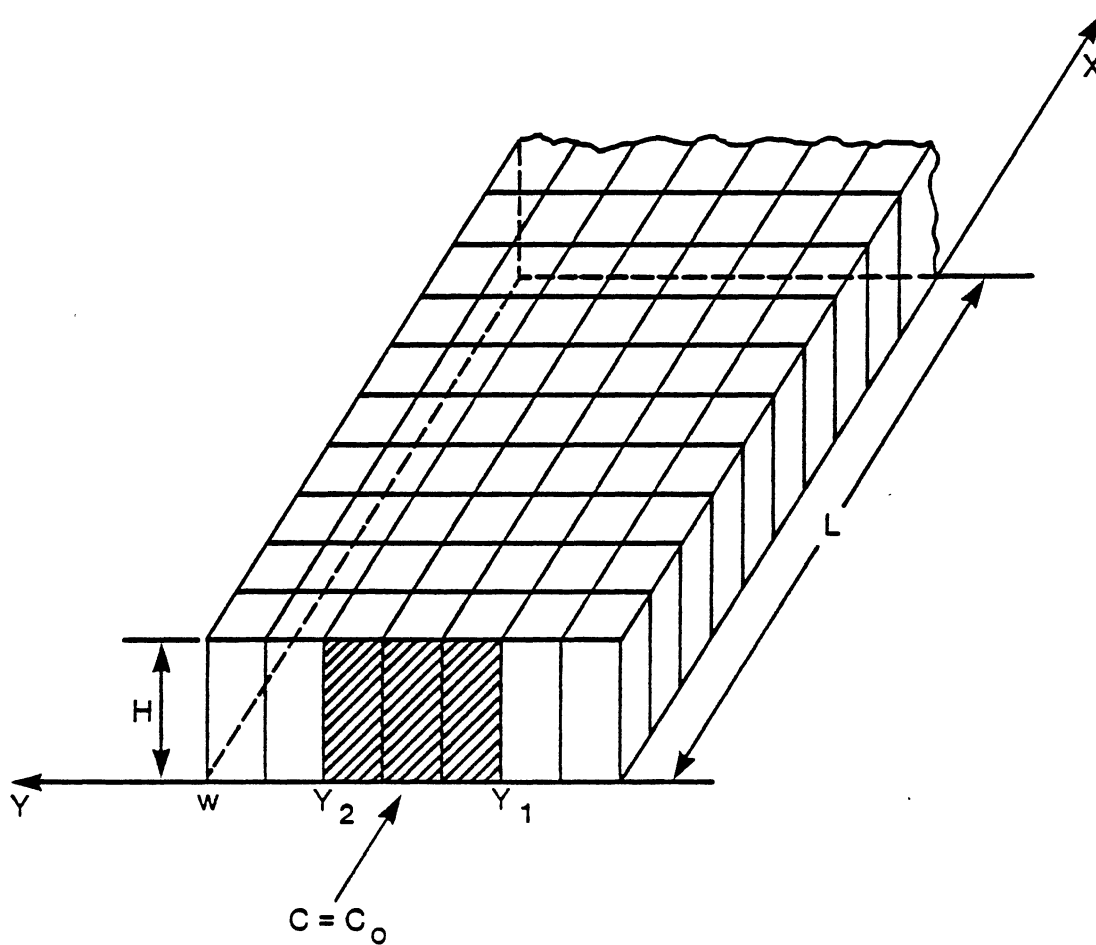


Figure 10. Model for One-Dimensional Testing

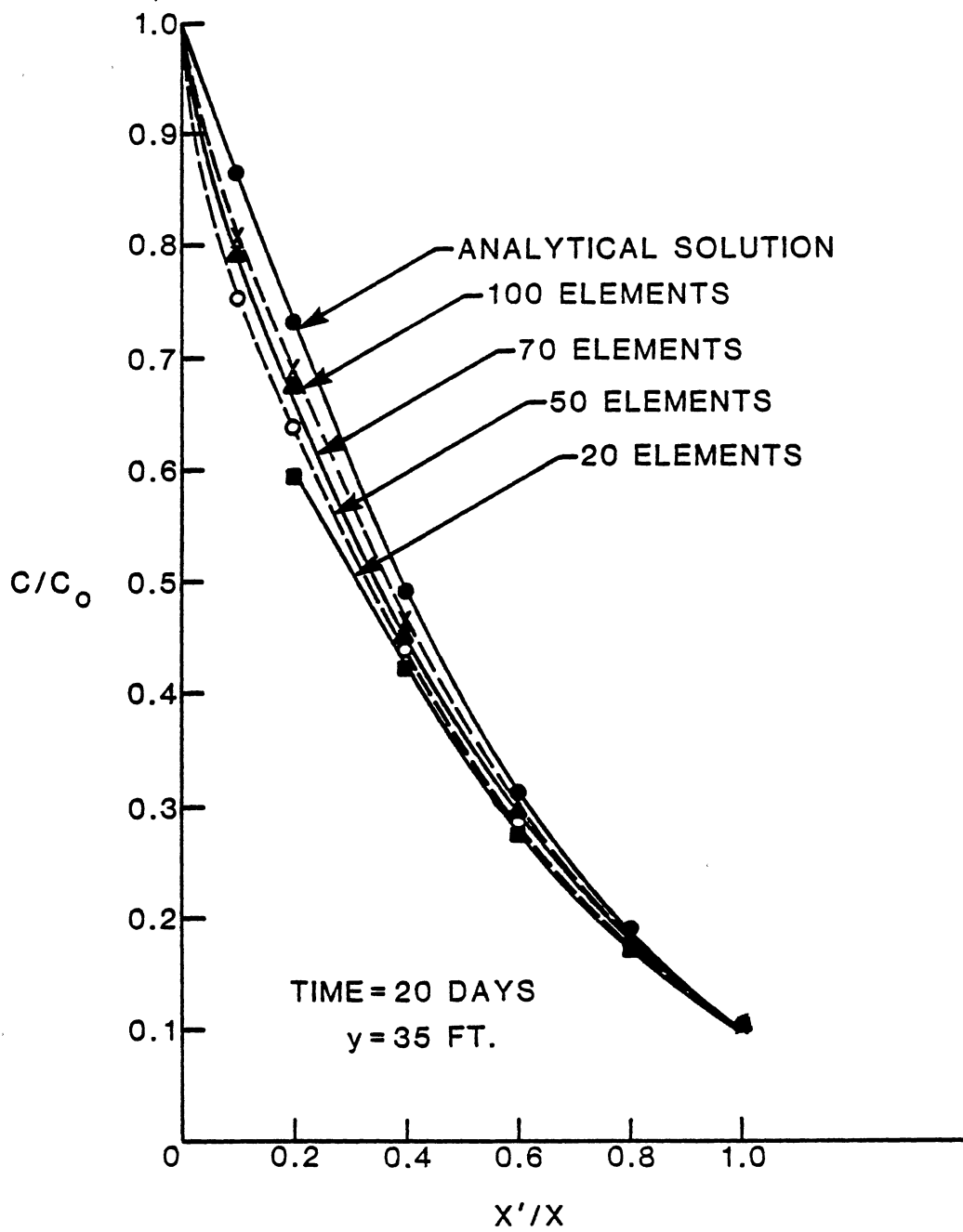


Figure 11. Comparison with Analytical Solution at Time = 20 Days

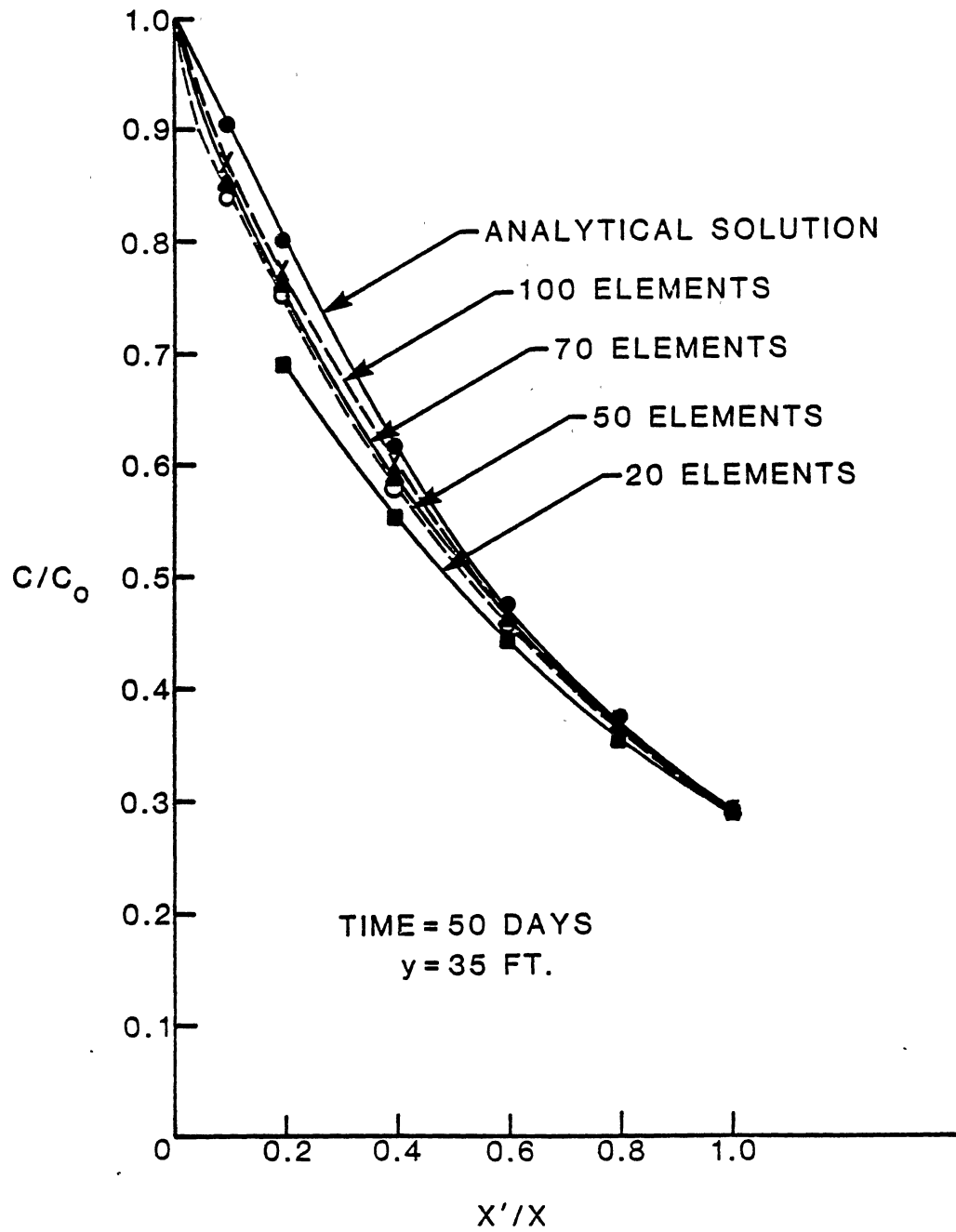


Figure 12. Comparison with Analytical Solution at Time = 50 Days

TABLE II
 COMPARISON OF ANALYTICAL SOLUTION WITH
 THE MODEL IN 20 DAYS
 Y = 35 FEET

Location From X Coordinate (Feet)	Analytical Solution Rel. Conc. ¹	100 Elements FEM ²	Percent Error	70 Elements FEM ²	Percent Error	50 Elements FEM ²	Percent Error	20 Elements FEM ²	Percent Error
10	0.867	0.805	7.2	0.796	8.2	0.754	13.0	NA ³	NA ³
20	0.731	0.690	5.6	0.679	7.1	0.643	12.1	0.595	18.6
40	0.491	0.450	3.3	0.465	5.3	0.446	9.2	0.421	14.3
60	0.311	0.305	1.9	0.300	3.5	0.284	8.7	0.276	11.2
80	0.186	0.187	0.0	0.183	1.7	0.173	7.5	0.171	8.5
100	0.104	0.105	0.0	0.103	0.9	0.102	1.9	0.101	2.8

- ¹ Relative Concentration
² Finite Element Method
³ Not Applicable

TABLE III
 COMPARISON OF ANALYTICAL SOLUTION WITH
 THE MODEL IN 50 DAYS
 Y = 35 FEET

Location From X Coordinate (Feet)	Analytical Solution Rel. Conc. ¹	100 Elements FEM ²	Percent Error	70 Elements FEM ²	Percent Error	50 Elements FEM ²	Percent Error	20 Elements FEM ²	Percent Error
10	0.902	0.873	3.2	0.856	5.0	0.845	6.3	NA	NA
20	0.800	0.776	3.0	0.763	4.6	0.758	5.2	0.693	12.4
40	0.616	0.602	2.3	0.590	3.5	0.581	4.0	0.554	10.0
60	0.477	0.468	1.9	0.465	2.5	0.462	3.2	0.446	6.5
80	0.372	0.373	0.0	0.364	2.1	0.362	2.6	0.359	3.4
100	0.289	0.294	0.0	0.292	0.0	0.290	0.0	0.290	0.0

¹ Relative Concentration

² Finite Element Method

³ Not Applicable

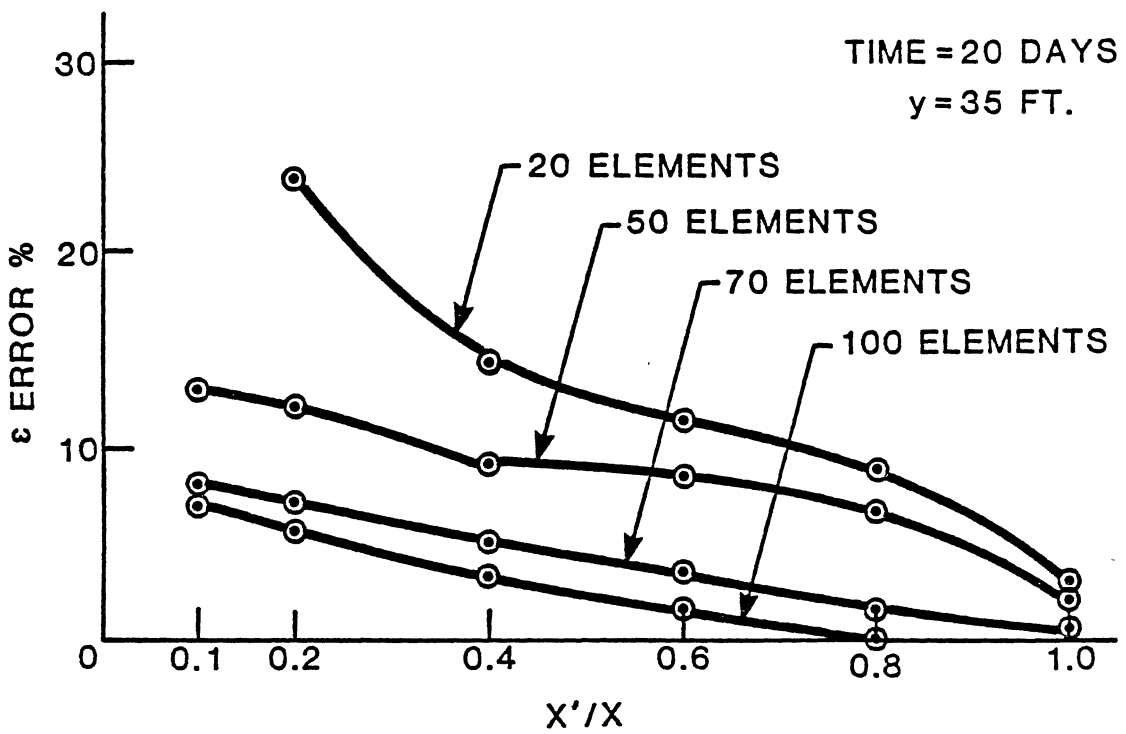


Figure 13. Error Percentage Versus x Distance at Time = 20 days

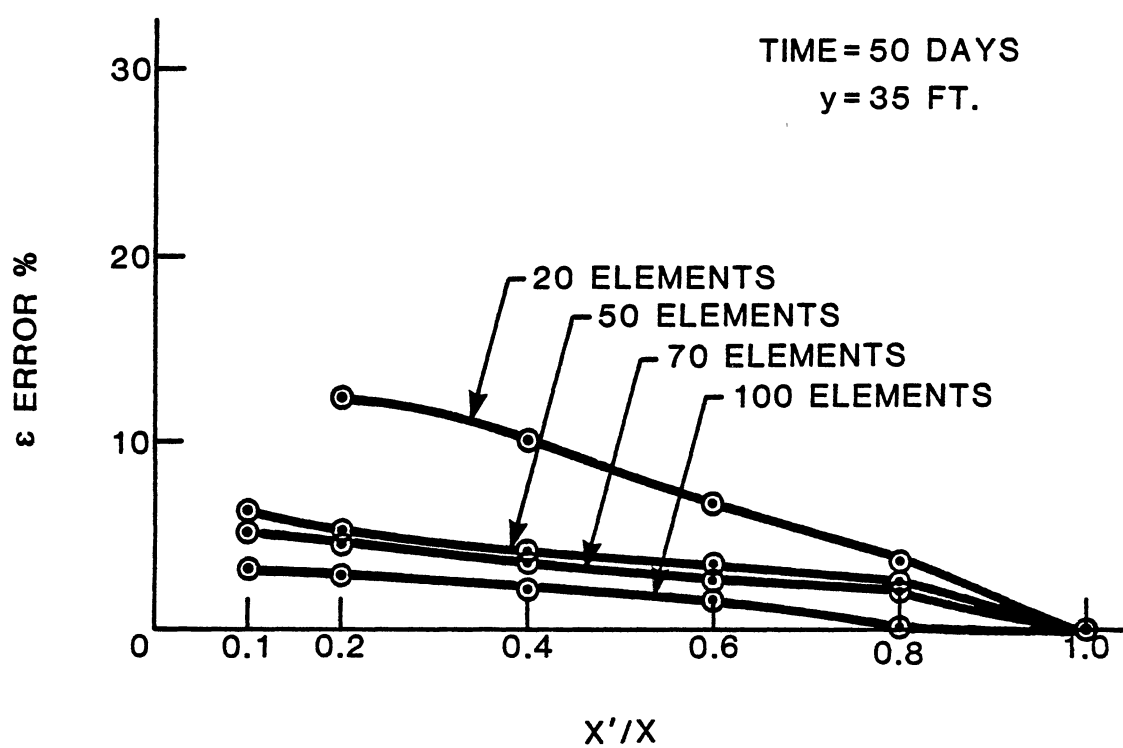


Figure 14. Error Percentage Versus x Distance at Time = 50 Days

varied from 0 to 7.2 percentage for 100 elements and 0 to 18.6 percentage for 20 elements.

Tables II and III show that with more elements and a longer period of time, the error will decrease. We also plot the figures to show the error versus the number of elements used (Figures 15 and 16). In this particular case, if we use more elements at a shorter distance from the strip source, we can get better results.

Thus, the developed model is compared against a two-dimensional analytical solution. By taking a slice in one direction, one-dimensional testing is accomplished using error analysis for different elements and times.

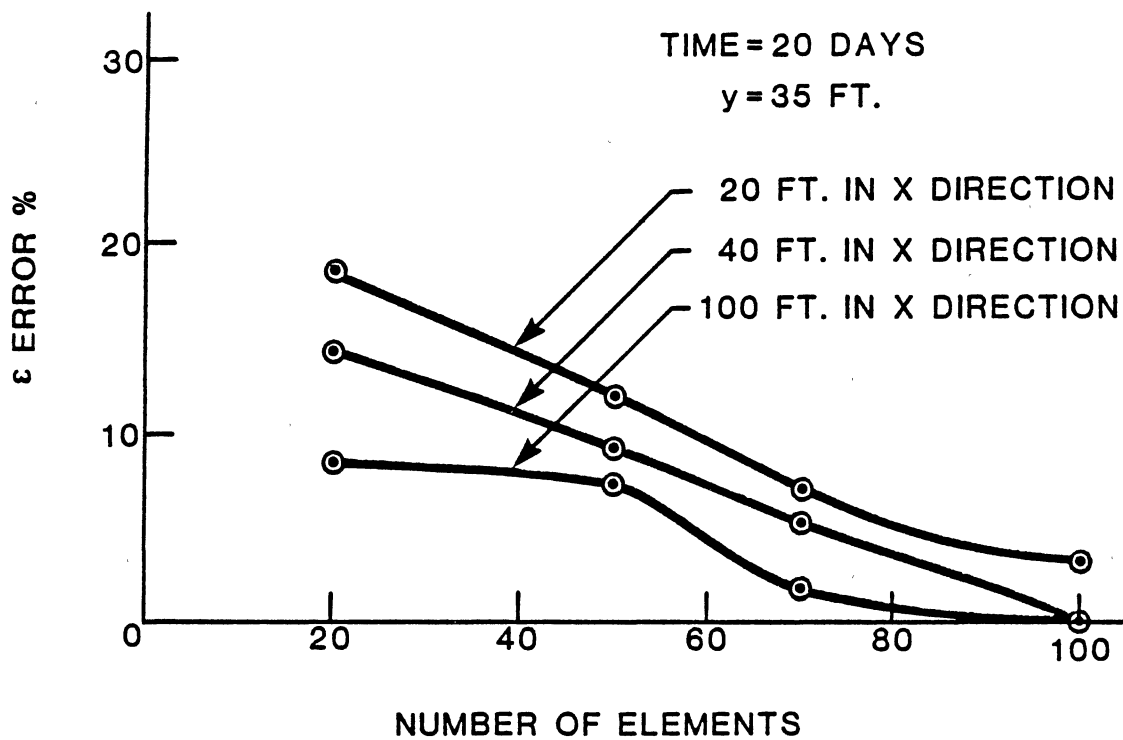


Figure 15. Error Percentage Versus No. of Elements
at Time = 20 Days

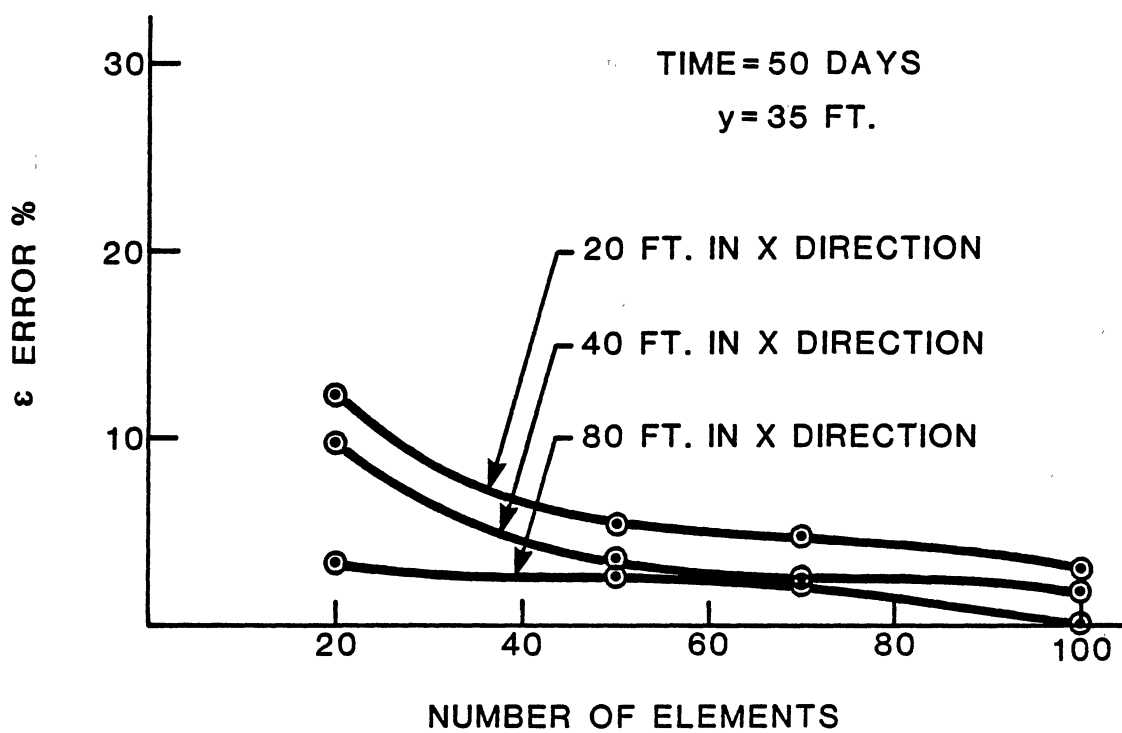


Figure 16. Error Percentage Versus No. of Elements
at Time = 50 Days

CHAPTER VIII

TWO-DIMENSIONAL VALIDATION

Example Problem

The analytical solution was presented by Cleary and Ung (1978) and the numerical model was that of Gureghian et al. (1980). The developed model also was compared with an analytical solution and a numerical model. The following equation represents the water quality model:

$$\frac{\partial C}{\partial t} = D_x \frac{\partial^2 C}{\partial x^2} + D_y \frac{\partial^2 C}{\partial y^2} - V_x \frac{\partial C}{\partial x} - V_y \frac{\partial C}{\partial y} - KC \quad (8.1)$$

The solute decay in accordance with first order kinetic K is zero in this case. The model will be subject to the following initial and boundary conditions.

$$C = C_1 \exp(-rt) \exp\left\{-\frac{(y - y_0)^2}{2s^2}\right\}; \quad x = 0$$

$$\frac{\partial C}{\partial y} \longrightarrow 0; \quad y \longrightarrow +\infty$$

$$\frac{\partial C}{\partial x} \longrightarrow 0; \quad x \longrightarrow +\infty \quad (8.2)$$

$$C = 0; \quad t = 0$$

where y_0 = centered location of the Gaussian Source (L)

C_1 = peak concentration at source (ML^{-3})

s = standard deviation of Gaussian distribution source

Analytical Solution

Gureghian et al. (1980) and Cleary and Ung (1978) gave the analytical solution as follows:

$$C(x,y,t) = \frac{C_1 X s}{2\sqrt{2\pi D_x}} \exp\left\{ \frac{V_x X}{2D_{xx}} - \frac{(y-y_0)^2}{2s^2} + \frac{s^2}{2} \left(\frac{V_y}{2D_{yy}} + \frac{(y-y_0)^2}{s^2} \right)^2 \right\}$$

$$\cdot \int_0^t \frac{\exp\left\{ \left(\frac{V_x^2}{4D_{xx}} - \frac{V_y^2}{4D_{yy}} \right) t \right\}}{t^{3/2} \left(D_{yy} t + \frac{s^2}{2} \right)^{1/2}} dt$$

$$\cdot \exp\left\{ \frac{-x^2}{4D_{xx}t} - \frac{\left(\frac{s^2 V_y}{2D_{yy}} + (y-y_0)^2 \right)}{4(D_{xx} + 0.5s^2)} \right\} dt \quad (8.3)$$

where y direction is infinite, $-\infty < y < \infty$, and

x direction is semi-infinite, $0 \leq x < \infty$

The peak concentration at source $C_1 = 1.0$, the centered location is 400 feet, and the standard deviation is 300.

Numerical Model

In this study, the size of the aquifer is 1800 by 900 feet and the thickness of the aquifer is 10 feet. The grids

used to compare the analytical solution include 81 elements, each of which measure 200 by 100 feet. Figure 17 shows the model with Gaussian distribution source.

In this test, Peclet numbers 10 and 500 are selected to do the comparison. In $P_e = V L/D$, V is the velocity, L is the characteristic length (element size), and D is the dispersion coefficient. In this study the simulation time is 175 days and the time increment is 25 days. The velocity in x direction is 4ft/day and in y direction is 1ft/day for both cases. For a Peclet number equal to 10, the dispersion coefficient is 80ft^2 in x direction and 10ft^2 in y direction. Thus, $P_e = 4 \times 200 / 80$ or $P_e = 1 \times 100 / 10$. For a Peclet equal to 500, dispersion coefficients in x and y directions are $1.6\text{ft}^2/\text{day}$ and $0.2\text{ft}^2/\text{day}$ respectively, $P_e = 4 \times 200 / 1.6$ or $1 \times 100 / 0.2$.

Validation

Figures 18 and 19 show the computed concentrations 0.2, 0.5, and 0.8 given by the analytical solution and the finite element method. In both cases, $P_e = 10$ and $P_e = 500$. At higher concentrations, the Gureghian (1981) and the developed model are close to the analytical solution, and at lower concentrations, both show an overshoot. For $P_e = 10$, when the model's solution versus the analytical solution, the error varied from 0% to 24%. When Gureghian's (1981) solution versus analytical solution, the error varied from 0% to 38%. The two numerical model solution's errors varied

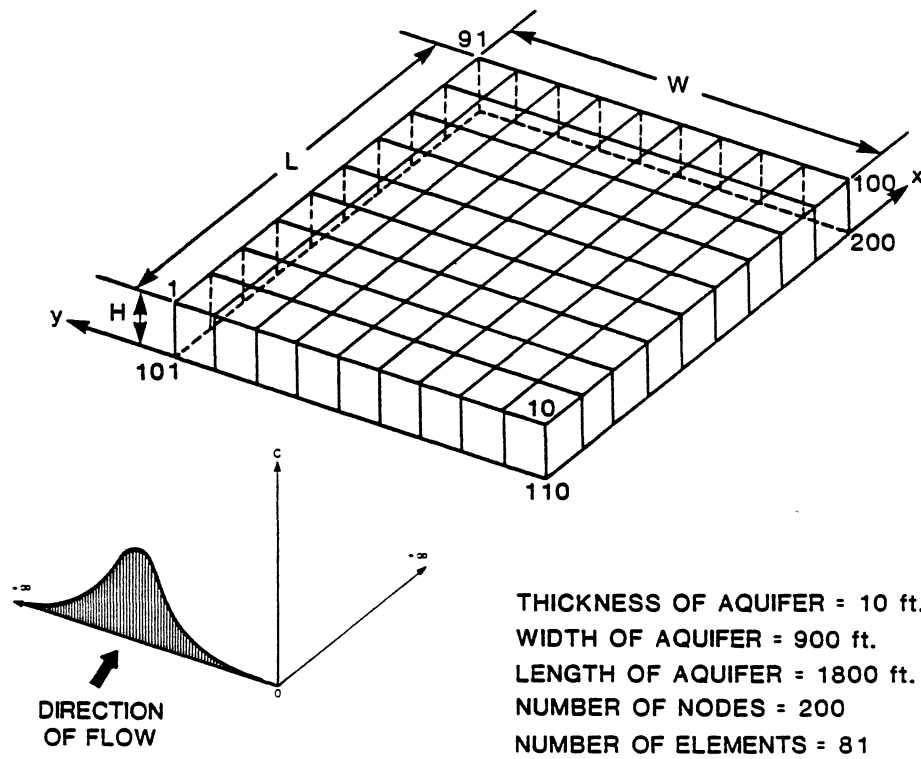


Figure 17. Model with Gaussian Distribution Source

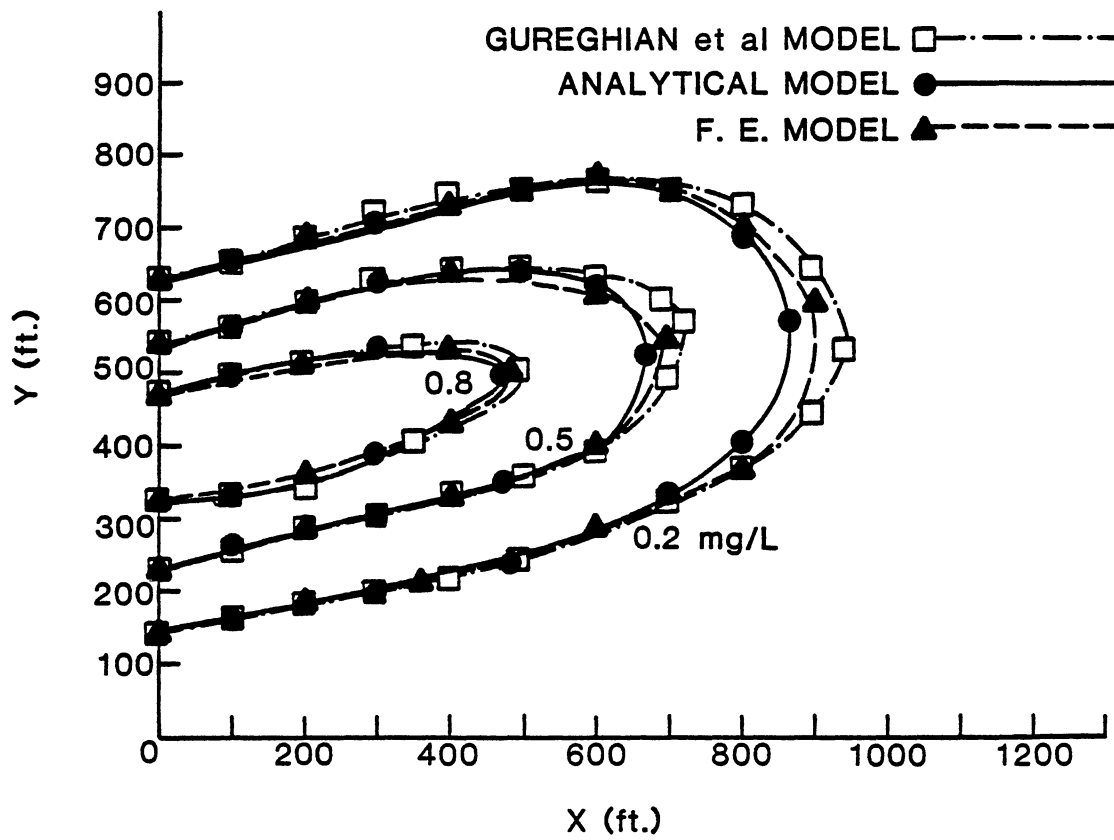


Figure 18. Concentration Variations for $P_e = 10$

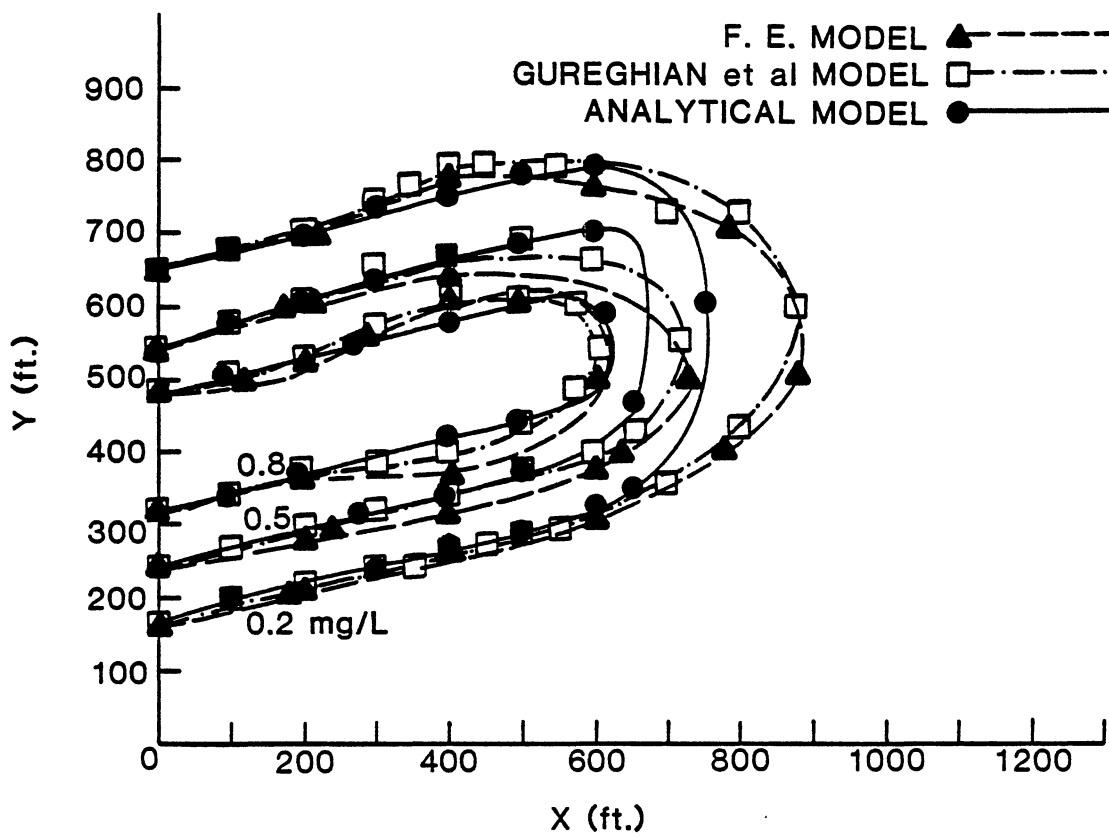


Figure 19. Concentration Variations for $P_e = 500$

from 0% to 12.55%. For $Pe = 500$, the error increased. When the analytical solution versus Gureghian's model's solution, error varied from 0% to 57.50%. When the developed model solution was compared with the analytical solution, the error varied from 0% to 56%. The two numerical model solution's errors varied only 1%. The error analysis is presented for the two-dimensional case. The error varies between 0% to 38% and 0% to 57.5% for the two solutions for only one node. For other nodes, the error for the two solutions varies between 0% to 20% and 0% to 22%. Thus, the developed model is tested against a two-dimensional solution and the numerical solution.

The numerical experiments in this study show that errors are larger for higher concentrations. For relatively low concentrations, errors become significant from 24% for low Peclet numbers (10) to 56% for high Peclet numbers (500). This perhaps caused the overshoot. Thus, the Peclet numbers should be kept relatively low where the concentrations are relatively small because the Peclet number is proportional to element size or length characteristics. The overshoot could be minimized by keeping the element size small in areas of low concentration.

CHAPTER IX

THREE-DIMENSIONAL VALIDATION

Example Problem

Not very many numerical solutions for three-dimensional testing have been developed. The AT123D Program developed by Yeh (1981) has been used to compare with the model developed in this study. He computed the spatio-temporal distribution of waste in the aquifer system. In his search for a closed-form solution, the application of Green's function is utilized to the optimum advantage. The following equation is established by Duguid and Reeves (1976) and Yeh (1981).

$$R_d \frac{\partial n_e C}{\partial t} = \nabla \cdot (n_e D \nabla C) - \nabla \cdot C \mathbf{V} + \dot{M} - K n_e R_d C - \lambda n_e R_d C \quad (9.1)$$

$$S = K_d C \quad (9.2)$$

where \dot{M} = rate of source ($ML^{-3}T^{-1}$)

K = distribution coefficient

ρ = bulk density of the media (ML^{-3})

$$R_d = 1 + \frac{\rho K_d}{n_e} \quad \text{retardation factor}$$

The other terms are the same as equation (4.1), thus allowing for comparison with the developed model. All the parameters should divide by the retardation factor. In this

testing, velocity is $0.48 \times 10^{-5} \text{m}^2/\text{hr}$; dispersion coefficients are $7.439 \times 10^{-5} \text{m}^2/\text{hr}$, $1.24 \times 10^{-4} \text{m}^2/\text{hr}$, and $1.240 \times 10^{-4} \text{m}^2/\text{hr}$ in x, y, z directions respectively. The retardation decay constant is .00000283 curie/hr. The two cases studied are the point source in x, y, z directions (0, 10,1) and the line source in x, y, z directions. Both cases are finite width and finite depth (Figure 20).

Analytical Solution

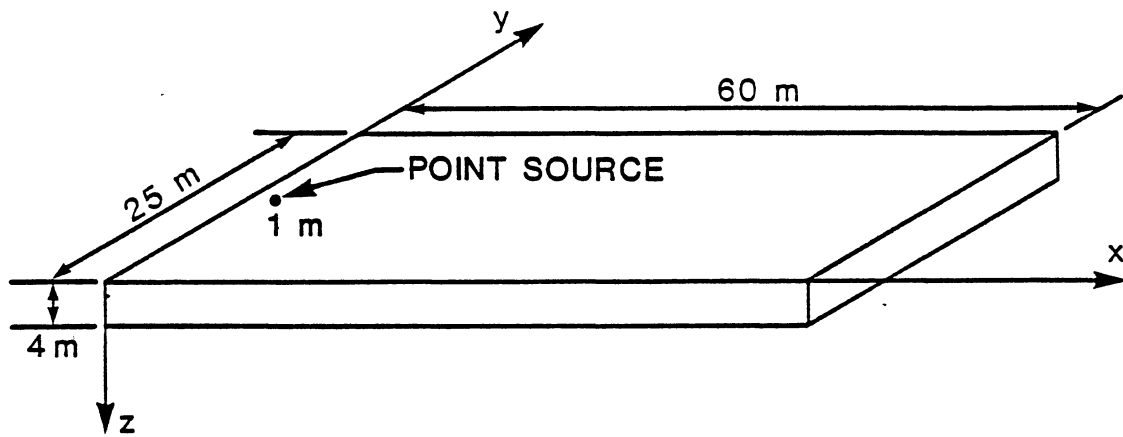
Various mathematical techniques can be applied to finding the analytical solutions. In the AT123D program, Green's function (Yeh, 1981) is used.

The initial condition is described as:

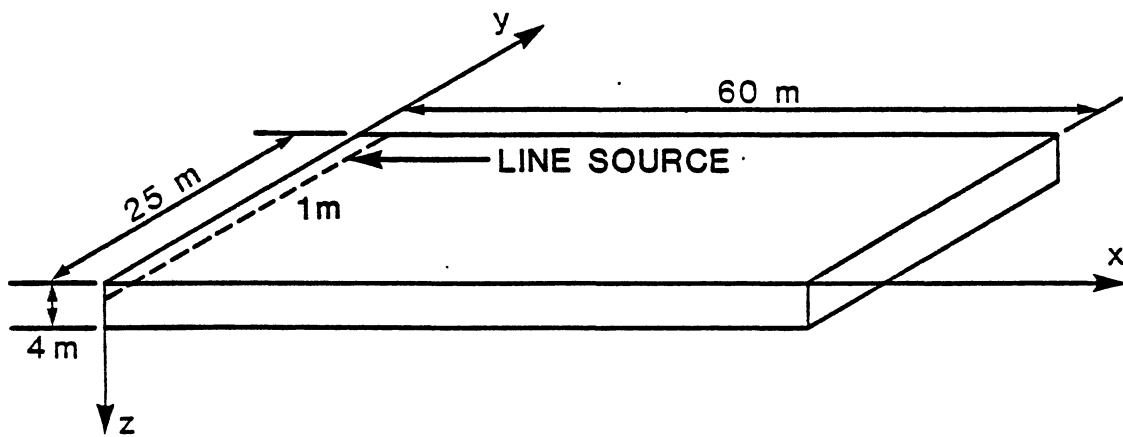
$$C = C_0(x,y,z,0), \text{ at } t = 0 \text{ and in } R \quad (9.3)$$

where C_0 is a given function of spatial coordinates x, y, and z; R is a region bounded by the curve, and $B(x,y,z) = 0$ as shown in Figure 21. This C_0 may also be obtained by simulating the steady-state version of equation (9.1) with steady boundary conditions and groundwater flow field. Three types of boundary conditions may be specified depending on the physical constraints. The first type of boundary condition is the Dirichlet, and the concentration prescribed is

$$C = C_1(x,y,z,t) \text{ on } B_1 \quad (9.4)$$

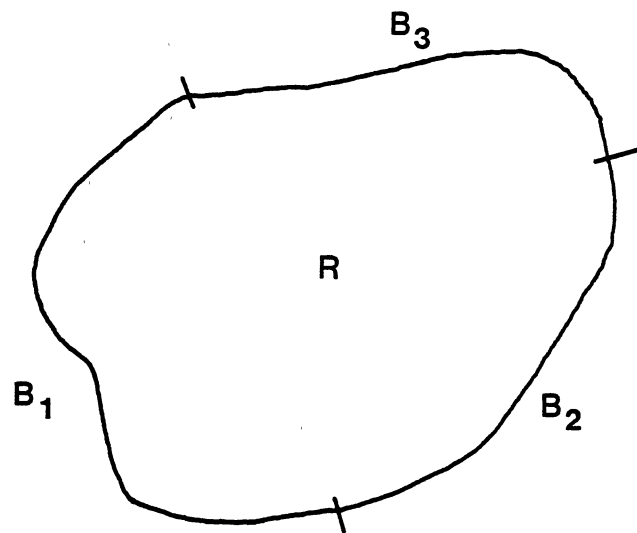


CASE 1 POINT SOURCE (0, 10, 1)



**CASE 2 LINE SOURCE $(x_s, y_s, z_s) = (0, 0, 1)$
 $(x_s, y_s, z_s) = (0, 25, 1)$**

Figure 20. Schematization of Source Dimensions and the Medium



$$B = B_1 \cup B_2 \cup B_3$$

Figure 21. Spatial Boundary of Region R

where B_1 is a portion of B and C_1 is a given function of time and the location on B_1 . The second type of boundary condition and the normal gradient of the concentration is described as

$$-n_e D \cdot \nabla C \cdot \vec{n} = q_2(x, y, z, t) \text{ on } B_2 \quad (9.5)$$

where \vec{n} is the directional cosine of the outward unit vector normal to the B_2 portion of the curve B .

The third type is the Cauchy boundary condition. It is applied to the flow-through boundaries with inflows into the region and is written as

$$-(n_e D \cdot \nabla C - VC) \vec{n} = q_3(x, y, z, t) \text{ on } B_3 \quad (9.6)$$

where q_3 is a given function of time and the points (x, y, z) are on the B_3 portion of B .

The solution of equation (9.1), subject to initial and boundary conditions, is

$$\begin{aligned} C(x, y, z, t) = & \int_0^t \int_R \frac{\dot{M}}{n_e R_d} G dR_0 d\tau + \int_R (GC_0)_{\tau=0} dR \\ & - \int_0^t \int_{B_2} D \cdot \nabla G \cdot \vec{n} C_1 dB_0 d\tau - \int_0^t \int_{B_2} \frac{Gq_2}{n_e R_d} dB_0 d\tau \\ & - \int_0^t \int_{B_3} \frac{Gq_2}{n_e R_d} dB_0 d\tau \end{aligned} \quad (9.7)$$

If $G(x, y, z; \alpha, \beta, r)$ satisfy the following conditions:

$$\lim_{t \rightarrow \tau} G = \delta(x-\alpha)\delta(y-\beta)\delta(z-r) \quad (9.8)$$

$$G = 0 \quad \text{for } t < \tau \quad (9.9)$$

$$G = 0 \quad \text{on } B_1 \quad (9.10)$$

$$(n_e D \cdot \nabla_0 G + \vec{V}G) \cdot \vec{n} = 0 \quad \text{on } B_2 \quad (9.11)$$

$$n_e D \cdot \nabla_0 G \cdot \vec{n} = 0 \quad \text{on } B_3 \quad (9.12)$$

$$\begin{aligned} -\partial G / \partial t &= \nabla_0 \cdot (K \cdot \nabla_0 G) + V \cdot \nabla G \\ &- (K/R_d + \lambda)G \quad \text{for } t > \tau \end{aligned} \quad (9.13)$$

where ∇_0 : Del operator with respect to α, β, r . The subscript '0' in equations (9.7) through (9.13) refers to the operation with respect to α, β, r rather than x, y, z . G is Green's function. If G is known, the problem is solved. It can be shown with simple geometry such as a separable coordinate system. Green's function may be expressed as

$$G(x, y, z, t; \alpha, \beta, r, \tau) = G_1(x, t; \alpha, \tau) G_2(y, t; \beta, \tau) G_3(z, t; r, \tau) \quad (9.14)$$

The derivation of G_1, G_2, G_3 can be found elsewhere (Fried, 1975) and Yeh and Tsai, 1976). If we further assume that no waste can flow across the impervious boundaries and the flows through open boundaries are located at infinity, then we obtain $C = 0, q_2 = 0, \text{ and } q_3 = 0$. For a continuous source, equation (9.7) reduces to

$$C(x,y,z,t) = \int_0^t \frac{\dot{M}}{n_e R_d} F_{ijk}(x,y,z,t;\tau) d\tau; \quad t < T \quad (9.15)$$

and

$$C(x,y,z,t) = \int_0^T \frac{\dot{M}}{n_e R_d} F_{ijk}(x,y,z,t;\tau) d\tau; \quad t > T \quad (9.16)$$

for F_{ijk} is the integral of Green's function (G) over the source space and T is the duration of waste release. F_{ijk} is given by

$$F_{ijk} = X_i Y_j Z_k \quad (9.17)$$

where $i = 1$ or 2 , $j = 1$ or 2 , and $k = 1$ or 2 , functions X_i , Y_j , and Z_k are given as follows.

For a point source:

In X direction:

$$X_1 = \frac{1}{\sqrt{4\pi D_{xx}(t-\tau)}} \exp\left[-\frac{\{(x-x_s)-V(t-\tau)\}^2}{4D_{xx}(t-\tau)} - \left(\frac{K}{R_d} + \lambda\right)(t-\tau)\right] \quad (9.18)$$

In Y direction:

$$Y_1 = \frac{1}{B} + \frac{2}{B} \sum_{i=1}^{\infty} \cos\left(\frac{i\pi y}{B}\right) \cdot \cos\left(\frac{i\pi y_s}{B}\right) \cdot \exp\left\{-\left(\frac{i\pi^2}{B}\right) D_{yy}(t-\tau)\right\} \quad (9.19)$$

In Z direction:

$$Z_1 = \sum_{i=1}^{\infty} \psi_i(z) \psi_i(z_s) \cdot \exp\{-k_i^2 K_{zz}(t-\tau)\} \quad (9.20)$$

For finite width and line source:

In X direction:

$$X_2 = 0.5 \left[\operatorname{erf} \left\{ \frac{x-L_1-V(t-\tau)}{\sqrt{4D_{XX}(t-\tau)}} \right\} - \operatorname{erf} \left\{ \frac{x-L_2-V(t-\tau)}{\sqrt{4D_{ZZ}(t-\tau)}} \right\} \right] \\ \cdot \exp \left\{ - \left(\frac{D}{R_d} + \lambda \right) (t-\tau) \right\} \quad (9.21)$$

In Y direction:

$$Y_2 = \frac{B_2-B_1}{B} + \frac{2}{B} \sum_{i=1}^{\infty} \cos \left(\frac{i\pi y}{B} \right) \cdot \frac{B}{if} \left\{ \sin \left(\frac{i\pi B_2}{B} \right) \sin \left(\frac{i\pi B_1}{B} \right) \right\} \\ \exp \left\{ - \left(\frac{i\pi^2}{3} \right) D_{yy}(t-\tau) \right\} \quad (9.22)$$

In Z direction:

$$Z_2 = \sum_{i=1}^{\infty} \Psi_i(Z) \left(\frac{a_i}{K_i} \right) \{ \sin(k_i H_2) - \sin(k_i H_1) \} \\ \cdot \exp \left\{ -K_i^2 2D_{ZZ}(t-\tau) \right\} \quad (9.23)$$

where B and H are the width and depth of the aquifer, L_1 , B_1 , H_1 , and L_2 , B_2 , and H_2 are the beginning x, y, z and ending x, y, z coordinates of the source; x_s , y_s , and z_s are the x, y, z coordinates of the point sources.

$$\Psi_1(z) = a_i \cos(k_i z) \quad (9.24)$$

and

$$a = 2/H \quad (9.25)$$

Numerical Model

The developed model uses the same parameters as those used in the example problem. The thickness of the aquifer is 4m, the width is 25m, and the length is 60m. The aquifer shown in Figure 22 is discretized into 90 elements and consists of 168 nodes.

In Case 1, the point source study, the concentration distribution of the continuous release of radioactive waste has a rate of 1.0 Ci/hr and lasts for 240 hours. A point source configuration is assumed for the radioactive waste, which is discharged into a three-dimensional porous medium of size 60 x 25 x 4 meters. Initially, no radioactivity is present in the porous medium. Case 2 has the same input parameters as Case 1, but uses a line source instead of a point source at a depth of 1 meter in the yz plane (Figure 23).

Validation

The error analyses of different nodes and times for both cases are listed in Tables IV to XXXIV (Appendix G). Figure 23 shows the diagram of the error analysis at plane 1, plane 2, and plane 3, located at 5m, 10m, and 20m, with depth at 1m, 2m, and 4m. Figures 24 through 41 show the error with distance in x direction for vertical planes

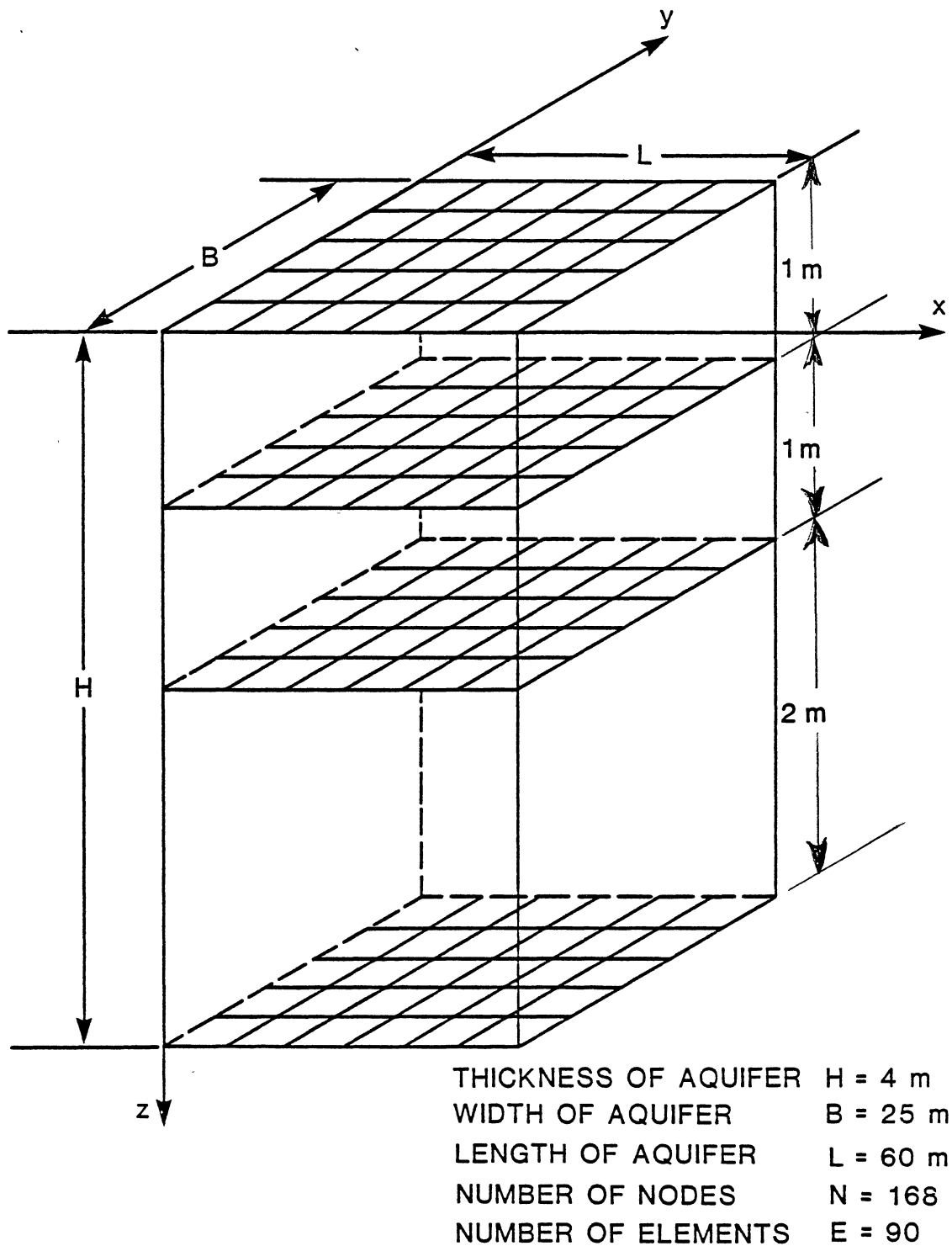


Figure 22. Three-Dimensional Testing Model

CASE 1 AND CASE 2

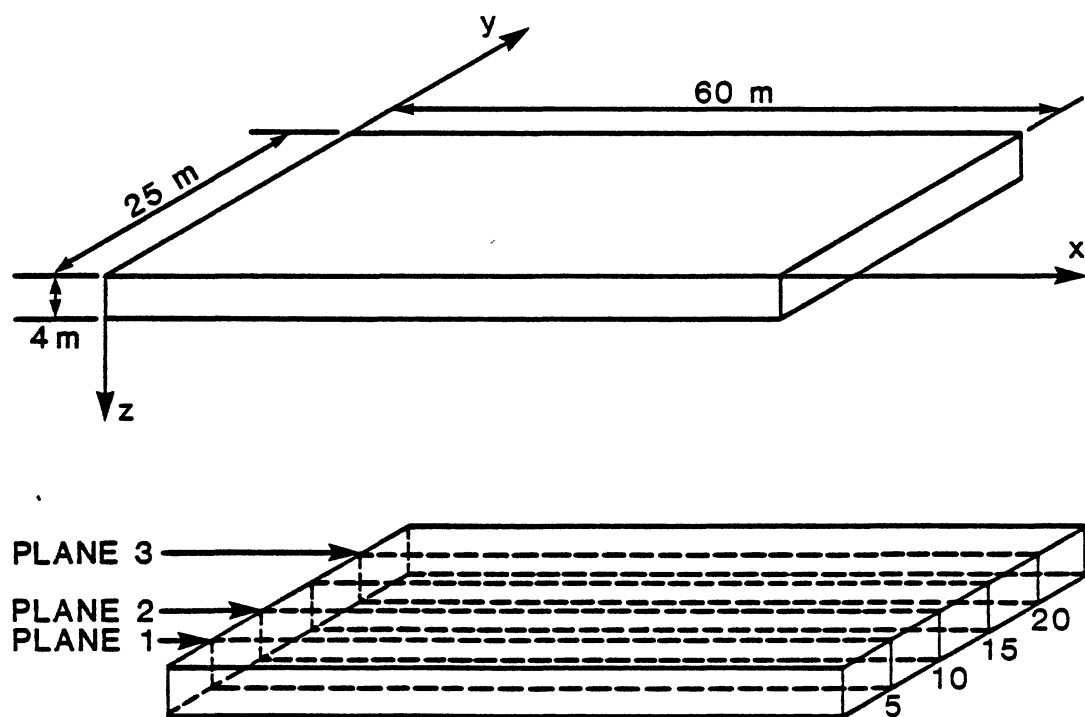


Figure 23. Schematic Diagram for Error Analysis and Comparison of Three-Dimensional and Analytical Solutions

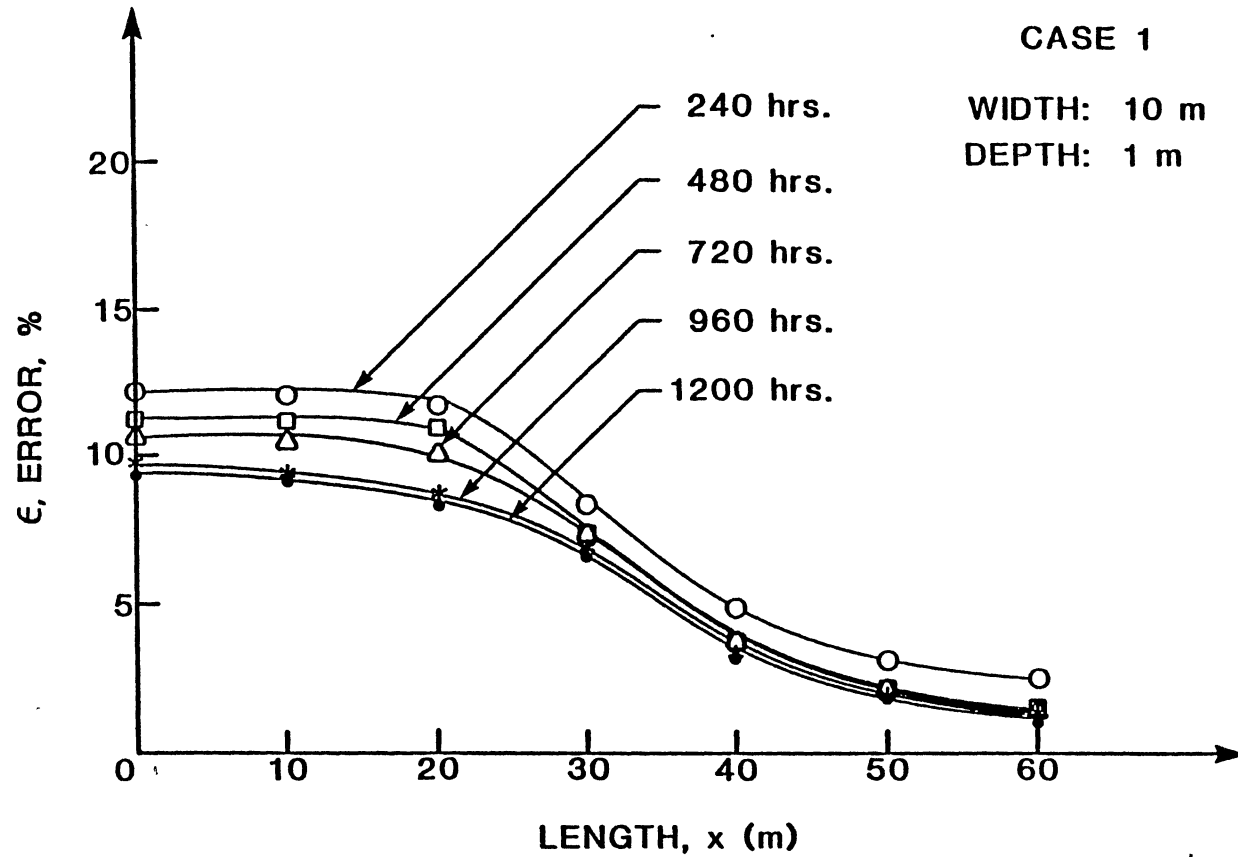


Figure 24. Error with Distance in x Direction for a Vertical Plane of 10 and 1 Meters in y and z Directions

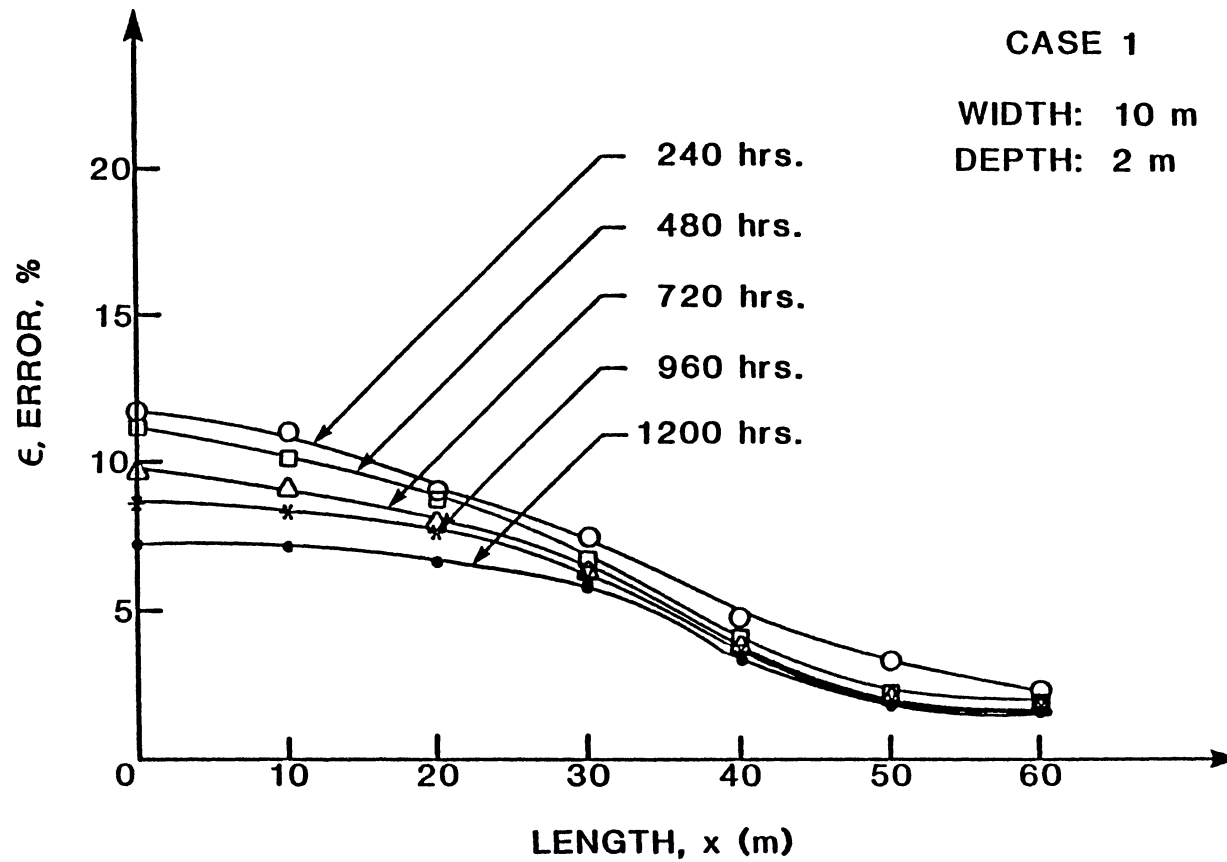


Figure 25. Error with Distance in x Direction for a Vertical Plane of 10 and 2 Meters in y and z Directions

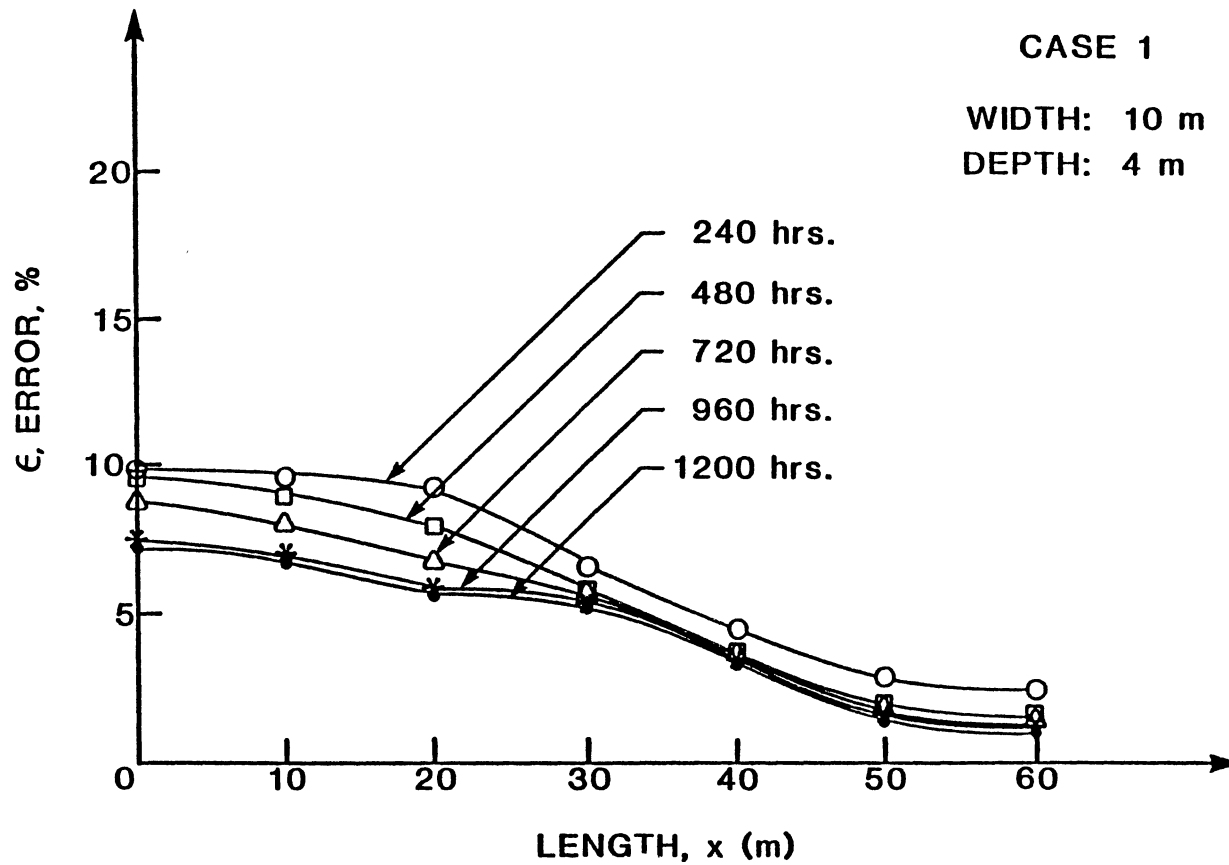


Figure 26. Error with Distance in x Direction for a Vertical Plane of 10 and 4 Meters in y and z Directions

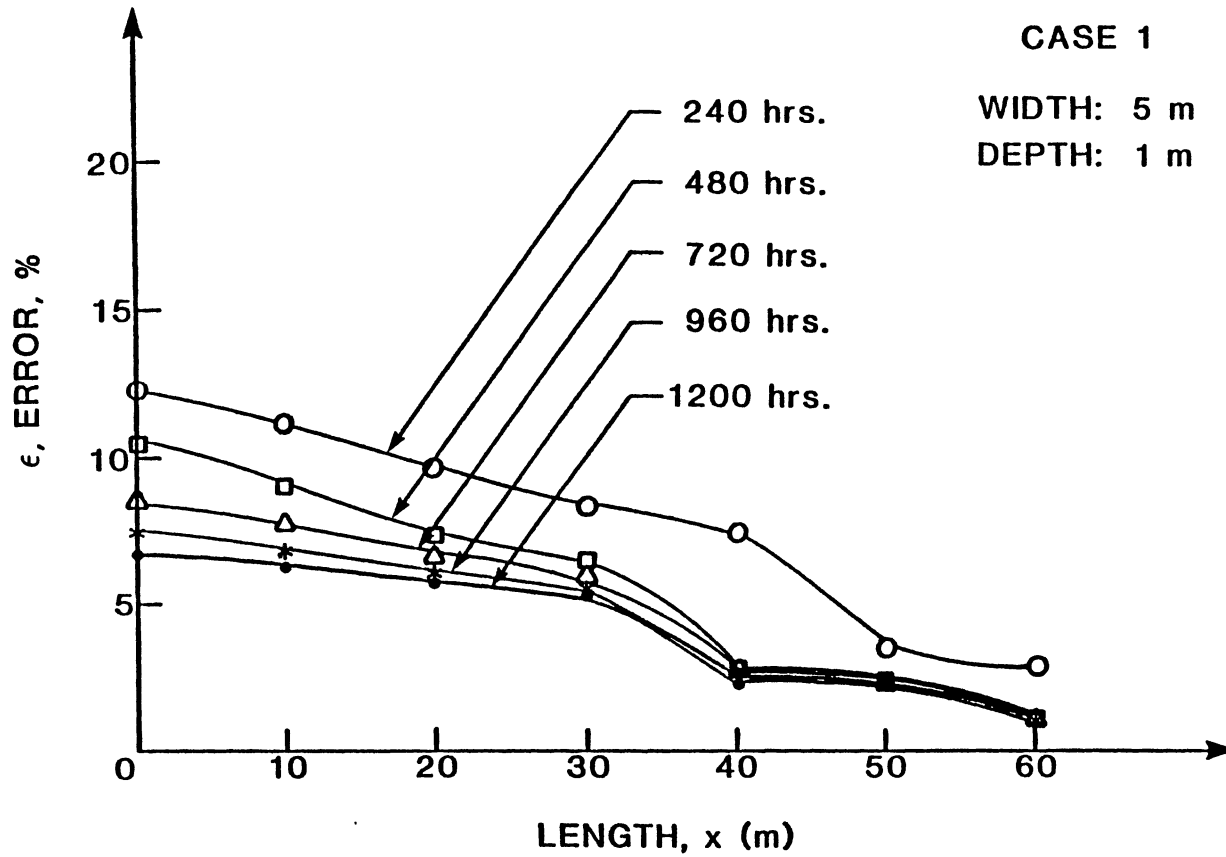


Figure 27. Error with Distance in x Direction for a Vertical Plane of 5 and 1 Meters in y and z Directions

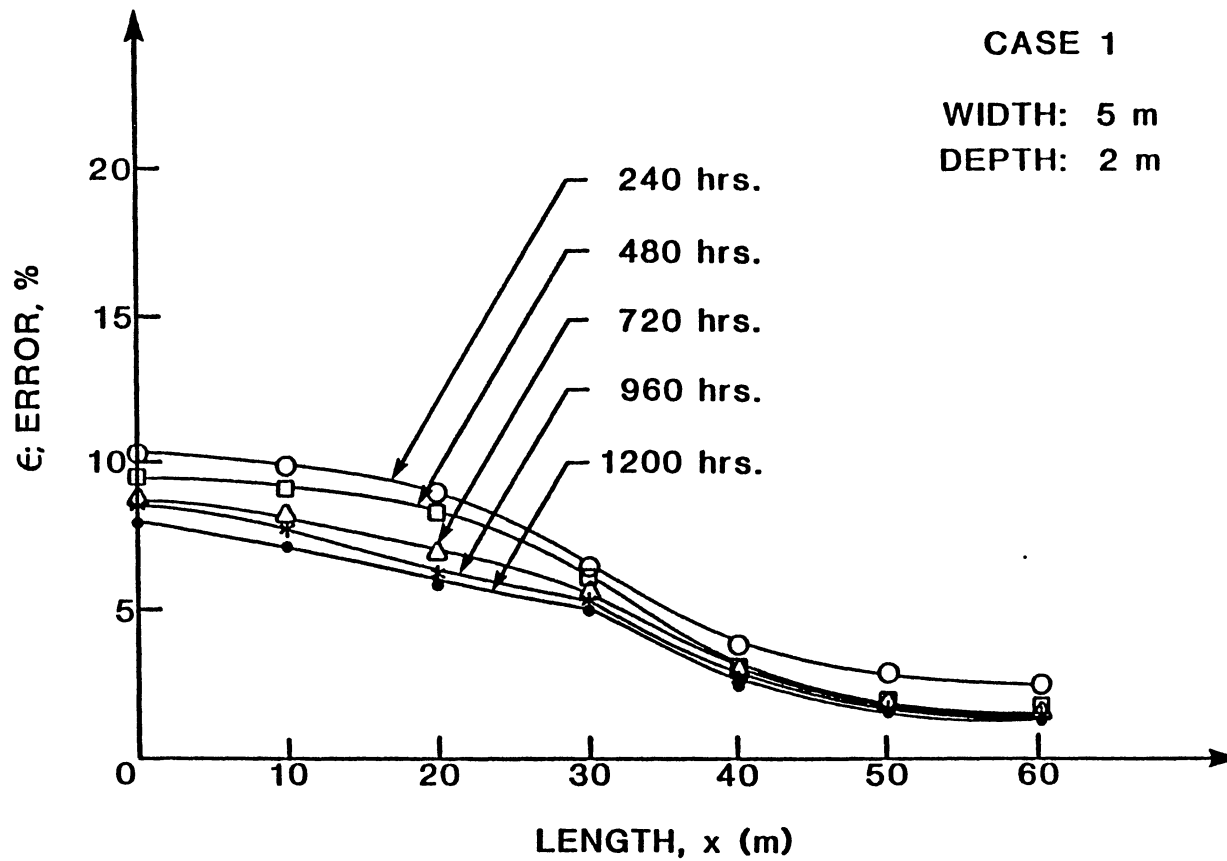


Figure 28. Error with Distance in x Direction for a Vertical Plane of 5 and 2 Meters in y and z Directions

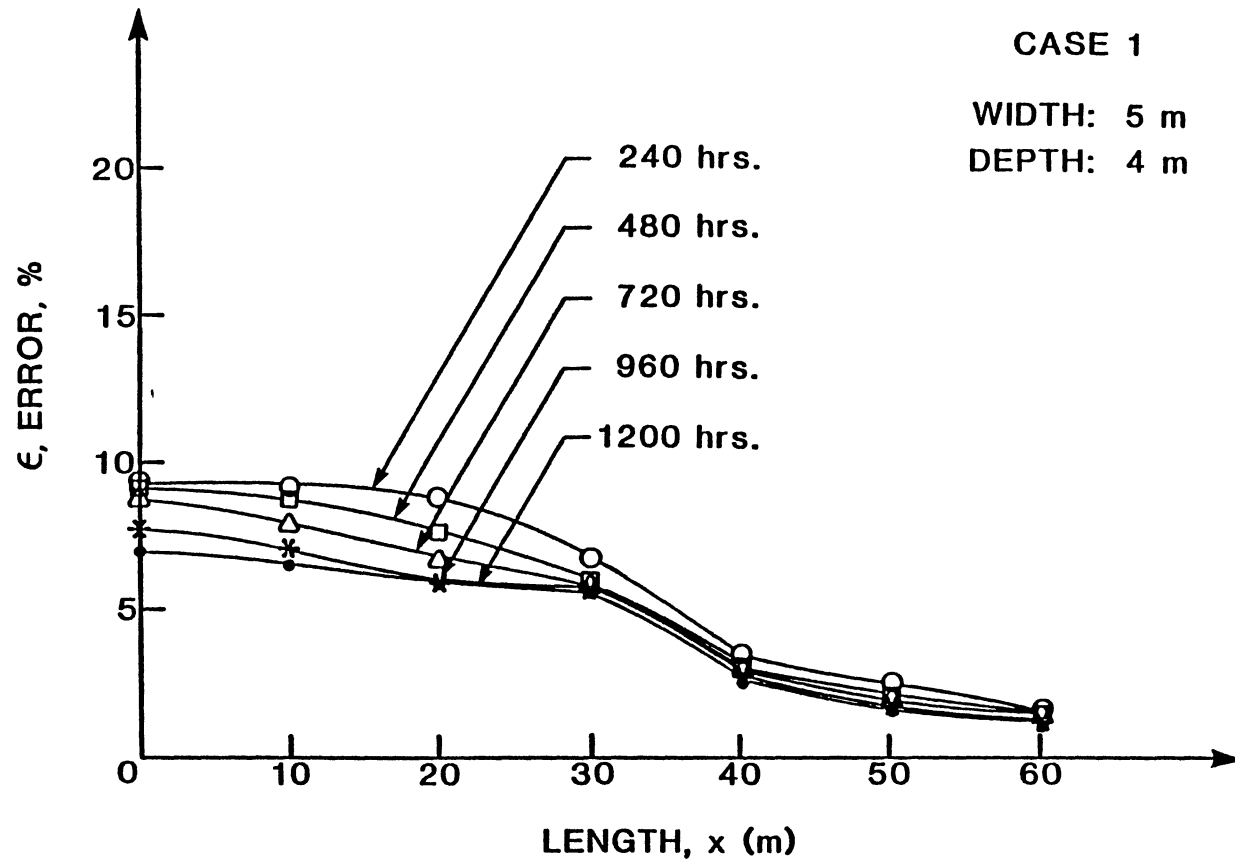


Figure 29. Error with Distance in x Direction for a Vertical Plane of 5 and 4 Meters in y and z Directions

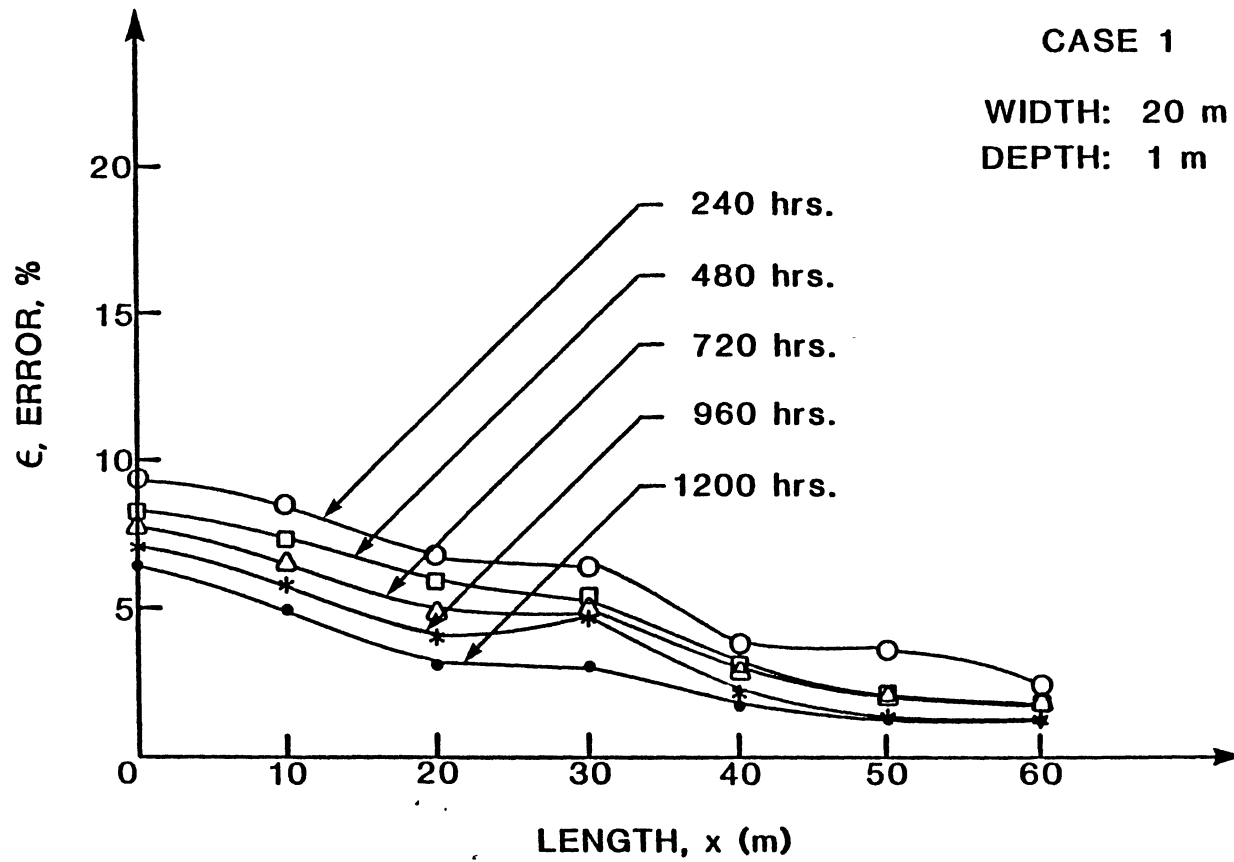


Figure 30. Error with Distance in x Direction for a Vertical Plane of 20 and 1 Meters in y and z Directions

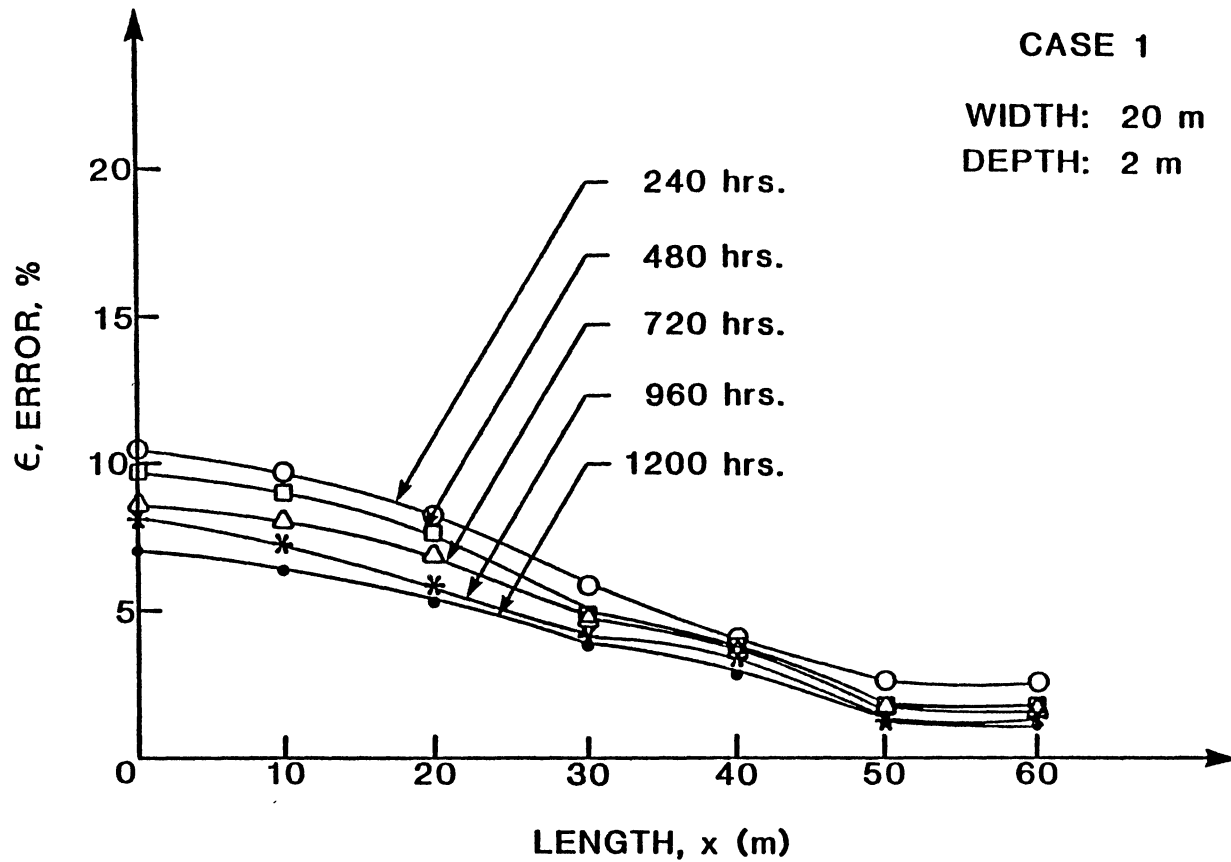


Figure 31. Error with Distance in x Direction for a Vertical Plane of 20 and 2 Meters in y and z Directions

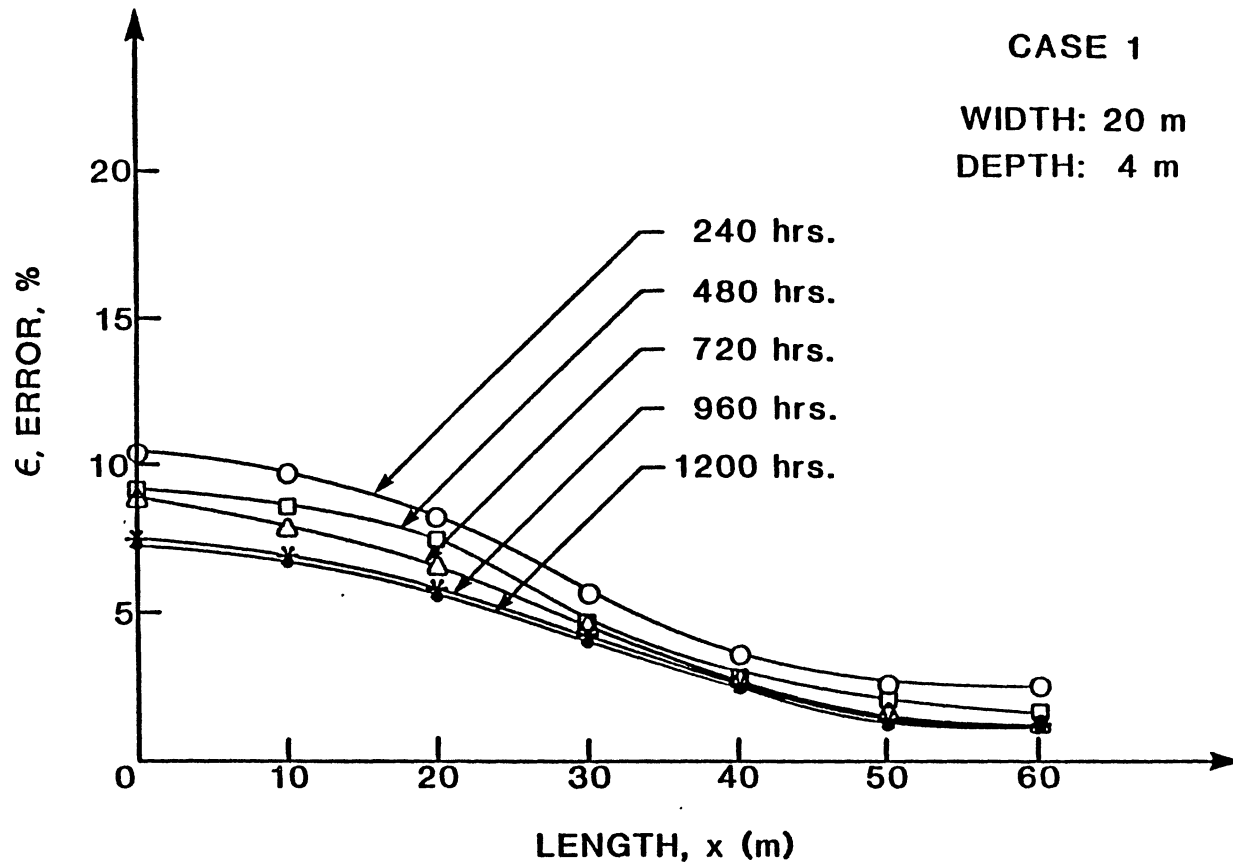


Figure 32. Error with Distance in x Direction for a Vertical Plane of 20 and 4 Meters in y and z Directions

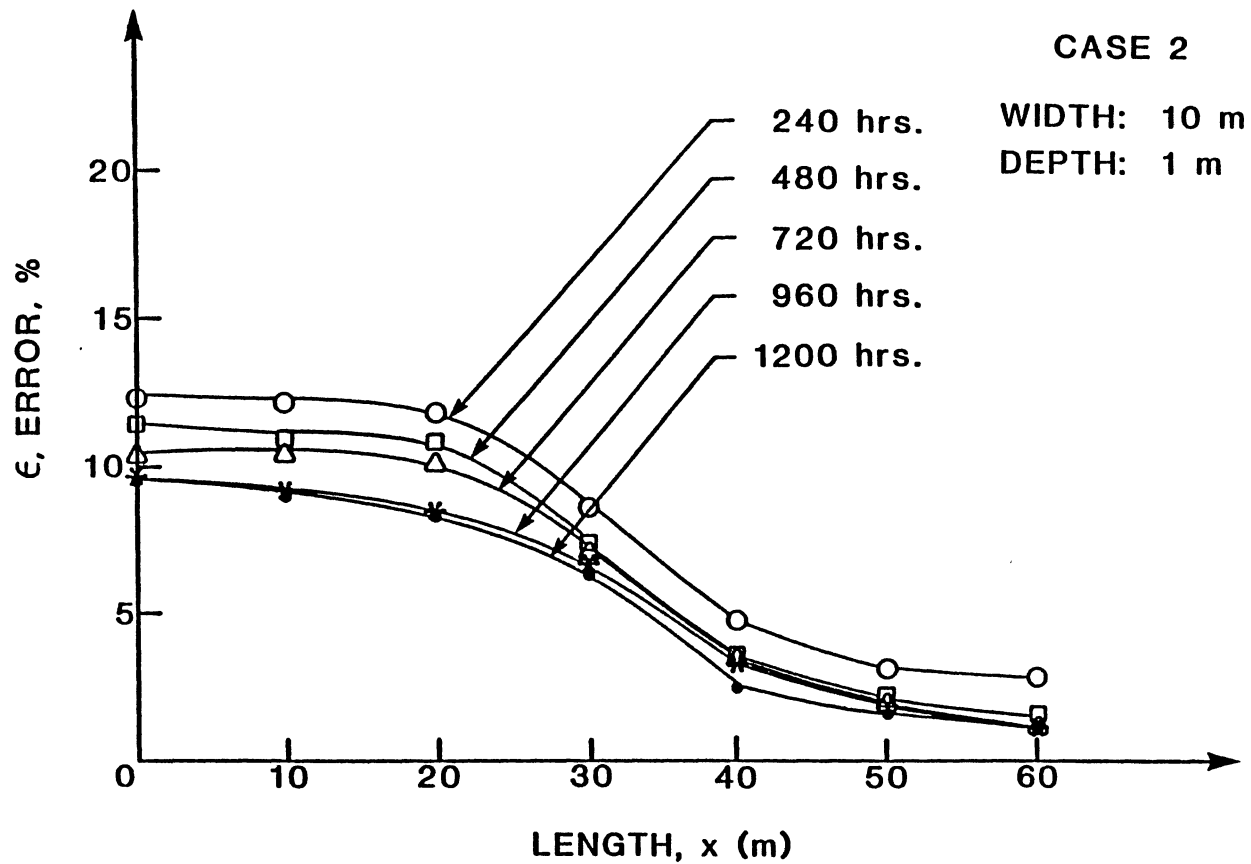


Figure 33. Error with Distance in x Direction for a Vertical Plane of 10 and 1 Meters in y and z Directions

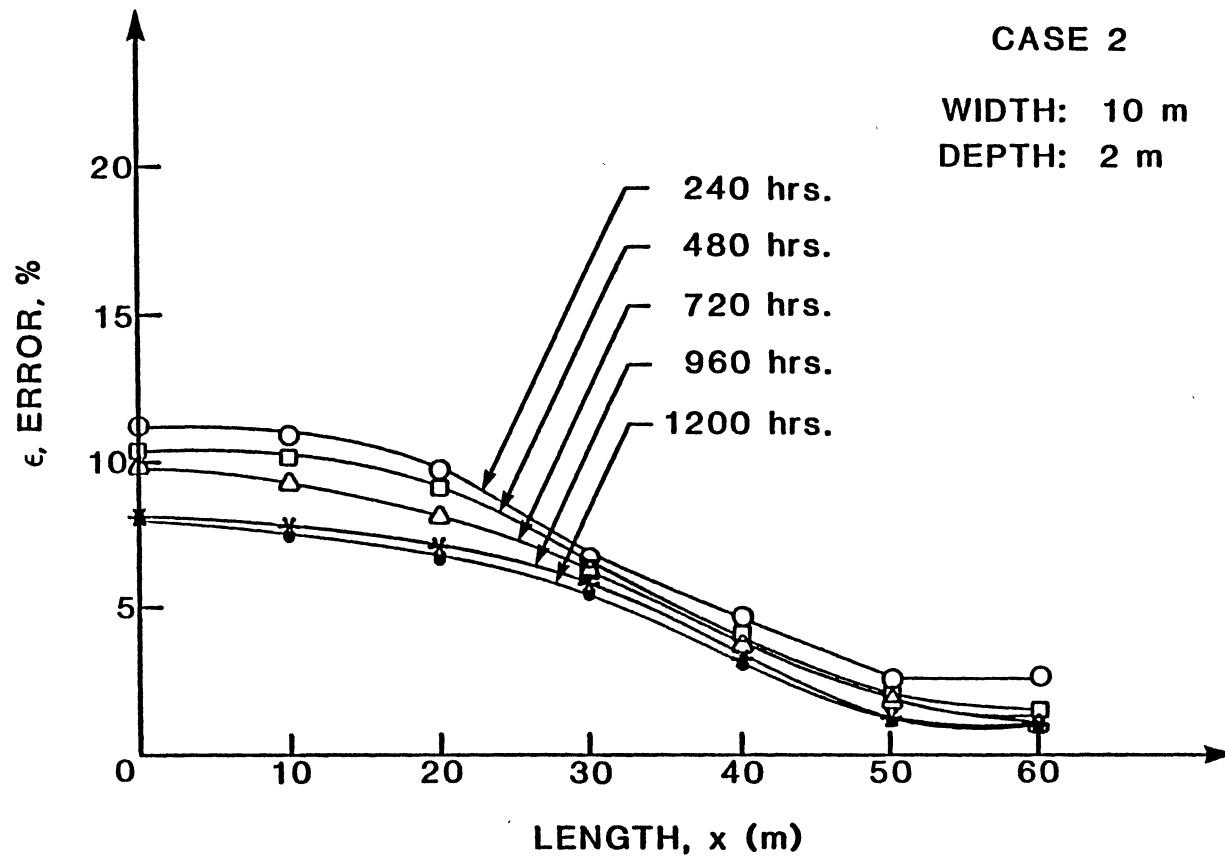


Figure 34. Error with Distance in x Direction for a Vertical Plane of 10 and 2 Meters in y and z Directions

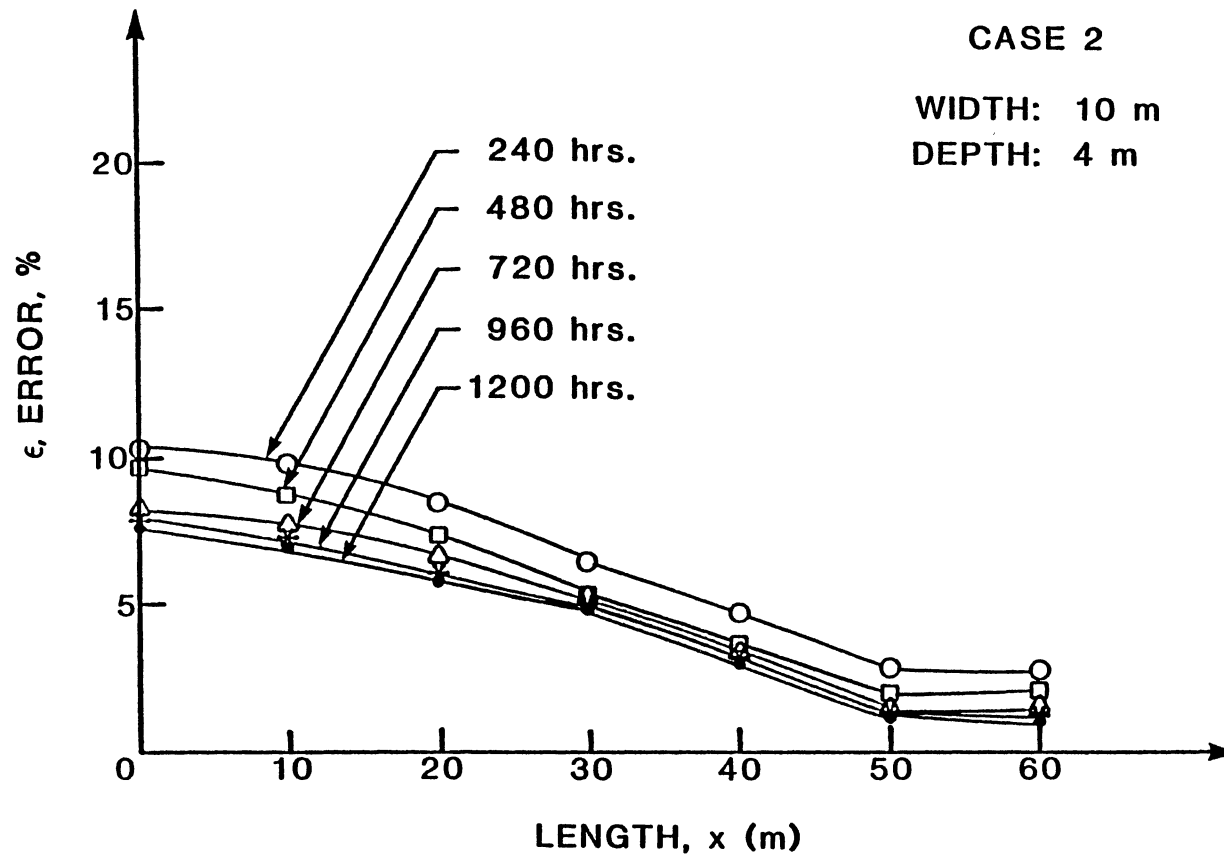


Figure 35. Error with Distance in x Direction for a Vertical Plane of 10 and 4 Meters in y and z Directions

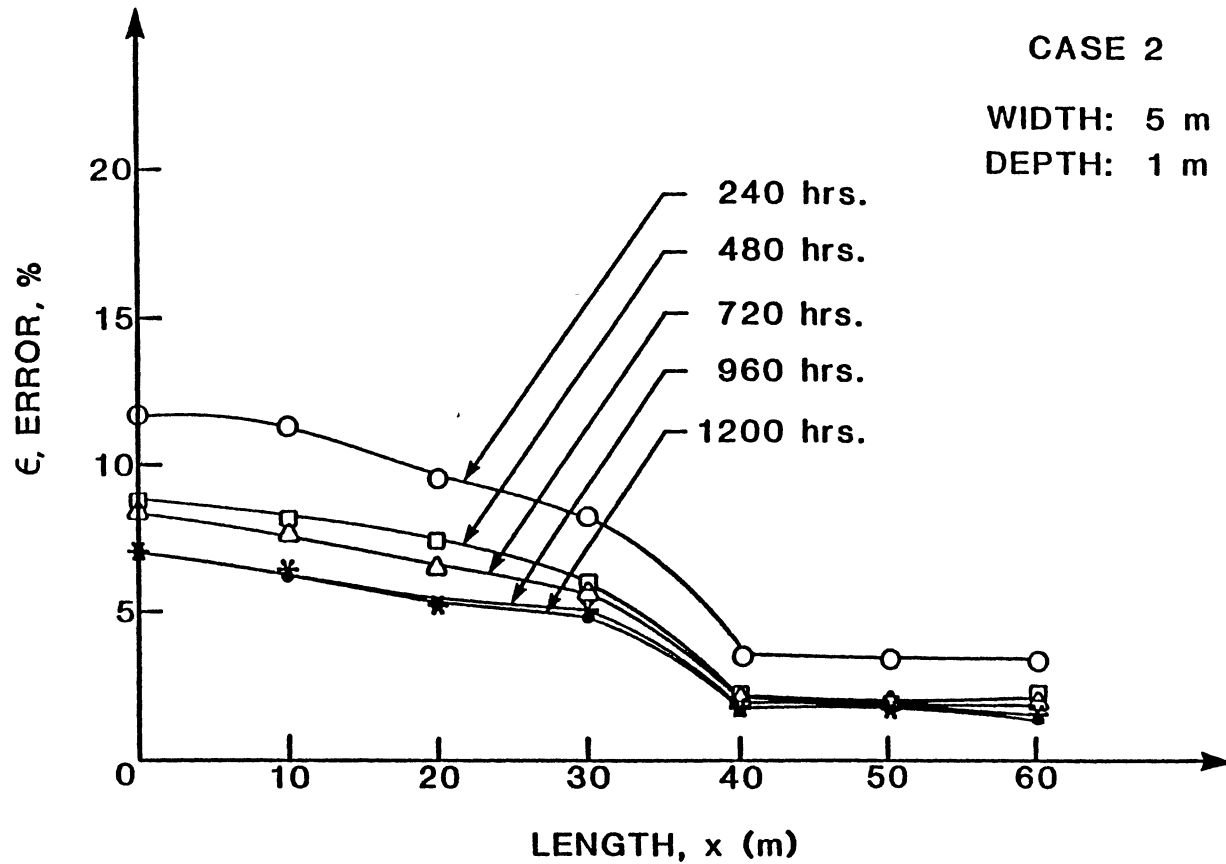


Figure 36. Error with Distance in x Direction for a Vertical Plane of 5 and 1 Meters in y and z Directions

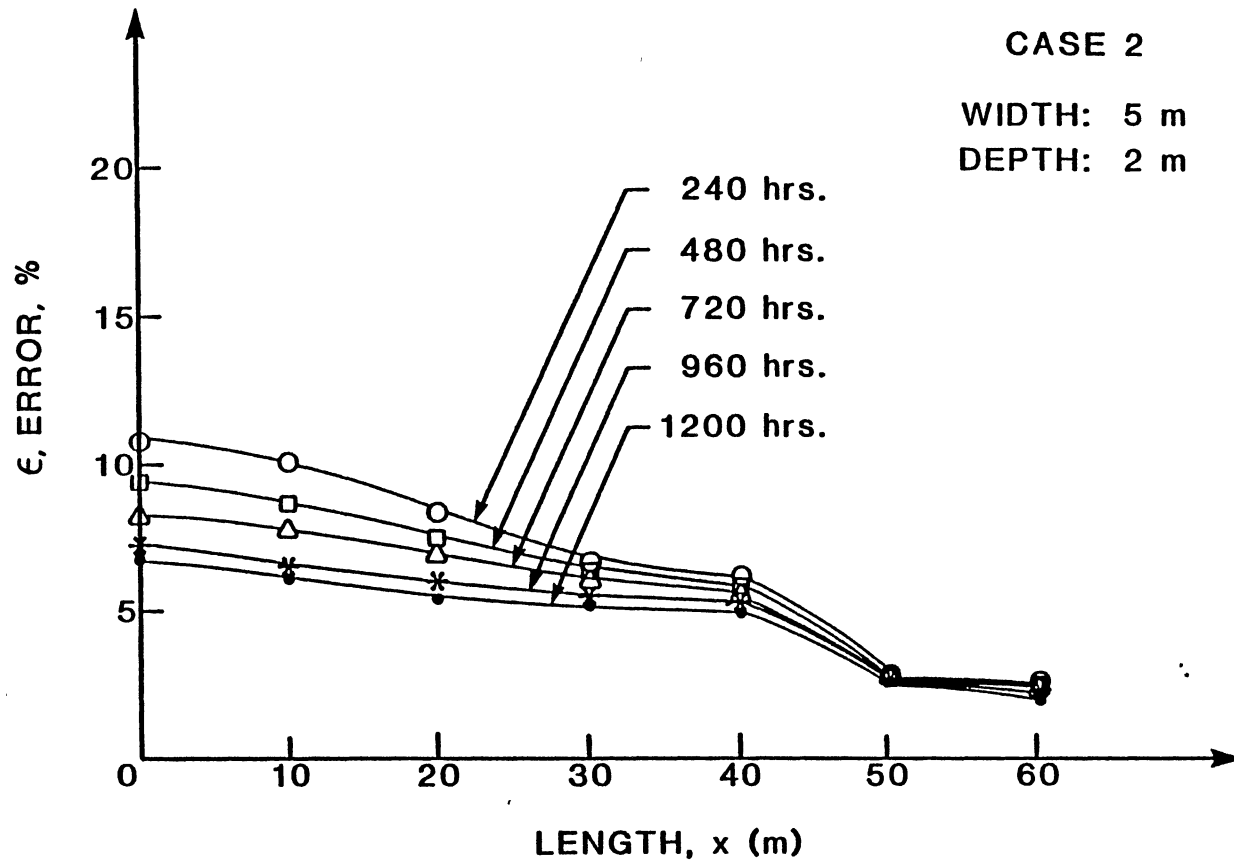


Figure 37. Error with Distance in x Direction for a Vertical Plane of 5 and 2 Meters in y and z Directions

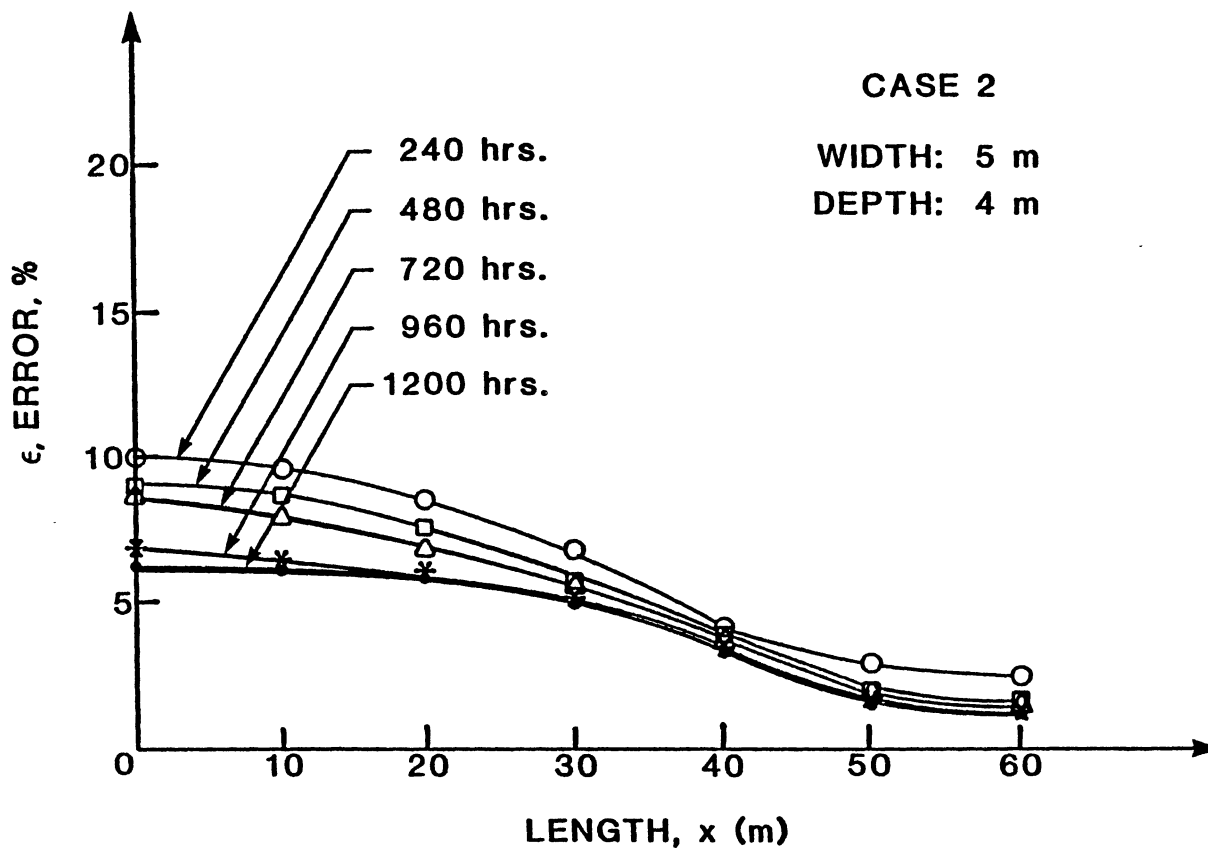


Figure 38. Error with Distance in x Direction for a Vertical Plane of 5 and 4 Meters in y and z Directions

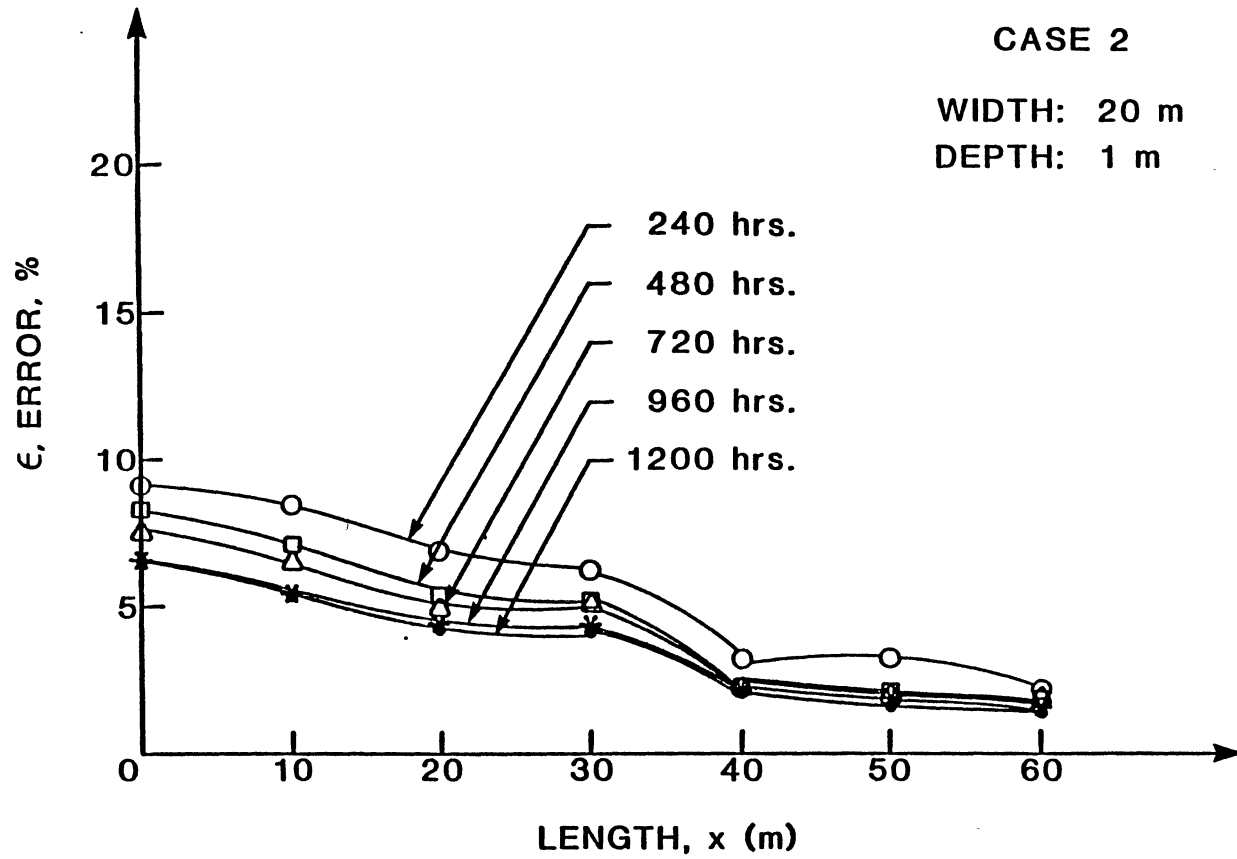


Figure 39. Error with Distance in x Direction for a Vertical Plane of 20 and 1 Meters in y and z Directions

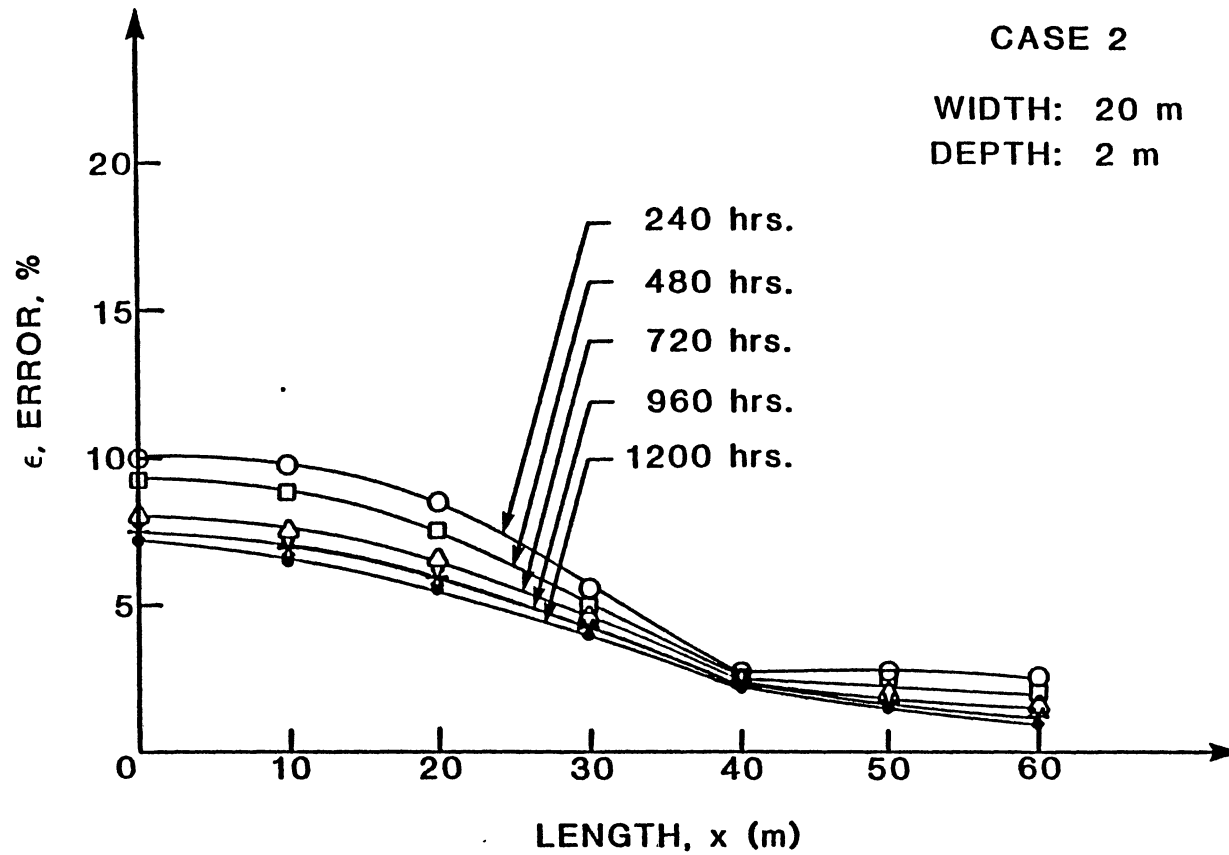


Figure 40. Error with Distance in x Direction for a Vertical Plane of 20 and 2 Meters in y and z Directions

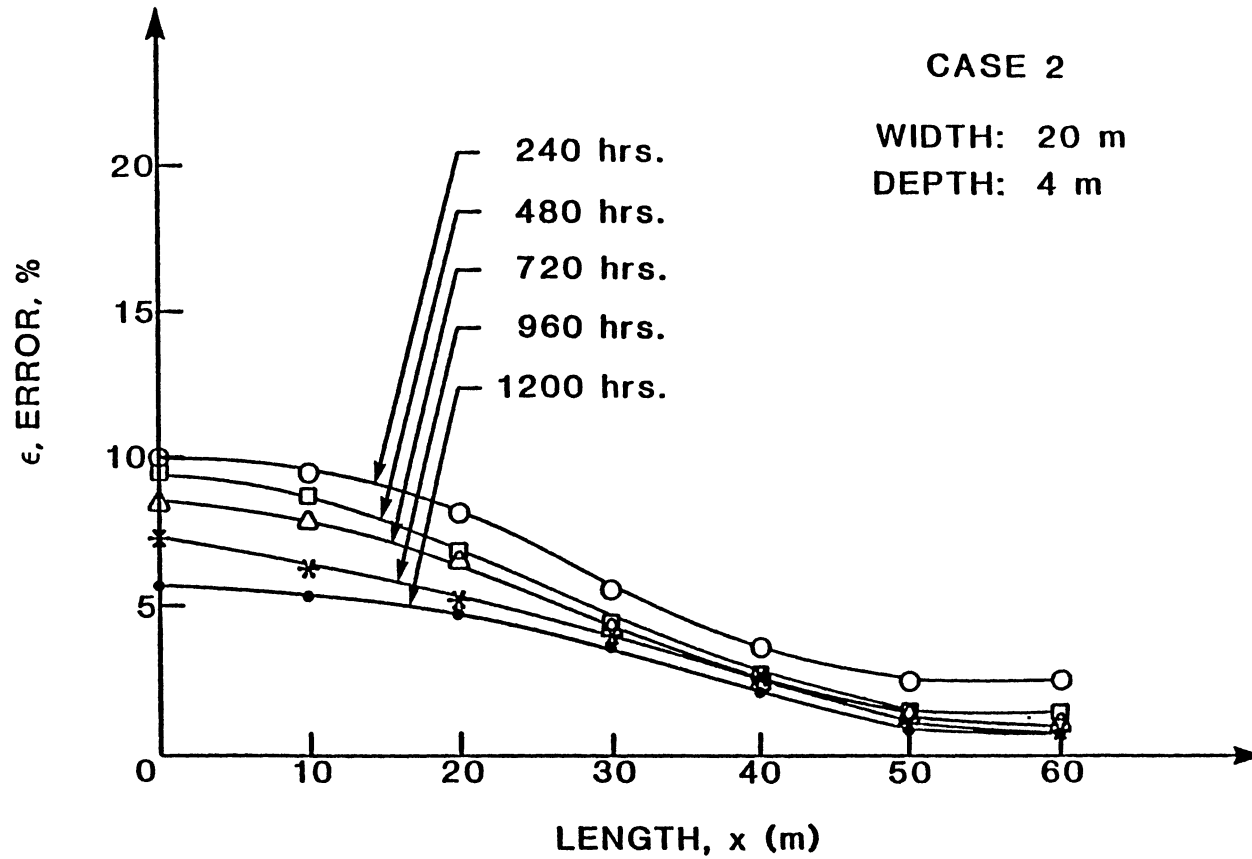


Figure 41. Error with Distance in x Direction for a Vertical Plane of 20 and 4 Meters in y and z Directions

according to y and z directions. The error, in percent, was derived from a comparison of the analytical solution with the developed model for the two cases. For Case 1, the maximum percentage of error is 12.50 and the minimum is 1.08. For Case 2, the percentage of error varied from 0.9 to 12.4. In both cases the error decreases as the distance from the point or line source increases; also, the error decreases with a longer time of application. The maximum percentage of errors is 12.5 and 12.4 for Case 1 and Case 2, respectively. This developed model, thus, gives close results with three-dimensional analytical solutions for a point source and a line source.

CHAPTER X

MODEL APPLICATION

Field Problem

This chapter describes the application of the model to a field problem. The Babylon landfill in Suffolk county, Long Island, New York. Kimmel and Braids (1974) provided the geographic map (Figure 42). The landfill for the city of Babylon is the main refuse disposal facility for a population of about 287,000. The landfill covers 35 acres, contains 1.7×10^8 ft³ of refuse, and is 40 years old. The landfill has an incinerator and receives scavenger waste. There is leachate movement in the saturated groundwater zone. The spread of contamination in the aquifer is a major concern because this aquifer yields nearly all of the county's public water supply.

The landfill is on an outwash plain that is underlain mainly by coarse sand, a few streaks of gravel, and fine sand. This is known as the upper glacial aquifer on Long Island. At the Babylon landfill, the bottom of the upper glacial aquifer is 70 feet (21m) below the water table, the top is 18 feet (4.6m) below the land surface, and the aquifer is underlain by a single 10 feet (3.3m) thick layer of Gardiner's clay (Figure 43, Cleary et al., 1981). At the

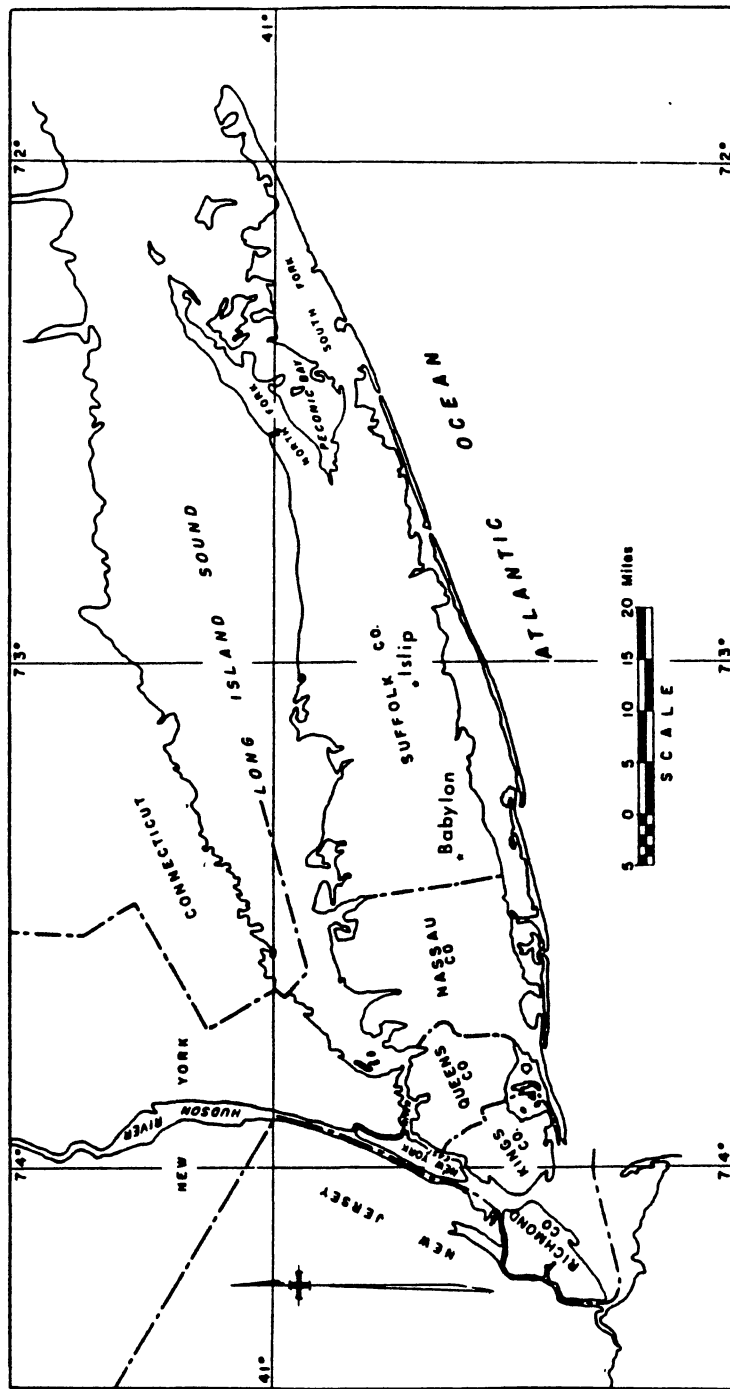
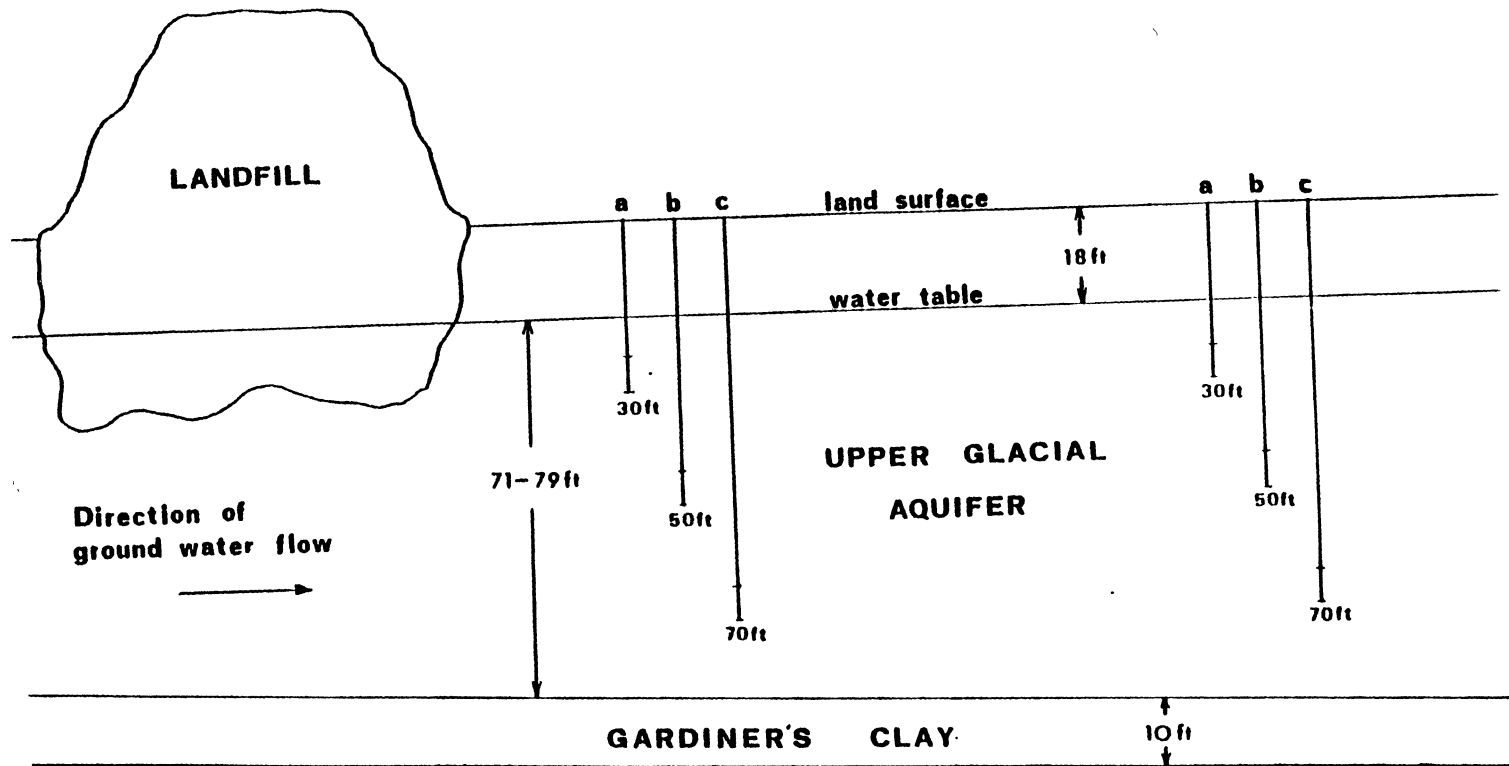


Figure 42. Location of Babylon in Suffolk County, New York



BABYLON LANDFILL, NEW YORK

MAGOTHY AQUIFER

Figure 43. Simplified Cross Section at the Landfill Site
Shown the Well Installation and Hydrological
Setting

Babylon site, the regional flow in the upper glacial aquifer is primarily parallel to the water table, and along the hydraulic gradient of 0.002ft/ft (Kimmel and Braids, 1974) is uniform and fairly constant throughout the year. Water levels recorded for 18 months on a monthly basis at observation wells near the landfill have shown the water table fluctuation of the groundwater movement to be acceptable.

The parameter of Gureghian et al. (1981) will be used in this study and the model's result compared with theirs. The chloride ion (cl^-) is chosen as the dispersion tracer because it is free of chemical reactions such as ion exchange, sorption, and precipitation.

Prediction

It was necessary to get the initial concentration at well numbers 1, 2, 8, 113, 125, 126, 200, 201, 202, and 203 (Figure 44), all located along Edison Avenue. These values were acquired from the November 1975 b-level well data (Figure 43). See Figure 45(a) for the first nine months of data for the initial nodal chloride ion concentration . Because we do not have exact information from these wells, we move the inclined line to the vertical line along the y-axis (Figure 45(b)). Gureghian et al. calibrated the model parameter to match the June 1976 isolength. The final model parameters are 3.1ft/day in x direction and $\hat{0}$.2ft/day in y direction. Dispersivity is 140 feet and 250 feet in

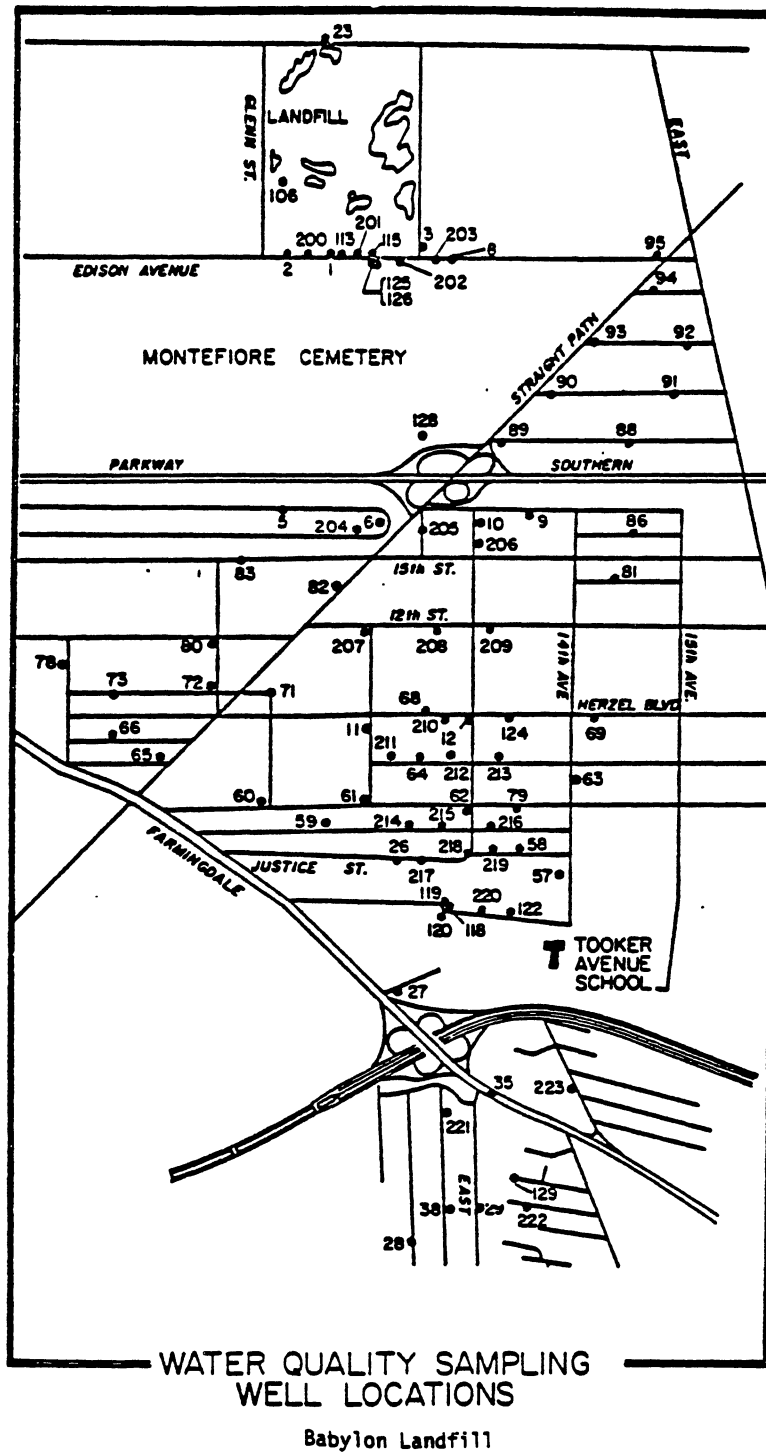
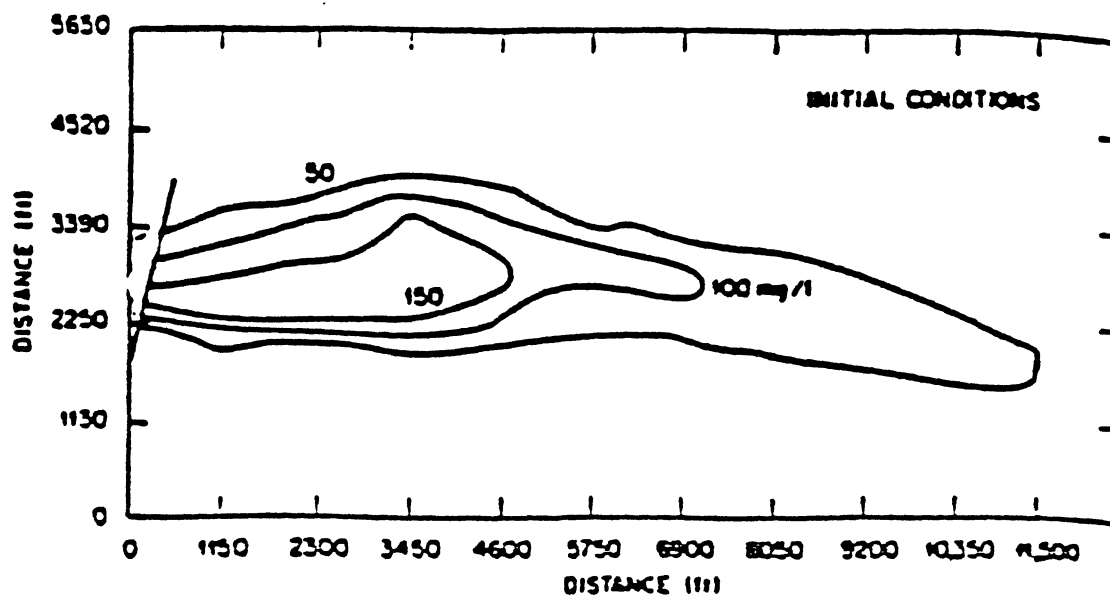
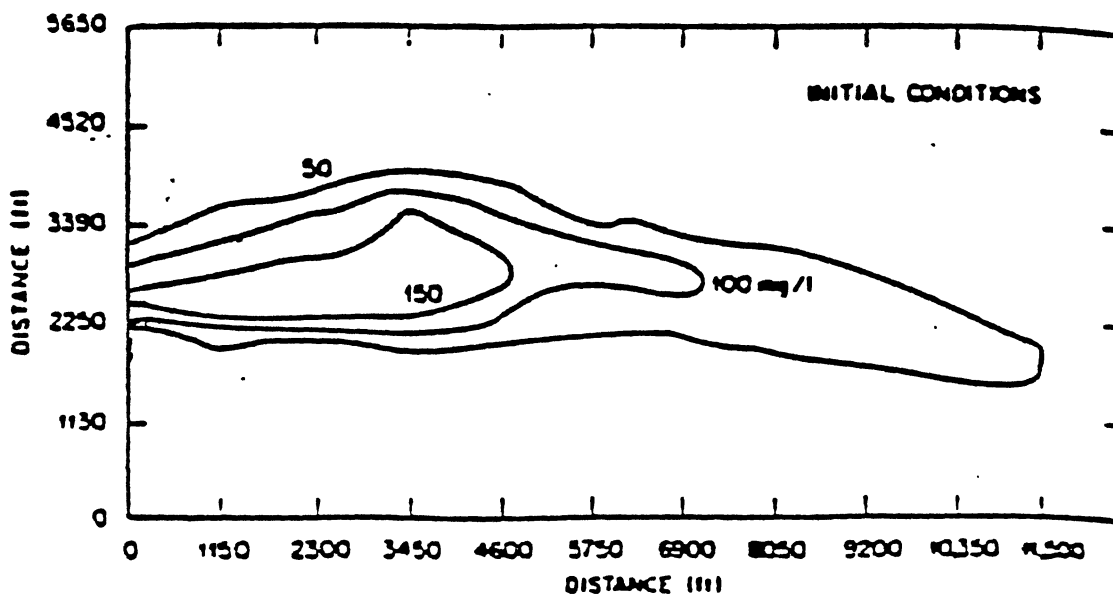


Figure 44. Water Quality Sampling Location



(a) Observed Initial Conditons



(b) Modified Initial conditions

Figure 45. Observed Initial and Modified Initial Conditions

longitudinal and transverse directions. The molecular diffusion coefficient is 1.0×10^{-7} ft²/day. This is too small compared to the other dispersivity, so in this case we assume the molecular diffusion coefficient to be zero. For the time parameters, an initial time step is two days with a cyclic multiplying factor of 1.2 and a maximum time step of 15 days. Smaller initial and maximum time steps provide additional accuracy. Lengths of sides of elements range from 200 to 1500 feet (Figure 46).

Comparison

The model results were compared with the predicted values of Gureghian et al. (1981) and with actual observation values at June 1976 (216 days) and December 1976 (396 days). At time equal to 216 days, the model's value is close to the observation values because the parameters used in the model are the final parameters, not the calibration value. At time equal to 396 days, the model value was in agreement with the value predicted by Gureghian et al. (1981) and with the observation value.

Moving the initial condition does not seem to seriously influence the final result (Figures 47 and 48). The difference between the developed model and Gureghian's model may be due to small difference of the data. The error range between 0% and 14.7%. The model, however, is applicable to the field problem.

longitudinal and transverse directions. The molecular diffusion coefficient is 1.0×10^{-7} ft²/day. This is too small compared to the other dispersivity, so we assume the molecular diffusion coefficient to be zero. For the time parameters, an initial time step is two days with a cyclic multiplying factor of 1.2 and a maximum time step of 15 days. Smaller initial and maximum time steps provide additional accuracy. Lengths of sides of elements range from 200 to 1500 feet (Figure 46).

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Moving the initial condition does not seriously influence the final result (Figures 47 and 48). The difference between the developed model and Gureghian's model may be due to small differences of the data. The error in the developed model and observed data ranges between 0% and 14.7%. The error between the developed model and Gureghians's model ranges between 0% and 12.2%. The model, however, is applicable to the field problem.

THICKNESS OF AQUIFER: $H = 10$ ft.
LENGTH OF AQUIFER: $L = 12650$ ft.
WIDTH OF AQUIFER: $W = 5650$ ft.
NUMBER OF NODES: 360
NUMBER OF ELEMENTS: 154

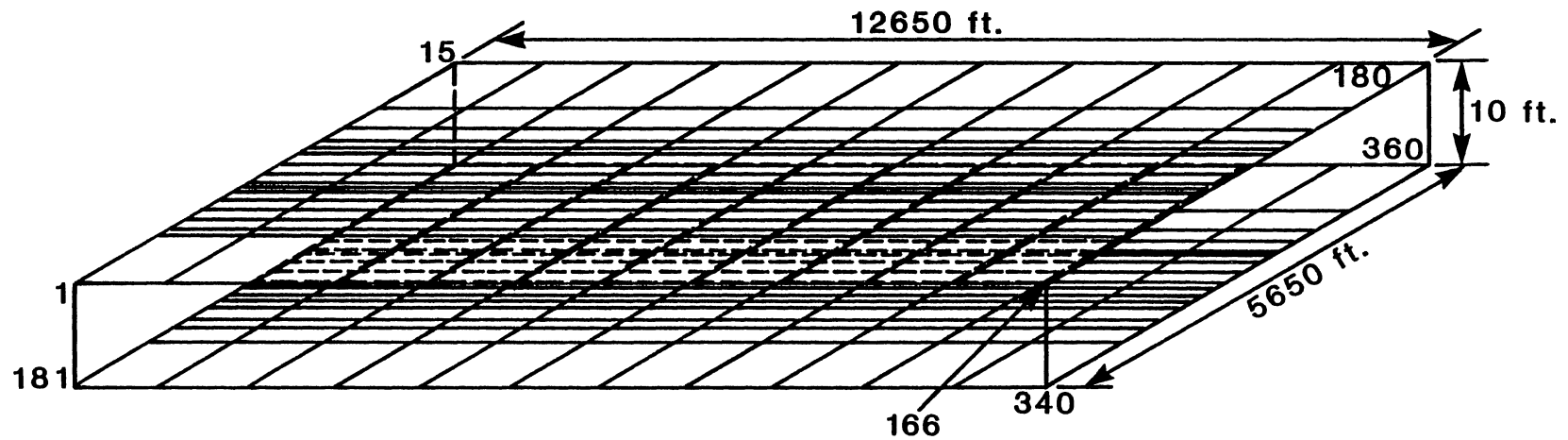


Figure 46. Three-Dimension Application to a Field Aquifer

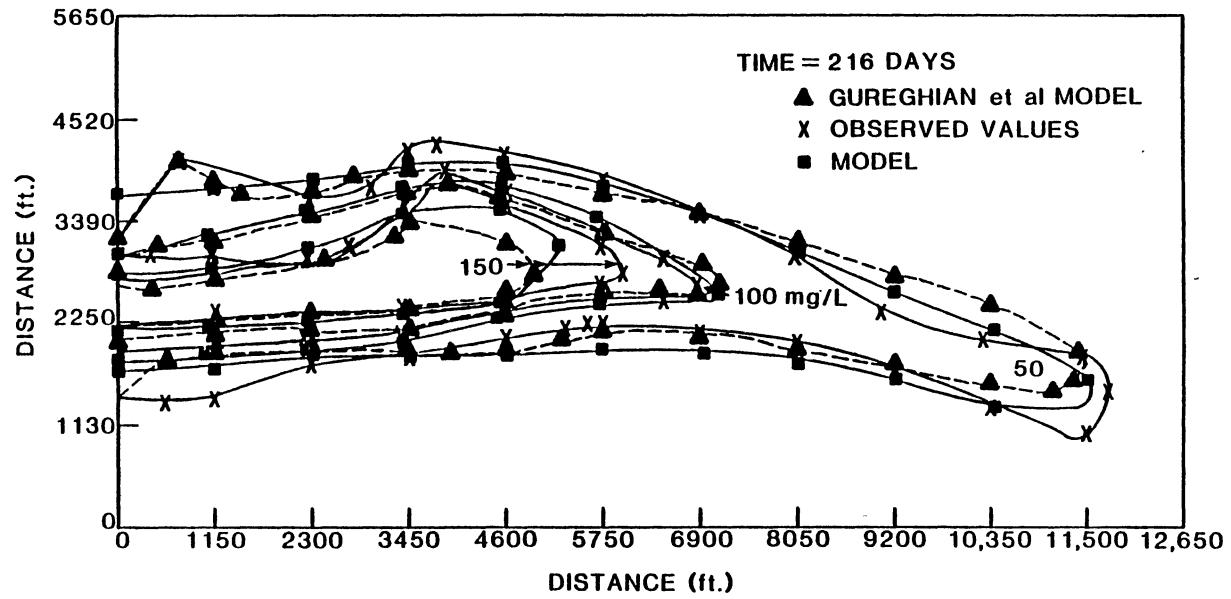


Figure 47. Chloride Concentrations Comparison at 216 Days

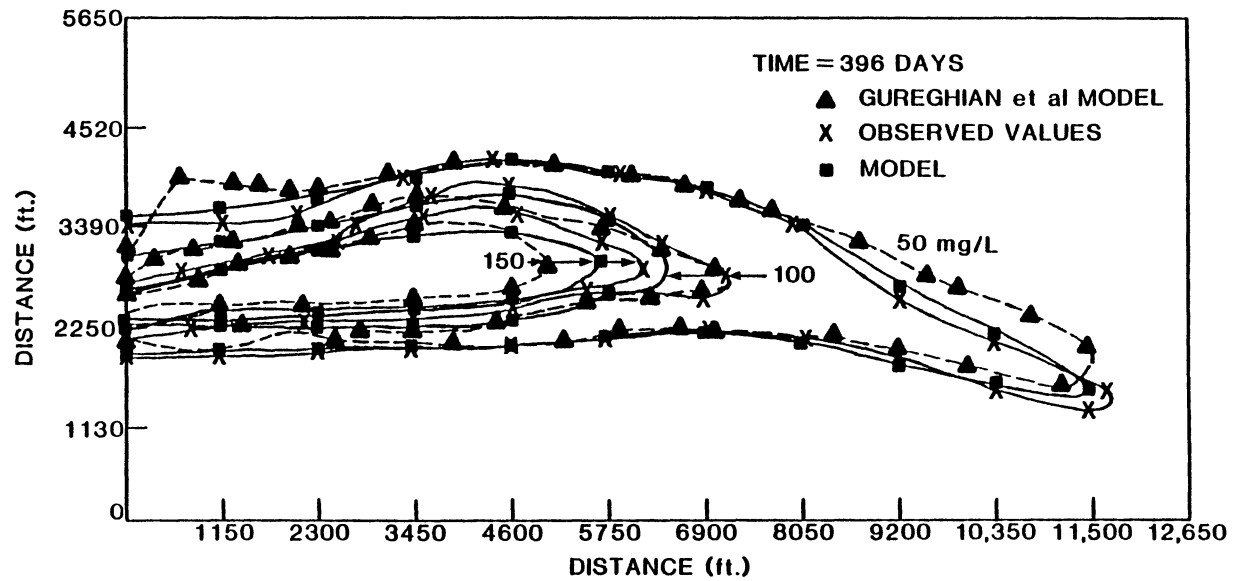


Figure 48. Chloride Concentrations Comparison at 396 Days

CHAPTER XI

CONCLUSIONS

The following conclusions can be drawn based on this study:

1. A three-dimensional transient model is developed using the Galerkin's finite element method to predict the migration of contaminants in saturated zones of aquifers.

2. The developed model has been validated against the existing analytical and numerical solutions in one, two and three dimensions.

3. Validation of the model for a one-dimensional case indicates that increasing the number of elements near a pollutant source improves the accuracy of the model. Away from the source, element size can be increased without sacrificing the accuracy.

4. The error analysis for the one-dimensional case indicates that the error varies from 0% to 13% using 20 to 100 elements in the problem.

5. The model is compared with a two-dimensional numerical model of Gureghian et al. (1980) and the analytical solution of Cleary and Ung (1978). The model results are in close agreement with the solutions of these two models for the same set of parameters.

6. The error analysis is presented for the two-dimensional case. The error varies between 0% to 38% and 0% to 57.5% for the two solutions for only one node. For other nodes, the error for the two solutions varies between 0 to 20% and 0 to 22%.

7. The Peclet number should be kept relatively low where the concentrations are relatively small, because the Peclet number is proportional to element size or length characteristics. The overshoot could be minimized by keeping the element size small in areas of low concentration.

8. The model is validated against two cases of three-dimensional analytical solutions, a point source and a line source (Yeh, 1981). Results of the model agree with those of the point and line source solutions.

9. The error analysis for the point source indicates that error between the developed model and the analytical solution varies from 1.08% to 12.50%. For the line source, the error ranges between 0.9% and 12.4%.

10. The developed model is applied to the Babylon landfill in Suffolk County, Long Island, New York. Chloride concentrations predicted by the model are in close agreement with the observed concentrations from a field of monitoring wells. The error ranges between 0% and 14.7%.

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APPENDIX A

LISTING OF COMPUTER PROGRAM


```

C * ETA LOCAL COORDINATE OF ELEMENT
C * FA DNI/OX * DETERMINANT OF J
C * FACT FACT =0 FOR STEADY STATE; 1 FOR TRANSIENT
C * FB DNI/OY * DETERMINANT OF J
C * FC DNI/OZ * DETERMINANT OF J
C * GAUSS SUBROUTINE THAT PERFORMS INTEGRATION
C * GQPO GAUSS INTEGRATION POINT
C * GQWT GAUSS INTEGRATION WEIGHT
C * GLOBMX GLOBAL STORATIVITY MATRIX
C * GLOBAL SUBPROGRAM THAT ASSEMBLES GLOBAL MATRIX
C * ID IDENTIFICATION FOR CONSTANT CONC OR FLUX
C * ID=0 CONSTANT FLUX; 1 CONSTANT CONC.
C * IN CARD READER PARAMETER
C * IT TOTAL NUMBER OF SIMULATION PERIOD
C * SOLUTION IS TO BE CARRIED OUT
C * MATNO MATERIAL NUMBER IF MORE THAN ONE
C * MAX TEMPORARY VARIABLE FOR BANDWIDTH
C * MAXGD BANDWIDTH OF GLOBAL MATRIX + 1
C * NEIMS TOTAL NUMBER OF ELEMENTS
C * MNODEP MAXIMUM NUMBER OF NODES FOR EACH ELEMENT
C * MK TEMPORARY VARIABLE FOR BANDWIDTH
C * MUDCL TYPE OF MODEL BEING DESIGNED, 1, 2, 3
C * MAXNOD TOTAL NUMBER OF NODES IN THE SYSTEM
C * NCONFN = 1 FOR CONFINED; 0 OTHERWISE
C * NCUBE NUMBER OF NODES PER ELEMENT
C * ND NODE FOR WHICH BOUNDARY CONDITION IS GIVEN
C * NOBC NUMBER OF FIXED BOUNDARY CONDITIONS
C * NE ELEMENT NUMBER
C * NHE NUMBER OF NODES FOR HEAD ESTIMATION
C * NN NUMBER OF NODES IN A GIVEN ELEMENT
C * NODE NODE NUMBERS FOR AN ELEMENT
C * NOROER ORDER OF GAUSS INTEGRATION
C * NUMAT TOTAL NUMBER OF MATERIALS IF MORE THAN ONE
C * NPPED NUMBER OF PUMPING PERIODS
C * NPT TOTAL NUMBER OF POINTS
C * NQW NUMBER OF SOURCE OR SINK PER ELEMENT
C * NSTEDY OPTION FOR STEADY STATE OR TRANSIENT CASE
C * NWELS NUMBER OF PUMPING WELLS
C * NSTEDY=1 FOR TRANSIENT, 0 FOR STEADY STATE
C * PHY LOCAL COORDINATE OF ELEMENT
C * PORS VALUE OF POROSITY
C * PT PRINT PARAMETER
C * QW SOURCE OR SINK(-VE FOR SINK,+VE SOURCE)
C * R(I,J) ELEMENT STORATIVITY MATRIX
C * RECT INTERMEDIATE RIGHTHAND SIDE VECTOR
C * S STORAGE COEFFICIENT/STORATIVITY OF AQUIFER
C * SIJ SUMMATION OF DERIV. OF SHAPE FUNCTIONS
C * WITH RESPECT TO X COORDINATE
C * SIKJO SUMMATION OF NI*NJ
C * SILJC SUMMATION OF NI AT NODE I
C * SISJ SNJ * SNIDU
C * SKJ SUMMATION OF DERIV. OF SHAPE FUNCTION
C * WITH RESPECT TO Y COORDINATE
C * SLJ SUMMATION OF DERIV. OF SHAPE FUNCTION
C * WITH RESPECT TO Z COORDINATE
C * SNIDU SNI * DU
C * SOLVLU SUBROUTINE THAT SOLVES SYSTEM'S EQUATIONS
C * SR REACTION CONSTANT
C * SS(I) TEMPORARY ARRAY FOR GAUSS POINTS
C * STOMX GLOBAL CONDUCTIVITY MATRIX
C * SUM TEMPORARY VARIABLE FOR RHS VECTOR
C * TOL TOLERANCE LIMIT FOR COMPUTATION
C * TOTAL FLAPSED TIME (IN USER'S CHOICE OF UNITS)
C * VLX VELOCITY RESPECT TO X DIRECTION
C * VLY VELOCITY RESPECT TO Y DIRECTION
C * VLZ VELOCITY RESPECT TO Z DIRECTION

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C * VOLUME      VOLUME OF ELEMENT      *
C * WK(I,J)    ELEMENT CONDUCTIVITY MATIX *
C * WIAV      AVERAGE WEIGHT FOR GAUSS INTEGRATION *
C * X          X COORDINATE IN GLOBAL SYSTEM *
C * Y          Y COORDINATE IN GLOBAL SYSTEM *
C * Z          Z COORDINATE IN GLOBAL SYSTEM *
C * ZETA      LOCAL COORDINATE OF ELEMENT *
C * ++++++
C
C MAIN PROGRAM
C PURPOSES:
C THE MAIN PROGRAM PRINTS THE TITLE OF THE PROBLEM, DIMENSION
C THE SIZE OF PROBLEM, CONTROL SEQUENCE OF COMPUTATIONS
C AND FINALLY PRINTS THE CONCENTRATION RESULTS FROM
C THE SUBROUTINE SOLVER
C -----
C
C IMPLICIT REAL*8 (A-H,O-Z)
C COMMON /SUBA/SIJ(400),SKJ(400),SLJ(400),SMJ(400),SWJ(400),
C 1SOJ(400),SIRJO(200),SILJC(200),DNIDX(2000),DNIDY(2000),
C 2DNIDZ(2000),WKX(400),WKY(400),WKZ(400),DXX(400),DYY(400),
C 3DZZ(400),VLX(400),VLY(400),VLZ(400),XQ(8),YQ(8),ZQ(8),AA(3)
C COMMON /SUBB/AA1(8),AA2(8),AA3(8),DSFXN(64),DSFYN(64),
C 1DSFZN(64),DSFX(64),DSFY(64),DSFZ(64),ETA(36),PHY(36),
C 2ZETA(64),SA(6),SFV(8),FX(8),FY(8),FZ(8),F(24),G(24),H(24),
C 3GQPO(5),GQWT(5),SS(6),DD(6),NODD(8),MATNO(8),MNO(8)
C COMMON /SUBC/STOMX(400,400),P(400,400),R(400,400)
C COMMON /SUBD/GLUBMX(400,400),RMX(400),RECT(400)
C COMMON /SUBE/TKX(400),TKY(400),TKZ(400),X(400),Y(400),Z(400)
C COMMON /SUBF/C(400),CINT(400),CULD(400),QW(400),BCD(8)
C COMMON /SUBG/ID(400),ND(400)
C COMMON /SUBH/NODE(400,400)
C -----
C DATA IN,LP/10.6/
C
C WRITE(PT,5)
C 5 FORMAT(1H1)
C WRITE(PT,10)
C 10 FORMAT(////////,44X,'INPUT DATA FOR THREE-DIMENSIONAL'//44X,
C 1'-----'//40X,
C 2'GROUNDWATER DISP BY FINITE ELEMENT METHOD'//40X,
C 3'-----')
C DIMENSION THE SIZE OF PROBLEM
C READ(IN,15)NELMS,MXNOD,MNOPE,NSTEDY,NDBC,DELT
C 15 FORMAT(5I4,F10.5)
C DO 25 J=1,NELMS
C READ(IN,20) (VLX(I),VLY(I),VLZ(I),I=1,MXNOD)
C READ(IN,20) (DXX(I),DYY(I),DZZ(I),I=1,MXNOD)
C 20 FORMAT(8D11.3)
C 25 CONTINUE
C CALL INPUT(NWELS,NPERS,NUMAT,NCE,IT,FACT,NELMS,MXNOD,
C 1MNOPE,NE,DELT,NSTEDY,LP,IN,NDBC)
C
C CALL SHAPE(NELMS,MXNOD,MODFL,NX,NN,INDEX,MNOPE)
C
C CALL BOUND(MXNOD,DELT,NDBC,NSTEDY)
C CALL WIDTH(BANDW,IROW,MXNOD)
C WRITE(PT,35)BANDW,IROW
C 30 FORMAT(/,5(5X,I4,4X,D11.3))
C 35 FORMAT(/36X,'MAXIMUM BANDWIDTH = ',I3,' ON ROW NO.',I3)
C
C CALL ADJUST(MXNOD,BANDW)
C WRITE(PT,40)
C 40 FORMAT(1H1)
C WRITE(PT,45)
C 45 FORMAT(////////,44X,'OUTPUT FOR THREE-DIMENSIONAL'//44X,

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40 FORMAT(/////25X,'STEP SIZE'                               =',F10.5/25X,
1'STATE OF PROBLEM'                                         =',I1/25X,
2'NO. OF SPECIFIED CONDITIONS'                             =',I1)
WRITE(PT,45)
45 FORMAT(1H1,////////,39X,'COORDINATES AND INITIAL CONCS OF NODES (L
1)')
WRITE(PT,50)
50 FORMAT(//25X,'NODES      Y(I)          X(I)          Z(I)
1 CINT(I)')
DO 65 I = 1,MXNOD
READ(IN,55)Y(I),X(I),Z(I),QW(I),CINT(I)
55 FORMAT(5D10.2)
WRITE(PT,60)I,X(I),Y(I),Z(I),CINT(I)
60 FORMAT(25X,I4,4(4X,D10.2))
65 CONTINUE
DO 70 J = 1,MXNOD
QW(J) = QW(J)*FACT3
70 CONTINUE
WRITE(PT,75)
75 FORMAT(1H1,/////////56X,'NODE-ELEMENT RELATIONSHIP')
WRITE(PT,80)
80 FORMAT(//25X,'ELEMS      N1      N2      N3      N4
1 N5      N6      N7      NB')
DO 100 JK = 1,NELMS
READ(IN,90)NE,(NODE(JK,I),I=1,MNOPE)
WRITE(PT,95)NE,(NODE(JK,I),I=1,MNOPE)
90 FORMAT(9I4)
95 FORMAT(26X,I4,8(GX,I4))
100 CONTINUE
WRITE(PT,105)
105 FORMAT(1H1,/////////44X,'FIXED BOUNDARY CONDITIONS'///5X,
15('NODE      ID',9X))
READ(IN,110)(ND(JK),JK=1,NDBC)
110 FORMAT(8I4)
READ(IN,125)(ID(ND(JK)),JK=1,NDBC)
115 FORMAT(6I2)
WRITE(PT,130)(ND(JK),ID(ND(JK)),JK=1,NDBC)
125 FORMAT(//.5(5X,I4,7X,12,4X))
RETURN
END
C
C
C SUBROUTINE SHAPE(NELMS,MXNOD,MODEL,NX,NN,INDEX,MNOPE)
C
C PURPOSE: THIS SUBROUTINE DOES THE INTERGRATION OF THE BASIS
C FUNCTION FOR ALL ELEMENTS USING GAUSSIAN QUADRATURE
C
C IMPLICIT REAL*8 (A-H,O-Z)
COMMON /SUBA/SIJ(400),SKJ(400),SLJ(400),SMJ(400),SWJ(400),
1SDJ(400),SIKJ(200),SILJC(200),DNIDX(2000),DNIDY(2000),
2DNIDZ(2000),WKX(400),WKY(400),WKZ(400),DXX(400),DYY(400),
3DZ(400),VLX(400),VLY(400),VLZ(400),XQ(8),YQ(8),ZQ(8),AA(3)
COMMON /SUBB/AA1(8),AA2(8),AA3(8),DSFXN(64),DSFYN(64),
1DSFZN(64),DSFX(64),DSFY(64),DSFZ(64),ETA(36),PHY(36),
2ZETA(64),SA(6),SFV(8),FX(8),FY(8),FZ(8),F(24),G(24),H(24),
3GQIN(5),GQW(5),SS(6),DN(6),NIND(8),MATND(8),MNO(8)
COMMON /SUBC/STOMX(400,400),P(400,400),R(400,400)
COMMON /SUBD/GLOBMX(400,400),RMX(400),RECT(400)
COMMON /SUBE/TKX(400),TKY(400),TKZ(400),X(400),Y(400),Z(400)
COMMON /SUBF/C(400),CINT(400),COLD(400),QW(400),BCD(8)
COMMON /SUBH/NODE(400,400)
C
C INFORMATION OF LOCAL COORDINATE FOR EACH ELEMENT
C
C DATA (ETA(I),I=1,36)/
1-1 DO, 1 DO, 1 DO, -1 DO, -1 DO, 1 DO, 1 DO, -1 DO,

```

```

20.DO,0.DO,0.DO,0.DO,
3-1.DO, 1.DO, -1.DO, 1.DO, -1.DO, 1.DO, 1.DO, -1.DO,
4-1.DO, -1.DO, 1.DO, 1.DO, -1.DO, -1.DO, 1.DO, 1.DO,
5-1.DO, -1.DO, 1.DO, 1.DO, 1.DO, 1 DO, -1.DO, -1.DO/
C -----
DATA (ZETA(I),I=1,36)/
C
1-1.DO,-1.DO,1.DO,1.DO,-1.DO,-1.DO,1.DO,1.DO,-1.DO,1.DO,-1.DO,1 DO,
20.DO,0.DO,0.DO,0.DO,
3-1.DO,-1.DO,1.DO,1.DO,-1.DO,-1.DO,1.DO,1.DO,
4-1 DO,-1.DO,1.DO,1.DO,-1 DO,-1.DO,-1.DO,-1.DO,1.DO,1.DO,1.DO,1.DO/
C -----
DATA (PHY(I),I=1,36)/
C
11.DO,1.DO,1.DO,1.DO,-1.DO,-1.DO,-1.DO,-1 DO,1.DO,1.DO,-1.DO,-1.DO,
21.DO,1.DO,-1.DO,-1.DO,-1.DO,0.DO,0.DO,0.DO,0.DO,
31.DO,1.DO,1.DO,1.DO,
4-1.DO,-1.DO,-1.DO,-1.DO,1.DO,1.DO,1.DO,1.DO,
5-1.DO,-1.DO,-1.DO,-1.DO/
C -----
DATA IN,LP/10,6/
INDEX=0
C
C INITIALIZING THE GLOBAL MATRICES AND VECTOR
C
DO 10 I = 1,MXNOD
DO 10 J = 1,MXNOD
GLOBMX(I,J)=0.0
STOMX(I,J)=0.0
10 RMX(I) = 0 0
C
C START THE INTEGRATION ELEMENT BY ELEMENT
C
DO 80 IL = 1,NELMS
15 MODEL = 3
NN = MNOPE
XX = 0.0
YY=0.0
ZZ=0.0
NORDER=2
C
C GAUSS INTEGRATION POINTS AND WEIGHTS
C
IF(NORDER-2)16,16,17
16 GQPO(1) = -0.577350269189626DO
GQPO(2) = 0.577350269189626DO
GQWT(1) = 1.00000000000000DO
GQWT(2) = 1.00000000000000DO
GO TO 19
17 IF(NORDER.GT.3)GO TO 18
GQPO(1) = -0.774596669241483DO
GQPO(2) = 0.00000000000000DO
GQPO(3) = 0.774596669241483DO
GQWT(1) = 0.555555555555556DO
GQWT(2) = 0.888888888888889DO
GQWT(3) = 0.555555555555556DO
GO TO 19
18 GQPO(1) = -0.861136311594053DO
GQPO(2) = -0.339981043584856DO
GQPO(3) = 0.339981043584836DO
GQPO(4) = 0.861136311594053DO
GQWT(1) = 0.347854845137454DO
GQWT(2) = 0.652145154862546DO
GQWT(3) = 0.652145154862546DO
GQWT(4) = 0.347854845137454DO
C

```

```

D11=0.
D12=0.
D13=0.
D21=0.
D22=0.
D23=0.
D31=0.
D32=0.
D33=0.
SS(1) = ET
SS(2) = ZT
SS(3) = YP
DO 67 I = 1,NN
IF(NODE(IL,I).EQ.O)GO TO 67
40 DD(1) =E1A(I)
DD(2) =ZETA(I)
DD(3) =PHI(I)
DO 41 KP=1,MODEL
41 AA(KP)=1.DO+DD(KP)*SS(KP)
C IF(I.GT.8)GO TO 60
ALP=O.125DO*(4-MODEL)
ALPHA=ALP*AA(1)*AA(2)*AA(3)
SFV(I)=ALPHA
DNET=ALP*DD(1)*AA(2)*AA(3)
DNZT=ALP*DD(2)*AA(1)*AA(3)
DNPH=ALP*DD(3)*AA(1)*AA(2)
GO TO 66
C
66 AA1(I)=DNET
AA2(I)=DNZT
AA3(I)=DNPH
YQQ =YQ(I)
XQQ =XQ(I)
ZQQ =ZQ(I)
C
C GENERATING THE JACOBIAN MATRIX
C D11 =DX/DET D12 =DY/DET D13 =DZ/DET
C D21 =DX/DZT D22 =DY/DZT D23 =DZ/DZT
C D31 =DX/DYP D32 =DY/DYP D33 =DZ/DYP
C
D11 =DNET*XQQ+D11
D12 =DNET*YQQ+D12
D13 =DNET*ZQQ+D13
D21 =DNZT*XQQ+D21
D22 =DNZT*YQQ+D22
D23 =DNZT*ZQQ+D23
D31 =DNPH*XQQ+D31
D32 =DNPH*YQQ+D32
D33 =DNPH*ZQQ+D33
67 CONTINUE
INDEX=IL
C
C COMPUTING THE DETERMINANT DU OF THE JACOBIAN MATRIX
C
DU=D11*D22*D33+D12*D23*D31+D13*D21*D32
1-D13*D22*D31-D21*D12*D33-D11*D32*D23
IF(DU.EQ.O.O)GO TO 68
DU=1./DU
GO TO 69
68 IF(INDEX.NE.1)GO TO 75
WRITE(PT,79)NE,ET,ZT,YP,(NODE(IL,I),XQ(I),
1YQ(I),ZQ(I),I=1,NN)
GO TO 75
C
C ESTIMATING THE DERIVATIVES OF THE SHAPE FUNCTION 'NI'
C WITH RESPECT TO THE X,Y,Z COORDINATE'S.

```

```

C      F(I) = DNI/DX  FY(I) = DNI/DY  FZ(I) = DNI/DZ
C
C      COMPUTING THE COFACTOR OF THE JACOBIAN MATRIX
C
69     COF1=(D22*D33-D23*D32)
        COF2=-(D21*D33-D23*D31)
        COF3=(D21*D32-D22*D31)
        COF4=-(D12*D33-D13*D32)
        COF5=(D11*D33-D13*D31)
        COF6=-(D11*D32-D12*D31)
        COF7=(D12*D23-D13*D22)
        COF8=-(D11*D23-D13*D21)
        COF9=(D11*D22-D12*D21)
C
        DO 70 I = 1,NN
        IF(NODE(IL,I).EQ.O)GO TO 70
        F(I) =DU*(AA1(I)*COF1+AA2(I)*COF4+AA3(I)*COF7)
        FY(I) =DU*(AA1(I)*COF2+AA2(I)*COF5+AA3(I)*COF8)
        FZ(I) =DU*(AA1(I)*COF3+AA2(I)*COF6+AA3(I)*COF9)
70     CONTINUE
C
        XJCOB = 1./DU
        DU = XJCOB*W
        II=0
C
71     DO 74 I = 1,NN
        IF(NODE(IL,I).EQ.O)GO TO 74
        II=II+1
        FA=F(I)*DU
        FB=FY(I)*DU
        FC=FZ(I)*DU
        SNI=SFV(I)
        SNIDU=SNI*DU
        SNI=SNI*W
        J2=0
C
        DO 73 J = 1,NN
        IF(NODE(IL,J).EQ.O)GO TO 73
        J2=J2+1
        FK=F(J)
        FYK=FY(J)
        FZK=FZ(J)
        SNJ=SFV(J)
        XIXJ=SNJ*SNIDU
        IJJ=(II-1)*NCUBE+J2
        SIKJO(IJJ)=SIKJO(IJJ)+XIXJ
        SIJ(IJJ)=SIJ(IJJ)+FA*FK
        SKJ(IJJ)=SKJ(IJJ)+FB*FYK
        SLJ(IJJ)=SLJ(IJJ)+FC*FZK
        WKX(IJJ)=WKX(IJJ)+SNIDU*FK
        WKY(IJJ)=WKY(IJJ)+SNIDU*FYK
        WKZ(IJJ)=WKZ(IJJ)+SNIDU*FZK
        KK=0
C
        DO 72 LO = 1,NN
        IF(NODE(IL,LO).EQ.O)GO TO 72
        KK=KK+1
        KIJ=(IJJ-1)*NCUBE+KK
        DNIDX(KIJ)=DNIDX(KIJ)+XIXJ*F(LO)
        DNIDY(KIJ)=DNIDY(KIJ)+XIXJ*FY(LO)
        DNIDZ(KIJ)=DNIDZ(KIJ)+XIXJ*FZ(LO)
72     CONTINUE
73     CONTINUE
C
        SILJC(II)=SILJC(II)+SNIDU
        IF(KX.NE.1)GO TO 74

```

```

C
19 KK = 0
   UO 20 J = 1,NN
   MATNO(J)=1
   K = NODE(IL,J)
   IF(K.EQ.O)GO TO 20
   KK=KK+1
   XQ(J)=X(K)
   YQ(J)=Y(K)
   ZQ(J)=Z(K)
   NODD(KK)=K
   MNO(KK) = MATNO(J)
20 CONTINUE
   NCUBE=KK

C
C   CHECKING AREA AND VOLUME OF EACH ELEMENT
C
   AREA(1) = (XQ(2)-XQ(1))*(YQ(4)-YQ(1))
   AREA(2) = (XQ(2)-XQ(1))*(ZQ(2)-ZQ(6))
   AREA(3) = (YQ(7)-YQ(6))*(ZQ(2)-ZQ(6))
   AREA(4) = (YQ(8)-YQ(5))*(XQ(6)-XQ(5))
   AREA(5) = (ZQ(4)-ZQ(8))*(XQ(7)-XQ(8))
   AREA(6) = (ZQ(1)-ZQ(5))*(YQ(8)-YQ(5))
   AREA1=AREA(1)+AREA(2)+AREA(3)
   AREA2=AREA(4)+AREA(5)+AREA(6)
27 IF((AREA1-AREA2).NE.O.O)GO TO 28
   VOLUME = (XQ(2)-XQ(1))*(YQ(3)-YQ(2))*(ZQ(1)-ZQ(5))
   GO TO 30
28 WRITE(PT,29)IL
30 DO 32 I=1,NCUBE
29 FORMAT(/12X,'ELEMENT NO. ',I3,' HAS NEGATIVE AREA')
32 SILJC(I) = 0.0
   NX2 = NCUBE*NCUBE
   DO 33 I = 1,NX2
   SIJ(I) = 0.0
   SKJ(I) = 0.0
   SLJ(I) = 0.0
   WKX(I) = 0.0
   WKY(I) = 0.0
   WKZ(I) = 0.0
   SIKJO(I) = 0.0
   DSFX(I) = 0.0
   DSFY(I) = 0.0
   DSFZ(I) = 0.0
33 CONTINUE
   NX3=NX2*NCUBE
   DO 34 I=1,NX3
   DNIDX(I)=0.0
   DNIDY(I)=0.0
   DNIDZ(I)=0.0
34 CONTINUE
   DO 35 I=1,3
35 AA(I)=1.DO
   THIRD=1.DO/3.DO
   THIRU2=2.DO/3.DO
   R964 =9.DO/64.DO
   R1972=19.DO/72.DO
   DO 75 KX =1,NORDER
   YP=GQPO(KX)
   WZ=GQWT(KX)
   DO 75 KT =1,NORDER
   ET=GQPO(KT)
   WS=GQWT(KT)*WZ
   DO 75 KN =1,NORDER
   ZT=GQPO(KN)
   W=WS*GQWT(KN)

```

```

      IF(KT.NF.1)GO TO 74
      IF(KN.NF.1)GO TO 74
      SNI-SFV(I)
      XX=XX+SNI*XQ(I)
      YY=YY+YQ(I)*SNI
      ZZ=ZZ+ZQ(I)*SNI
      WIAV-SIV(I)
      IF(NORDER.EQ.2)GO TO 74
      DSFXN(II)=F(I)
      DSFYN(II)=FY(I)
      DSI ZN(II)=I Z(I)
74  CONTINUE
75  CONTINUE
      ET =0.
      ZT =0.
      YP =0
      II = 1
C
      CALL GLOBAL(NCUBE,II)
79  FORMAT(////,I3,5X,3F11.4/(40X,I2,3F11.4))
80  CONTINUE
      RETURN
      END
C
      .....
      SUBROUTINE GLOBAL(NCUBE,II)
C
C      PURPOSE: THIS SUBROUTINE ASSEMBLE ELEMENT MATRICES INTO THE
C      GLOBAL SYSTEM
C      .....
C
      IMPLICIT REAL*8 (A-H,O-Z)
      COMMON /SUBA/SIJ(400),SKJ(400),SLJ(400),SMJ(400),SWJ(400),
      ISIJ(400),SIKJO(200),SILJC(200),DNIDX(2000),DNIDY(2000),
      2DNIDZ(2000),WKX(400),WKY(400),WKZ(400),DXX(400),DYY(400),
      3DZZ(400),VLX(400),VLY(400),VLZ(400),XQ(8),YQ(8),ZQ(8),AA(3)
      COMMON /SUBB/AA1(8),AA2(8),AA3(8),DSFXN(64),DSFYN(64),
      1DSFZN(64),DSFX(64),DSFY(64),DSFZ(64),ETA(36),PHY(36),
      2ZETA(64),SA(6),SFV(8),FX(8),FY(8),FZ(8),F(24),G(24),H(24),
      3GUPU(5),GUPV(5),SS(6),DD(6),NUDD(8),MATNU(8),MNU(8)
      COMMON /SUBC/SIOMX(400,400),P(400,400),R(400,400)
      COMMON /SUBD/GLORMX(400,400),RMX(400),RECT(400)
      COMMON /SUBF/C(400),CINT(400),COLD(400),QW(400),BCD(8)
C
      DO 5 I = 1,NCUBE
      DO 5 J = 1,NCUBE
      TA=WKX(II)*VLX(NUDD(J))+WKY(II)*VLY(NUDD(J))+WKZ(II)*(NUDD(J))
      TB=DNIDX(II)*VLX(NUDD(J))+DNIDY(II)*VLY(NUDD(J))+DNIDZ(II)*VLZ(
      1NUDD(J))
      TC=SIJ(II)*DXX(NUDD(J))+SLJ(II)*DYY(NUDD(J))+SKJ(II)*DZZ(NUDD(J))
      P(I,J)=TA+TB+TC
      COEFF=1
      R(I,J)=COEFF*SIKJO(II)
      II =II+1
      GLORMX(NUDD(I),NUDD(J))=GLORMX(NUDD(I),NUDD(J))+P(I,J)
      STOMX(NUDD(I),NUDD(J))=STOMX(NUDD(I),NUDD(J))+R(I,J)
      RMX(NUDD(I)) = RMX(NUDD(I))+SILJC(I)*QW(NUDD(I))
5  CONTINUE
      RETURN
      END
C
      .....
      SUBROUTINE BOUND(MXNOD,DELT,NDBC,NSTEDY)
C
C      PURPOSE: THIS SUBROUTINE MODIFIES THE GLOBAL MATRIX WITH KNOWN
C      BOUNDARY CONDITIONS
C      .....
C

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```

      IMPLICIT REAL*8 (A-H,O-Z)
      COMMON /SUBC/STOMX(400,400),P(400,400),R(400,400)
      COMMON /SUBD/GLOBMX(400,400),RMX(400),RECT(400)
      COMMON /SUBF/C(400),CINT(400),COLD(400),QW(400),BCD(8)
      COMMON /SUBG/ID(400),ND(400)
C-----
C
      DO 5 I = 1,MXNOD
      DO 5 J = 1,MXNOD
      STOMX(I,J) = STOMX(I,J)/DEL I
      GLOBMX(I,J) = GLOBMX(I,J)+FAC I*STOMX(I,J)
5     CONTINUE
      DO 25 I = 1,NIDBC
      IF (ID(ND(I)) NE 1)GO TO 20
      DO 15 J = 1,MXNOD
      IF (J EQ ND(I))GO TO 10
      GLOBMX(ND(I),J) = 0.0
C
      RMX(J) = RMX(J)+GLOBMX(J,ND(I))*CINT(ND(I))
      GLOBMX(J,ND(I)) = 0.0
      GO TO 15
10    RMX(J) = GLOBMX(ND(I),ND(I))*CINT(ND(I))
15    CONTINUE
      GO TO 25
20    IF (ID(ND(I)).NE.0)GO TO 25
C
      RMX(ND(I)) = RMX(ND(I))+BCD(ND(I))
25    CONTINUE
      DO 30 KS = 1,MXNOD
30    COLD(KS) = CINT(KS)
      RETURN
      END
C
      *****
      SUBROUTINE WIDTHI(BANDW,IROW,MXNOD)
C
C     PURPOSE:THIS SUBROUTINE CALCULATES THE BANDWIDTH OF THE
C     GLOBAL MATRIX .
C     *****
      IMPLICIT REAL*8 (A-H,O-Z)
      COMMON /SUBD/GLOBMX(400,400),RMX(400),RECT(400)
      COMMON /SUBC/STOMX(400,400),P(400,400),R(400,400)
      MAX = 0
      DO 10 I = 1,MXNOD
      DO 5 J = 1,MXNOD
      IF (GLOBMX(I,J).EQ.0.0)GO TO 5
      BANDW = J-I
      IF (BANDW LE MAX)GO TO 5
      MAX = BANDW
      IROW = I
5     CONTINUE
      BANDW = 0
10    CONTINUE
      BANDW = MAX
      BANDW = BANDW+1
      DO 20 I = 1,MXNOD
      DO 15 J = 1,BANDW
      IF (I+J-1.GT.MXNOD)GO TO 30
      GLOBMX(I,J) = GLOBMX(I,I+J-1)
      STOMX(I,J) = STOMX(I,I+J-1)
15    CONTINUE
20    CONTINUE
      RETURN
      END
C
      *****
      SUBROUTINE ADJUST(MXNOD,BANDW)
C

```



```

C      PURPOSE: THIS SUBROUTINE DECOMPOSES THE MATRIX INTO AN UPPER
C      TRIANGULAR MATRIX USING THE GAUSSIAN ELEMINATION PROCEDURES.
C      .....
C
      IMPLICIT REAL*8 (A-H,O-Z)
      COMMON /SUBD/GLORMX(400,400),RMX(400),RECT(400)
      KA = MXNOD-1
      DO 15 I=1,KA
      KB = I+BANDW-1
      IF(KB.GT.MXNOD)KB=MXNOD
      KC = I+1
      KD = BANDW
      IF((MXNOD-I+1).LT.BANDW)KD=MXNOD-I+1
      KE = 0
      DO 10 J= KC,KB
      KD = KD-1
      KE = KE+1
      KF = KE+1
      EM=GLOBMX(I,KF)/GLOBMX(I,I)
      IF(EM.EQ.O.O)GO TO 10
      DO 5 K=1,KD
      KG = KC+K
      5  GLOBMX(J,K)=GLOBMX(J,K)-EM*GLOBMX(I,KF)
      10 CONTINUE
      15 CONTINUE
      RETURN
      END
C      .....
C      SUBROUTINE RIGHTV(MXNOD,BANDW)
C
C      PURPOSE: THIS SUBROUTINE GENERATE RECT VECTOR AT EACH
C      TIME STEPS.
C      .....
C
      IMPLICIT REAL*8 (A-H,O-Z)
      COMMON /SUBC/STOMX(400,400),P(400,400),R(400,400)
      COMMON /SUBD/GLORMX(400,400),RMX(400),RECT(400)
      COMMON /SUBF/C(400),CINT(400),COLD(400),QW(400),BCD(8)
      DO 15 I=1, MXNOD
      SUM=0.0
      K=I-1
      DO 10 J=2,BANDW
      M=J+I-1
      IF(M.GT.MXNOD) GO TO 5
      SUM=SUM+STOMX(I,J)*COLD(M)
      5  IF(K.LE.O) GO TO 10
      SUM=SUM+STOMX(K,J)*COLD(K)
      K=K-1
      10 CONTINUE
      15 RECT(I)=SUM+STOMX(I,1)*COLD(I)
      RETURN
      END
C      .....
C      SUBROUTINE SOLVER(MXNOD,BANDW,NDBC)
C
C      PURPOSE: THIS SUBROUTINE SOLVES THE SYSTEM EQUATIONS
C      USING BACKWARD SUBSTITUTION.
C      .....
C
      IMPLICIT REAL*8 (A-H,O-Z)
      COMMON /SUBC/STOMX(400,400),P(400,400),R(400,400)
      COMMON /SUBD/GLORMX(400,400),RMX(400),RECT(400)
      COMMON /SUBF/C(400),CINT(400),COLD(400),QW(400),BCD(8)
      COMMON /SUBG/ID(400),ND(400)
      KA = MXNOD-1
      DO 5 I=1,KA

```

```

      KR = I+BANDW-1
      II (KB.GT.MXNOD)KB-MXNOD
      KC = I+1
      L-1
      DO 5 J = NJ,MJ
      L L,1
      RECT(J)=RECT(J)-GLOBMX(I,L)*RECT(I)/GLOBMX(I,1)
5     CONTINUE
      C(MXNOD) = RECT(MXNOD)/GLOBMX(MXNOD,1)
      DO 15 K=1,KA
      I = MXNOD-K
      KB = BANDW
      IF((I+BANDW-1).GT.MXNOD)KB=MXNOD-I+1
      SUM = 0.0
      DO 10 J=2,KB
      N = I+J-1
      IF(N.GT.MXNOD)GO TO 15
10     SUM=SUM+GLOBMX(I,J)*C(N)
15     C(I) = (RECT(I)-SUM)/GLOBMX(I,1)
      DO 25 I=1,MXNOD
      DO 20 JK=1,NDBC
      IF (ND(JK).EQ.I)C(I)=CINI(I)
20     CONTINUE
25     CONTINUE
C     RETURN
      END
$ENTRY
$IBSYS
//

```

APPENDIX B
GUIDE FOR DATA INPUT

This group of cards, which are read by the main program and input subroutine, contains data required to dimension the model. The reader should refer to Appendix A for the definition of the variables.

Card	Column	Format	Variable
1	1-4	I4	NELMS
	5-8	I4	MNOPE
	9-12	I4	NSTEDY
	13-16	I4	NDBC
	17-26	F10.2	DELT
2	1-11	nD11.3	VLX(I)
	12-23	nD11.3	VLX(I)
	24-34	nD11.3	VLZ(I)
3	1-11	nD11.3	DXX(I)
	12-23	nD11.3	DYY(I)
	24-34	nD11.3	DZZ(I)
4	1-4	I4	NWELLS
	5-8	I4	NPERS
	9-12	I4	NOMAT
	13-16	I4	NCE
	17-20	I4	IT
	21-30	F10.5	FACT
	31-40	F10.5	FACTA
5	1-10	D10.2	X(I)
	11-20	D10.2	Y(I)
	21-30	D10.2	Z(I)
	31-40	D10.2	QW(I)
	41-50	D10.2	CMT(I)

6	1-4	I 4	NE
	5-40	8 I 4	NODE(I, J)
7	1-40	20 I 4	ND(I)
8	1-80	40 I 2	ID(I)

Note: Cards 2 and 3, with no specification, depend on how many nodes, one set for each node is needed for each card. For card 5, each element requires a card. For cards 7 and 8, if nodes are more than specified in the above table, an additional card is required.

APPENDIX C

INPUT/OUTPUT OF ONE-DIMENSIONAL TESTING
20, 50, 70, AND 100 ELEMENT TESTINGS

20 Elements

INPUT DATA FOR THREE-DIMENSIONAL
 GROUNDWATER DISP BY FINITE ELEMENT METHOD

TOTAL NO OF ELEMENTS : 20
 TOTAL NO OF NODES : 60
 MAXIMUM NO OF NODES PER ELEMENT : 8
 TOTAL NO OF MATERIALS : 1
 NUMBER OF PUMPING WELLS : 0
 NUMBER OF CONC'S TO BE ESTIMATED : 54

NUMBER OF PUMPING PERIODS : 0
 TOTAL SIMULATION PERIODS : 5
 FACTOR MULTIPLYING COMPUTED CONC'S : 1.00000

STEP SIZE : 10.00000
 STATE OF PROBLEM : 1
 NO OF SPECIFIED CONDITIONS : 36

MID-ELEMENT RELATIONSHIP

ELEMS	N1	N2	N3	N4	N5	N6	N7	N8
1	7	1	2	8	37	31	32	38
2	8	2	3	9	38	32	33	39
3	9	3	4	10	39	33	34	40
4	10	4	5	11	40	34	35	41
5	11	5	6	12	41	35	36	42
6	13	7	8	14	43	37	38	44
7	14	8	9	15	44	38	39	45
8	15	9	10	16	45	39	40	46
9	16	10	11	17	46	40	41	47
10	17	11	12	18	47	41	42	48
11	19	13	14	20	49	43	44	50
12	20	14	15	21	50	44	45	51
13	21	15	16	22	51	45	46	52
14	22	16	17	23	52	46	47	53
15	23	17	18	24	53	47	48	54
16	25	19	20	26	55	49	50	56
17	26	20	21	27	56	50	51	57
18	27	21	22	28	57	51	52	58
19	28	22	23	29	58	52	53	59
20	29	23	24	30	59	53	54	60

FIXED BOUNDARY CONDITIONS

NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID
1	0	2	0	3	0	4	0	5	0
6	0	7	0	8	0	9	0	10	0
19	1	24	0	28	0	28	0	27	0
28	0	29	0	30	0	31	0	32	0
33	0	34	0	35	0	36	0	37	1
42	0	43	1	48	0	49	1	54	0
55	0	56	0	57	0	58	0	59	0
60	0								

MAXIMUM BANDWIDTH = 38 ON ROW NO 1

OUTPUT FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENTS METHOD

INITIAL CONC DISTRIBUTION AT TIME = 0.000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000 00	2	0.0000 00	3	0.0000 00	4	0.0000 00	5	0.0000 00	6	0.0000 00
8	0.0000 00	7	0.0000 00	8	0.0000 00	9	0.0000 00	10	0.0000 00	11	0.0000 00
14	0.0000 00	13	0.0000 00	14	0.0000 00	15	0.0000 00	16	0.0000 00	17	0.0000 00
20	0.0000 00	19	0.0000 00	20	0.0000 00	21	0.0000 00	22	0.0000 00	23	0.0000 00
26	0.0000 00	25	0.0000 00	26	0.0000 00	27	0.0000 00	28	0.0000 00	29	0.0000 00
31	0.0000 00	30	0.0000 00	31	0.0000 00	32	0.0000 00	33	0.0000 00	34	0.0000 00
36	0.0000 00	35	0.0000 00	36	0.0000 00	37	0.0000 00	38	0.0000 00	39	0.0000 00
41	0.0000 00	40	0.0000 00	41	0.0000 00	42	0.0000 00	43	0.0000 00	44	0.0000 00
46	0.0000 00	45	0.0000 00	46	0.0000 00	47	0.0000 00	48	0.0000 00	49	0.0000 00
51	0.0000 00	50	0.0000 00	51	0.0000 00	52	0.0000 00	53	0.0000 00	54	0.0000 00
56	0.0000 00	55	0.0000 00	56	0.0000 00	57	0.0000 00	58	0.0000 00	59	0.0000 00

INITIAL CONC DISTRIBUTION AT TIME = 10.000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000 00	2	0.0000 00	3	0.4730-03	4	0.3000-03	5	0.1700-03	6	0.1700-03
8	0.0000 00	7	0.1000 01	8	0.6610 00	9	0.5780 00	10	0.5140 00	11	0.5140 00
14	0.4810 00	13	0.4040 00	14	0.1000 01	15	0.3080 00	16	0.2480 00	17	0.2480 00
20	0.5780 00	19	0.5390-01	20	0.1840-01	21	0.1000 01	22	0.8510 00	23	0.8510 00
26	0.0000 00	25	0.5140 00	26	0.4810 00	27	0.4040 00	28	0.0000 00	29	0.0000 00
31	0.0000 00	30	0.4700-03	31	0.5000-03	32	0.1700-02	33	0.0000 00	34	0.0000 00
36	0.0000 00	35	0.0000 00	36	0.4730-03	37	0.5000-03	38	0.5000-03	39	0.5000-03
41	0.0000 00	40	0.1000 01	41	0.6610 00	42	0.5780 00	43	0.5140 00	44	0.5140 00
46	0.4810 00	45	0.4040 00	46	0.1000 01	47	0.3080 00	48	0.2480 00	49	0.2480 00
51	0.5780 00	50	0.5390-01	51	0.1840-01	52	0.1000 01	53	0.8510 00	54	0.8510 00
56	0.0000 00	55	0.5140 00	56	0.4810 00	57	0.4040 00	58	0.0000 00	59	0.0000 00

INITIAL CONC DISTRIBUTION AT TIME = 20.000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000	2	0.1140	3	0.2910	4	0.3600	5	0.3290
6	0.2440	7	0.1000	8	0.7240	9	0.6700	10	0.4000
11	0.5710	12	0.5880	13	0.1000	14	0.6900	15	0.5000
16	0.2760	17	0.1710	18	0.1010	19	0.1000	20	0.2440
21	0.6740	22	0.6180	23	0.5710	24	0.5500	25	0.6600
26	0.1140	27	0.2910	28	0.3600	29	0.3290	30	0.4000
31	0.0000	32	0.1140	33	0.2910	34	0.3600	35	0.3290
36	0.2440	37	0.1000	38	0.7240	39	0.6700	40	0.4000
41	0.5710	42	0.5880	43	0.1000	44	0.6900	45	0.5000
46	0.2760	47	0.1710	48	0.1010	49	0.1000	50	0.2440
51	0.6740	52	0.6180	53	0.5710	54	0.5500	55	0.6600
56	0.1140	57	0.2910	58	0.3600	59	0.3290	60	0.4000

INITIAL CONC DISTRIBUTION AT TIME = 30.000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000	2	0.2320	3	0.5480	4	0.7230	5	0.7360
6	0.6490	7	0.1000	8	0.7620	9	0.7290	10	0.6880
11	0.6450	12	0.6230	13	0.1000	14	0.7250	15	0.4840
16	0.3560	17	0.2530	18	0.1800	19	0.1000	20	0.7620
21	0.7290	22	0.6880	23	0.6450	24	0.6250	25	0.0000
26	0.2320	27	0.5480	28	0.7230	29	0.7360	30	0.6490
31	0.0000	32	0.2320	33	0.5480	34	0.7230	35	0.7360
36	0.6190	37	0.1000	38	0.7620	39	0.7290	40	0.6880
41	0.6450	42	0.6230	43	0.1000	44	0.7250	45	0.4840
46	0.3560	47	0.2530	48	0.1800	49	0.1000	50	0.7620
51	0.7290	52	0.6880	53	0.6450	54	0.6250	55	0.0000
56	0.2320	57	0.5480	58	0.7230	59	0.7360	60	0.6490

INITIAL CONC DISTRIBUTION AT TIME = 40.000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000	2	0.2400-01	3	0.7620-01	4	0.1040	5	0.1040	6	0.1130
6	0.1090	7	0.1000	8	0.7490	9	0.7700	10	0.7700	11	0.7400
11	0.7050	12	0.6840	13	0.1000	14	0.6990	15	0.6990	16	0.5250
16	0.4070	17	0.2410	18	0.2410	19	0.1000	20	0.1000	21	0.7840
21	0.7700	22	0.7400	23	0.7050	24	0.6840	25	0.6840	26	0.0000
26	0.3400-01	27	0.7620-01	28	0.1040	29	0.1040	30	0.1130	31	0.1090
31	0.0000	32	0.2400-01	33	0.7490	34	0.7700	35	0.7700	36	0.7400
36	0.1090	37	0.1000	38	0.7490	39	0.7700	40	0.7400	41	0.5250
41	0.7050	42	0.6840	43	0.1000	44	0.6990	45	0.6990	46	0.7840
46	0.4070	47	0.2410	48	0.2410	49	0.1000	50	0.1000	51	0.7400
51	0.7700	52	0.7400	53	0.7050	54	0.6840	55	0.6840	56	0.0000
56	0.3400-01	57	0.7620-01	58	0.1040	59	0.1040	60	0.1130		

INITIAL CONC DISTRIBUTION AT TIME = 80.000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000	2	0.4330-01	3	0.9450-01	4	0.1310	5	0.1310	6	0.1470
6	0.1500	7	0.1000	8	0.8430	9	0.8010	10	0.8010	11	0.7820
11	0.7550	12	0.7340	13	0.1000	14	0.6930	15	0.6930	16	0.5540
16	0.4460	17	0.3590	18	0.2970	19	0.1000	20	0.1000	21	0.8430
21	0.8010	22	0.7820	23	0.7550	24	0.7340	25	0.7340	26	0.0000
26	0.4330-01	27	0.9450-01	28	0.1310	29	0.1310	30	0.1450	31	0.1500
31	0.0000	32	0.4330-01	33	0.9450-01	34	0.1310	35	0.1310	36	0.1470
36	0.1500	37	0.1000	38	0.8430	39	0.8010	40	0.8010	41	0.7820
41	0.7550	42	0.7340	43	0.1000	44	0.6930	45	0.6930	46	0.5540
46	0.4460	47	0.3590	48	0.2970	49	0.1000	50	0.1000	51	0.8430
51	0.8010	52	0.7820	53	0.7550	54	0.7340	55	0.7340	56	0.0000
56	0.4330-01	57	0.9450-01	58	0.1310	59	0.1310	60	0.1450		

50 Elements

INPUT DATA FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENT METHOD

TOTAL NO OF ELEMENTS • 50
 TOTAL NO OF NODES • 152
 TOTAL NO OF EDGES PER ELEMENT • 6
 TOTAL NO OF MATERIALS • 1
 NUMBER OF PUMPING WELLS • 0
 NUMBER OF CONCS TO BE ESTIMATED • 124

NUMBER OF PUMPING PERIODS • 0
 TOTAL SIMULATION PERIODS • 5
 FACTOR MULTIPLYING COMPUTED CONCS • 1 00000

STEP SIZE • 10 00000
 STATE OF PROBLEM • 1
 NO OF SPECIFIED CONDITIONS • 60

COORDINATES AND INITIAL CONCS OF NODES (L)

NODES	Y(I)	X(I)	Z(I)	CINT(I)
1	0.000 00	0.000 00	0.100 03	0.000 00
2	0.100 03	0.000 00	0.100 03	0.000 00
3	0.200 02	0.000 00	0.100 03	0.000 00
4	0.300 01	0.000 00	0.100 03	0.000 00
5	0.400 01	0.000 00	0.100 03	0.000 00
6	0.500 01	0.000 00	0.100 03	0.000 00
7	0.600 01	0.000 00	0.100 03	0.000 00
8	0.700 02	0.000 00	0.100 03	0.000 00
9	0.800 02	0.000 00	0.100 03	0.000 00
10	0.900 02	0.000 00	0.100 03	0.000 00
11	0.100 03	0.000 00	0.100 03	0.000 00
12	0.000 00	0.200 02	0.100 03	0.100 01
13	0.100 02	0.200 02	0.100 03	0.000 00
14	0.200 02	0.200 02	0.100 03	0.000 00
15	0.300 02	0.200 02	0.100 03	0.000 00
16	0.400 02	0.200 02	0.100 03	0.000 00
17	0.500 02	0.200 02	0.100 03	0.000 00
18	0.600 02	0.200 02	0.100 03	0.000 00
19	0.700 02	0.200 02	0.100 03	0.000 00
20	0.800 02	0.200 02	0.100 03	0.000 00
21	0.900 02	0.200 02	0.100 03	0.000 00
22	0.000 00	0.200 02	0.100 03	0.000 00
23	0.100 02	0.350 01	0.100 03	0.000 00
24	0.200 02	0.350 01	0.100 03	0.000 00
25	0.300 02	0.350 01	0.100 03	0.000 00
26	0.400 02	0.350 01	0.100 03	0.000 00
27	0.500 02	0.350 01	0.100 03	0.000 00
28	0.600 02	0.350 01	0.100 03	0.000 00
29	0.700 02	0.350 01	0.100 03	0.000 00
30	0.800 02	0.350 01	0.100 03	0.000 00
31	0.900 02	0.350 01	0.100 03	0.000 00
32	0.000 00	0.350 01	0.100 03	0.000 00
33	0.100 03	0.400 02	0.100 03	0.000 00
34	0.200 02	0.400 02	0.100 03	0.100 01
35	0.300 02	0.400 02	0.100 03	0.000 00
36	0.400 02	0.400 02	0.100 03	0.000 00
37	0.500 02	0.400 02	0.100 03	0.000 00
38	0.600 02	0.400 02	0.100 03	0.000 00
39	0.700 02	0.400 02	0.100 03	0.000 00
40	0.800 02	0.400 02	0.100 03	0.000 00
41	0.900 02	0.400 02	0.100 03	0.000 00
42	0.000 00	0.400 02	0.100 03	0.000 00
43	0.100 03	0.500 02	0.100 03	0.000 00
44	0.200 02	0.500 02	0.100 03	0.100 01
45	0.300 02	0.500 02	0.100 03	0.000 00
46	0.400 02	0.500 02	0.100 03	0.000 00
47	0.500 02	0.500 02	0.100 03	0.000 00

NODE - ELEMENT RELATIONSHIP

ELEMS	N1	N2	N3	N4	N5	N6	N7	N8
1	1	3	13	12	67	68	79	78
2	2	3	14	13	68	69	80	79
3	3	4	15	14	69	70	81	80
4	4	5	16	15	70	71	82	81
5	5	6	17	16	71	72	83	82
6	6	7	18	17	72	73	84	83
7	7	8	19	18	73	74	85	84
8	8	9	20	19	74	75	86	85
9	9	10	21	20	75	76	87	86
10	10	11	22	21	76	77	88	87
11	11	12	23	22	77	78	89	88
12	12	13	24	23	78	79	90	89
13	13	14	25	24	79	80	91	90
14	14	15	26	25	80	81	92	91
15	15	16	27	26	81	82	93	92
16	16	17	28	27	82	83	94	93
17	17	18	29	28	83	84	95	94
18	18	19	30	29	84	85	96	95
19	19	20	31	30	85	86	97	96
20	20	21	32	31	86	87	98	97
21	21	22	33	32	87	88	99	98
22	22	23	34	33	88	89	100	99
23	23	24	35	34	89	90	101	100
24	24	25	36	35	90	91	102	101
25	25	26	37	36	91	92	103	102
26	26	27	38	37	92	93	104	103
27	27	28	39	38	93	94	105	104
28	28	29	40	39	94	95	106	105
29	29	30	41	40	95	96	107	106
30	30	31	42	41	96	97	108	107
31	31	32	43	42	97	98	109	108
32	32	33	44	43	98	99	110	109
33	33	34	45	44	99	100	111	110
34	34	35	46	45	100	101	112	111
35	35	36	47	46	101	102	113	112
36	36	37	48	47	102	103	114	113
37	37	38	49	48	103	104	115	114
38	38	39	50	49	104	105	116	115
39	39	40	51	50	105	106	117	116
40	40	41	52	51	106	107	118	117
41	41	42	53	52	107	108	119	118
42	42	43	54	53	108	109	120	119
43	43	44	55	54	109	110	121	120
44	44	45	56	55	110	111	122	121
45	45	46	57	56	111	112	123	122
46	46	47	58	57	112	113	124	123
47	47	48	59	58	113	114	125	124
48	48	49	60	59	114	115	126	125
49	49	50	61	60	115	116	127	126
50	50	51	62	61	116	117	128	127

 OUTPUT FOR THREE-DIMENSIONAL
 GROUNDWATER DISP BY FINITE ELEMENTS METHOD

INITIAL CONC DISTRIBUTION AT TIME = 0.000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000 00	2	0.0000 00	3	0.0000 00	4	0.0000 00	5	0.0000 00
6	0.0000 00	7	0.0000 00	8	0.0000 00	9	0.0000 00	10	0.0000 00
11	0.0000 00	12	0.0000 00	13	0.0000 00	14	0.0000 00	15	0.0000 00
16	0.0000 00	17	0.0000 00	18	0.0000 00	19	0.0000 00	20	0.0000 00
21	0.0000 00	22	0.0000 00	23	0.0000 00	24	0.0000 00	25	0.0000 00
26	0.0000 00	27	0.0000 00	28	0.0000 00	29	0.0000 00	30	0.0000 00
31	0.0000 00	32	0.0000 00	33	0.0000 00	34	0.0000 00	35	0.0000 00
36	0.0000 00	37	0.0000 00	38	0.0000 00	39	0.0000 00	40	0.0000 00
41	0.0000 00	42	0.0000 00	43	0.0000 00	44	0.0000 00	45	0.0000 00
46	0.0000 00	47	0.0000 00	48	0.0000 00	49	0.0000 00	50	0.0000 00
51	0.0000 00	52	0.0000 00	53	0.0000 00	54	0.0000 00	55	0.0000 00
56	0.0000 00	57	0.0000 00	58	0.0000 00	59	0.0000 00	60	0.0000 00
61	0.0000 00	62	0.0000 00	63	0.0000 00	64	0.0000 00	65	0.0000 00
66	0.0000 00	67	0.0000 00	68	0.0000 00	69	0.0000 00	70	0.0000 00
71	0.0000 00	72	0.0000 00	73	0.0000 00	74	0.0000 00	75	0.0000 00
76	0.0000 00	77	0.0000 00	78	0.0000 00	79	0.0000 00	80	0.0000 00
81	0.0000 00	82	0.0000 00	83	0.0000 00	84	0.0000 00	85	0.0000 00
86	0.0000 00	87	0.0000 00	88	0.0000 00	89	0.0000 00	90	0.0000 00
91	0.0000 00	92	0.0000 00	93	0.0000 00	94	0.0000 00	95	0.0000 00
96	0.0000 00	97	0.0000 00	98	0.0000 00	99	0.0000 00	100	0.0000 00
101	0.0000 00	102	0.0000 00	103	0.0000 00	104	0.0000 00	105	0.0000 00
106	0.0000 00	107	0.0000 00	108	0.0000 00	109	0.0000 00	110	0.0000 00
111	0.0000 00	112	0.0000 00	113	0.0000 00	114	0.0000 00	115	0.0000 00
116	0.0000 00	117	0.0000 00	118	0.0000 00	119	0.0000 00	120	0.0000 00
121	0.0000 00	122	0.0000 00	123	0.0000 00	124	0.0000 00	125	0.0000 00
126	0.0000 00	127	0.0000 00	128	0.0000 00	129	0.0000 00	130	0.0000 00
131	0.0000 00	132	0.0000 00						

CONC DISTRIBUTION AT TIME = 10 0070 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000 00	2	0.0000 00	3	0.0000 00	4	0.0000 00	5	0.3500-02	6	0.3500-02	7	0.3500-02
6	0.6300-02	7	0.8460-02	8	0.3870-02	9	0.7180-02	10	0.1850-02	11	0.7230 00	12	0.7230 00
11	0.0000 00	12	0.1000 01	13	0.3700 00	14	0.5370 00	15	0.7120 00	16	0.5010 00	17	0.5010 00
16	0.6120 00	17	0.3700 01	18	0.4770 00	19	0.1000 01	20	0.7010 00	21	0.5550 00	22	0.5550 00
21	0.4840 00	22	0.4770 00	23	0.2050 00	24	0.2130 00	25	0.1430 00	26	0.8080-01	27	0.8080-01
26	0.4170 00	27	0.2050 00	28	0.2740-01	29	0.5100-03	30	0.1000 01	31	0.6880 00	32	0.6880 00
31	0.9550-01	32	0.2740-01	33	0.3980 00	34	0.2880 00	35	0.1000 01	36	0.1340 00	37	0.1340 00
36	0.9350 00	37	0.3980 00	38	0.5180-01	39	0.2880-01	40	0.1590-01	41	0.1000 01	42	0.1000 01
41	0.8530-01	42	0.5180-01	43	0.7230 00	44	0.8010 00	45	0.6120 00	46	0.4770 00	47	0.4770 00
46	0.7780 00	47	0.7230 00	48	0.9120 00	49	0.8010 00	50	0.4840 00	51	0.9300-03	52	0.9300-03
51	0.5370 00	52	0.9120 00	53	0.0000 00	54	0.0000 00	55	0.3500-02	56	0.3500-02	57	0.3500-02
56	0.0000 00	57	0.0000 00	58	0.0000 00	59	0.0000 00	60	0.0000 00	61	0.1850-02	62	0.1850-02
61	0.6300-02	62	0.9460-02	63	0.3070-02	64	0.3670-02	65	0.0000 00	66	0.0000 00	67	0.0000 00
66	0.0000 00	67	0.0000 00	68	0.3070-02	69	0.3670-02	70	0.0000 00	71	0.3500-03	72	0.3500-03
71	0.3340-02	72	0.6300-02	73	0.8460-02	74	0.3070-02	75	0.3670-02	76	0.1850-02	77	0.1850-02
76	0.9300-03	77	0.6300-02	78	0.0000 00	79	0.1000 01	80	0.7780 00	81	0.7230 00	82	0.7230 00
81	0.6600 00	82	0.0000 00	83	0.1000 01	84	0.3070 00	85	0.5370 00	86	0.7230 00	87	0.7230 00
86	0.5010 00	87	0.8120 00	88	0.4840 00	89	0.3070 00	90	0.1000 01	91	0.7010 00	92	0.7010 00
91	0.5550 00	92	0.4170 00	93	0.4840 00	94	0.3070 00	95	0.2120 00	96	0.1430 00	97	0.1430 00
96	0.9080-01	97	0.9550-01	98	0.4170 00	99	0.2740-01	100	0.5100-03	101	0.1000 01	102	0.1000 01
101	0.6880 00	102	0.9550-01	103	0.3880 00	104	0.3880 00	105	0.2880 00	106	0.2010 00	107	0.2010 00
106	0.1340 00	107	0.8120 00	108	0.5180-01	109	0.5180-01	110	0.2880-01	111	0.1590-01	112	0.1590-01
111	0.1000 01	112	0.8120 00	113	0.5180-01	114	0.7230 00	115	0.6000 00	116	0.6120 00	117	0.6120 00
116	0.5700 00	117	0.5370 00	118	0.5370 00	119	0.5120 00	120	0.5010 00	121	0.4840 00	122	0.4840 00
121	0.4770 00	122	0.0000 00	123	0.0000 00	124	0.0000 00	125	0.0000 00	126	0.3500-02	127	0.3500-02
126	0.5340-02	127	0.0000 00	128	0.5460-02	129	0.5460-02	130	0.3670-02	131	0.3670-02	132	0.3670-02
131	0.9300-03	132	0.0000 00	133	0.0000 00	134	0.0000 00	135	0.0000 00	136	0.0000 00	137	0.0000 00

CONC DISTRIBUTION AT TIME = 20.000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000 00	2	0.2600-02	3	0.1230-01	4	0.2210-01	5	0.3050-01	6	0.2800-01
6	0.3620-01	7	0.3750-01	8	0.3680-01	9	0.3350-01	10	0.7410 00	11	0.7410 00
11	0.2340-01	12	0.1000 01	13	0.8400 00	14	0.7830 00	15	0.5810 00	16	0.5810 00
16	0.7050 00	17	0.8700 00	18	0.3260 00	19	0.6050 00	20	0.6430 00	21	0.6430 00
21	0.5350 00	22	0.5350 00	23	0.1000 01	24	0.2840 00	25	0.2230 00	26	0.2230 00
26	0.1730 00	27	0.4400 00	28	0.3560 00	29	0.1000 01	30	0.7390 00	31	0.7390 00
31	0.1730 00	32	0.4380 00	33	0.8740-01	34	0.1000 01	35	0.2690 00	36	0.2690 00
36	0.6190 00	37	0.5180 00	38	0.8740-01	39	0.3280 00	40	0.1000 01	41	0.1000 01
41	0.2120 00	42	0.6850 00	43	0.1240 00	44	0.9730-01	45	0.6700 00	46	0.6700 00
46	0.8400 00	47	0.7830 00	48	0.7410 00	49	0.7050 00	50	0.5360 00	51	0.5360 00
51	0.6360 00	52	0.6050 00	53	0.5910 00	54	0.5560 00	55	0.3050-01	56	0.3050-01
56	0.0000 00	57	0.2600-02	58	0.1230-01	59	0.2210-01	60	0.2080-01	61	0.2080-01
61	0.2340-01	62	0.3750-01	63	0.3680-01	64	0.3350-01	65	0.7410 00	66	0.7410 00
66	0.3050-01	67	0.0000 00	68	0.2600-02	69	0.1230-01	70	0.2210-01	71	0.2210-01
71	0.2800-01	72	0.3620-01	73	0.3750-01	74	0.3680-01	75	0.3350-01	76	0.3350-01
76	0.7410 00	77	0.2240-01	78	0.1000 01	79	0.8400 00	80	0.7830 00	81	0.7830 00
81	0.2810 00	82	0.7050 00	83	0.6700 00	84	0.6360 00	85	0.6050 00	86	0.6050 00
86	0.5810 00	87	0.8560 00	88	0.4400 00	89	0.1000 01	90	0.2840 00	91	0.2840 00
91	0.4430 00	92	0.8350 00	93	0.4200 00	94	0.3560 00	95	0.7540 00	96	0.7540 00
96	0.2230 00	97	0.1730 00	98	0.1380 00	99	0.8740-01	100	0.1000 01	101	0.1000 01
101	0.7390 00	102	0.6190 00	103	0.5100 00	104	0.4180 00	105	0.3280 00	106	0.3280 00
106	0.2690 00	107	0.2120 00	108	0.1650 00	109	0.1240 00	110	0.9730-01	111	0.9730-01
111	0.1000 01	112	0.8400 00	113	0.7830 00	114	0.7410 00	115	0.7050 00	116	0.7050 00
116	0.6700 00	117	0.6400 00	118	0.6050 00	119	0.5810 00	120	0.5560 00	121	0.5560 00
121	0.5360 00	122	0.5180 00	123	0.5000 00	124	0.4820-01	125	0.4640-01	126	0.4640-01
126	0.3050-01	127	0.2820-01	128	0.2600-02	129	0.2420-01	130	0.2240-01	131	0.2240-01
131	0.2080-01	132	0.2340-01	133	0.2340-01	134	0.2340-01	135	0.2340-01	136	0.2340-01

CONC DISTRIBUTION AT TIME = 30 000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000	2	0.8700-03	3	0.2480-01	4	0.4200-01	5	0.5690-01	6	0.7270-00	7	0.8740-01	8	0.9950-01
9	0.8740-01	10	0.7240-00	11	0.1000-01	12	0.7490-00	13	0.8440-00	14	0.8100-01	15	0.7400-01	16	0.7400-01
17	0.7550-00	18	0.7270-00	19	0.5980-00	20	0.7270-00	21	0.5980-00	22	0.5980-00	23	0.5980-00	24	0.5980-00
25	0.8220-00	26	0.8220-00	27	0.5020-00	28	0.4270-00	29	0.4270-00	30	0.4270-00	31	0.4270-00	32	0.4270-00
33	0.2550-00	34	0.2100-00	35	0.2100-00	36	0.1720-00	37	0.1720-00	38	0.1720-00	39	0.1720-00	40	0.1720-00
41	0.8570-00	42	0.5810-00	43	0.2440-00	44	0.2020-00	45	0.2020-00	46	0.2020-00	47	0.1650-00	48	0.1650-00
49	0.8440-00	50	0.8150-00	51	0.6720-00	52	0.6480-00	53	0.6480-00	54	0.6220-00	55	0.6220-00	56	0.5980-00
57	0.0000-00	58	0.8700-03	59	0.7340-00	60	0.7480-01	61	0.7480-01	62	0.7480-01	63	0.7400-01	64	0.7400-01
65	0.6200-01	66	0.6200-01	67	0.0000-00	68	0.8700-03	69	0.8700-03	70	0.8700-03	71	0.8700-03	72	0.8700-03
73	0.8590-01	74	0.6740-01	75	0.6740-01	76	0.6740-01	77	0.6740-01	78	0.6740-01	79	0.6740-01	80	0.6740-01
81	0.7840-00	82	0.7840-00	83	0.7840-00	84	0.7840-00	85	0.7840-00	86	0.7840-00	87	0.7840-00	88	0.7840-00
89	0.6820-00	90	0.6820-00	91	0.6820-00	92	0.6820-00	93	0.6820-00	94	0.6820-00	95	0.6820-00	96	0.6820-00
97	0.3040-00	98	0.3040-00	99	0.3040-00	100	0.3040-00	101	0.3040-00	102	0.3040-00	103	0.3040-00	104	0.3040-00
105	0.7640-00	106	0.7640-00	107	0.7640-00	108	0.7640-00	109	0.7640-00	110	0.7640-00	111	0.7640-00	112	0.7640-00
113	0.3450-01	114	0.1000-01	115	0.2810-00	116	0.2810-00	117	0.2810-00	118	0.2810-00	119	0.2810-00	120	0.2810-00
121	0.7270-00	122	0.8440-00	123	0.8440-00	124	0.8440-00	125	0.8440-00	126	0.8440-00	127	0.8440-00	128	0.8440-00
129	0.5980-01	130	0.0000-00	131	0.0000-00	132	0.0000-00	133	0.0000-00	134	0.0000-00	135	0.0000-00	136	0.0000-00
137	0.8590-01	138	0.8590-01	139	0.8590-01	140	0.8590-01	141	0.8590-01	142	0.8590-01	143	0.8590-01	144	0.8590-01
145	0.8590-01	146	0.8590-01	147	0.8590-01	148	0.8590-01	149	0.8590-01	150	0.8590-01	151	0.8590-01	152	0.8590-01
153	0.8590-01	154	0.8590-01	155	0.8590-01	156	0.8590-01	157	0.8590-01	158	0.8590-01	159	0.8590-01	160	0.8590-01
161	0.8590-01	162	0.8590-01	163	0.8590-01	164	0.8590-01	165	0.8590-01	166	0.8590-01	167	0.8590-01	168	0.8590-01
169	0.8590-01	170	0.8590-01	171	0.8590-01	172	0.8590-01	173	0.8590-01	174	0.8590-01	175	0.8590-01	176	0.8590-01
177	0.8590-01	178	0.8590-01	179	0.8590-01	180	0.8590-01	181	0.8590-01	182	0.8590-01	183	0.8590-01	184	0.8590-01
185	0.8590-01	186	0.8590-01	187	0.8590-01	188	0.8590-01	189	0.8590-01	190	0.8590-01	191	0.8590-01	192	0.8590-01
193	0.8590-01	194	0.8590-01	195	0.8590-01	196	0.8590-01	197	0.8590-01	198	0.8590-01	199	0.8590-01	200	0.8590-01

CONC DISTRIBUTION AT TIME = 40 ECO DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0 0000 00	7	0 898D-02	3	0 358D-01	4	0 587D-01	5	0 781D-01				
6	0 944D-01	12	0 104D 00	8	0 111D 00	9	0 111D 00	10	0 111D 00				
11	0 104D 00	17	0 100D 01	13	0 861D 00	14	0 837D 00	15	0 815D C3				
16	0 789D 00	22	0 765D 00	18	0 741D 00	19	0 719D C0	20	0 705D C3				
21	0 678D 00	27	0 654D 00	23	0 100D 01	24	0 833D 00	25	0 705D C0				
26	0 645D 00	32	0 628D 00	28	0 490D 00	29	0 425D 00	30	0 371D C3				
31	0 326D 00	37	0 289D 00	33	0 230D 00	34	0 100D 01	35	0 782D C0				
36	0 680D 00	42	0 592D 00	38	0 519D 00	39	0 449D 00	40	0 391D C0				
41	0 342D 00	47	0 301D 00	43	0 271D 00	44	0 224D 00	45	0 100D 01				
46	0 861D 00	52	0 837D 00	48	0 815D 00	49	0 789D C0	50	0 766D C0				
51	0 741D 00	57	0 718D 00	53	0 705D 00	54	0 678D C0	55	0 654D C0				
56	0 000D 00	62	0 998D-02	58	0 358D-01	59	0 587D-01	60	0 781D-01				
61	0 944D-01	67	0 104D 00	63	0 111D 00	64	0 111D 00	65	0 110D 00				
66	0 104D 00	72	0 000D 00	68	0 988D-02	69	0 358D-01	70	0 587D-01				
71	0 781D-01	77	0 844D-01	73	0 104D 00	74	0 111D 00	75	0 111D 00				
76	0 110D 00	82	0 104D 00	78	0 100D 01	79	0 861D 00	80	0 837D 00				
81	0 815D 00	87	0 789D 00	83	0 765D 00	84	0 741D 00	85	0 719D 00				
86	0 705D 00	92	0 678D 00	88	0 654D 00	89	0 100D 01	90	0 930D 00				
91	0 371D 00	97	0 645D 00	93	0 592D 00	94	0 490D 00	95	0 430D C3				
96	0 782D 00	102	0 326D 00	98	0 289D 00	99	0 230D 00	100	0 100D 01				
101	0 391D 00	107	0 860D 00	103	0 892D 00	104	0 819D 00	105	0 490D 00				
106	0 100D 01	112	0 342D 00	108	0 301D 00	109	0 271D 00	110	0 224D C3				
111	0 100D 01	117	0 861D 00	113	0 837D 00	114	0 815D 00	115	0 789D C0				
116	0 786D 00	122	0 741D 00	118	0 718D 00	119	0 705D 00	120	0 678D 00				
121	0 654D 00	127	0 000D 00	123	0 000D 00	124	0 358D-01	125	0 587D-01				
126	0 781D-01	132	0 944D-01	128	0 104D 00	129	0 111D 00	130	0 111D 00				
131	0 110D 00	137	0 104D 00	134	0 104D 00	135	0 104D 00	136	0 111D 00				
131		132		138		139		139					

CONC DISTRIBUTION AT TIME = 50 000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0 0000 00	2	0 189D-01	3	0 452D-01	4	0 720D-01	5	0 959D-01		
6	0 115D 00	7	0 128D 00	8	0 139D 00	9	0 145D 00	10	0 145D 00		
11	0 139D 00	12	0 100D 01	13	0 876D 00	14	0 855D 00	15	0 837D 00		
16	0 813D 00	17	0 795D 00	18	0 772D 00	19	0 755D 00	20	0 742D 00		
21	0 718D 00	22	0 704D 00	23	0 100D 01	24	0 854D 00	25	0 758D 00		
26	0 666D 00	27	0 583D 00	28	0 512D 00	29	0 452D 00	30	0 399D 00		
31	0 352D 00	32	0 311D 00	33	0 274D 00	34	0 100D 01	35	0 196D 00		
36	0 699D 00	37	0 613D 00	38	0 538D 00	39	0 477D 00	40	0 423D 00		
41	0 318D 00	42	0 340D 00	43	0 301D 00	44	0 266D 00	45	0 100D 01		
48	0 816D 00	49	0 859D 00	50	0 837D 00	51	0 813D 00	52	0 795D 00		
51	0 722D 00	52	0 758D 00	53	0 742D 00	54	0 718D 00	55	0 704D 00		
56	0 000D 00	57	0 188D-01	58	0 452D-01	59	0 720D-01	60	0 958D-01		
61	0 115D 00	62	0 128D 00	63	0 139D 00	64	0 145D 00	65	0 145D 00		
66	0 139D 00	67	0 100D 01	68	0 876D 00	69	0 855D 00	70	0 837D 00		
71	0 813D 00	72	0 115D 00	73	0 128D 00	74	0 139D 00	75	0 145D 00		
76	0 139D 00	77	0 100D 01	78	0 100D 01	79	0 876D 00	80	0 855D 00		
81	0 813D 00	82	0 813D 00	83	0 795D 00	84	0 772D 00	85	0 758D 00		
86	0 742D 00	87	0 718D 00	88	0 704D 00	89	0 100D 01	90	0 854D 00		
91	0 758D 00	92	0 666D 00	93	0 583D 00	94	0 512D 00	95	0 452D 00		
96	0 399D 00	97	0 352D 00	98	0 311D 00	99	0 274D 00	100	0 100D 01		
101	0 796D 00	102	0 699D 00	103	0 613D 00	104	0 538D 00	105	0 477D 00		
106	0 423D 00	107	0 378D 00	108	0 340D 00	109	0 301D 00	110	0 266D 00		
111	0 100D 01	112	0 876D 00	113	0 855D 00	114	0 837D 00	115	0 813D 00		
116	0 795D 00	117	0 772D 00	118	0 755D 00	119	0 742D 00	120	0 718D 00		
121	0 704D 00	122	0 000D 00	123	0 189D-01	124	0 452D-01	125	0 720D-01		
126	0 958D-01	127	0 115D 00	128	0 139D 00	129	0 159D 00	130	0 145D 00		
131	0 145D 00	132	0 139D 00	133	0 139D 00	134	0 139D 00	135	0 145D 00		

70 Elements

INPUT DATA FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENT METHOD

TOTAL NO OF ELEMENTS - 70
 TOTAL NO OF NODES - 176
 MAXIMUM NO OF NODES PER ELEMENT - 8
 TOTAL NO OF MATERIALS - 1
 NUMBER OF PUMPING WELLS - 0
 NUMBER OF CONCS TO BE ESTIMATED - 1GR

NUMBER OF PUMPING PERIODS - 0
 TOTAL SIMULATION PERIODS - 5
 FACTOR MULTIPLYING COMPUTED CONCS - 1.00000

STEP SIZE - 10.00000
 STATE OF PROBLEM - 1
 NO OF SPECIFIED CONDITIONS - 68

NODE-ELEMENT RELATIONSHIP

ELEMS	N1	N2	N3	N4	N5	N6	N7	N8
1	1	12	12	2	89	100	101	80
2	2	13	14	3	90	101	102	91
3	3	14	15	4	91	102	103	92
4	4	15	16	5	92	103	104	93
5	5	16	17	6	93	104	105	94
6	6	17	18	7	94	105	106	95
7	7	18	19	8	95	106	107	96
8	8	19	20	9	96	107	108	97
9	9	20	21	10	97	108	109	98
10	10	21	22	11	98	109	110	99
11	11	22	23	12	99	110	111	100
12	12	23	24	13	100	111	112	101
13	13	24	25	14	101	112	113	102
14	14	25	26	15	102	113	114	103
15	15	26	27	16	103	114	115	104
16	16	27	28	17	104	115	116	105
17	17	28	29	18	105	116	117	106
18	18	29	30	19	106	117	118	107
19	19	30	31	20	107	118	119	108
20	20	31	32	21	108	119	120	109
21	21	32	33	22	109	120	121	110
22	22	33	34	23	110	121	122	111
23	23	34	35	24	111	122	123	112
24	24	35	36	25	112	123	124	113
25	25	36	37	26	113	124	125	114
26	26	37	38	27	114	125	126	115
27	27	38	39	28	115	126	127	116
28	28	39	40	29	116	127	128	117
29	29	40	41	30	117	128	129	118
30	30	41	42	31	118	129	130	119
31	31	42	43	32	119	130	131	120
32	32	43	44	33	120	131	132	121
33	33	44	45	34	121	132	133	122
34	34	45	46	35	122	133	134	123
35	35	46	47	36	123	134	135	124
36	36	47	48	37	124	135	136	125
37	37	48	49	38	125	136	137	126
38	38	49	50	39	126	137	138	127
39	39	50	51	40	127	138	139	128
40	40	51	52	41	128	139	140	129
41	41	52	53	42	129	140	141	130
42	42	53	54	43	130	141	142	131
43	43	54	55	44	131	142	143	132
44	44	55	56	45	132	143	144	133
45	45	56	57	46	133	144	145	134
46	46	57	58	47	134	145	146	135
47	47	58	59	48	135	146	147	136
48	48	59	60	49	136	147	148	137
49	49	60	61	50	137	148	149	138
50	50	61	62	51	138	149	150	139

47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70
51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88
62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88
63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88
52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88
139 140 141 142 143 144 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168 169 170 171 172 173 174 175 176
150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168 169 170 171 172 173 174 175 176
151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168 169 170 171 172 173 174 175 176
140 141 142 143 144 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165

FIXED BOUNDARY CONDITIONS

NODE	ID	INDE	ID	MODE	ID	MODE	ID	MODE	ID	MODE	ID
1	0	7	0	3	0	1	0	5	0	0	0
6	0	12	0	8	0	9	0	10	0	0	0
11	0	44	0	22	0	23	0	23	0	0	0
34	1	67	0	45	0	55	1	56	0	0	0
66	0	99	0	77	0	78	0	88	1	0	0
89	1	113	0	100	0	110	0	116	0	0	0
112	0	118	0	114	0	115	0	116	0	0	0
117	0	123	0	119	0	120	0	121	0	0	0
122	0	128	0	124	0	125	0	126	0	0	0
127	0	133	0	129	0	130	0	131	0	0	0
132	0	165	0	143	0	144	0	145	0	0	0
155	1	188	0	166	0	176	1	177	0	0	0
187	0	220	0	198	0	199	0	209	1	0	0
210	1	234	0	221	0	231	0	232	0	0	0
233	0	239	0	235	0	236	0	237	0	0	0
278	0		0	240	0	241	0	242	0	0	0

MAXIMUM BANDWIDTH = 176 ON ROW NO

OUTPUT FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENTS METHOD

INITIAL CONC DISTRIBUTION AT TIME = 0.000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000	2	0.0000	3	0.0000	4	0.0000	5	0.0000	6	0.0000	7	0.0000
8	0.0000	9	0.0000	10	0.0000	11	0.0000	12	0.0000	13	0.0000	14	0.0000
15	0.0000	16	0.0000	17	0.0000	18	0.0000	19	0.0000	20	0.0000	21	0.0000
22	0.0000	23	0.0000	24	0.0000	25	0.0000	26	0.0000	27	0.0000	28	0.0000
29	0.0000	30	0.0000	31	0.0000	32	0.0000	33	0.0000	34	0.0000	35	0.0000
36	0.0000	37	0.0000	38	0.0000	39	0.0000	40	0.0000	41	0.0000	42	0.0000
43	0.0000	44	0.0000	45	0.0000	46	0.0000	47	0.0000	48	0.0000	49	0.0000
50	0.0000	51	0.0000	52	0.0000	53	0.0000	54	0.0000	55	0.0000	56	0.0000
57	0.0000	58	0.0000	59	0.0000	60	0.0000	61	0.0000	62	0.0000	63	0.0000
64	0.0000	65	0.0000	66	0.0000	67	0.0000	68	0.0000	69	0.0000	70	0.0000
71	0.0000	72	0.0000	73	0.0000	74	0.0000	75	0.0000	76	0.0000	77	0.0000
78	0.0000	79	0.0000	80	0.0000	81	0.0000	82	0.0000	83	0.0000	84	0.0000
85	0.0000	86	0.0000	87	0.0000	88	0.0000	89	0.0000	90	0.0000	91	0.0000
92	0.0000	93	0.0000	94	0.0000	95	0.0000	96	0.0000	97	0.0000	98	0.0000
99	0.0000	100	0.0000	101	0.0000	102	0.0000	103	0.0000	104	0.0000	105	0.0000
106	0.0000	107	0.0000	108	0.0000	109	0.0000	110	0.0000	111	0.0000	112	0.0000
113	0.0000	114	0.0000	115	0.0000	116	0.0000	117	0.0000	118	0.0000	119	0.0000
120	0.0000	121	0.0000	122	0.0000	123	0.0000	124	0.0000	125	0.0000	126	0.0000
127	0.0000	128	0.0000	129	0.0000	130	0.0000	131	0.0000	132	0.0000	133	0.0000
134	0.0000	135	0.0000	136	0.0000	137	0.0000	138	0.0000	139	0.0000	140	0.0000
141	0.0000	142	0.0000	143	0.0000	144	0.0000	145	0.0000	146	0.0000	147	0.0000
148	0.0000	149	0.0000	150	0.0000	151	0.0000	152	0.0000	153	0.0000	154	0.0000
155	0.0000	156	0.0000	157	0.0000	158	0.0000	159	0.0000	160	0.0000	161	0.0000
162	0.0000	163	0.0000	164	0.0000	165	0.0000	166	0.0000	167	0.0000	168	0.0000
169	0.0000	170	0.0000	171	0.0000	172	0.0000	173	0.0000	174	0.0000	175	0.0000
176	0.0000	177	0.0000	178	0.0000	179	0.0000	180	0.0000	181	0.0000	182	0.0000
183	0.0000	184	0.0000	185	0.0000	186	0.0000	187	0.0000	188	0.0000	189	0.0000
190	0.0000	191	0.0000	192	0.0000	193	0.0000	194	0.0000	195	0.0000	196	0.0000
197	0.0000	198	0.0000	199	0.0000	200	0.0000	201	0.0000	202	0.0000	203	0.0000
204	0.0000	205	0.0000	206	0.0000	207	0.0000	208	0.0000	209	0.0000	210	0.0000
211	0.0000	212	0.0000	213	0.0000	214	0.0000	215	0.0000	216	0.0000	217	0.0000
218	0.0000	219	0.0000	220	0.0000	221	0.0000	222	0.0000	223	0.0000	224	0.0000
225	0.0000	226	0.0000	227	0.0000	228	0.0000	229	0.0000	230	0.0000	231	0.0000
232	0.0000	233	0.0000	234	0.0000	235	0.0000	236	0.0000	237	0.0000	238	0.0000
239	0.0000	240	0.0000	241	0.0000	242	0.0000	243	0.0000	244	0.0000	245	0.0000

CONC DISTRIBUTION AT TIME = 10 000 DAYS

MCES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES
1	0 0000 00	2	0 0000 00	3	0 0000 00	4	0 4000-02	5	0 6000-02			
6	0 7000-02	7	0 6000-02	8	0 4000-02	9	0 2000-02	10	0 2000-02			
11	0 0000 00	12	0 0000 00	13	0 2400-01	14	0 2400-01	15	0 4900-01			
16	0 4700-01	17	0 4100-01	18	0 3200-01	19	0 3200-01	20	0 2400-01			
21	0 1200-01	22	0 8000-02	23	0 1000-01	24	0 8570 00	25	0 8160 00			
26	0 7150 00	27	0 6510 00	28	0 5200 00	29	0 6140 00	30	0 5490 00			
31	0 5350 00	32	0 5200 00	33	0 3620 00	34	0 8110 00	35	0 6850 00			
36	0 5000 00	37	0 4820-01	38	0 2610 00	39	0 1600-01	40	0 1210 00			
41	0 7800-01	42	0 5820 00	43	0 4820 00	44	0 3800-01	45	0 1000 01			
46	0 7830 00	47	0 5820 00	48	0 4310 00	49	0 4310 00	50	0 2170 00			
51	0 1430 00	52	0 9160-01	53	0 7670 00	54	0 8600-01	55	0 1700-01			
56	0 1000 01	57	0 7410 00	58	0 8040 00	59	0 8040 00	60	0 3200-01			
61	0 2290 00	62	0 1830 00	63	0 8700-01	64	0 6000-01	65	0 3500-01			
66	0 1800-01	67	0 1000 01	68	0 7930 00	69	0 5820 00	70	0 4310 00			
71	0 3120 00	72	0 2170 00	73	0 1430 00	74	0 9100-01	75	0 4310 00			
76	0 3620 00	77	0 1700-01	78	0 1000 01	79	0 8100-01	80	0 5600-01			
81	0 4600-01	82	0 2810 00	83	0 1820 00	84	0 6850 00	85	0 7800-01			
86	0 8160 00	87	0 2800-01	88	0 1600-01	89	0 1000 01	90	0 7800-01			
91	0 5490 00	92	0 7150 00	93	0 6810 00	94	0 6140 00	95	0 8570 00			
96	0 4900 00	97	0 5350 00	98	0 5200 00	99	0 5110 00	100	0 8000 00			
101	0 2400-01	102	0 4200-01	103	0 4900-01	104	0 4900-01	105	0 4100-01			
106	0 3200-01	107	0 2400-01	108	0 1700-01	109	0 4700-01	110	0 8000-02			
111	0 0000 00	112	0 0000 00	113	0 0000 00	114	0 1200-01	115	0 6000-02			
116	0 7000-02	117	0 6000-02	118	0 4000-02	119	0 2000-02	120	0 1000-02			
121	0 0000 00	122	0 0000 00	123	0 0000 00	124	0 0000 00	125	0 4000-02			
126	0 6000-02	127	0 7000-02	128	0 0000 00	129	0 0000 00	130	0 2000-02			
131	0 4900-01	132	0 0000 00	133	0 0000 00	134	0 2400-01	135	0 2000-02			
136	0 1700-01	137	0 4700-01	138	0 0000 00	139	0 3200-01	140	0 4200-01			
141	0 1700-01	142	0 1200-01	143	0 1000-01	144	0 1000 01	145	0 2400-01			
146	0 8160 00	147	0 7150 00	148	0 8000-02	149	0 1000 01	150	0 8570 00			
151	0 5490 00	152	0 5350 00	153	0 8160 00	154	0 6140 00	155	0 5730 00			
156	0 6850 00	157	0 8000 00	158	0 8200 00	159	0 5110 00	160	0 1000 01			
161	0 1210 00	162	0 7800-01	163	0 3620 00	164	0 2610 00	165	0 1820 00			
166	0 1000 01	167	0 7530 00	168	0 4820-01	169	0 2800-01	170	0 1600-01			
171	0 1700-01	172	0 1430 00	173	0 8110 00	174	0 4310 00	175	0 3120 00			
176	0 1700-01	177	0 1000 01	178	0 1000 01	179	0 6040 00	180	0 3200-01			
181	0 3290 00	182	0 2290 00	183	0 1800-01	184	0 6040 00	185	0 4520 00			
186	0 3500-01	187	0 1800-01	188	0 1000 01	189	0 9700-01	190	0 5820 00			
191	0 4310 00	192	0 3120 00	193	0 2170 00	194	0 7530 00	195	0 8100-01			
196	0 5600-01	197	0 3200-01	198	0 1700-01	199	0 1430 00	200	0 6850 00			
201	0 5000 00	202	0 3620 00	203	0 2610 00	204	0 1600 01	205	0 1210 00			
206	0 7800-01	207	0 4820-01	208	0 8600-01	209	0 1820 00	210	0 1000 01			
211	0 8570 00	212	0 8160 00	213	0 7150 00	214	0 6810 00	215	0 6140 00			
216	0 5730 00	217	0 5490 00	218	0 8350 00	219	0 5200 00	220	0 5110 00			
221	0 0000 00	222	0 2400-01	223	0 4200-01	224	0 4900-01	225	0 1140 00			
226	0 4100-01	227	0 3200-01	228	0 2400-01	229	0 1700-01	230	0 4700-01			
231	0 8000-02	232	0 0000 00	233	0 3400-01	234	0 4000 00	235	0 1200-01			
236	0 6000-02	237	0 7000-02	238	0 6000-02	239	0 4000 00	240	0 4000-02			
241	0 1000-02	242	0 0000 00	243	0 0000 00	244	0 6000-02	245	0 2000-02			

CONC DISTRIBUTION AT TIME = 30 000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0 0000 00	3	0 8000-02	2	0 2700-01	4	0 4500-01	5	0 6100-01				
6	0 7200-01	7	0 7800-01	8	0 8000-01	9	0 8000-01	10	0 7400-01				
11	0 6600-01	12	0 6000 00	13	0 4700-01	14	0 4700-01	15	0 1140 00				
16	0 1200 00	17	0 3150-01	18	0 1320 00	19	0 1260 00	20	0 1180 00				
21	0 1050 00	22	0 8100-01	23	0 1000 01	24	0 8150 00	25	0 8000 00				
26	0 6430 00	27	0 8710 00	28	0 7780 00	29	0 7440 00	30	0 7170 00				
31	0 5930 00	32	0 8630 00	33	0 8360 00	34	0 1000 01	35	0 7510 00				
36	0 6120 00	37	0 8130 00	38	0 4400 00	39	0 3780 00	40	0 3210 00				
41	0 2350 00	42	0 2340 00	43	0 1950 00	44	0 1610 00	45	0 1600 01				
46	0 8280 00	47	0 7100 00	48	0 6020 00	49	0 5140 00	50	0 4260 00				
51	0 3670 00	52	0 3100 00	53	0 2610 00	54	0 2150 00	55	0 1760 00				
56	0 1600 01	57	0 8450 00	58	0 7370 00	59	0 6310 00	60	0 5330 00				
61	0 1880 00	62	0 3850 00	63	0 3250 00	64	0 2720 00	65	0 2240 00				
66	0 1830 00	67	0 1000 01	68	0 8280 00	69	0 7100 00	70	0 6020 00				
71	0 5140 00	72	0 4360 00	73	0 3670 00	74	0 3100 00	75	0 2610 00				
76	0 2150 00	77	0 1760 00	78	0 1000 01	79	0 7510 00	80	0 6120 00				
81	0 5130 00	82	0 4400 00	83	0 3780 00	84	0 3210 00	85	0 2750 00				
86	0 2340 00	87	0 1850 00	88	0 1610 00	89	0 1600 01	90	0 9150 00				
91	0 8000 00	92	0 8430 00	93	0 8110 00	94	0 7780 00	95	0 7440 00				
96	0 7170 00	97	0 6830 00	98	0 6530 00	99	0 6360 00	100	0 6000 00				
101	0 4700-01	102	0 8700-01	103	0 1140 00	104	0 1300 00	105	0 1350-01				
106	0 1330 00	107	0 1260 00	108	0 1180 00	109	0 1060 00	110	0 9300-01				
111	0 0000 00	112	0 9000-02	113	0 3700-01	114	0 4500-01	115	0 6100-01				
116	0 7200-01	117	0 7800-01	118	0 8000-01	119	0 7800-01	120	0 7400-01				
121	0 6600-01	122	0 0000 00	123	0 8000-02	124	0 3700-01	125	0 4500-01				
126	0 6100-01	127	0 7200-01	128	0 7600-01	129	0 8000-01	130	0 7800-01				
131	0 7400-01	132	0 5600-01	133	0 0000 00	134	0 4700-01	135	0 8700-01				
136	0 1140 00	137	0 1300 00	138	0 1060 00	139	0 1320 00	140	0 1260 00				
141	0 1180 00	142	0 1060 00	143	0 1060 00	144	0 9200-01	145	0 9150 00				
146	0 8000 00	147	0 8430 00	148	0 8110 00	149	0 7780 00	150	0 7440 00				
151	0 7170 00	152	0 6830 00	153	0 6530 00	154	0 6360 00	155	0 6000 01				
156	0 7510 00	157	0 8120 00	158	0 8130 00	159	0 4000 00	160	0 3780 00				
161	0 3210 00	162	0 2750 00	163	0 2340 00	164	0 1950 00	165	0 1610 00				
166	0 1000 01	167	0 8280 00	168	0 8710 00	169	0 7100 00	170	0 6140 00				
171	0 4360 00	172	0 3670 00	173	0 3100 00	174	0 2610 00	175	0 2150 00				
176	0 1760 00	177	0 1000 01	178	0 8450 00	179	0 7370 00	180	0 6310 00				
181	0 5350 00	182	0 4580 00	183	0 3850 00	184	0 3250 00	185	0 2720 00				
186	0 2240 00	187	0 1830 00	188	0 1000 01	189	0 8280 00	190	0 7100 00				
191	0 6020 00	192	0 5140 00	193	0 4260 00	194	0 3670 00	195	0 3100 00				
196	0 2610 00	197	0 2150 00	198	0 1760 00	199	0 1000 01	200	0 7510 00				
205	0 2750 00	206	0 1320 00	207	0 1320 00	208	0 4400 00	209	0 3780 00				
211	0 9150 00	212	0 8800 00	213	0 8430 00	214	0 8110 00	215	0 7880 00				
216	0 7440 00	217	0 7170 00	218	0 6830 00	219	0 6530 00	220	0 6360 00				
221	0 0000 00	222	0 4700-01	223	0 8700-01	224	0 1180 00	225	0 1060 00				
226	0 1350-01	227	0 1330 00	228	0 1260 00	229	0 1180 00	230	0 1060 00				
231	0 9300-01	232	0 0000 00	233	0 9000-02	234	0 8000-02	235	0 7800-01				
236	0 6100-01	237	0 7100-01	238	0 6600-01	239	0 7800-01	240	0 4500-01				
241	0 7400-01	242	0 6600-01	243	0 6600-01	244	0 6600-01	245	0 4500-01				
246	0 7400-01	247	0 6600-01	248	0 6600-01	249	0 6600-01	250	0 4500-01				

CONC DISTRIBUTION AT TIME = 40 000 DAYS

MODES	CONCS	MODES	CONCS	MODES	CONCS	MODES	CONCS	MODES	CONCS	MODES	CONCS
1	0.0000	2	0.1500-01	3	0.3900-01	4	0.8300-01	5	0.8400-01		
6	0.1010	7	0.1110	8	0.1180	9	0.1190	10	0.1160		
11	0.1560	12	0.0000	13	0.9400-01	14	0.1010	15	0.1240		
16	0.1520	17	0.1680	18	0.1680	19	0.1670	20	0.1520		
21	0.8720	22	0.1400	23	0.1000	24	0.8280	25	0.9020		
26	0.8440	27	0.8460	28	0.8170	29	0.7890	30	0.7630		
31	0.5230	32	0.7160	33	0.6900	34	0.1000	35	0.7630		
36	0.5230	37	0.5420	38	0.4750	39	0.1000	40	0.3880		
41	0.2260	42	0.2880	43	0.2520	44	0.2180	45	0.1000		
46	0.8740	47	0.7220	48	0.6320	49	0.5510	50	0.4790		
51	0.1000	52	0.3840	53	0.3180	54	0.2740	55	0.2360		
56	0.5020	57	0.8610	58	0.7600	59	0.6620	60	0.5770		
61	0.2420	62	0.4240	63	0.3790	64	0.3300	65	0.2840		
66	0.2420	67	0.1000	68	0.8440	69	0.7320	70	0.6220		
71	0.2740	72	0.4790	73	0.4160	74	0.3640	75	0.3180		
76	0.2740	77	0.2260	78	0.1000	79	0.7630	80	0.6220		
81	0.8420	82	0.4750	83	0.4180	84	0.3650	85	0.3260		
86	0.2890	87	0.2820	88	0.2180	89	0.1680	90	0.9290		
91	0.8020	92	0.8720	93	0.8460	94	0.8170	95	0.7890		
96	0.7650	97	0.7440	98	0.7160	99	0.6890	100	0.6620		
101	0.5400-01	102	0.1010	103	0.1340	104	0.1560	105	0.1660		
106	0.1680	107	0.1670	108	0.1620	109	0.1520	110	0.1400		
111	0.0000	112	0.1500-01	113	0.3900-01	114	0.8300-01	115	0.8400-01		
116	0.1010	117	0.1110	118	0.1180	119	0.1190	120	0.1160		
121	0.1100	122	0.0000	123	0.1500-01	124	0.3900-01	125	0.6200-01		
126	0.8400-01	127	0.1010	128	0.1110	129	0.1180	130	0.1190		
131	0.1160	132	0.1100	133	0.1000	134	0.8400-01	135	0.1010		
136	0.1340	137	0.1560	138	0.1620	139	0.1680	140	0.1670		
141	0.1620	142	0.1820	143	0.1860	144	0.1800	145	0.9290		
146	0.9020	147	0.8720	148	0.8460	149	0.8170	150	0.7890		
151	0.7650	152	0.7440	153	0.7160	154	0.6900	155	0.1000		
156	0.2680	157	0.6230	158	0.5420	159	0.4750	160	0.4180		
161	0.1000	162	0.3260	163	0.2890	164	0.2520	165	0.2180		
166	0.1000	167	0.8440	168	0.7320	169	0.6320	170	0.5510		
171	0.4790	172	0.4160	173	0.3640	174	0.3180	175	0.2740		
176	0.2360	177	0.1000	178	0.8610	179	0.7600	180	0.6620		
181	0.5770	182	0.5020	183	0.4340	184	0.3790	185	0.3300		
186	0.2840	187	0.2420	188	0.2000	189	0.1640	190	0.1340		
191	0.6320	192	0.5510	193	0.4790	194	0.4160	195	0.3640		
196	0.3180	197	0.2740	198	0.2360	199	0.1000	200	0.7650		
201	0.3260	202	0.5420	203	0.4750	204	0.4180	205	0.3680		
206	0.3260	207	0.2890	208	0.2520	209	0.2180	210	0.1000		
211	0.9290	212	0.8720	213	0.8280	214	0.7890	215	0.7440		
216	0.7890	217	0.7650	218	0.7440	219	0.7160	220	0.6900		
221	0.0000	222	0.5400-01	223	0.1010	224	0.1340	225	0.1560		
226	0.1560	227	0.1680	228	0.1670	229	0.1620	230	0.1520		
231	0.1400	232	0.0000	233	0.0000	234	0.1500-01	235	0.6200-01		
236	0.8400-01	237	0.1010	238	0.1010	239	0.3900-01	240	0.8400-01		
241	0.1160	242	0.1100	243	0.1110	244	0.1110	245	0.1180		

COORDINATES AND INITIAL CONCS OF NODES (L)

NODES	Y(I)	X(I)	Z(I)	CINI(I)
1	0.000 00	0.000 00	0.100 03	0.000 00
2	0.100 02	0.000 00	0.100 03	0.000 00
3	0.200 02	0.000 00	0.100 03	0.000 00
4	0.300 02	0.000 00	0.100 03	0.000 00
5	0.400 02	0.000 00	0.100 03	0.000 00
6	0.500 02	0.000 00	0.100 03	0.000 00
7	0.600 02	0.000 00	0.100 03	0.000 00
8	0.700 02	0.000 00	0.100 03	0.000 00
9	0.800 02	0.000 00	0.100 03	0.000 00
10	0.900 02	0.000 00	0.100 03	0.000 00
11	0.000 00	0.000 00	0.100 03	0.000 00
12	0.000 00	0.100 02	0.100 03	0.000 00
13	0.100 02	0.100 02	0.100 03	0.000 00
14	0.200 02	0.100 02	0.100 03	0.000 00
15	0.300 02	0.100 02	0.100 03	0.000 00
16	0.400 02	0.100 02	0.100 03	0.000 00
17	0.500 02	0.100 02	0.100 03	0.000 00
18	0.600 02	0.100 02	0.100 03	0.000 00
19	0.700 02	0.100 02	0.100 03	0.000 00
20	0.800 02	0.100 02	0.100 03	0.000 00
21	0.900 02	0.100 02	0.100 03	0.000 00
22	0.000 00	0.100 02	0.100 03	0.100 01
23	0.100 02	0.200 01	0.100 03	0.000 00
24	0.200 02	0.200 01	0.100 03	0.000 00
25	0.300 02	0.200 01	0.100 03	0.000 00
26	0.400 02	0.200 01	0.100 03	0.000 00
27	0.500 02	0.200 01	0.100 03	0.000 00
28	0.600 02	0.200 01	0.100 03	0.000 00
29	0.700 02	0.200 01	0.100 03	0.000 00
30	0.800 02	0.200 01	0.100 03	0.000 00
31	0.900 02	0.200 01	0.100 03	0.000 00
32	0.000 00	0.200 01	0.100 03	0.000 00
33	0.100 02	0.300 02	0.100 03	0.000 00
34	0.200 02	0.300 02	0.100 03	0.000 00
35	0.300 02	0.300 02	0.100 03	0.000 00
36	0.400 02	0.300 02	0.100 03	0.000 00
37	0.500 02	0.300 02	0.100 03	0.000 00
38	0.600 02	0.300 02	0.100 03	0.000 00
39	0.700 02	0.300 02	0.100 03	0.000 00
40	0.800 02	0.300 02	0.100 03	0.000 00
41	0.900 02	0.300 02	0.100 03	0.000 00
42	0.000 00	0.300 02	0.100 03	0.000 00
43	0.100 02	0.300 02	0.100 03	0.000 00
44	0.200 02	0.300 02	0.100 03	0.000 00
45	0.300 02	0.300 02	0.100 03	0.000 00
46	0.400 02	0.350 02	0.100 03	0.000 00
47	0.500 02	0.350 02	0.100 03	0.000 00

OUTPUT FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENTS METHOD

NODES	INITIAL CONC DISTRIBUTION AT TIME = 0.000 DAYS			
	CONCS	NODES	CONCS	NODES
1	0.0000	00	0.0000	00
4	0.0000	00	0.0000	00
11	0.0000	00	0.0000	00
16	0.0000	00	0.0000	00
21	0.0000	00	0.0000	00
26	0.0000	00	0.0000	00
31	0.0000	00	0.0000	00
36	0.0000	00	0.0000	00
41	0.0000	00	0.0000	00
46	0.0000	00	0.0000	00
51	0.0000	00	0.0000	00
56	0.0000	00	0.0000	00
61	0.0000	00	0.0000	00
66	0.0000	00	0.0000	00
71	0.0000	00	0.0000	00
76	0.0000	00	0.0000	00
81	0.0000	00	0.0000	00
86	0.0000	00	0.0000	00
91	0.0000	00	0.0000	00
96	0.0000	00	0.0000	00
101	0.0000	00	0.0000	00
106	0.0000	00	0.0000	00
111	0.0000	00	0.0000	00
116	0.0000	00	0.0000	00
121	0.0000	00	0.0000	00
126	0.0000	00	0.0000	00
131	0.0000	00	0.0000	00
136	0.0000	00	0.0000	00
141	0.0000	00	0.0000	00
146	0.0000	00	0.0000	00
151	0.0000	00	0.0000	00
156	0.0000	00	0.0000	00
161	0.0000	00	0.0000	00
166	0.0000	00	0.0000	00
171	0.0000	00	0.0000	00
176	0.0000	00	0.0000	00
2	0.0000	00	0.0000	00
7	0.0000	00	0.0000	00
12	0.0000	00	0.0000	00
17	0.0000	00	0.0000	00
22	0.0000	00	0.0000	00
27	0.0000	00	0.0000	00
32	0.0000	00	0.0000	00
37	0.0000	00	0.0000	00
42	0.0000	00	0.0000	00
47	0.0000	00	0.0000	00
52	0.0000	00	0.0000	00
57	0.0000	00	0.0000	00
62	0.0000	00	0.0000	00
67	0.0000	00	0.0000	00
72	0.0000	00	0.0000	00
77	0.0000	00	0.0000	00
82	0.0000	00	0.0000	00
87	0.0000	00	0.0000	00
92	0.0000	00	0.0000	00
97	0.0000	00	0.0000	00
102	0.0000	00	0.0000	00
107	0.0000	00	0.0000	00
112	0.0000	00	0.0000	00
117	0.0000	00	0.0000	00
122	0.0000	00	0.0000	00
127	0.0000	00	0.0000	00
132	0.0000	00	0.0000	00
137	0.0000	00	0.0000	00
142	0.0000	00	0.0000	00
147	0.0000	00	0.0000	00
152	0.0000	00	0.0000	00
157	0.0000	00	0.0000	00
162	0.0000	00	0.0000	00
167	0.0000	00	0.0000	00
172	0.0000	00	0.0000	00
3	0.0000	00	0.0000	00
8	0.0000	00	0.0000	00
13	0.0000	00	0.0000	00
18	0.0000	00	0.0000	00
23	0.0000	00	0.0000	00
28	0.0000	00	0.0000	00
33	0.0000	00	0.0000	00
38	0.0000	00	0.0000	00
43	0.0000	00	0.0000	00
48	0.0000	00	0.0000	00
53	0.0000	00	0.0000	00
58	0.0000	00	0.0000	00
63	0.0000	00	0.0000	00
68	0.0000	00	0.0000	00
73	0.0000	00	0.0000	00
78	0.0000	00	0.0000	00
83	0.0000	00	0.0000	00
88	0.0000	00	0.0000	00
93	0.0000	00	0.0000	00
98	0.0000	00	0.0000	00
103	0.0000	00	0.0000	00
108	0.0000	00	0.0000	00
113	0.0000	00	0.0000	00
118	0.0000	00	0.0000	00
123	0.0000	00	0.0000	00
128	0.0000	00	0.0000	00
133	0.0000	00	0.0000	00
138	0.0000	00	0.0000	00
143	0.0000	00	0.0000	00
148	0.0000	00	0.0000	00
153	0.0000	00	0.0000	00
158	0.0000	00	0.0000	00
163	0.0000	00	0.0000	00
168	0.0000	00	0.0000	00
173	0.0000	00	0.0000	00
4	0.0000	00	0.0000	00
9	0.0000	00	0.0000	00
14	0.0000	00	0.0000	00
19	0.0000	00	0.0000	00
24	0.0000	00	0.0000	00
29	0.0000	00	0.0000	00
34	0.0000	00	0.0000	00
39	0.0000	00	0.0000	00
44	0.0000	00	0.0000	00
49	0.0000	00	0.0000	00
54	0.0000	00	0.0000	00
59	0.0000	00	0.0000	00
64	0.0000	00	0.0000	00
69	0.0000	00	0.0000	00
74	0.0000	00	0.0000	00
79	0.0000	00	0.0000	00
84	0.0000	00	0.0000	00
89	0.0000	00	0.0000	00
94	0.0000	00	0.0000	00
99	0.0000	00	0.0000	00
104	0.0000	00	0.0000	00
109	0.0000	00	0.0000	00
114	0.0000	00	0.0000	00
119	0.0000	00	0.0000	00
124	0.0000	00	0.0000	00
129	0.0000	00	0.0000	00
134	0.0000	00	0.0000	00
139	0.0000	00	0.0000	00
144	0.0000	00	0.0000	00
149	0.0000	00	0.0000	00
154	0.0000	00	0.0000	00
159	0.0000	00	0.0000	00
164	0.0000	00	0.0000	00
169	0.0000	00	0.0000	00
174	0.0000	00	0.0000	00
5	0.0000	00	0.0000	00
10	0.0000	00	0.0000	00
15	0.0000	00	0.0000	00
20	0.0000	00	0.0000	00
25	0.0000	00	0.0000	00
30	0.0000	00	0.0000	00
35	0.0000	00	0.0000	00
40	0.0000	00	0.0000	00
45	0.0000	00	0.0000	00
50	0.0000	00	0.0000	00
55	0.0000	00	0.0000	00
60	0.0000	00	0.0000	00
65	0.0000	00	0.0000	00
70	0.0000	00	0.0000	00
75	0.0000	00	0.0000	00
80	0.0000	00	0.0000	00
85	0.0000	00	0.0000	00
90	0.0000	00	0.0000	00
95	0.0000	00	0.0000	00
100	0.0000	00	0.0000	00
105	0.0000	00	0.0000	00
110	0.0000	00	0.0000	00
115	0.0000	00	0.0000	00
120	0.0000	00	0.0000	00
125	0.0000	00	0.0000	00
130	0.0000	00	0.0000	00
135	0.0000	00	0.0000	00
140	0.0000	00	0.0000	00
145	0.0000	00	0.0000	00
150	0.0000	00	0.0000	00
155	0.0000	00	0.0000	00
160	0.0000	00	0.0000	00
165	0.0000	00	0.0000	00
170	0.0000	00	0.0000	00
175	0.0000	00	0.0000	00

CONC DISTRIBUTION AT TIME = 40 000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0 0000 00	3	0 1500-01	3	0 3780-01	4	0 8700-01	5	0 8250-01		
6	0 8570-01	7	0 1100 00	8	0 1170 00	8	0 1170 00	8	0 1160 00		
11	0 1100 00	12	0 0000 00	13	0 0260-01	14	0 9930-01	10	0 1330 00		
16	0 1530 00	17	0 1650 00	18	0 1670 00	19	0 1680 00	15	0 1620 00		
21	0 1520 00	22	0 1400 00	23	0 1000 01	24	0 5050 00	20	0 8840 00		
26	0 8600 00	27	0 8330 00	28	0 8090 00	29	0 8090 00	25	0 7590 00		
31	0 7440 00	32	0 7160 00	33	0 6900 00	34	0 7820 00	30	0 8250 00		
36	0 7180 00	37	0 6250 00	38	0 5430 00	39	0 1000 01	35	0 8250 00		
41	0 3610 00	42	0 3180 00	43	0 2740 00	44	0 4740 00	40	0 4130 00		
46	0 8420 00	47	0 7450 00	48	0 6530 00	49	0 2360 00	45	0 1000 01		
51	0 4310 00	52	0 3760 00	53	0 3200 00	54	0 5690 00	50	0 4960 00		
56	0 1000 01	57	0 9090 00	58	0 8840 00	59	0 2840 00	55	0 2430 00		
61	0 8090 00	62	0 7820 00	63	0 7530 00	64	0 7440 00	60	0 8330 00		
66	0 6900 00	67	0 0000 00	68	0 8260-01	69	0 8930-01	65	0 7160 00		
71	0 1530 00	72	0 1650 00	73	0 1670 00	74	0 1650 00	70	0 1330 00		
76	0 1530 00	77	0 1400 00	78	0 0000 00	79	0 1500-01	75	0 1620 00		
81	0 6200-01	82	0 8250-01	83	0 1160 00	84	0 1100-01	80	0 3780-01		
86	0 1170-01	87	0 1160 00	88	0 6200-01	89	0 1100 00	85	0 1170-01		
91	0 3780-01	92	0 1170 00	93	0 1170 00	94	0 8970-01	90	0 1500-01		
96	0 1170 00	97	0 1170 00	98	0 1160 00	99	0 9970-01	95	0 1100 00		
101	0 5260-01	102	0 8230-01	103	0 8230-01	104	0 1330 00	100	0 0000 00		
106	0 1870 00	107	0 1680 00	108	0 1620 00	109	0 1520 00	105	0 1650 00		
111	0 1000 01	112	0 9090 00	113	0 8840 00	114	0 8500 00	110	0 1400 00		
116	0 8090 00	117	0 7820 00	118	0 7590 00	119	0 7440 00	115	0 6330 00		
121	0 5900 00	122	0 1000 01	123	0 8250 00	124	0 7180 00	120	0 7160 00		
126	0 5430 00	127	0 4740 00	128	0 4130 00	129	0 3610 00	125	0 6250 00		
131	0 2740 00	132	0 2360 00	133	0 1000 01	134	0 8420 00	130	0 3180 00		
136	0 5430 00	137	0 5690 00	138	0 4860 00	139	0 4310 00	135	0 3780 00		
141	0 2900 00	142	0 3840 00	143	0 2430 00	144	0 1000 01	140	0 7450 00		
146	0 8840 00	147	0 8600 00	148	0 8330 00	149	0 8090 00	145	0 5050 00		
151	0 7530 00	152	0 7440 00	153	0 7160 00	154	0 6900 00	150	0 7820 00		
156	0 5260-01	157	0 8930-01	158	0 1330 00	159	0 5900 00	155	0 0000 00		
161	0 1670 00	162	0 8930-01	163	0 1620 00	164	0 1530 00	160	0 1650 00		
166	0 0000 00	167	0 1500-01	168	0 3780-01	169	0 4200-01	165	0 1400 00		
171	0 8970-01	172	0 1100-01	173	0 1170-01	174	0 1170-01	170	0 8250-01		
176	0 1100 00							175	0 1160 00		

CONC DISTRIBUTION AT TIME • 80.000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000 00	3	0.3000-01	4	0.4770-01	5	0.7050-01	6	0.1010 00	7	0.1220 00
4	0.1220 00	6	0.1360 00	8	0.1470 00	9	0.1530 00	10	0.1530 00	11	0.1470 00
11	0.1470 00	12	0.0000 00	13	0.5800-01	14	0.1100 00	15	0.1480 00	16	0.1480 00
16	0.1740 00	17	0.1890 00	18	0.1950 00	19	0.1950 00	20	0.1970 00	21	0.1900 00
21	0.1900 00	22	0.1800 00	23	0.1600 01	24	0.1600 00	25	0.9020 00	26	0.8840 00
26	0.8840 00	27	0.8590 00	28	0.8400 00	29	0.8250 00	30	0.9020 00	31	0.7830 00
31	0.7830 00	32	0.7580 00	33	0.7430 00	34	0.7150 00	35	0.7970 00	36	0.7360 00
36	0.7360 00	37	0.6470 00	38	0.6580 00	39	0.1000 01	40	0.8410 00	41	0.3990 00
41	0.3990 00	42	0.3590 00	43	0.3180 00	44	0.3040 00	45	0.4470 00	46	0.8020 00
46	0.8020 00	47	0.8000 00	48	0.7030 00	49	0.5040 00	50	0.1000 01	51	0.4170 00
51	0.4170 00	52	0.4210 00	53	0.3720 00	54	0.5160 00	55	0.5410 00	56	0.1000 01
56	0.1000 01	57	0.8230 00	58	0.8030 00	59	0.3280 00	60	0.2890 00	61	0.8400 00
61	0.8400 00	62	0.8150 00	63	0.7870 00	64	0.8840 00	65	0.8590 00	66	0.7830 00
66	0.7830 00	67	0.0000 00	68	0.5800-01	69	0.7830 00	70	0.7580 00	71	0.1740 00
71	0.1740 00	72	0.1880 00	73	0.1880 00	74	0.1080 00	75	0.1480 00	76	0.1900 00
76	0.1900 00	77	0.1800 00	78	0.0000 00	79	0.1950 00	80	0.1970 00	81	0.7060 00
81	0.7060 00	82	0.1010 00	83	0.1220 00	84	0.1360 00	85	0.4770-01	86	0.1530 00
86	0.1530 00	87	0.1530 00	88	0.1470 00	89	0.0000 00	90	0.1470 00	91	0.4770-01
91	0.4770-01	92	0.7050-01	93	0.1010 00	94	0.1220 00	95	0.2000-01	96	0.1470 00
96	0.1470 00	97	0.1530 00	98	0.1530 00	99	0.1470 00	100	0.0000 00	101	0.5800-01
101	0.5800-01	102	0.1100 00	103	0.1480 00	104	0.1740 00	105	0.0000 00	106	0.1470 00
106	0.1470 00	107	0.1890 00	108	0.1970 00	109	0.1900 00	110	0.1800 00	111	0.1000 01
111	0.1000 01	112	0.8230 00	113	0.8150 00	114	0.8030 00	115	0.8590 00	116	0.8400 00
116	0.8400 00	117	0.7970 00	118	0.7970 00	119	0.8840 00	120	0.7580 00	121	0.7830 00
121	0.7830 00	122	0.1000 01	123	0.8410 00	124	0.7360 00	125	0.6470 00	126	0.5580 00
126	0.5580 00	127	0.3040 00	128	0.4470 00	129	0.3990 00	130	0.5470 00	131	0.3180 00
131	0.3180 00	132	0.2810 00	133	0.1000 01	134	0.3020 00	135	0.3590 00	136	0.7030 00
136	0.7030 00	137	0.8160 00	138	0.8410 00	139	0.8020 00	140	0.8000 00	141	0.3720 00
141	0.3720 00	142	0.3280 00	143	0.2890 00	144	0.4770 00	145	0.4310 00	146	0.3020 00
146	0.3020 00	147	0.8840 00	148	0.8590 00	149	0.8400 01	150	0.8150 00	151	0.7970 00
151	0.7970 00	152	0.7830 00	153	0.7580 00	154	0.7430 00	155	0.6150 00	156	0.0000 00
156	0.0000 00	157	0.8000-01	158	0.7580 00	159	0.1740 00	160	0.1890 00	161	0.1960 00
161	0.1960 00	162	0.1860 00	163	0.1480 00	164	0.1970 00	165	0.1800 00	166	0.0000 00
166	0.0000 00	167	0.2000-01	168	0.4770-01	169	0.7050 00	170	0.1010 00	171	0.1220 00
171	0.1220 00	172	0.1360 00	173	0.1470 00	174	0.1530 00	175	0.1010 00	176	0.1370 00

100 Elements

INPUT DATA FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENT METHOD

TOTAL NO OF ELEMENTS : 100
TOTAL NO OF NODES : 252
MAXIMUM NO. OF NODES PER ELEMENT : 8
TOTAL NO. OF MATERIALS : 1
NUMBER OF PUMPING WELLS : 0
NUMBER OF CONCS TO BE ESTIMATED : 228

NUMBER OF PUMPING PERIODS : 0
TOTAL SIMULATION PERIODS : 3
FACTOR MULTIPLYING COMPUTED CONCS : 1.00000

STEP SIZE : 10.00000
STATE OF PROBLEM : 1
NO OF SPECIFIED CONDITIONS : 80

COORDINATES AND INITIAL CONCS OF NODES (L)

NODES	V(I)	X(I)	Z(I)	CINI(I)
1	0.000 00	0.000 00	0.100 03	0.000 00
2	0.100 02	0.000 00	0.100 03	0.000 00
3	0.200 02	0.000 00	0.100 03	0.000 00
4	0.300 02	0.000 00	0.100 03	0.000 00
5	0.400 02	0.000 00	0.100 03	0.000 00
6	0.500 02	0.000 00	0.100 03	0.000 00
7	0.600 02	0.000 00	0.100 03	0.000 00
8	0.700 02	0.000 00	0.100 03	0.000 00
9	0.800 02	0.000 00	0.100 03	0.000 00
10	0.900 02	0.000 00	0.100 03	0.000 00
11	0.100 03	0.000 00	0.100 03	0.000 00
12	0.000 00	0.100 02	0.100 03	0.000 00
13	0.100 02	0.100 02	0.100 03	0.000 00
14	0.200 02	0.100 02	0.100 03	0.000 00
15	0.300 02	0.100 02	0.100 03	0.000 00
16	0.400 02	0.100 02	0.100 03	0.000 00
17	0.500 02	0.100 02	0.100 03	0.000 00
18	0.600 02	0.100 02	0.100 03	0.000 00
19	0.700 02	0.100 02	0.100 03	0.000 00
20	0.800 02	0.100 02	0.100 03	0.000 00
21	0.900 02	0.100 02	0.100 03	0.000 00
22	0.100 03	0.100 02	0.100 03	0.000 00
23	0.000 00	0.200 02	0.100 03	0.100 01
24	0.100 02	0.200 02	0.100 03	0.000 00
25	0.200 02	0.200 02	0.100 03	0.000 00
26	0.300 02	0.200 02	0.100 03	0.000 00
27	0.400 02	0.200 02	0.100 03	0.000 00
28	0.500 02	0.200 02	0.100 03	0.000 00
29	0.600 02	0.200 02	0.100 03	0.000 00
30	0.700 02	0.200 02	0.100 03	0.000 00
31	0.800 02	0.200 02	0.100 03	0.000 00
32	0.900 02	0.200 02	0.100 03	0.000 00
33	0.100 03	0.300 02	0.100 03	0.000 00
34	0.000 00	0.300 02	0.100 03	0.100 01
35	0.100 02	0.300 02	0.100 03	0.000 00
36	0.200 02	0.300 02	0.100 03	0.000 00
37	0.300 02	0.300 02	0.100 03	0.000 00
38	0.400 02	0.300 02	0.100 03	0.000 00
39	0.500 02	0.300 02	0.100 03	0.000 00
40	0.600 02	0.300 02	0.100 03	0.000 00
41	0.700 02	0.300 02	0.100 03	0.000 00
42	0.800 02	0.300 02	0.100 03	0.000 00
43	0.900 02	0.300 02	0.100 03	0.000 00
44	0.100 03	0.400 02	0.100 03	0.000 00
45	0.000 00	0.400 02	0.100 03	0.100 01
46	0.100 02	0.400 02	0.100 03	0.000 00
47	0.200 02	0.400 02	0.100 03	0.000 00

48	0.300 03	0.200 02	0.100 03	0.000 00	108	0.800 03	0.400 02	0.100 03	0.000 00
49	0.500 03	0.300 02	0.100 03	0.000 00	109	0.900 03	0.500 02	0.100 03	0.000 00
50	0.700 03	0.400 02	0.100 03	0.000 00	110	0.100 03	0.600 02	0.100 03	0.000 00
51	0.600 03	0.300 02	0.100 03	0.000 00	111	0.000 00	0.700 02	0.100 03	0.000 00
52	0.800 03	0.500 02	0.100 03	0.000 00	112	0.100 03	0.800 02	0.100 03	0.000 00
53	0.900 03	0.600 02	0.100 03	0.000 00	113	0.200 03	0.900 02	0.100 03	0.000 00
54	0.100 03	0.200 02	0.100 03	0.000 00	114	0.300 03	0.100 02	0.100 03	0.000 00
55	0.000 00	0.350 02	0.100 03	0.000 01	115	0.400 03	0.200 02	0.100 03	0.000 00
57	0.100 03	0.350 02	0.100 03	0.000 00	116	0.500 03	0.300 02	0.100 03	0.000 00
58	0.200 03	0.350 02	0.100 03	0.000 00	117	0.600 03	0.400 02	0.100 03	0.000 00
59	0.300 03	0.350 02	0.100 03	0.000 00	118	0.700 03	0.500 02	0.100 03	0.000 00
60	0.400 03	0.350 02	0.100 03	0.000 00	119	0.800 03	0.600 02	0.100 03	0.000 00
61	0.500 03	0.350 02	0.100 03	0.000 00	120	0.900 03	0.700 02	0.100 03	0.000 00
62	0.600 03	0.350 02	0.100 03	0.000 00	121	0.100 03	0.800 02	0.100 03	0.000 00
63	0.700 03	0.350 02	0.100 03	0.000 00	122	0.000 00	0.900 02	0.100 03	0.000 00
64	0.800 03	0.350 02	0.100 03	0.000 00	123	0.100 03	0.000 00	0.000 00	0.000 00
65	0.900 03	0.350 02	0.100 03	0.000 00	124	0.200 03	0.100 00	0.000 00	0.000 00
66	0.100 03	0.400 02	0.100 03	0.000 00	125	0.300 03	0.200 00	0.000 00	0.000 00
67	0.000 00	0.400 02	0.100 03	0.000 01	126	0.400 03	0.300 00	0.000 00	0.000 00
68	0.100 03	0.400 02	0.100 03	0.000 00	127	0.500 03	0.400 00	0.000 00	0.000 00
69	0.200 03	0.400 02	0.100 03	0.000 00	128	0.600 03	0.500 00	0.000 00	0.000 00
70	0.300 03	0.400 02	0.100 03	0.000 00	129	0.700 03	0.600 00	0.000 00	0.000 00
71	0.400 03	0.400 02	0.100 03	0.000 00	130	0.800 03	0.700 00	0.000 00	0.000 00
72	0.500 03	0.400 02	0.100 03	0.000 00	131	0.900 03	0.800 00	0.000 00	0.000 00
73	0.600 03	0.400 02	0.100 03	0.000 00	132	0.100 03	0.900 00	0.000 00	0.000 00
74	0.700 03	0.400 02	0.100 03	0.000 00	133	0.000 00	0.000 00	0.000 00	0.000 00
75	0.800 03	0.400 02	0.100 03	0.000 00	134	0.100 03	0.100 00	0.000 00	0.000 00
76	0.900 03	0.400 02	0.100 03	0.000 00	135	0.200 03	0.200 00	0.000 00	0.000 00
77	0.100 03	0.400 02	0.100 03	0.000 01	136	0.300 03	0.300 00	0.000 00	0.000 00
78	0.000 00	0.450 02	0.100 03	0.000 00	137	0.400 03	0.400 00	0.000 00	0.000 00
79	0.100 03	0.450 02	0.100 03	0.000 00	138	0.500 03	0.500 00	0.000 00	0.000 00
80	0.200 03	0.450 02	0.100 03	0.000 00	139	0.600 03	0.600 00	0.000 00	0.000 00
81	0.300 03	0.450 02	0.100 03	0.000 00	140	0.700 03	0.700 00	0.000 00	0.000 00
82	0.400 03	0.450 02	0.100 03	0.000 00	141	0.800 03	0.800 00	0.000 00	0.000 00
83	0.500 03	0.450 02	0.100 03	0.000 00	142	0.900 03	0.900 00	0.000 00	0.000 00
84	0.600 03	0.450 02	0.100 03	0.000 00	143	0.100 03	0.100 00	0.000 00	0.000 00
85	0.700 03	0.450 02	0.100 03	0.000 00	144	0.200 03	0.200 00	0.000 00	0.000 00
86	0.800 03	0.450 02	0.100 03	0.000 00	145	0.300 03	0.300 00	0.000 00	0.000 00
87	0.900 03	0.450 02	0.100 03	0.000 00	146	0.400 03	0.400 00	0.000 00	0.000 00
88	0.100 03	0.450 02	0.100 03	0.000 00	147	0.500 03	0.500 00	0.000 00	0.000 00
89	0.000 00	0.450 02	0.100 03	0.000 01	148	0.600 03	0.600 00	0.000 00	0.000 00
90	0.100 03	0.500 02	0.100 03	0.000 00	149	0.700 03	0.700 00	0.000 00	0.000 00
91	0.200 03	0.500 02	0.100 03	0.000 00	150	0.800 03	0.800 00	0.000 00	0.000 00
92	0.300 03	0.500 02	0.100 03	0.000 00	151	0.900 03	0.900 00	0.000 00	0.000 00
93	0.400 03	0.500 02	0.100 03	0.000 00	152	0.100 03	0.100 00	0.000 00	0.000 00
94	0.500 03	0.500 02	0.100 03	0.000 00	153	0.200 03	0.200 00	0.000 00	0.000 00
95	0.600 03	0.500 02	0.100 03	0.000 00	154	0.300 03	0.300 00	0.000 00	0.000 00
96	0.700 03	0.500 02	0.100 03	0.000 00	155	0.400 03	0.400 00	0.000 00	0.000 00
97	0.800 03	0.500 02	0.100 03	0.000 00	156	0.500 03	0.500 00	0.000 00	0.000 00
98	0.900 03	0.500 02	0.100 03	0.000 00	157	0.600 03	0.600 00	0.000 00	0.000 00
99	0.100 03	0.500 02	0.100 03	0.000 00	158	0.700 03	0.700 00	0.000 00	0.000 00
100	0.000 00	0.500 02	0.100 03	0.000 00	159	0.800 03	0.800 00	0.000 00	0.000 00
101	0.100 03	0.500 02	0.100 03	0.000 00	160	0.900 03	0.900 00	0.000 00	0.000 00
102	0.200 03	0.500 02	0.100 03	0.000 00	161	0.100 03	0.100 00	0.000 00	0.000 00
103	0.300 03	0.500 02	0.100 03	0.000 00	162	0.200 03	0.200 00	0.000 00	0.000 00
104	0.400 03	0.500 02	0.100 03	0.000 00	163	0.300 03	0.300 00	0.000 00	0.000 00
105	0.500 03	0.500 02	0.100 03	0.000 00	164	0.400 03	0.400 00	0.000 00	0.000 00
106	0.600 03	0.500 02	0.100 03	0.000 00	165	0.500 03	0.500 00	0.000 00	0.000 00
107	0.700 03	0.500 02	0.100 03	0.000 00	166	0.600 03	0.600 00	0.000 00	0.000 00
					167	0.700 03	0.700 00	0.000 00	0.000 00

NODE-ELEMENT RELATIONSHIP

ELEMS	N1	N2	N3	N4	N5	N6	N7	N8
1	1	12	12	2	122	133	134	133
2	2	13	14	3	123	134	135	134
3	3	14	15	4	124	135	136	135
4	4	15	16	5	125	136	137	136
5	5	16	17	6	126	137	138	137
6	6	17	18	7	127	138	139	138
7	7	18	19	8	128	139	140	139
8	8	19	20	9	129	140	141	140
9	9	20	21	10	130	141	142	141
10	10	21	22	11	131	142	143	142
11	11	22	23	12	132	143	144	143
12	12	23	24	13	133	144	145	144
13	13	24	25	14	134	145	146	145
14	14	25	26	15	135	146	147	146
15	15	26	27	16	136	147	148	147
16	16	27	28	17	137	148	149	148
17	17	28	29	18	138	149	150	149
18	18	29	30	19	139	150	151	150
19	19	30	31	20	140	151	152	151
20	20	31	32	21	141	152	153	152
21	21	32	33	22	142	153	154	153
22	22	33	34	23	143	154	155	154
23	23	34	35	24	144	155	156	155
24	24	35	36	25	145	156	157	156
25	25	36	37	26	146	157	158	157
26	26	37	38	27	147	158	159	158
27	27	38	39	28	148	159	160	159
28	28	39	40	29	149	160	161	160
29	29	40	41	30	150	161	162	161
30	30	41	42	31	151	162	163	162
31	31	42	43	32	152	163	164	163
32	32	43	44	33	153	164	165	164
33	33	44	45	34	154	165	166	165
34	34	45	46	35	155	166	167	166
35	35	46	47	36	156	167	168	167
36	36	47	48	37	157	168	169	168
37	37	48	49	38	158	169	170	169
38	38	49	50	39	159	170	171	170
39	39	50	51	40	160	171	172	171
40	40	51	52	41	161	172	173	172
41	41	52	53	42	162	173	174	173
42	42	53	54	43	163	174	175	174
43	43	54	55	44	164	175	176	175
44	44	55	56	45	165	176	177	176
45	45	56	57	46	166	177	178	177
46	46	57	58	47	167	178	179	178
47	47	58	59	48	168	179	180	179
48	48	59	60	49	169	180	181	180
49	49	60	61	50	170	181	182	181
50	50	61	62	51	171	182	183	182

47	63	173	184	193	184	173
48	64	174	185	184	185	174
49	65	175	186	185	186	175
50	66	176	187	186	187	176
51	67	177	188	187	188	177
52	68	178	189	188	189	178
53	69	179	190	189	190	179
54	70	180	191	190	191	180
55	71	181	192	191	192	181
56	72	182	193	192	193	182
57	73	183	194	193	194	183
58	74	184	195	194	195	184
59	75	185	196	195	196	185
60	76	186	197	196	197	186
61	77	187	198	197	198	187
62	78	188	199	198	199	188
63	79	189	200	199	200	189
64	80	190	201	200	201	190
65	81	191	202	201	202	191
66	82	192	203	202	203	192
67	83	193	204	203	204	193
68	84	194	205	204	205	194
69	85	195	206	205	206	195
70	86	196	207	206	207	196
71	87	197	208	207	208	197
72	88	198	209	208	209	198
73	89	199	210	209	210	199
74	90	200	211	210	211	200
75	91	201	212	211	212	201
76	92	202	213	212	213	202
77	93	203	214	213	214	203
78	94	204	215	214	215	204
79	95	205	216	215	216	205
80	96	206	217	216	217	206
81	97	207	218	217	218	207
82	98	208	219	218	219	208
83	99	209	220	219	220	209
84	100	210	221	220	221	210
85	101	211	222	221	222	211
86	102	212	223	222	223	212
87	103	213	224	223	224	213
88	104	214	225	224	225	214
89	105	215	226	225	226	215
90	106	216	227	226	227	216
91	107	217	228	227	228	217
92	108	218	229	228	229	218
93	109	219	230	229	230	219
94	110	220	231	230	231	220
95	111	221	232	231	232	221
96	112	222	233	232	233	222
97	113	223	234	233	234	223
98	114	224	235	234	235	224
99	115	225	236	235	236	225
100	116	226	237	236	237	226
	117	227	238	237	238	227
	118	228	239	238	239	228
	119	229	240	239	240	229
	120	230	241	240	241	230
	121	231	242	241	242	231

APPENDIX D**INPUT/OUTPUT OF TWO-DIMENSIONAL TESTING**

INPUT DATA FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENT METHOD

TOTAL NO OF ELEMENTS • 81
TOTAL NO OF NODES • 200
MAXIMUM NO OF MODES PER ELEMENT • 8
TOTAL NO OF MATERIALS • 1
NUMBER OF PUMPING WELLS • 0
NUMBER OF CONCS TO BE ESTIMATED • 180

NUMBER OF PUMPING PERIODS • 0
TOTAL SIMULATION PERIODS • 7
FACTOR MULTIPLYING COMPUTED CONCS • 1.00000

STEP SIZE • 25.00000
STATE OF PROBLEM • 1
NO OF SPECIFIED CONDITIONS • 62

NODES	COORDINATES AND INITIAL CONCS OF NODES (L)				CINT(I)
	V(I)	X(I)	Z(I)		
1	0.000 00	0.000 00	0.100 02	0.800-02	
2	0.100 03	0.000 00	0.100 02	0.700-01	
3	0.200 03	0.000 00	0.100 02	0.310 00	
4	0.300 03	0.000 00	0.100 02	0.740 00	
5	0.400 03	0.000 00	0.100 02	0.100 01	
6	0.500 03	0.000 00	0.100 02	0.740 00	
7	0.600 03	0.000 00	0.100 02	0.310 00	
8	0.700 03	0.000 00	0.100 02	0.700-01	
9	0.800 03	0.000 00	0.100 02	0.800-02	
10	0.900 03	0.000 00	0.100 02	0.000 00	
11	0.000 00	0.200 03	0.100 02	0.000 00	
12	0.100 03	0.200 03	0.100 02	0.000 00	
13	0.200 03	0.200 03	0.100 02	0.000 00	
14	0.300 03	0.200 03	0.100 02	0.000 00	
15	0.400 03	0.200 03	0.100 02	0.000 00	
16	0.500 03	0.200 03	0.100 02	0.000 00	
17	0.600 03	0.200 03	0.100 02	0.000 00	
18	0.700 03	0.200 03	0.100 02	0.000 00	
19	0.800 03	0.200 03	0.100 02	0.000 00	
20	0.900 03	0.200 03	0.100 02	0.000 00	
21	0.000 00	0.400 03	0.100 02	0.000 00	
22	0.100 03	0.400 03	0.100 02	0.000 00	
23	0.200 03	0.400 03	0.100 02	0.000 00	
24	0.300 03	0.400 03	0.100 02	0.000 00	
25	0.400 03	0.400 03	0.100 02	0.000 00	
26	0.500 03	0.400 03	0.100 02	0.000 00	
27	0.600 03	0.400 03	0.100 02	0.000 00	
28	0.700 03	0.400 03	0.100 02	0.000 00	
29	0.800 03	0.400 03	0.100 02	0.000 00	
30	0.900 03	0.400 03	0.100 02	0.000 00	
31	0.000 00	0.600 03	0.100 02	0.000 00	
32	0.100 03	0.600 03	0.100 02	0.000 00	
33	0.200 03	0.600 03	0.100 02	0.000 00	
34	0.300 03	0.600 03	0.100 02	0.000 00	
35	0.400 03	0.600 03	0.100 02	0.000 00	
36	0.500 03	0.600 03	0.100 02	0.000 00	
37	0.600 03	0.600 03	0.100 02	0.000 00	
38	0.700 03	0.600 03	0.100 02	0.000 00	
39	0.800 03	0.600 03	0.100 02	0.000 00	
40	0.900 03	0.600 03	0.100 02	0.000 00	
41	0.000 00	0.800 03	0.100 02	0.000 00	
42	0.100 03	0.800 03	0.100 02	0.000 00	
43	0.200 03	0.800 03	0.100 02	0.000 00	
44	0.300 03	0.800 03	0.100 02	0.000 00	
45	0.400 03	0.800 03	0.100 02	0.000 00	
46	0.500 03	0.800 03	0.100 02	0.000 00	
47	0.600 03	0.800 03	0.100 02	0.000 00	

48	0.700 03	0.800 03	0.100 02	0.000 00
49	0.800 03	0.800 03	0.100 02	0.000 00
50	0.900 03	0.800 03	0.100 02	0.000 00
51	0.000 00	0.100 04	0.100 02	0.000 00
52	0.100 03	0.100 04	0.100 02	0.000 00
53	0.200 03	0.100 04	0.100 02	0.000 00
54	0.300 03	0.100 04	0.100 02	0.000 00
55	0.400 03	0.100 04	0.100 02	0.000 00
56	0.500 03	0.100 04	0.100 02	0.000 00
57	0.600 03	0.100 04	0.100 02	0.000 00
58	0.700 03	0.100 04	0.100 02	0.000 00
59	0.800 03	0.100 04	0.100 02	0.000 00
60	0.900 03	0.100 04	0.100 02	0.000 00
61	0.000 00	0.120 04	0.100 02	0.000 00
62	0.100 03	0.120 04	0.100 02	0.000 00
63	0.200 03	0.120 04	0.100 02	0.000 00
64	0.300 03	0.120 04	0.100 02	0.000 00
65	0.400 03	0.120 04	0.100 02	0.000 00
66	0.500 03	0.120 04	0.100 02	0.000 00
67	0.600 03	0.120 04	0.100 02	0.000 00
68	0.700 03	0.120 04	0.100 02	0.000 00
69	0.800 03	0.120 04	0.100 02	0.000 00
70	0.900 03	0.120 04	0.100 02	0.000 00
71	0.000 00	0.140 04	0.100 02	0.000 00
72	0.100 03	0.140 04	0.100 02	0.000 00
73	0.200 03	0.140 04	0.100 02	0.000 00
74	0.300 03	0.140 04	0.100 02	0.000 00
75	0.400 03	0.140 04	0.100 02	0.000 00
76	0.500 03	0.140 04	0.100 02	0.000 00
77	0.600 03	0.140 04	0.100 02	0.000 00
78	0.700 03	0.140 04	0.100 02	0.000 00
79	0.800 03	0.140 04	0.100 02	0.000 00
80	0.900 03	0.140 04	0.100 02	0.000 00
81	0.000 00	0.160 04	0.100 02	0.000 00
82	0.100 03	0.160 04	0.100 02	0.000 00
83	0.200 03	0.160 04	0.100 02	0.000 00
84	0.300 03	0.160 04	0.100 02	0.000 00
85	0.400 03	0.160 04	0.100 02	0.000 00
86	0.500 03	0.160 04	0.100 02	0.000 00
87	0.600 03	0.160 04	0.100 02	0.000 00
88	0.700 03	0.160 04	0.100 02	0.000 00
89	0.800 03	0.160 04	0.100 02	0.000 00
90	0.900 03	0.160 04	0.100 02	0.000 00
91	0.000 00	0.180 04	0.100 02	0.000 00
92	0.100 03	0.180 04	0.100 02	0.000 00
93	0.200 03	0.180 04	0.100 02	0.000 00
94	0.300 03	0.180 04	0.100 02	0.000 00
95	0.400 03	0.180 04	0.100 02	0.000 00
96	0.500 03	0.180 04	0.100 02	0.000 00
97	0.600 03	0.180 04	0.100 02	0.000 00
98	0.700 03	0.180 04	0.100 02	0.000 00
99	0.800 03	0.180 04	0.100 02	0.000 00
100	0.900 03	0.180 04	0.100 02	0.000 00
101	0.000 00	0.000 00	0.000 00	0.900-02
102	0.100 03	0.000 00	0.000 00	0.700-01
103	0.200 03	0.000 00	0.000 00	0.310 00
104	0.300 03	0.000 00	0.000 00	0.740 00
105	0.400 03	0.000 00	0.000 00	0.100 01
106	0.500 03	0.000 00	0.000 00	0.740 00
107	0.600 03	0.000 00	0.000 00	0.310 00

ELEMS	N1	N2	N3	N4	N5	N6	N7	N8
1	1	11	13	3	101	111	112	102
2	2	12	14	4	102	112	113	103
3	3	13	15	5	103	113	114	104
4	4	14	16	6	104	114	115	105
5	5	15	17	7	105	115	116	106
6	6	16	18	8	106	116	117	107
7	7	17	19	9	107	117	118	108
8	8	18	20	10	108	118	119	109
9	9	19	21	11	109	119	120	110
10	10	20	22	12	110	120	121	111
11	11	21	23	13	111	121	122	112
12	12	22	24	14	112	122	123	113
13	13	23	25	15	113	123	124	114
14	14	24	26	16	114	124	125	115
15	15	25	27	17	115	125	126	116
16	16	26	28	18	116	126	127	117
17	17	27	29	19	117	127	128	118
18	18	28	30	20	118	128	129	119
19	19	29	31	21	119	129	130	120
20	20	30	32	22	120	130	131	121
21	21	31	33	23	121	131	132	122
22	22	32	34	24	122	132	133	123
23	23	33	35	25	123	133	134	124
24	24	34	36	26	124	134	135	125
25	25	35	37	27	125	135	136	126
26	26	36	38	28	126	136	137	127
27	27	37	39	29	127	137	138	128
28	28	38	40	30	128	138	139	129
29	29	39	41	31	129	139	140	130
30	30	40	42	32	130	140	141	131
31	31	41	43	33	131	141	142	132
32	32	42	44	34	132	142	143	133
33	33	43	45	35	133	143	144	134
34	34	44	46	36	134	144	145	135
35	35	45	47	37	135	145	146	136
36	36	46	48	38	136	146	147	137
37	37	47	49	39	137	147	148	138
38	38	48	50	40	138	148	149	139
39	39	49	51	41	139	149	150	140
40	40	50	52	42	140	150	151	141
41	41	51		43	141	151		142
42	42	52		44	142	152		143
43	43			45	143	153		144
44	44			46	144	154		145
45	45			47	145	155		146
46	46			48	146	156		147
				49	147	157		148
				50	148	158		149
				51	149	159		150
				52	150	160		151
					151	161		152

47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81
 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100
 101 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120
 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140
 141 142 143 144 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168 169 170 171 172 173 174 175 176 177 178 179 180 181 182 183 184 185 186 187 188 189 190
 191 192 193 194 195 196 197 198 199 200
 201 202 203 204 205 206 207 208 209 210 211 212 213 214 215 216 217 218 219 220 221 222 223 224 225 226 227 228 229 230 231 232 233 234 235 236 237 238 239 240 241 242 243 244 245 246 247 248 249 250
 251 252 253 254 255 256 257 258 259 260 261 262 263 264 265 266 267 268 269 270 271 272 273 274 275 276 277 278 279 280 281 282 283 284 285 286 287 288 289 290 291 292 293 294 295 296 297 298 299 300
 301 302 303 304 305 306 307 308 309 310 311 312 313 314 315 316 317 318 319 320 321 322 323 324 325 326 327 328 329 330 331 332 333 334 335 336 337 338 339 340 341 342 343 344 345 346 347 348 349 350
 351 352 353 354 355 356 357 358 359 360 361 362 363 364 365 366 367 368 369 370 371 372 373 374 375 376 377 378 379 380 381 382 383 384 385 386 387 388 389 390 391 392 393 394 395 396 397 398 399 400
 401 402 403 404 405 406 407 408 409 410 411 412 413 414 415 416 417 418 419 420 421 422 423 424 425 426 427 428 429 430 431 432 433 434 435 436 437 438 439 440 441 442 443 444 445 446 447 448 449 450
 451 452 453 454 455 456 457 458 459 460 461 462 463 464 465 466 467 468 469 470 471 472 473 474 475 476 477 478 479 480 481 482 483 484 485 486 487 488 489 490 491 492 493 494 495 496 497 498 499 500
 501 502 503 504 505 506 507 508 509 510 511 512 513 514 515 516 517 518 519 520 521 522 523 524 525 526 527 528 529 530 531 532 533 534 535 536 537 538 539 540 541 542 543 544 545 546 547 548 549 550
 551 552 553 554 555 556 557 558 559 560 561 562 563 564 565 566 567 568 569 570 571 572 573 574 575 576 577 578 579 580 581 582 583 584 585 586 587 588 589 590 591 592 593 594 595 596 597 598 599 600
 601 602 603 604 605 606 607 608 609 610 611 612 613 614 615 616 617 618 619 620 621 622 623 624 625 626 627 628 629 630 631 632 633 634 635 636 637 638 639 640 641 642 643 644 645 646 647 648 649 650
 651 652 653 654 655 656 657 658 659 660 661 662 663 664 665 666 667 668 669 670 671 672 673 674 675 676 677 678 679 680 681 682 683 684 685 686 687 688 689 690 691 692 693 694 695 696 697 698 699 700
 701 702 703 704 705 706 707 708 709 710 711 712 713 714 715 716 717 718 719 720 721 722 723 724 725 726 727 728 729 730 731 732 733 734 735 736 737 738 739 740 741 742 743 744 745 746 747 748 749 750
 751 752 753 754 755 756 757 758 759 760 761 762 763 764 765 766 767 768 769 770 771 772 773 774 775 776 777 778 779 780 781 782 783 784 785 786 787 788 789 790 791 792 793 794 795 796 797 798 799 800
 801 802 803 804 805 806 807 808 809 810 811 812 813 814 815 816 817 818 819 820 821 822 823 824 825 826 827 828 829 830 831 832 833 834 835 836 837 838 839 840 841 842 843 844 845 846 847 848 849 850
 851 852 853 854 855 856 857 858 859 860 861 862 863 864 865 866 867 868 869 870 871 872 873 874 875 876 877 878 879 880 881 882 883 884 885 886 887 888 889 890 891 892 893 894 895 896 897 898 899 900
 901 902 903 904 905 906 907 908 909 910 911 912 913 914 915 916 917 918 919 920 921 922 923 924 925 926 927 928 929 930 931 932 933 934 935 936 937 938 939 940 941 942 943 944 945 946 947 948 949 950
 951 952 953 954 955 956 957 958 959 960 961 962 963 964 965 966 967 968 969 970 971 972 973 974 975 976 977 978 979 980 981 982 983 984 985 986 987 988 989 990 991 992 993 994 995 996 997 998 999 1000

OUTPUT FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENTS METHOD

INITIAL CONC DISTRIBUTION AT TIME = 0.000 DAYS									
NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000	3	0.0000	4	0.0000	5	0.0000		
6	0.0000	8	0.0000	9	0.0000	10	0.0000		
11	0.0000	13	0.0000	14	0.0000	15	0.0000		
16	0.0000	18	0.0000	19	0.0000	20	0.0000		
21	0.0000	22	0.0000	24	0.0000	25	0.0000		
26	0.0000	28	0.0000	29	0.0000	30	0.0000		
31	0.0000	33	0.0000	34	0.0000	35	0.0000		
36	0.0000	38	0.0000	39	0.0000	40	0.0000		
41	0.0000	43	0.0000	44	0.0000	45	0.0000		
46	0.0000	48	0.0000	49	0.0000	50	0.0000		
51	0.0000	53	0.0000	54	0.0000	55	0.0000		
56	0.0000	58	0.0000	59	0.0000	60	0.0000		
61	0.0000	63	0.0000	64	0.0000	65	0.0000		
66	0.0000	68	0.0000	69	0.0000	70	0.0000		
71	0.0000	73	0.0000	74	0.0000	75	0.0000		
76	0.0000	78	0.0000	79	0.0000	80	0.0000		
81	0.0000	83	0.0000	84	0.0000	85	0.0000		
86	0.0000	88	0.0000	89	0.0000	90	0.0000		
91	0.0000	93	0.0000	94	0.0000	95	0.0000		
96	0.0000	98	0.0000	99	0.0000	100	0.0000		
101	0.0000	103	0.0000	104	0.0000	105	0.0000		
106	0.0000	108	0.0000	109	0.0000	110	0.0000		
111	0.0000	113	0.0000	114	0.0000	115	0.0000		
116	0.0000	118	0.0000	119	0.0000	120	0.0000		
121	0.0000	123	0.0000	124	0.0000	125	0.0000		
126	0.0000	128	0.0000	129	0.0000	130	0.0000		
131	0.0000	132	0.0000	133	0.0000	135	0.0000		
136	0.0000	137	0.0000	138	0.0000	140	0.0000		
141	0.0000	142	0.0000	143	0.0000	145	0.0000		
146	0.0000	145	0.0000	147	0.0000	149	0.0000		
151	0.0000	152	0.0000	154	0.0000	155	0.0000		
156	0.0000	157	0.0000	159	0.0000	160	0.0000		
161	0.0000	163	0.0000	164	0.0000	165	0.0000		
166	0.0000	167	0.0000	169	0.0000	170	0.0000		
171	0.0000	173	0.0000	174	0.0000	175	0.0000		
176	0.0000	177	0.0000	179	0.0000	180	0.0000		
181	0.0000	183	0.0000	184	0.0000	185	0.0000		
186	0.0000	187	0.0000	189	0.0000	190	0.0000		
191	0.0000	193	0.0000	194	0.0000	195	0.0000		
196	0.0000	198	0.0000	199	0.0000	200	0.0000		

CONIC DISCRIMINANTI AL TIPO - 175,000 DAYS

NUMF\$	CONICS	INDICES	CONICS	INDICES	CONICS	INDICES	CONICS	INDICES	CONICS	INDICES	CONICS	INDICES	CONICS	INDICES
1	0 8000-02	2	0 7000-01	3	0 3060-00	4	0 7410-02	5	0 1000-01					
6	0 7410-00	7	0 3060-00	8	0 7000-01	9	0 9020-02	10	0 1000-01					
11	0 1000-02	12	0 3200-01	13	0 1920-00	14	0 5320-00	15	0 9020-02					
16	0 8410-00	17	0 5280-00	18	0 1800-00	19	0 0900-00	20	0 9070-00					
21	0 0000-00	22	0 0000-00	23	0 8000-02	24	0 2820-00	25	0 0000-00					
26	0 9840-00	27	0 8110-00	28	0 4020-00	29	0 1200-00	30	0 0000-00					
31	0 0000-00	32	0 0000-00	33	0 0000-00	34	0 2000-00	35	0 0000-00					
36	0 7700-00	37	0 7100-00	38	0 4140-00	39	0 1020-00	40	0 0000-00					
41	0 0000-00	42	0 0000-00	43	0 0000-00	44	0 0000-00	45	0 1670-00					
46	0 3520-00	47	0 3770-00	48	0 1870-00	49	0 0000-00	50	0 0000-00					
51	0 0000-00	52	0 0000-00	53	0 0000-00	54	0 0000-00	55	0 0000-00					
56	0 0000-00	57	0 0000-00	58	0 0000-00	59	0 0000-00	60	0 0000-00					
61	0 0000-00	62	0 0000-00	63	0 0000-00	64	0 0000-00	65	0 0000-00					
66	0 0000-00	67	0 0000-00	68	0 0000-00	69	0 0000-00	70	0 0000-00					
71	0 0000-00	72	0 0000-00	73	0 0000-00	74	0 0000-00	75	0 0000-00					
76	0 0000-00	77	0 0000-00	78	0 0000-00	79	0 0000-00	80	0 0000-00					
81	0 0000-00	82	0 0000-00	83	0 0000-00	84	0 0000-00	85	0 0000-00					
86	0 0000-00	87	0 0000-00	88	0 0000-00	89	0 0000-00	90	0 0000-00					
91	0 0000-00	92	0 0000-00	93	0 0000-00	94	0 0000-00	95	0 0000-00					
96	0 0000-00	97	0 0000-00	98	0 0000-00	99	0 0000-00	100	0 0000-00					
101	0 8000-02	102	0 7000-01	103	0 3060-00	104	0 7410-02	105	0 1000-01					
106	0 7410-00	107	0 3060-00	108	0 7000-01	109	0 8000-02	110	0 1000-01					
111	0 1000-02	112	0 3200-01	113	0 1920-00	114	0 5320-00	115	0 9070-00					
116	0 8410-00	117	0 5280-00	118	0 1800-00	119	0 0900-00	120	0 9070-00					
121	0 0000-00	122	0 0000-00	123	0 8000-02	124	0 2820-00	125	0 0000-00					
126	0 9840-00	127	0 8110-00	128	0 4020-00	129	0 1200-00	130	0 0000-00					
131	0 0000-00	132	0 0000-00	133	0 0000-00	134	0 2000-00	135	0 0000-00					
136	0 7700-00	137	0 7100-00	138	0 4140-00	139	0 1020-00	140	0 0000-00					
141	0 0000-00	142	0 0000-00	143	0 0000-00	144	0 0000-00	145	0 1670-00					
146	0 3520-00	147	0 3770-00	148	0 1870-00	149	0 0000-00	150	0 0000-00					
151	0 0000-00	152	0 0000-00	153	0 0000-00	154	0 0000-00	155	0 0000-00					
156	0 0000-00	157	0 0000-00	158	0 0000-00	159	0 0000-00	160	0 0000-00					
161	0 0000-00	162	0 0000-00	163	0 0000-00	164	0 0000-00	165	0 0000-00					
166	0 0000-00	167	0 0000-00	168	0 0000-00	169	0 0000-00	170	0 0000-00					
171	0 0000-00	172	0 0000-00	173	0 0000-00	174	0 0000-00	175	0 0000-00					
176	0 0000-00	177	0 0000-00	178	0 0000-00	179	0 0000-00	180	0 0000-00					
181	0 0000-00	182	0 0000-00	183	0 0000-00	184	0 0000-00	185	0 0000-00					
186	0 0000-00	187	0 0000-00	188	0 0000-00	189	0 0000-00	190	0 0000-00					
191	0 0000-00	192	0 0000-00	193	0 0000-00	194	0 0000-00	195	0 0000-00					
196	0 0000-00	197	0 0000-00	198	0 0000-00	199	0 0000-00	200	0 0000-00					

INPUT DATA FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENT METHOD.

TOTAL NO OF ELEMENTS : 81
TOTAL NO OF NODES : 200
MAXIMUM NO OF NODES PER ELEMENT : 8
TOTAL NO OF MATERIALS : 1
NUMBER OF PUMPING WELLS : 0
NUMBER OF CONCS TO BE ESTIMATED : 180

NUMBER OF PUMPING PERIODS : 0
TOTAL SIMULATION PERIODS : 7
FACTOR MULTIPLYING COMPUTED CONCS : 1 00000

STEP SIZE : 25 00000
STATE OF PROBLEM : 1
NO OF SPECIFIED CONDITIONS : 62

NODE - ELEMENT RELATIONSHIP

ELEMS	N1	N2	N3	N4	N5	N6	N7	N8
1	1	11	12	2	101	111	112	102
2	2	12	13	3	102	112	113	103
3	3	13	14	4	103	113	114	104
4	4	14	15	5	104	114	115	105
5	5	15	16	6	105	115	116	106
6	6	16	17	7	106	116	117	107
7	7	17	18	8	107	117	118	108
8	8	18	19	9	108	118	119	109
9	9	19	20	10	109	119	120	110
10	10	20	21	11	110	120	121	111
11	11	21	22	12	111	121	122	112
12	12	22	23	13	112	122	123	113
13	13	23	24	14	113	123	124	114
14	14	24	25	15	114	124	125	115
15	15	25	26	16	115	125	126	116
16	16	26	27	17	116	126	127	117
17	17	27	28	18	117	127	128	118
18	18	28	29	19	118	128	129	119
19	19	29	30	20	119	129	130	120
20	20	30	31	21	120	130	131	121
21	21	31	32	22	121	131	132	122
22	22	32	33	23	122	132	133	123
23	23	33	34	24	123	133	134	124
24	24	34	35	25	124	134	135	125
25	25	35	36	26	125	135	136	126
26	26	36	37	27	126	136	137	127
27	27	37	38	28	127	137	138	128
28	28	38	39	29	128	138	139	129
29	29	39	40	30	129	139	140	130
30	30	40	41	31	130	140	141	131
31	31	41	42	32	131	141	142	132
32	32	42	43	33	132	142	143	133
33	33	43	44	34	133	143	144	134
34	34	44	45	35	134	144	145	135
35	35	45	46	36	135	145	146	136
36	36	46	47	37	136	146	147	137
37	37	47	48	38	137	147	148	138
38	38	48	49	39	138	148	149	139
39	39	49	50	40	139	149	150	140
40	40	50	51	41	140	150	151	141
41	41	51	52	42	141	151	152	142
42	42	52	53	43	142	152	153	143
43	43	53	54	44	143	153	154	144
44	44	54	55	45	144	154	155	145
45	45	55	56	46	145	155	156	146
46	46	56	57	47	146	156	157	147
47	47	57	58	48	147	157	158	148
48	48	58	59	49	148	158	159	149
49	49	59	60	50	149	159	160	150
50	50	60	61	51	150	160	161	151
51	51	61	62	52	151	161	162	152

47	52	57	62	67	72	77	82	87	92	97	102	107	112	117	122	127	132	137	142	147	152	157	162	167	172	177	182	187	192	197	202
48	53	58	63	68	73	78	83	88	93	98	103	108	113	118	123	128	133	138	143	148	153	158	163	168	173	178	183	188	193	198	203
49	54	59	64	69	74	79	84	89	94	99	104	109	114	119	124	129	134	139	144	149	154	159	164	169	174	179	184	189	194	199	204
50	55	60	65	70	75	80	85	90	95	100	105	110	115	120	125	130	135	140	145	150	155	160	165	170	175	180	185	190	195	200	205
51	56	61	66	71	76	81	86	91	96	101	106	111	116	121	126	131	136	141	146	151	156	161	166	171	176	181	186	191	196	201	206
52	57	62	67	72	77	82	87	92	97	102	107	112	117	122	127	132	137	142	147	152	157	162	167	172	177	182	187	192	197	202	207
53	58	63	68	73	78	83	88	93	98	103	108	113	118	123	128	133	138	143	148	153	158	163	168	173	178	183	188	193	198	203	208
54	59	64	69	74	79	84	89	94	99	104	109	114	119	124	129	134	139	144	149	154	159	164	169	174	179	184	189	194	199	204	209
55	60	65	70	75	80	85	90	95	100	105	110	115	120	125	130	135	140	145	150	155	160	165	170	175	180	185	190	195	200	205	210
56	61	66	71	76	81	86	91	96	101	106	111	116	121	126	131	136	141	146	151	156	161	166	171	176	181	186	191	196	201	206	211
57	62	67	72	77	82	87	92	97	102	107	112	117	122	127	132	137	142	147	152	157	162	167	172	177	182	187	192	197	202	207	212
58	63	68	73	78	83	88	93	98	103	108	113	118	123	128	133	138	143	148	153	158	163	168	173	178	183	188	193	198	203	208	213
59	64	69	74	79	84	89	94	99	104	109	114	119	124	129	134	139	144	149	154	159	164	169	174	179	184	189	194	199	204	209	214
60	65	70	75	80	85	90	95	100	105	110	115	120	125	130	135	140	145	150	155	160	165	170	175	180	185	190	195	200	205	210	215
61	66	71	76	81	86	91	96	101	106	111	116	121	126	131	136	141	146	151	156	161	166	171	176	181	186	191	196	201	206	211	216
62	67	72	77	82	87	92	97	102	107	112	117	122	127	132	137	142	147	152	157	162	167	172	177	182	187	192	197	202	207	212	217
63	68	73	78	83	88	93	98	103	108	113	118	123	128	133	138	143	148	153	158	163	168	173	178	183	188	193	198	203	208	213	218
64	69	74	79	84	89	94	99	104	109	114	119	124	129	134	139	144	149	154	159	164	169	174	179	184	189	194	199	204	209	214	219
65	70	75	80	85	90	95	100	105	110	115	120	125	130	135	140	145	150	155	160	165	170	175	180	185	190	195	200	205	210	215	220
66	71	76	81	86	91	96	101	106	111	116	121	126	131	136	141	146	151	156	161	166	171	176	181	186	191	196	201	206	211	216	221
67	72	77	82	87	92	97	102	107	112	117	122	127	132	137	142	147	152	157	162	167	172	177	182	187	192	197	202	207	212	217	222
68	73	78	83	88	93	98	103	108	113	118	123	128	133	138	143	148	153	158	163	168	173	178	183	188	193	198	203	208	213	218	223
69	74	79	84	89	94	99	104	109	114	119	124	129	134	139	144	149	154	159	164	169	174	179	184	189	194	199	204	209	214	219	224
70	75	80	85	90	95	100	105	110	115	120	125	130	135	140	145	150	155	160	165	170	175	180	185	190	195	200	205	210	215	220	225
71	76	81	86	91	96	101	106	111	116	121	126	131	136	141	146	151	156	161	166	171	176	181	186	191	196	201	206	211	216	221	226
72	77	82	87	92	97	102	107	112	117	122	127	132	137	142	147	152	157	162	167	172	177	182	187	192	197	202	207	212	217	222	227
73	78	83	88	93	98	103	108	113	118	123	128	133	138	143	148	153	158	163	168	173	178	183	188	193	198	203	208	213	218	223	228
74	79	84	89	94	99	104	109	114	119	124	129	134	139	144	149	154	159	164	169	174	179	184	189	194	199	204	209	214	219	224	229
75	80	85	90	95	100	105	110	115	120	125	130	135	140	145	150	155	160	165	170	175	180	185	190	195	200	205	210	215	220	225	230
76	81	86	91	96	101	106	111	116	121	126	131	136	141	146	151	156	161	166	171	176	181	186	191	196	201	206	211	216	221	226	231
77	82	87	92	97	102	107	112	117	122	127	132	137	142	147	152	157	162	167	172	177	182	187	192	197	202	207	212	217	222	227	232
78	83	88	93	98	103	108	113	118	123	128	133	138	143	148	153	158	163	168	173	178	183	188	193	198	203	208	213	218	223	228	233
79	84	89	94	99	104	109	114	119	124	129	134	139	144	149	154	159	164	169	174	179	184	189	194	199	204	209	214	219	224	229	234
80	85	90	95	100	105	110	115	120	125	130	135	140	145	150	155	160	165	170	175	180	185	190	195	200	205	210	215	220	225	230	235
81	86	91	96	101	106	111	116	121	126	131	136	141	146	151	156	161	166	171	176	181	186	191	196	201	206	211	216	221	226	231	236

FIXED BOUNDARY CONDITIONS

NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID																																																																																																																																																																																																																																																																																																																																																																																																																																																	
1	1	2	1	3	1	4	1	5	1	6	1	7	1	8	1	9	1	10	1	11	1	12	1	13	1	14	1	15	1	16	1	17	1	18	1	19	1	20	1	21	1	22	1	23	1	24	1	25	1	26	1	27	1	28	1	29	1	30	1	31	1	32	1	33	1	34	1	35	1	36	1	37	1	38	1	39	1	40	1	41	1	42	1	43	1	44	1	45	1	46	1	47	1	48	1	49	1	50	1	51	1	52	1	53	1	54	1	55	1	56	1	57	1	58	1	59	1	60	1	61	1	62	1	63	1	64	1	65	1	66	1	67	1	68	1	69	1	70	1	71	1	72	1	73	1	74	1	75	1	76	1	77	1	78	1	79	1	80	1	81	1	82	1	83	1	84	1	85	1	86	1	87	1	88	1	89	1	90	1	91	1	92	1	93	1	94	1	95	1	96	1	97	1	98	1	99	1	100	1	101	1	102	1	103	1	104	1	105	1	106	1	107	1	108	1	109	1	110	1	111	1	112	1	113	1	114	1	115	1	116	1	117	1	118	1	119	1	120	1	121	1	122	1	123	1	124	1	125	1	126	1	127	1	128	1	129	1	130	1	131	1	132	1	133	1	134	1	135	1	136	1	137	1	138	1	139	1	140	1	141	1	142	1	143	1	144	1	145	1	146	1	147	1	148	1	149	1	150	1	151	1	152	1	153	1	154	1	155	1	156	1	157	1	158	1	159	1	160	1	161	1	162	1	163	1	164	1	165	1	166	1	167	1	168	1	169	1	170	1	171	1	172	1	173	1	174	1	175	1	176	1	177	1	178	1	179	1	180	1	181	1	182	1	183	1	184	1	185	1	186	1	187	1	188	1	189	1	190	1	191	1	192	1	193	1	194	1	195	1	196	1	197	1	198	1	199	1	200	1	201	1	202	1	203	1	204	1	205	1	206	1	207	1	208	1	209	1	210	1	211	1	212	1	213	1	214	1	215	1	216	1	217	1	218	1	219	1	220	1	221	1	222	1	223	1	224	1	225	1	226	1	227	1	228	1	229	1	230	1	231	1	232	1	233	1	23

APPENDIX E**INPUT/OUTPUT OF THREE-DIMENSIONAL TESTING**

POINT SOURCE

INPUT DATA FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENT METHOD

TOTAL NO OF ELEMENTS : 90
TOTAL NO OF NODES : 168
MAXIMUM NO OF NODES PER ELEMENT : 8
TOTAL NO OF MATERIALS : 1
NUMBER OF PUMPING WELLS : 0
NUMBER OF CONCS TO BE ESTIMATED : 168

NUMBER OF PUMPING PERIODS : 0
TOTAL SIMULATION PERIODS : 50
FACTOR MULTIPLYING COMPUTED CONCS : 1 00000

STEP SIZE : 24 00000
STATE OF PROBLEM : 1
NO OF SPECIFIED CONDITIONS : 88

COORDINATES AND INITIAL CONCS OF MODES (L)

MODES	Y(I)	X(I)	Z(I)	CINT(I)
1	0.000 00	0.000 00	0.000 00	0.000 00
2	0.000 00	0.500 01	0.000 00	0.000 00
3	0.000 00	0.100 02	0.000 00	0.000 00
4	0.000 00	0.150 02	0.000 00	0.000 00
5	0.000 00	0.200 02	0.000 00	0.000 00
6	0.000 00	0.250 02	0.000 00	0.000 00
7	0.100 02	0.300 02	0.000 00	0.000 00
8	0.100 02	0.400 02	0.000 00	0.000 00
9	0.100 02	0.500 01	0.000 00	0.000 00
10	0.100 02	0.100 02	0.000 00	0.000 00
11	0.100 02	0.150 02	0.000 00	0.000 00
12	0.100 02	0.200 02	0.000 00	0.000 00
13	0.200 02	0.250 02	0.000 00	0.000 00
14	0.200 02	0.300 02	0.000 00	0.000 00
15	0.200 02	0.400 02	0.000 00	0.000 00
16	0.200 02	0.500 01	0.000 00	0.000 00
17	0.300 02	0.100 02	0.000 00	0.000 00
18	0.300 02	0.150 02	0.000 00	0.000 00
19	0.300 02	0.200 02	0.000 00	0.000 00
20	0.300 02	0.300 02	0.000 00	0.000 00
21	0.300 02	0.400 02	0.000 00	0.000 00
22	0.300 02	0.500 01	0.000 00	0.000 00
23	0.400 02	0.100 02	0.000 00	0.000 00
24	0.400 02	0.150 02	0.000 00	0.000 00
25	0.400 02	0.200 02	0.000 00	0.000 00
26	0.400 02	0.300 02	0.000 00	0.000 00
27	0.400 02	0.400 02	0.000 00	0.000 00
28	0.400 02	0.500 01	0.000 00	0.000 00
29	0.500 01	0.100 02	0.000 00	0.000 00
30	0.500 01	0.150 02	0.000 00	0.000 00
31	0.500 01	0.200 02	0.000 00	0.000 00
32	0.500 01	0.300 02	0.000 00	0.000 00
33	0.500 01	0.400 02	0.000 00	0.000 00
34	0.500 01	0.500 01	0.000 00	0.000 00
35	0.500 01	0.100 02	0.000 00	0.000 00
36	0.500 01	0.150 02	0.000 00	0.000 00
37	0.500 01	0.200 02	0.000 00	0.000 00
38	0.500 01	0.300 02	0.000 00	0.000 00
39	0.500 01	0.400 02	0.000 00	0.000 00
40	0.500 01	0.500 01	0.000 00	0.000 00
41	0.500 01	0.100 02	0.000 00	0.000 00
42	0.500 01	0.150 02	0.000 00	0.000 00
43	0.500 01	0.200 02	0.000 00	0.000 00
44	0.500 01	0.300 02	0.000 00	0.000 00
45	0.500 01	0.400 02	0.000 00	0.000 00
46	0.500 01	0.500 01	0.000 00	0.000 00
47	0.000 00	0.100 02	0.100 01	0.000 00
48	0.000 00	0.100 02	0.100 01	0.000 00
49	0.100 02	0.100 02	0.100 01	0.000 00
50	0.100 02	0.150 02	0.100 01	0.000 00
51	0.100 02	0.200 02	0.100 01	0.000 00
52	0.100 02	0.250 02	0.100 01	0.000 00
53	0.100 02	0.300 02	0.100 01	0.000 00
54	0.100 02	0.400 02	0.100 01	0.000 00
55	0.200 02	0.500 01	0.100 01	0.000 00
56	0.200 02	0.100 02	0.100 01	0.000 00
57	0.200 02	0.150 02	0.100 01	0.000 00
58	0.200 02	0.200 02	0.100 01	0.000 00
59	0.200 02	0.250 02	0.100 01	0.000 00
60	0.200 02	0.300 02	0.100 01	0.000 00
61	0.200 02	0.400 02	0.100 01	0.000 00
62	0.200 02	0.500 01	0.100 01	0.000 00
63	0.300 02	0.100 02	0.100 01	0.000 00
64	0.300 02	0.150 02	0.100 01	0.000 00
65	0.300 02	0.200 02	0.100 01	0.000 00
66	0.300 02	0.250 02	0.100 01	0.000 00
67	0.300 02	0.300 02	0.100 01	0.000 00
68	0.300 02	0.400 02	0.100 01	0.000 00
69	0.300 02	0.500 01	0.100 01	0.000 00
70	0.400 02	0.100 02	0.100 01	0.000 00
71	0.400 02	0.150 02	0.100 01	0.000 00
72	0.400 02	0.200 02	0.100 01	0.000 00
73	0.400 02	0.250 02	0.100 01	0.000 00
74	0.500 02	0.300 02	0.100 01	0.000 00
75	0.500 02	0.400 02	0.100 01	0.000 00
76	0.500 02	0.500 01	0.100 01	0.000 00
77	0.500 02	0.100 02	0.100 01	0.000 00
78	0.500 02	0.150 02	0.100 01	0.000 00
79	0.500 02	0.200 02	0.100 01	0.000 00
80	0.500 02	0.250 02	0.100 01	0.000 00
81	0.600 02	0.300 02	0.100 01	0.000 00
82	0.600 02	0.400 02	0.100 01	0.000 00
83	0.600 02	0.500 01	0.100 01	0.000 00
84	0.600 02	0.100 02	0.100 01	0.000 00
85	0.600 02	0.150 02	0.100 01	0.000 00
86	0.600 02	0.200 02	0.100 01	0.000 00
87	0.600 02	0.250 02	0.100 01	0.000 00
88	0.600 02	0.300 02	0.100 01	0.000 00
89	0.600 02	0.400 02	0.100 01	0.000 00
90	0.600 02	0.500 01	0.100 01	0.000 00
91	0.100 02	0.100 02	0.200 01	0.000 00
92	0.100 02	0.150 02	0.200 01	0.000 00
93	0.100 02	0.200 02	0.200 01	0.000 00
94	0.100 02	0.250 02	0.200 01	0.000 00
95	0.100 02	0.300 02	0.200 01	0.000 00
96	0.100 02	0.400 02	0.200 01	0.000 00
97	0.100 02	0.500 01	0.200 01	0.000 00
98	0.200 02	0.100 02	0.200 01	0.000 00
99	0.200 02	0.150 02	0.200 01	0.000 00
100	0.200 02	0.200 02	0.200 01	0.000 00
101	0.200 02	0.250 02	0.200 01	0.000 00
102	0.200 02	0.300 02	0.200 01	0.000 00
103	0.200 02	0.400 02	0.200 01	0.000 00
104	0.200 02	0.500 01	0.200 01	0.000 00
105	0.300 02	0.100 02	0.200 01	0.000 00
106	0.300 02	0.150 02	0.200 01	0.000 00
107	0.300 02	0.200 02	0.200 01	0.000 00

	168	0 600 02	0 250 02	0 400 01	0 000 00
108	0 300 02	0 250 02	0 200 01	0 000 00	0 000 00
109	0 400 02	0 000 00	0 200 01	0 000 00	0 000 00
110	0 400 02	0 500 01	0 200 01	0 000 00	0 000 00
111	0 400 02	0 100 02	0 200 01	0 000 00	0 000 00
112	0 400 02	0 150 02	0 200 01	0 000 00	0 000 00
113	0 400 02	0 200 02	0 200 01	0 000 00	0 000 00
114	0 400 02	0 250 02	0 200 01	0 000 00	0 000 00
115	0 500 02	0 000 00	0 200 01	0 000 00	0 000 00
116	0 500 02	0 500 01	0 200 01	0 000 00	0 000 00
117	0 500 02	0 100 02	0 200 01	0 000 00	0 000 00
118	0 500 02	0 150 02	0 200 01	0 000 00	0 000 00
119	0 500 02	0 200 02	0 200 01	0 000 00	0 000 00
120	0 500 02	0 250 02	0 200 01	0 000 00	0 000 00
121	0 600 02	0 000 00	0 200 01	0 000 00	0 000 00
122	0 600 02	0 500 01	0 200 01	0 000 00	0 000 00
123	0 600 02	0 100 02	0 200 01	0 000 00	0 000 00
124	0 600 02	0 150 02	0 200 01	0 000 00	0 000 00
125	0 600 02	0 200 02	0 200 01	0 000 00	0 000 00
126	0 600 02	0 250 02	0 200 01	0 000 00	0 000 00
127	0 000 00	0 000 00	0 400 01	0 000 00	0 000 00
128	0 000 00	0 500 01	0 400 01	0 000 00	0 000 00
129	0 000 00	0 100 02	0 400 01	0 000 00	0 000 00
130	0 000 00	0 150 02	0 400 01	0 000 00	0 000 00
131	0 000 00	0 200 02	0 400 01	0 000 00	0 000 00
132	0 000 00	0 250 02	0 400 01	0 000 00	0 000 00
133	0 100 02	0 000 00	0 400 01	0 000 00	0 000 00
134	0 100 02	0 500 01	0 400 01	0 000 00	0 000 00
135	0 100 02	0 100 02	0 400 01	0 000 00	0 000 00
136	0 100 02	0 150 02	0 400 01	0 000 00	0 000 00
137	0 100 02	0 200 02	0 400 01	0 000 00	0 000 00
138	0 100 02	0 250 02	0 400 01	0 000 00	0 000 00
139	0 200 02	0 000 00	0 400 01	0 000 00	0 000 00
140	0 200 02	0 500 01	0 400 01	0 000 00	0 000 00
141	0 200 02	0 100 02	0 400 01	0 000 00	0 000 00
142	0 200 02	0 150 02	0 400 01	0 000 00	0 000 00
143	0 200 02	0 200 02	0 400 01	0 000 00	0 000 00
144	0 200 02	0 250 02	0 400 01	0 000 00	0 000 00
145	0 300 02	0 000 00	0 400 01	0 000 00	0 000 00
146	0 300 02	0 500 01	0 400 01	0 000 00	0 000 00
147	0 300 02	0 100 02	0 400 01	0 000 00	0 000 00
148	0 300 02	0 150 02	0 400 01	0 000 00	0 000 00
149	0 300 02	0 200 02	0 400 01	0 000 00	0 000 00
150	0 300 02	0 250 02	0 400 01	0 000 00	0 000 00
151	0 400 02	0 000 00	0 400 01	0 000 00	0 000 00
152	0 400 02	0 500 01	0 400 01	0 000 00	0 000 00
153	0 400 02	0 100 02	0 400 01	0 000 00	0 000 00
154	0 400 02	0 150 02	0 400 01	0 000 00	0 000 00
155	0 400 02	0 200 02	0 400 01	0 000 00	0 000 00
156	0 400 02	0 250 02	0 400 01	0 000 00	0 000 00
157	0 500 02	0 000 00	0 400 01	0 000 00	0 000 00
158	0 500 02	0 500 01	0 400 01	0 000 00	0 000 00
159	0 500 02	0 100 02	0 400 01	0 000 00	0 000 00
160	0 500 02	0 150 02	0 400 01	0 000 00	0 000 00
161	0 500 02	0 200 02	0 400 01	0 000 00	0 000 00
162	0 500 02	0 250 02	0 400 01	0 000 00	0 000 00
163	0 600 02	0 000 00	0 400 01	0 000 00	0 000 00
164	0 600 02	0 500 01	0 400 01	0 000 00	0 000 00
165	0 600 02	0 100 02	0 400 01	0 000 00	0 000 00
166	0 600 02	0 150 02	0 400 01	0 000 00	0 000 00
167	0 600 02	0 200 02	0 400 01	0 000 00	0 000 00

MODE-ELEMENT RELATIONSHIP

ELEMS	N1	N2	N3	N4	N5	N6	N7	N8
1	1	3	8	7	43	44	50	49
2	2	4	9	18	44	45	51	50
3	3	5	10	19	45	46	52	51
4	4	6	11	20	46	47	53	52
5	5	7	12	21	47	48	54	53
6	6	8	13	22	48	49	55	54
7	7	9	14	23	49	50	56	55
8	8	10	15	24	50	51	57	56
9	9	11	16	25	51	52	58	57
10	10	12	17	26	52	53	59	58
11	11	13	18	27	53	54	60	59
12	12	14	19	28	54	55	61	60
13	13	15	20	29	55	56	62	61
14	14	16	21	30	56	57	63	62
15	15	17	22	31	57	58	64	63
16	16	18	23	32	58	59	65	64
17	17	19	24	33	59	60	66	65
18	18	20	25	34	60	61	67	66
19	19	21	26	35	61	62	68	67
20	20	22	27	36	62	63	69	68
21	21	23	28	37	63	64	70	69
22	22	24	29	38	64	65	71	70
23	23	25	30	39	65	66	72	71
24	24	26	31	40	66	67	73	72
25	25	27	32	41	67	68	74	73
26	26	28	33	42	68	69	75	74
27	27	29	34	43	69	70	76	75
28	28	30	35	44	70	71	77	76
29	29	31	36	45	71	72	78	77
30	30	32	37	46	72	73	79	78
31	31	33	38	47	73	74	80	79
32	32	34	39	48	74	75	81	80
33	33	35	40	49	75	76	82	81
34	34	36	41	50	76	77	83	82
35	35	37	42	51	77	78	84	83
36	36	38	43	52	78	79	85	84
37	37	39	44	53	79	80	86	85
38	38	40	45	54	80	81	87	86
39	39	41	46	55	81	82	88	87
40	40	42	47	56	82	83	89	88
41	41	43	48	57	83	84	90	89
42	42	44	49	58	84	85	91	90
43	43	45	50	59	85	86	92	91
44	44	46	51	60	86	87	93	92
45	45	47	52	61	87	88	94	93
46	46	48	53	62	88	89	95	94
47	47	49	54	63	89	90	96	95
48	48	50	55	64	90	91	97	96
49	49	51	56	65	91	92	98	97
50	50	52	57	66	92	93	99	98
51	51	53	58	67	93	94	100	99
52	52	54	59	68	94	95	101	100
53	53	55	60	69	95	96	102	101
54	54	56	61	70	96	97	103	102
55	55	57	62	71	97	98	104	103
56	56	58	63	72	98	99	105	104
57	57	59	64	73	99	100	106	105
58	58	60	65	74	100	101	107	106
59	59	61	66	75	101	102	108	107
60	60	62	67	76	102	103	109	108
61	61	63	68	77	103	104	110	109

FIXED BOUNDARY CONDITIONS

NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID
1	0	3	0	4	0	5	0	6	0	7	0	8	0	9	0
6	0	12	0	13	0	18	0	19	0	24	0	25	0	30	0
19	0	25	0	30	0	31	0	36	0	37	0	38	0	39	0
36	0	38	0	39	0	40	0	41	0	42	0	43	0	44	0
41	0	43	0	44	0	45	0	46	0	47	0	48	0	49	0
46	0	48	0	49	0	54	0	55	0	60	0	61	0	66	0
55	0	60	0	66	0	67	0	72	0	73	0	78	0	80	0
72	0	73	0	78	0	80	0	81	0	82	0	83	0	85	0
81	0	82	0	83	0	85	0	86	0	87	0	88	0	89	0
86	0	87	0	88	0	89	0	91	0	96	0	97	0	102	0
91	0	96	0	97	0	102	0	99	0	108	0	111	0	115	0
108	0	99	0	108	0	111	0	115	0	121	0	122	0	124	0
121	0	122	0	124	0	125	0	126	0	127	0	128	0	129	0
126	0	127	0	128	0	129	0	131	0	132	0	133	0	138	0
131	0	132	0	133	0	138	0	134	0	145	0	153	0	151	0
134	0	145	0	151	0	153	0	157	0	162	0	163	0	164	0
157	0	162	0	163	0	164	0	166	0	167	0	168	0	165	0
166	0	167	0	168	0	165	0								

MAXIMUM BANDWIDTH = 53 ON ROW NO. 23

CONCENTRATION DISTRIBUTION AT TIME = 120 000 HOURS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.443D 00	3	0.626D 03	2	0.920D 05	4	0.626D 03	5	0.661D 00	6	0.480D 03	7	0.378D 03
6	0.194D 00	7	0.335D 00	8	0.378D 03	9	0.480D 03	10	0.378D 03	11	0.335D 00	12	0.194D 00
11	0.349D 00	12	0.990D 01	13	0.990D 01	14	0.248D 02	15	0.956D 02	16	0.507D 03	17	0.856D 02
16	0.856D 02	17	0.374D 01	18	0.374D 01	19	0.800D 02	20	0.617D 05	21	0.214D 01	22	0.208D 03
21	0.124D 03	22	0.841D 01	23	0.841D 01	24	0.927D 02	25	0.208D 03	26	0.454D 05	27	0.202D 01
26	0.202D 01	27	0.841D 00	28	0.167D 02	29	0.202D 01	30	0.692D 05	31	0.113D 05	32	0.167D 02
31	0.103D 07	32	0.512D 04	33	0.167D 02	34	0.167D 02	35	0.973D 04	36	0.159D 07	37	0.167D 02
36	0.173D 08	37	0.728D 11	38	0.346D 07	39	0.346D 07	40	0.973D 04	41	0.159D 07	42	0.167D 02
41	0.110D 10	42	0.792D 12	43	0.467D 00	44	0.467D 00	45	0.973D 04	46	0.346D 07	47	0.167D 02
46	0.580D 03	47	0.524D 00	48	0.264D 00	49	0.264D 00	50	0.980D 03	51	0.129D 06	52	0.343D 03
51	0.642D 05	52	0.343D 03	53	0.327D 00	54	0.327D 00	55	0.243D 00	56	0.343D 03	57	0.642D 05
56	0.503D 03	57	0.994D 04	58	0.503D 03	59	0.303D 02	60	0.131D 00	61	0.245D 01	62	0.503D 03
61	0.581D 03	62	0.186D 01	63	0.150D 03	64	0.150D 03	65	0.348D 01	66	0.116D 01	67	0.581D 03
66	0.213D 03	67	0.413D 05	68	0.182D 01	69	0.182D 01	70	0.781D 00	71	0.649D 03	72	0.213D 03
71	0.622D 05	72	0.106D 08	73	0.932D 08	74	0.932D 08	75	0.459D 04	76	0.182D 01	77	0.622D 05
76	0.459D 04	77	0.143D 07	78	0.155D 08	79	0.155D 08	80	0.664D 11	81	0.314D 08	82	0.459D 04
81	0.876D 06	82	0.314D 08	83	0.100D 10	84	0.100D 10	85	0.703D 12	86	0.314D 08	87	0.876D 06
86	0.428D 03	87	0.944D 05	88	0.428D 03	89	0.285D 05	90	0.365D 00	89	0.285D 05	90	0.428D 03
90	0.131D 00	91	0.248D 02	92	0.248D 02	93	0.285D 05	94	0.248D 02	91	0.131D 00	92	0.131D 00
92	0.538D 01	93	0.142D 01	94	0.367D 02	95	0.367D 02	96	0.306D 04	93	0.142D 01	94	0.538D 01
96	0.213D 01	97	0.844D 02	98	0.379D 03	99	0.379D 03	100	0.306D 04	95	0.192D 00	96	0.213D 01
101	0.537D 01	102	0.970D 03	103	0.379D 03	104	0.379D 03	105	0.248D 02	97	0.192D 00	98	0.537D 01
104	0.537D 01	105	0.122D 03	106	0.122D 03	107	0.291D 05	108	0.291D 05	99	0.105D 00	100	0.537D 01
111	0.537D 00	112	0.124D 01	113	0.444D 05	114	0.444D 05	115	0.137D 01	101	0.105D 00	102	0.537D 00
116	0.498D 11	117	0.110D 02	118	0.343D 04	119	0.343D 04	120	0.685D 06	103	0.134D 01	104	0.498D 11
121	0.498D 11	122	0.233D 07	123	0.645D 06	124	0.645D 06	125	0.107D 07	105	0.134D 01	106	0.498D 11
126	0.517D 12	127	0.376D 01	128	0.108D 03	129	0.108D 03	130	0.107D 07	107	0.683D 08	108	0.517D 12
131	0.395D 01	132	0.906D 02	133	0.376D 01	134	0.654D 04	135	0.233D 07	109	0.108D 03	110	0.395D 01
136	0.654D 02	137	0.231D 01	138	0.506D 02	139	0.506D 02	140	0.654D 04	111	0.108D 03	112	0.654D 02
141	0.445D 03	142	0.960D 01	143	0.323D 02	144	0.323D 02	145	0.654D 04	113	0.233D 07	114	0.445D 03
146	0.374D 00	147	0.960D 01	148	0.374D 00	149	0.374D 00	150	0.654D 04	115	0.323D 02	116	0.374D 00
151	0.744D 06	152	0.146D 02	153	0.146D 02	154	0.146D 02	155	0.117D 03	117	0.323D 02	118	0.744D 06
156	0.132D 06	157	0.378D 02	158	0.378D 02	159	0.126D 00	160	0.117D 03	119	0.323D 02	120	0.132D 06
161	0.310D 08	162	0.201D 08	163	0.201D 08	164	0.890D 06	165	0.115D 04	121	0.323D 02	122	0.310D 08
166	0.685D 08	167	0.251D 09	168	0.251D 09	169	0.153D 11	170	0.890D 06	123	0.323D 02	124	0.685D 08
			0.225D 11	168	0.134D 12					125	0.688D 08	126	

CONCENTRATION DISTRIBUTION AT TIME = 960.000 HOURS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.3740-00	2	0.8020-02	3	0.1080-05	4	0.5020-03	5	0.5130-00	6	0.5130-00	7	0.5130-00	8	0.5130-00
6	0.1620-00	7	0.2520-00	8	0.3940-03	9	0.5180-05	10	0.3940-03	11	0.3940-03	12	0.3940-03	13	0.3940-03
11	0.3760-00	12	0.1080-00	13	0.5100-01	14	0.9900-02	15	0.9900-02	16	0.9900-02	17	0.9900-02	18	0.9900-02
16	0.9900-02	17	0.8040-01	18	0.2220-01	19	0.3750-02	20	0.3750-02	21	0.3750-02	22	0.3750-02	23	0.3750-02
21	0.7770-03	22	0.9350-01	23	0.8510-02	24	0.1480-02	25	0.1480-02	26	0.1480-02	27	0.1480-02	28	0.1480-02
26	0.3030-00	27	0.1820-02	28	0.3030-00	29	0.1740-00	30	0.1420-03	31	0.1420-03	32	0.1420-03	33	0.1420-03
31	0.8870-06	32	0.3630-02	33	0.1740-00	34	0.3630-02	35	0.1340-05	36	0.1340-05	37	0.1340-05	38	0.1340-05
36	0.2480-05	37	0.3370-08	38	0.1590-04	39	0.6050-03	40	0.6050-03	41	0.6050-03	42	0.6050-03	43	0.6050-03
41	0.5170-08	42	0.2200-08	43	0.3940-00	44	0.5020-03	45	0.1080-06	46	0.1080-06	47	0.1080-06	48	0.1080-06
46	0.5020-03	47	0.1120-00	48	0.2220-00	49	0.2630-00	50	0.3560-03	51	0.3560-03	52	0.3560-03	53	0.3560-03
51	0.7020-05	52	0.3530-00	53	0.3530-00	54	0.1440-00	55	0.1440-00	56	0.1440-00	57	0.1440-00	58	0.1440-00
56	0.9040-02	57	0.1780-05	58	0.8040-02	59	0.7180-01	60	0.7180-01	61	0.7180-01	62	0.7180-01	63	0.7180-01
61	0.3650-02	62	0.8880-01	63	0.8870-03	64	0.8180-01	65	0.8180-01	66	0.8180-01	67	0.8180-01	68	0.8180-01
66	0.1650-02	67	0.8880-01	68	0.2780-00	69	0.1980-02	70	0.2750-00	71	0.2750-00	72	0.2750-00	73	0.2750-00
71	0.1290-03	72	0.2360-04	73	0.8110-06	74	0.3250-02	75	0.1640-00	76	0.1640-00	77	0.1640-00	78	0.1640-00
76	0.3250-02	77	0.1210-05	78	0.3280-06	79	0.3060-08	80	0.1440-04	81	0.1440-04	82	0.1440-04	83	0.1440-04
81	0.5500-03	82	0.1440-04	83	0.4700-08	84	0.6370-09	85	0.2090-00	86	0.2090-00	87	0.2090-00	88	0.2090-00
86	0.3610-03	87	0.4900-05	88	0.3610-03	89	0.3080-00	90	0.8860-01	91	0.8860-01	92	0.8860-01	93	0.8860-01
91	0.1400-00	92	0.2580-02	93	0.3060-05	94	0.2580-02	95	0.2070-00	96	0.2070-00	97	0.2070-00	98	0.2070-00
96	0.5820-01	97	0.3030-01	98	0.6560-02	99	0.6560-02	100	0.6560-02	101	0.6560-02	102	0.6560-02	103	0.6560-02
101	0.4500-01	102	0.1220-01	103	0.2180-02	104	0.5960-01	105	0.4610-03	106	0.4610-03	107	0.4610-03	108	0.4610-03
106	0.5960-01	107	0.3260-02	108	0.8140-03	109	0.5680-04	110	0.2000-00	111	0.2000-00	112	0.2000-00	113	0.2000-00
111	0.1100-02	112	0.2000-00	113	0.8520-04	114	0.1840-04	115	0.5630-06	116	0.5630-06	117	0.5630-06	118	0.5630-06
116	0.2410-02	117	0.1080-00	118	0.2410-02	119	0.8520-06	120	0.1480-06	121	0.1480-06	122	0.1480-06	123	0.1480-06
121	0.2220-08	122	0.1060-04	123	0.3860-03	124	0.1060-04	125	0.3410-08	126	0.3410-08	127	0.3410-08	128	0.3410-08
126	0.4440-08	127	0.2370-01	128	0.9500-02	129	0.5030-04	130	0.9500-02	131	0.9500-02	132	0.9500-02	133	0.9500-02
131	0.3450-01	132	0.7740-02	133	0.1670-01	134	0.6780-02	135	0.3490-04	136	0.3490-04	137	0.3490-04	138	0.3490-04
136	0.1670-01	137	0.2420-01	138	0.9340-02	139	0.4080-02	140	0.1740-02	141	0.1740-02	142	0.1740-02	143	0.1740-02
141	0.8420-03	142	0.4080-02	143	0.9340-02	144	0.5250-02	145	0.3550-03	146	0.3550-03	147	0.3550-03	148	0.3550-03
146	0.1560-01	147	0.4080-02	148	0.9340-02	149	0.5250-02	150	0.8800-04	151	0.8800-04	152	0.8800-04	153	0.8800-04
151	0.1130-04	152	0.7030-02	153	0.5490-01	154	0.5480-01	155	0.6700-04	156	0.6700-04	157	0.6700-04	158	0.6700-04
156	0.2680-05	157	0.1340-06	158	0.2130-01	159	0.5480-01	160	0.1700-04	161	0.1700-04	162	0.1700-04	163	0.1700-04
161	0.2050-06	162	0.2600-07	163	0.6030-09	164	0.2350-01	165	0.6750-03	166	0.6750-03	167	0.6750-03	168	0.6750-03
166	0.3030-05	167	0.9310-09	168	0.9170-10	169	0.3030-05	170	0.3030-05	171	0.3030-05	172	0.3030-05	173	0.3030-05

CONCENTRATION DISTRIBUTION AT TIME = 1200.000 HOURS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.3200-00	2	0.4840-03	3	0.6870-05	4	0.4840-03	5	0.4940-00				
6	0.1440-00	7	0.2540-00	8	0.3820-03	9	0.9230-05	10	0.3920-03				
11	0.3780-00	12	0.1080-00	13	0.7880-01	14	0.1380-03	15	0.1650-05				
16	0.1280-03	17	0.1200-00	18	0.3400-01	19	0.1030-01	20	0.2160-02				
21	0.2150-04	22	0.2160-02	23	0.1640-01	24	0.4160-02	25	0.5780-03				
26	0.1470-01	27	0.1220-03	28	0.1470-01	29	0.8680-03	30	0.2190-03				
31	0.1410-04	32	0.4510-01	33	0.2980-01	34	0.4510-01	35	0.2110-04				
36	0.4830-05	37	0.1880-06	38	0.6100-03	39	0.3180-01	40	0.6100-03				
41	0.2380-05	42	0.4680-07	43	0.3470-00	44	0.4480-03	45	0.9500-05				
46	0.4480-03	47	0.4640-00	48	0.1840-00	49	0.2660-00	50	0.3530-03				
51	0.7070-05	52	0.4830-03	53	0.3560-00	54	0.1460-00	55	0.8150-01				
56	0.1250-03	57	0.3120-05	58	0.1250-03	59	0.1120-00	60	0.4340-01				
61	0.1030-01	62	0.1950-02	63	0.2810-04	64	0.1950-02	65	0.1440-01				
66	0.5100-02	67	0.8000-03	68	0.1330-01	69	0.1360-03	70	0.1330-01				
71	0.8040-03	72	0.3190-03	73	0.1410-04	74	0.4050-01	75	0.3040-01				
76	0.4050-01	77	0.1940-04	78	0.4840-05	79	0.1580-06	80	0.5510-03				
81	0.3070-01	82	0.5510-03	83	0.2170-06	84	0.4680-07	85	0.1850-00				
86	0.2310-03	87	0.4090-08	88	0.3210-03	89	0.2730-00	90	0.7830-01				
91	0.1420-00	92	0.2570-03	93	0.3090-05	94	0.2570-03	95	0.2080-00				
96	0.5840-01	97	0.4450-01	98	0.8860-02	99	0.8700-00	100	0.8960-02				
101	0.6600-01	102	0.1810-01	103	0.5870-02	104	0.2100-00	105	0.1250-04				
106	0.2100-00	107	0.8750-02	108	0.2310-02	109	0.3380-03	110	0.8630-00				
111	0.7160-02	112	0.9630-00	113	0.5050-03	114	0.1230-03	115	0.8570-05				
116	0.1280-04	117	0.1770-01	118	0.1280-04	119	0.1280-04	120	0.2790-05				
121	0.2760-07	122	0.4030-03	123	0.1950-01	124	0.4030-03	125	0.1500-06				
126	0.3000-01	127	0.2100-01	128	0.8500-02	129	0.4470-04	130	0.8500-02				
131	0.3480-02	132	0.6890-02	133	0.1660-01	134	0.3480-02	135	0.6710-03				
136	0.1180-04	137	0.2400-01	138	0.5330-02	139	0.5640-02	140	0.2360-03				
141	0.3650-01	142	0.3360-02	143	0.8200-01	144	0.1760-02	145	0.8490-03				
146	0.5670-04	147	0.1710-03	148	0.3650-01	149	0.1240-02	150	0.2510-03				
151	0.1520-04	152	0.2610-00	153	0.1110-02	154	0.2610-00	155	0.8280-02				
156	0.2530-05	157	0.1680-05	158	0.8130-02	159	0.3180-00	160	0.8130-02				
161	0.1120-03	162	0.4020-06	163	0.2260-07	164	0.1120-03	165	0.4040-02				
166		167	0.3440-07	168	0.4620-08								

LINE SOURCES

INPUT DATA FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENT METHOD

TOTAL NO OF ELEMENTS . 80
 TOTAL NO OF NODES . 168
 MAXIMUM NO OF NODES PER ELEMENT . 8
 TOTAL NO OF MATERIALS . 1
 NUMBER OF PUMPING WELLS . 0
 NUMBER OF CONCS TO BE ESTIMATED . 168

NUMBER OF PUMPING PERIODS . 0
 TOTAL SIMULATION PERIODS . 50
 FACTOR MULTIPLYING COMPUTED CONCS . 1.00000

STEP SIZE . 24.00000
 STATE OF PROBLEM . 1
 NO OF SPECIFIED CONDITIONS . 88

NODES	Y(I)	X(I)	Z(I)	CINT(I)
1	0.000 00	0.000 00	0.000 00	0.100 13
2	0.000 00	0.500 01	0.000 00	0.100 02
3	0.000 00	0.100 02	0.000 00	0.000 00
4	0.000 00	0.150 02	0.000 00	0.000 00
5	0.000 00	0.200 02	0.000 00	0.000 00
6	0.000 00	0.250 02	0.000 00	0.000 00
7	0.100 02	0.000 00	0.000 00	0.000 00
8	0.100 02	0.500 01	0.000 00	0.000 00
9	0.100 02	0.100 02	0.000 00	0.000 00
10	0.100 02	0.150 02	0.000 00	0.000 00
11	0.100 02	0.200 02	0.000 00	0.000 00
12	0.100 02	0.250 02	0.000 00	0.000 00
13	0.200 02	0.000 00	0.000 00	0.000 00
14	0.200 02	0.500 01	0.000 00	0.000 00
15	0.200 02	0.100 02	0.000 00	0.000 00
16	0.200 02	0.150 02	0.000 00	0.000 00
17	0.200 02	0.200 02	0.000 00	0.000 00
18	0.200 02	0.250 02	0.000 00	0.000 00
19	0.300 02	0.000 00	0.000 00	0.000 00
20	0.300 02	0.500 01	0.000 00	0.000 00
21	0.300 02	0.100 02	0.000 00	0.000 00
22	0.300 02	0.150 02	0.000 00	0.000 00
23	0.300 02	0.200 02	0.000 00	0.000 00
24	0.300 02	0.250 02	0.000 00	0.000 00
25	0.400 02	0.000 00	0.000 00	0.000 00
26	0.400 02	0.500 01	0.000 00	0.000 00
27	0.400 02	0.100 02	0.000 00	0.000 00
28	0.400 02	0.150 02	0.000 00	0.000 00
29	0.400 02	0.200 02	0.000 00	0.000 00
30	0.400 02	0.250 02	0.000 00	0.000 00
31	0.500 02	0.000 00	0.000 00	0.000 00
32	0.500 02	0.500 01	0.000 00	0.000 00
33	0.500 02	0.100 02	0.000 00	0.000 00
34	0.500 02	0.150 02	0.000 00	0.000 00
35	0.500 02	0.200 02	0.000 00	0.000 00
36	0.500 02	0.250 02	0.000 00	0.000 00
37	0.600 02	0.000 00	0.000 00	0.000 00
38	0.600 02	0.500 01	0.000 00	0.000 00
39	0.600 02	0.100 02	0.000 00	0.000 00
40	0.600 02	0.150 02	0.000 00	0.000 00
41	0.600 02	0.200 02	0.000 00	0.000 00
42	0.600 02	0.250 02	0.000 00	0.000 00
43	0.000 00	0.000 00	0.100 01	0.000 00
44	0.000 00	0.500 01	0.100 01	0.000 00
45	0.000 00	0.100 02	0.100 01	0.000 00
46	0.000 00	0.150 02	0.100 01	0.000 00
47	0.000 00	0.200 02	0.100 01	0.000 00
48	0.000 00	0.000 00	0.250 02	0.000 00
49	0.100 02	0.000 00	0.000 00	0.000 00
50	0.100 02	0.500 01	0.000 00	0.000 00
51	0.100 02	0.100 02	0.000 00	0.000 00
52	0.100 02	0.150 02	0.000 00	0.000 00
53	0.100 02	0.200 02	0.000 00	0.000 00
54	0.100 02	0.250 02	0.000 00	0.000 00
55	0.200 02	0.000 00	0.000 00	0.000 00
56	0.200 02	0.500 01	0.000 00	0.000 00
57	0.200 02	0.100 02	0.000 00	0.000 00
58	0.200 02	0.150 02	0.000 00	0.000 00
59	0.200 02	0.200 02	0.000 00	0.000 00
60	0.200 02	0.250 02	0.000 00	0.000 00
61	0.200 02	0.000 00	0.000 00	0.000 00
62	0.200 02	0.500 01	0.000 00	0.000 00
63	0.200 02	0.100 02	0.000 00	0.000 00
64	0.200 02	0.150 02	0.000 00	0.000 00
65	0.200 02	0.200 02	0.000 00	0.000 00
66	0.200 02	0.250 02	0.000 00	0.000 00
67	0.400 02	0.000 00	0.000 00	0.000 00
68	0.400 02	0.500 01	0.000 00	0.000 00
69	0.400 02	0.100 02	0.000 00	0.000 00
70	0.400 02	0.150 02	0.000 00	0.000 00
71	0.400 02	0.200 02	0.000 00	0.000 00
72	0.400 02	0.250 02	0.000 00	0.000 00
73	0.500 02	0.000 00	0.000 00	0.000 00
74	0.500 02	0.500 01	0.000 00	0.000 00
75	0.500 02	0.100 02	0.000 00	0.000 00
76	0.500 02	0.150 02	0.000 00	0.000 00
77	0.500 02	0.200 02	0.000 00	0.000 00
78	0.500 02	0.250 02	0.000 00	0.000 00
79	0.500 02	0.000 00	0.000 00	0.000 00
80	0.500 02	0.500 01	0.000 00	0.000 00
81	0.500 02	0.100 02	0.000 00	0.000 00
82	0.500 02	0.150 02	0.000 00	0.000 00
83	0.500 02	0.200 02	0.000 00	0.000 00
84	0.500 02	0.250 02	0.000 00	0.000 00
85	0.000 00	0.000 00	0.000 00	0.000 00
86	0.000 00	0.500 01	0.000 00	0.000 00
87	0.000 00	0.100 02	0.000 00	0.000 00
88	0.000 00	0.150 02	0.000 00	0.000 00
89	0.000 00	0.200 02	0.000 00	0.000 00
90	0.000 00	0.250 02	0.000 00	0.000 00
91	0.100 02	0.000 00	0.000 00	0.000 00
92	0.100 02	0.500 01	0.000 00	0.000 00
93	0.100 02	0.100 02	0.000 00	0.000 00
94	0.100 02	0.150 02	0.000 00	0.000 00
95	0.100 02	0.200 02	0.000 00	0.000 00
96	0.100 02	0.250 02	0.000 00	0.000 00
97	0.200 02	0.000 00	0.000 00	0.000 00
98	0.200 02	0.500 01	0.000 00	0.000 00
99	0.200 02	0.100 02	0.000 00	0.000 00
100	0.200 02	0.150 02	0.000 00	0.000 00
101	0.200 02	0.200 02	0.000 00	0.000 00
102	0.200 02	0.250 02	0.000 00	0.000 00
103	0.300 02	0.000 00	0.000 00	0.000 00
104	0.300 02	0.500 01	0.000 00	0.000 00
105	0.300 02	0.100 02	0.000 00	0.000 00
106	0.300 02	0.150 02	0.000 00	0.000 00
107	0.300 02	0.200 02	0.000 00	0.000 00

108	0.300 02	0.250 02	0.200 01	0.000 00
109	0.400 02	0.000 00	0.200 01	0.000 00
110	0.400 02	0.500 01	0.200 01	0.000 00
111	0.400 02	0.100 02	0.200 01	0.000 00
112	0.400 02	0.150 02	0.200 01	0.000 00
113	0.400 02	0.200 02	0.200 01	0.000 00
114	0.400 02	0.250 02	0.200 01	0.000 00
115	0.500 02	0.000 00	0.200 01	0.000 00
116	0.500 02	0.500 01	0.200 01	0.000 00
117	0.500 02	0.100 02	0.200 01	0.000 00
118	0.500 02	0.150 02	0.200 01	0.000 00
119	0.500 02	0.200 02	0.200 01	0.000 00
120	0.500 02	0.250 02	0.200 01	0.000 00
121	0.600 02	0.000 00	0.200 01	0.000 00
122	0.600 02	0.500 01	0.200 01	0.000 00
123	0.600 02	0.100 02	0.200 01	0.000 00
124	0.600 02	0.150 02	0.200 01	0.000 00
125	0.600 02	0.200 02	0.200 01	0.000 00
126	0.600 02	0.250 02	0.200 01	0.000 00
127	0.000 00	0.000 00	0.400 01	0.000 00
128	0.000 00	0.500 01	0.400 01	0.000 00
129	0.000 00	0.100 02	0.400 01	0.000 00
130	0.000 00	0.150 02	0.400 01	0.000 00
131	0.000 00	0.200 02	0.400 01	0.000 00
132	0.000 00	0.250 02	0.400 01	0.000 00
133	0.100 02	0.000 00	0.400 01	0.000 00
134	0.100 02	0.500 01	0.400 01	0.000 00
135	0.100 02	0.100 02	0.400 01	0.000 00
136	0.100 02	0.150 02	0.400 01	0.000 00
137	0.100 02	0.200 02	0.400 01	0.000 00
138	0.100 02	0.250 02	0.400 01	0.000 00
139	0.200 02	0.000 00	0.400 01	0.000 00
140	0.200 02	0.500 01	0.400 01	0.000 00
141	0.200 02	0.100 02	0.400 01	0.000 00
142	0.200 02	0.150 02	0.400 01	0.000 00
143	0.200 02	0.200 02	0.400 01	0.000 00
144	0.300 02	0.250 02	0.400 01	0.000 00
145	0.300 02	0.000 00	0.400 01	0.000 00
146	0.300 02	0.500 01	0.400 01	0.000 00
147	0.300 02	0.100 02	0.400 01	0.000 00
148	0.300 02	0.150 02	0.400 01	0.000 00
149	0.300 02	0.200 02	0.400 01	0.000 00
150	0.300 02	0.250 02	0.400 01	0.000 00
151	0.400 02	0.000 00	0.400 01	0.000 00
152	0.400 02	0.500 01	0.400 01	0.000 00
153	0.400 02	0.100 02	0.400 01	0.000 00
154	0.400 02	0.150 02	0.400 01	0.000 00
155	0.400 02	0.200 02	0.400 01	0.000 00
156	0.400 02	0.250 02	0.400 01	0.000 00
157	0.500 02	0.000 00	0.400 01	0.000 00
158	0.500 02	0.500 01	0.400 01	0.000 00
159	0.500 02	0.100 02	0.400 01	0.000 00
160	0.500 02	0.150 02	0.400 01	0.000 00
161	0.500 02	0.200 02	0.400 01	0.000 00
162	0.500 02	0.250 02	0.400 01	0.000 00
163	0.600 02	0.000 00	0.400 01	0.000 00
164	0.600 02	0.500 01	0.400 01	0.000 00
165	0.600 02	0.100 02	0.400 01	0.000 00
166	0.600 02	0.150 02	0.400 01	0.000 00
167	0.600 02	0.200 02	0.400 01	0.000 00
168	0.600 02	0.250 02	0.400 01	0.000 00

MODE-ELEMENT RELATIONSHIP

ELEMS	N1	N2	N3	N4	N5	N6	N7	N8
1	1	3	8	7	43	44	50	49
2	2	4	9	18	44	48	51	50
3	3	5	10	18	46	48	52	51
4	4	6	11	20	46	47	53	51
5	5	7	12	21	47	48	54	53
6	6	8	14	13	48	50	56	55
7	7	9	14	14	50	51	57	56
8	8	10	16	16	51	52	58	57
9	9	11	17	16	52	53	59	58
10	10	12	18	17	53	54	60	59
11	11	13	20	19	55	56	62	61
12	12	14	21	20	56	57	63	62
13	13	15	22	21	57	58	64	63
14	14	16	22	22	58	59	65	64
15	15	17	23	23	59	60	66	65
16	16	18	24	23	60	61	67	66
17	17	20	26	25	61	62	68	67
18	18	21	27	26	62	63	69	68
19	19	22	28	27	63	64	70	69
20	20	23	28	28	64	65	71	70
21	21	24	30	29	65	66	72	71
22	22	25	32	31	67	68	74	73
23	23	26	32	32	68	69	75	74
24	24	27	33	33	69	70	76	75
25	25	28	34	34	70	71	77	76
26	26	29	35	35	71	72	78	77
27	27	30	36	36	72	73	80	79
28	28	31	38	37	73	74	81	80
29	29	32	39	38	74	75	82	81
30	30	33	40	39	75	76	83	82
31	31	34	41	40	76	77	84	83
32	32	35	42	41	77	78	84	83
33	33	36	44	43	85	86	92	91
34	34	37	51	50	86	87	93	92
35	35	38	52	51	87	88	94	93
36	36	39	53	52	88	89	95	94
37	37	40	54	53	89	90	96	95
38	38	41	55	54	90	91	97	96
39	39	42	56	55	91	92	98	97
40	40	43	57	56	92	93	98	98
41	41	44	58	57	93	94	100	99
42	42	45	58	58	94	95	101	100
43	43	46	60	59	95	96	102	101
44	44	47	62	61	96	97	103	102
45	45	48	63	62	98	99	105	104
46	46	49	64	63	99	100	106	105
		50	65	64	100	101	107	106
		51	66	65	101	102	108	107
		52	67	66	102	103	110	108

47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120
 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120
 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120
 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168
 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168
 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168
 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168

FIXED BOUNDARY CONDITIONS

NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID
1	0	2	0	3	0	4	0	5	0
6	0	7	0	12	0	13	0	18	0
19	0	24	0	25	0	30	0	31	0
36	0	37	0	38	0	39	0	40	0
41	0	42	0	43	0	44	0	45	0
49	0	47	0	48	0	49	0	54	0
53	0	60	0	61	0	66	0	67	0
72	0	73	0	78	0	79	0	80	0
81	0	82	0	83	0	84	0	85	0
86	0	87	0	88	0	89	0	90	0
91	0	96	0	97	0	102	0	103	0
108	0	109	0	114	0	115	0	120	0
121	0	122	0	123	0	124	0	125	0
125	0	127	0	128	0	129	0	130	0
131	0	132	0	133	0	138	0	139	0
144	0	145	0	150	0	151	0	156	0
157	0	162	0	163	0	164	0	165	0
165	0	167	0	168	0				

MAXIMUM BANDWIDTH = 53 ON ROW NO 23

OUTPUT FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENTS METHOD

INITIAL CONC DISTRIBUTION AT TIME = 0.000 HOURS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000 00	7	0.0000 00	3	0.0000 00	4	0.0000 00	5	0.0000 00	10	0.0000 00
6	0.0000 00	8	0.0000 00	8	0.0000 00	8	0.0000 00	10	0.0000 00	16	0.0000 00
11	0.0000 00	12	0.0000 00	13	0.0000 00	14	0.0000 00	16	0.0000 00	18	0.0000 00
16	0.0000 00	17	0.0000 00	18	0.0000 00	19	0.0000 00	20	0.0000 00	21	0.0000 00
21	0.0000 00	22	0.0000 00	23	0.0000 00	24	0.0000 00	25	0.0000 00	26	0.0000 00
26	0.0000 00	27	0.0000 00	28	0.0000 00	29	0.0000 00	30	0.0000 00	31	0.0000 00
31	0.0000 00	32	0.0000 00	33	0.0000 00	34	0.0000 00	35	0.0000 00	36	0.0000 00
36	0.0000 00	37	0.0000 00	38	0.0000 00	39	0.0000 00	40	0.0000 00	41	0.0000 00
41	0.0000 00	42	0.0000 00	43	0.0000 00	44	0.0000 00	45	0.0000 00	46	0.0000 00
46	0.0000 00	47	0.0000 00	48	0.0000 00	49	0.0000 00	50	0.0000 00	51	0.0000 00
51	0.0000 00	52	0.0000 00	53	0.0000 00	54	0.0000 00	55	0.0000 00	56	0.0000 00
56	0.0000 00	57	0.0000 00	58	0.0000 00	59	0.0000 00	60	0.0000 00	61	0.0000 00
61	0.0000 00	62	0.0000 00	63	0.0000 00	64	0.0000 00	65	0.0000 00	66	0.0000 00
66	0.0000 00	67	0.0000 00	68	0.0000 00	69	0.0000 00	70	0.0000 00	71	0.0000 00
71	0.0000 00	72	0.0000 00	73	0.0000 00	74	0.0000 00	75	0.0000 00	76	0.0000 00
76	0.0000 00	77	0.0000 00	78	0.0000 00	79	0.0000 00	80	0.0000 00	81	0.0000 00
81	0.0000 00	82	0.0000 00	83	0.0000 00	84	0.0000 00	85	0.0000 00	86	0.0000 00
86	0.0000 00	87	0.0000 00	88	0.0000 00	89	0.0000 00	90	0.0000 00	91	0.0000 00
91	0.0000 00	92	0.0000 00	93	0.0000 00	94	0.0000 00	95	0.0000 00	96	0.0000 00
96	0.0000 00	97	0.0000 00	98	0.0000 00	99	0.0000 00	100	0.0000 00	101	0.0000 00
101	0.0000 00	102	0.0000 00	103	0.0000 00	104	0.0000 00	105	0.0000 00	106	0.0000 00
106	0.0000 00	107	0.0000 00	108	0.0000 00	109	0.0000 00	110	0.0000 00	111	0.0000 00
111	0.0000 00	112	0.0000 00	113	0.0000 00	114	0.0000 00	115	0.0000 00	116	0.0000 00
116	0.0000 00	117	0.0000 00	118	0.0000 00	119	0.0000 00	120	0.0000 00	121	0.0000 00
121	0.0000 00	122	0.0000 00	123	0.0000 00	124	0.0000 00	125	0.0000 00	126	0.0000 00
126	0.0000 00	127	0.0000 00	128	0.0000 00	129	0.0000 00	130	0.0000 00	131	0.0000 00
131	0.0000 00	132	0.0000 00	133	0.0000 00	134	0.0000 00	135	0.0000 00	136	0.0000 00
136	0.0000 00	137	0.0000 00	138	0.0000 00	139	0.0000 00	140	0.0000 00	141	0.0000 00
141	0.0000 00	142	0.0000 00	143	0.0000 00	144	0.0000 00	145	0.0000 00	146	0.0000 00
146	0.0000 00	147	0.0000 00	148	0.0000 00	149	0.0000 00	150	0.0000 00	151	0.0000 00
151	0.0000 00	152	0.0000 00	153	0.0000 00	154	0.0000 00	155	0.0000 00	156	0.0000 00
156	0.0000 00	157	0.0000 00	158	0.0000 00	159	0.0000 00	160	0.0000 00	161	0.0000 00
161	0.0000 00	162	0.0000 00	163	0.0000 00	164	0.0000 00	165	0.0000 00	166	0.0000 00
166	0.0000 00	167	0.0000 00	168	0.0000 00	169	0.0000 00	170	0.0000 00	171	0.0000 00

CONCENTRATION DISTRIBUTION AT TIME = 480 000 HOURS

MINES	CONCS	MINES	CUNCS	MINES	CONCS	MINES	CONCS	MINES	CONCS	MINES	CONCS
1	0.5780 00	2	0.7750 03	3	0.1210 05	4	0.7750 03	5	0.8530 00		
6	0.2550 00	7	0.1680 00	8	0.3190 03	9	0.3420 03	10	0.3190 03		
11	0.2520 00	12	0.6850-01	13	0.4170-03	14	0.1500 02	15	0.2970 03		
16	0.1500 02	17	0.6280-02	18	0.1370-02	19	0.1840-04	20	0.8530-01		
21	0.3100 01	22	0.8530-01	23	0.2850-04	24	0.3850-05	25	0.1670-07		
26	0.7900-04	27	0.2120-02	28	0.2820-04	29	0.2820-07	30	0.1710-08		
31	0.2400-11	32	0.8480-08	33	0.2620-05	34	0.8480-08	35	0.3220-11		
36	0.1420-12	37	0.5090-16	38	0.1520-12	39	0.3660-11	40	0.1620-12		
41	0.5680-16	42	0.1750-17	43	0.4150 00	44	0.7120 03	45	0.1730 06		
46	0.7120 03	47	0.8220 00	48	0.3550 00	49	0.1700 00	50	0.2880 03		
51	0.4290 05	52	0.2880 03	53	0.3270 02	54	0.8560-01	55	0.3830-02		
56	0.1370 04	57	0.7900 03	58	0.1270 02	59	0.8720-02	60	0.1330-02		
61	0.1670-04	62	0.8300-01	63	0.3140 01	64	0.8300-01	65	0.2590-04		
66	0.3180-05	67	0.1820-07	68	0.2180-04	69	0.1840-02	70	0.7160-04		
71	0.2310-07	72	0.1540-08	73	0.2180-11	74	0.8530-08	75	0.2070-06		
76	0.8530-08	77	0.2840-11	78	0.4680-16	79	0.4680-16	80	0.1480-12		
81	0.3330-11	82	0.1480-12	83	0.2810-16	84	0.1570-17	85	0.3210 00		
86	0.8210 03	87	0.7140 05	88	0.8210-16	89	0.4740 00	90	0.1390 00		
91	0.8450-01	92	0.2090 03	93	0.2060 05	94	0.2090 03	95	0.1410 00		
96	0.3790-01	97	0.2550-02	98	0.8900 00	99	0.8180 03	100	0.8900 00		
101	0.3840-02	102	0.7880-03	103	0.1230-04	104	0.6280-01	105	0.2070 01		
106	0.6180-01	107	0.1920-04	108	0.2240-05	109	0.1130-07	110	0.8340-04		
111	0.1420-02	112	0.5240-04	113	0.1140-07	114	0.1120-08	115	0.1670-11		
116	0.6440-08	117	0.1850-06	118	0.8440-08	119	0.1110-12	120	0.8550-13		
121	0.3510-16	122	0.1110-12	123	0.2430-11	124	0.7240 04	125	0.3890-16		
126	0.1180-17	127	0.3470-01	128	0.1360 03	129	0.8540 02	130	0.1360 03		
131	0.5000-01	132	0.1650-01	133	0.1300-01	134	0.8540 02	135	0.2690 04		
136	0.5540 02	137	0.1880-01	138	0.4000-02	139	0.8530-03	140	0.2750 01		
141	0.1050 03	142	0.2750 01	143	0.8350-03	144	0.1290-03	145	0.3510-05		
146	0.1780-01	147	0.8400 04	148	0.1780-01	149	0.5480-08	150	0.5050-06		
151	0.3510-08	152	0.1580-04	153	0.4090-03	154	0.1580-04	155	0.5180-08		
156	0.2970-08	157	0.1580-04	158	0.1950-08	159	0.4630-07	160	0.1950-08		
161	0.6780-12	162	0.2120-12	163	0.1110-16	164	0.3410-13	165	0.7630-12		
166	0.3410-13	167	0.1200-16	168	0.2430-18	169	0.3410-13	170	0.7630-12		

CONCENTRATION DISTRIBUTION AT TIME = 240.000 HOURS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.125D-01	2	0.116D-04	3	0.373D-06	4	0.116D-04	5	0.177D-01						
6	0.613D-00	7	0.265D-01	8	0.128D-03	9	0.500D-04	10	0.123D-03						
11	0.285D-01	12	0.782D-02	13	0.412D-04	14	0.194D-01	15	0.476D-01						
16	0.184D-00	17	0.643D-04	18	0.369D-08	19	0.217D-08	20	0.650D-05						
21	0.141D-03	22	0.850D-05	23	0.103D-08	24	0.678D-10	25	0.236D-14						
26	0.504D-11	27	0.103D-08	28	0.504D-11	29	0.170D-14	30	0.179D-16						
31	0.478D-23	32	0.845D-19	33	0.207D-31	34	0.647D-19	35	0.266D-22						
36	0.578D-25	37	0.207D-31	38	0.325D-28	39	0.638D-27	40	0.325D-27						
41	0.912D-20	42	0.233D-36	43	0.146D-01	44	0.105D-04	45	0.512D-06						
46	0.105D-04	47	0.170D-01	48	0.107D-01	49	0.240D-01	50	0.111D-03						
51	0.465D-04	52	0.111D-03	53	0.347D-01	54	0.670D-02	55	0.373D-04						
56	0.174D-00	57	0.441D-01	58	0.174D-00	59	0.586D-04	60	0.231D-05						
61	0.194D-08	62	0.587D-05	63	0.131D-03	64	0.587D-05	65	0.259D-08						
66	0.612D-10	67	0.207D-14	68	0.441D-11	69	0.845D-10	70	0.441D-11						
71	0.775D-19	72	0.163D-16	73	0.436D-22	74	0.775D-19	75	0.156D-17						
76	0.540D-27	77	0.242D-22	78	0.624D-25	79	0.188D-31	80	0.257D-28						
81	0.780D-03	82	0.287D-28	83	0.893D-32	84	0.208D-35	85	0.683D-00						
86	0.170D-01	87	0.157D-06	88	0.780D-03	89	0.950D-00	90	0.323D-00						
91	0.454D-02	92	0.834D-02	93	0.378D-04	94	0.834D-02	95	0.248D-01						
96	0.431D-04	97	0.280D-04	98	0.131D-00	99	0.335D-01	100	0.131D-00						
101	0.822D-05	102	0.240D-05	103	0.483D-10	104	0.482D-05	105	0.100D-02						
106	0.715D-10	107	0.161D-08	108	0.463D-10	109	0.156D-14	110	0.246D-11						
111	0.890D-18	112	0.346D-11	113	0.165D-14	114	0.121D-16	115	0.333D-22						
116	0.140D-31	117	0.180D-17	118	0.690D-18	119	0.185D-22	120	0.391D-25						
121	0.157D-25	122	0.226D-28	123	0.439D-27	124	0.226D-28	125	0.674D-32						
126	0.803D-01	127	0.551D-01	128	0.203D-03	129	0.232D-02	130	0.203D-03						
131	0.232D-02	132	0.191D-01	133	0.436D-02	134	0.232D-02	135	0.818D-03						
136	0.880D-00	137	0.656D-02	138	0.910D-03	139	0.877D-05	140	0.392D-01						
141	0.980D-00	142	0.382D-01	143	0.132D-04	144	0.674D-05	145	0.470D-09						
146	0.138D-05	147	0.308D-04	148	0.138D-05	149	0.498D-08	150	0.134D-17						
151	0.499D-18	152	0.109D-11	153	0.224D-10	154	0.109D-11	155	0.365D-16						
156	0.350D-17	157	0.107D-22	158	0.189D-18	159	0.189D-18	160	0.189D-18						
161	0.588D-23	162	0.114D-25	163	0.460D-32	164	0.376D-18	165	0.141D-27						
166	0.722D-28	167	0.216D-32	168	0.457D-36	169	0.722D-28	170	0.722D-28						

OUTPUT FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENTS METHOD

INITIAL CONC DISTRIBUTION AT TIME = 0.000 HOURS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000 00	2	0.0000 00	3	0.0000 00	4	0.0000 00	5	0.0000 00	6	0.0000 00	7	0.0000 00
6	0.0000 00	7	0.0000 00	8	0.0000 00	9	0.0000 00	10	0.0000 00	11	0.0000 00	12	0.0000 00
11	0.0000 00	12	0.0000 00	13	0.0000 00	14	0.0000 00	15	0.0000 00	16	0.0000 00	17	0.0000 00
16	0.0000 00	17	0.0000 00	18	0.0000 00	19	0.0000 00	20	0.0000 00	21	0.0000 00	22	0.0000 00
21	0.0000 00	22	0.0000 00	23	0.0000 00	24	0.0000 00	25	0.0000 00	26	0.0000 00	27	0.0000 00
26	0.0000 00	27	0.0000 00	28	0.0000 00	29	0.0000 00	30	0.0000 00	31	0.0000 00	32	0.0000 00
31	0.0000 00	32	0.0000 00	33	0.0000 00	34	0.0000 00	35	0.0000 00	36	0.0000 00	37	0.0000 00
36	0.0000 00	37	0.0000 00	38	0.0000 00	39	0.0000 00	40	0.0000 00	41	0.0000 00	42	0.0000 00
41	0.0000 00	42	0.0000 00	43	0.0000 00	44	0.0000 00	45	0.0000 00	46	0.0000 00	47	0.0000 00
46	0.0000 00	47	0.0000 00	48	0.0000 00	49	0.0000 00	50	0.0000 00	51	0.0000 00	52	0.0000 00
51	0.0000 00	52	0.0000 00	53	0.0000 00	54	0.0000 00	55	0.0000 00	56	0.0000 00	57	0.0000 00
56	0.0000 00	57	0.0000 00	58	0.0000 00	59	0.0000 00	60	0.0000 00	61	0.0000 00	62	0.0000 00
61	0.0000 00	62	0.0000 00	63	0.0000 00	64	0.0000 00	65	0.0000 00	66	0.0000 00	67	0.0000 00
66	0.0000 00	67	0.0000 00	68	0.0000 00	69	0.0000 00	70	0.0000 00	71	0.0000 00	72	0.0000 00
71	0.0000 00	72	0.0000 00	73	0.0000 00	74	0.0000 00	75	0.0000 00	76	0.0000 00	77	0.0000 00
76	0.0000 00	77	0.0000 00	78	0.0000 00	79	0.0000 00	80	0.0000 00	81	0.0000 00	82	0.0000 00
81	0.0000 00	82	0.0000 00	83	0.0000 00	84	0.0000 00	85	0.0000 00	86	0.0000 00	87	0.0000 00
86	0.0000 00	87	0.0000 00	88	0.0000 00	89	0.0000 00	90	0.0000 00	91	0.0000 00	92	0.0000 00
91	0.0000 00	92	0.0000 00	93	0.0000 00	94	0.0000 00	95	0.0000 00	96	0.0000 00	97	0.0000 00
96	0.0000 00	97	0.0000 00	98	0.0000 00	99	0.0000 00	100	0.0000 00	101	0.0000 00	102	0.0000 00
101	0.0000 00	102	0.0000 00	103	0.0000 00	104	0.0000 00	105	0.0000 00	106	0.0000 00	107	0.0000 00
106	0.0000 00	107	0.0000 00	108	0.0000 00	109	0.0000 00	110	0.0000 00	111	0.0000 00	112	0.0000 00
111	0.0000 00	112	0.0000 00	113	0.0000 00	114	0.0000 00	115	0.0000 00	116	0.0000 00	117	0.0000 00
116	0.0000 00	117	0.0000 00	118	0.0000 00	119	0.0000 00	120	0.0000 00	121	0.0000 00	122	0.0000 00
121	0.0000 00	122	0.0000 00	123	0.0000 00	124	0.0000 00	125	0.0000 00	126	0.0000 00	127	0.0000 00
126	0.0000 00	127	0.0000 00	128	0.0000 00	129	0.0000 00	130	0.0000 00	131	0.0000 00	132	0.0000 00
131	0.0000 00	132	0.0000 00	133	0.0000 00	134	0.0000 00	135	0.0000 00	136	0.0000 00	137	0.0000 00
136	0.0000 00	137	0.0000 00	138	0.0000 00	139	0.0000 00	140	0.0000 00	141	0.0000 00	142	0.0000 00
141	0.0000 00	142	0.0000 00	143	0.0000 00	144	0.0000 00	145	0.0000 00	146	0.0000 00	147	0.0000 00
146	0.0000 00	147	0.0000 00	148	0.0000 00	149	0.0000 00	150	0.0000 00	151	0.0000 00	152	0.0000 00
151	0.0000 00	152	0.0000 00	153	0.0000 00	154	0.0000 00	155	0.0000 00	156	0.0000 00	157	0.0000 00
156	0.0000 00	157	0.0000 00	158	0.0000 00	159	0.0000 00	160	0.0000 00	161	0.0000 00	162	0.0000 00
161	0.0000 00	162	0.0000 00	163	0.0000 00	164	0.0000 00	165	0.0000 00	166	0.0000 00	167	0.0000 00
166	0.0000 00	167	0.0000 00	168	0.0000 00	169	0.0000 00	170	0.0000 00	171	0.0000 00	172	0.0000 00

CONCENTRATION DISTRIBUTION AT TIME = 720.000 HOURS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.462D 00	2	0.606D 03	3	0.108D 06	4	0.806D 03	5	0.634D 00						
6	0.230D 00	7	0.247D 00	8	0.367D 01	9	0.352D 05	10	0.367D 03						
11	0.244D 00	12	0.116D 00	13	0.257D 01	14	0.339D 02	15	0.551D 04						
16	0.339D 02	17	0.367D 01	18	0.110D 00	19	0.610D 03	20	0.206D 01						
21	0.126D 03	22	0.206D 01	23	0.907D 03	24	0.214D 03	25	0.441D 05						
28	0.186D 01	27	0.823D 00	28	0.186D 01	29	0.671D 05	30	0.111D 05						
31	0.100D 07	32	0.496D 04	33	0.162D 02	34	0.496D 04	35	0.154D 07						
36	0.166D 08	37	0.708D 11	38	0.335D 03	39	0.842D 06	40	0.335D 07						
41	0.106D 10	42	0.766D 12	43	0.417D 00	44	0.565D 03	45	0.105D 06						
46	0.565D 03	47	0.585D 00	48	0.317D 00	49	0.219D 00	50	0.333D 03						
51	0.526D 05	52	0.333D 03	53	0.307D 00	54	0.106D 00	55	0.224D 01						
56	0.490D 02	57	0.510D 04	58	0.450D 02	59	0.329D 01	60	0.980D 02						
61	0.350D 03	62	0.181D 01	63	0.116D 03	64	0.181D 01	65	0.817D 03						
66	0.192D 03	67	0.398D 05	68	0.178D 01	69	0.747D 00	70	0.178D 01						
71	0.603D 05	72	0.140D 05	73	0.907D 08	74	0.447D 04	75	0.147D 02						
76	0.447D 04	77	0.204D 07	78	0.150D 08	79	0.648D 11	80	0.304D 07						
81	0.854D 06	82	0.204D 07	83	0.171D 11	84	0.691D 12	85	0.262D 00						
86	0.418D 03	87	0.610D 05	88	0.418D 03	89	0.373D 00	90	0.126D 00						
91	0.137D 00	92	0.247D 03	93	0.329D 05	94	0.247D 03	95	0.197D 00						
96	0.830D 01	97	0.147D 01	98	0.363D 02	99	0.336D 04	100	0.363D 02						
101	0.215D 01	102	0.637D 02	103	0.383D 03	104	0.135D 01	105	0.797D 02						
106	0.135D 01	107	0.571D 03	108	0.128D 03	109	0.291D 05	110	0.129D 01						
111	0.337D 00	112	0.129D 01	113	0.442D 05	114	0.691D 06	115	0.689D 08						
116	0.337D 00	117	0.105D 02	118	0.337D 04	119	0.106D 07	120	0.108D 08						
121	0.493D 11	122	0.130D 01	123	0.839D 06	124	0.230D 07	125	0.747D 11						
126	0.813D 12	127	0.330D 07	128	0.121D 03	129	0.722D 04	130	0.121D 03						
131	0.800D 01	132	0.360D 01	133	0.191D 01	134	0.716D 02	135	0.406D 04						
136	0.216D 02	137	0.284D 01	138	0.835D 02	139	0.256D 02	140	0.107D 02						
141	0.527D 03	142	0.107D 02	143	0.381D 02	144	0.773D 03	145	0.107D 02						
146	0.408D 00	147	0.167D 02	148	0.408D 00	149	0.132D 03	150	0.878D 04						
151	0.816D 08	152	0.406D 02	153	0.406D 00	154	0.406D 02	155	0.219D 04						
156	0.151D 06	157	0.317D 08	158	0.139D 00	159	0.406D 02	160	0.126D 05						
161	0.324D 08	162	0.281D 09	163	0.107D 04	164	0.317D 03	165	0.107D 04						
166	0.742D 08	167	0.242D 11	168	0.164D 11	169	0.742D 08	170	0.197D 06						

CONCENTRATION DISTRIBUTION AT TIME = 860.000 HOURS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.385D 00	2	0.523D 03	3	0.810D 05	4	0.523D 03	5	0.523D 03	6	0.523D 03	7	0.523D 03
6	0.193D 00	7	0.252D 00	8	0.381D 03	9	0.381D 03	10	0.600D 05	11	0.600D 05	12	0.600D 05
11	0.371D 00	12	0.127D 00	13	0.127D 00	14	0.350D 01	15	0.350D 01	16	0.350D 01	17	0.350D 01
16	0.970D 02	17	0.127D 00	18	0.350D 01	19	0.350D 01	20	0.378D 02	21	0.378D 02	22	0.378D 02
21	0.837D 03	22	0.804D 01	23	0.804D 01	24	0.350D 01	25	0.198D 02	26	0.198D 02	27	0.198D 02
26	0.294D 00	27	0.197D 02	28	0.394D 00	29	0.394D 00	30	0.352D 02	31	0.352D 02	32	0.352D 02
31	0.867D 06	32	0.352D 02	33	0.172D 00	34	0.172D 00	35	0.352D 02	36	0.352D 02	37	0.352D 02
36	0.248D 06	37	0.378D 02	38	0.391D 04	39	0.391D 04	40	0.584D 03	41	0.584D 03	42	0.584D 03
41	0.501D 08	42	0.704D 06	43	0.352D 00	44	0.352D 00	45	0.491D 03	46	0.491D 03	47	0.491D 03
46	0.491D 03	47	0.491D 03	48	0.178D 00	49	0.178D 00	50	0.236D 00	51	0.236D 00	52	0.236D 00
51	0.574D 05	52	0.348D 00	53	0.348D 00	54	0.320D 00	55	0.717D 00	56	0.717D 00	57	0.717D 00
56	0.883D 02	57	0.145D 06	58	0.883D 02	59	0.883D 02	60	0.705D 01	61	0.705D 01	62	0.705D 01
61	0.337D 02	62	0.745D 05	63	0.745D 05	64	0.711D 03	65	0.785D 01	66	0.785D 01	67	0.785D 01
66	0.141D 02	67	0.637D 04	68	0.268D 00	69	0.268D 00	70	0.180D 02	71	0.180D 02	72	0.180D 02
71	0.123D 03	72	0.300D 04	73	0.778D 06	74	0.778D 06	75	0.318D 02	76	0.318D 02	77	0.318D 02
76	0.318D 02	77	0.117D 05	78	0.223D 08	79	0.223D 08	80	0.299D 08	81	0.299D 08	82	0.299D 08
81	0.525D 03	82	0.140D 04	83	0.453D 08	84	0.453D 08	85	0.630D 08	86	0.630D 08	87	0.630D 08
86	0.362D 03	87	0.549D 05	88	0.362D 03	89	0.362D 03	90	0.314D 00	91	0.314D 00	92	0.314D 00
91	0.148D 00	92	0.258D 03	93	0.258D 03	94	0.359D 05	95	0.258D 03	96	0.258D 03	97	0.258D 03
96	0.703D 01	97	0.316D 01	98	0.651D 02	99	0.651D 02	100	0.743D 04	101	0.743D 04	102	0.743D 04
101	0.454D 01	102	0.142D 01	103	0.226D 02	104	0.226D 02	105	0.589D 01	106	0.589D 01	107	0.589D 01
106	0.589D 01	107	0.328D 02	108	0.328D 02	109	0.328D 02	110	0.578D 04	111	0.578D 04	112	0.578D 04
111	0.231D 02	112	0.193D 00	113	0.193D 00	114	0.858D 04	115	0.198D 04	116	0.198D 04	117	0.198D 04
116	0.231D 02	117	0.111D 00	118	0.338D 02	119	0.338D 02	120	0.652D 06	121	0.652D 06	122	0.652D 06
121	0.227D 08	122	0.105D 04	123	0.387D 03	124	0.387D 03	125	0.105D 04	126	0.105D 04	127	0.105D 04
126	0.447D 09	127	0.291D 01	128	0.291D 01	129	0.291D 01	130	0.617D 04	131	0.617D 04	132	0.617D 04
131	0.431D 09	132	0.101D 01	133	0.305D 01	134	0.305D 01	135	0.746D 02	136	0.746D 02	137	0.746D 02
136	0.145D 02	137	0.300D 01	138	0.300D 01	139	0.691D 02	140	0.488D 02	141	0.488D 02	142	0.488D 02
141	0.101D 02	142	0.826D 02	143	0.826D 02	144	0.175D 01	145	0.158D 02	146	0.158D 02	147	0.158D 02
146	0.175D 01	147	0.826D 02	148	0.826D 02	149	0.244D 01	150	0.612D 03	151	0.612D 03	152	0.612D 03
151	0.175D 01	152	0.591D 01	153	0.591D 01	154	0.244D 01	155	0.591D 01	156	0.591D 01	157	0.591D 01
156	0.223D 05	157	0.148D 06	158	0.148D 06	159	0.264D 01	160	0.264D 01	161	0.264D 01	162	0.264D 01
161	0.223D 05	162	0.302D 07	163	0.302D 07	164	0.655D 09	165	0.655D 09	166	0.655D 09	167	0.655D 09
166	0.327D 06	167	0.101D 08	168	0.101D 08	169	0.104D 09	170	0.104D 09	171	0.104D 09	172	0.104D 09
172	0.104D 09	173	0.104D 09	174	0.104D 09	175	0.104D 09	176	0.104D 09	177	0.104D 09	178	0.104D 09
178	0.104D 09	179	0.104D 09	180	0.104D 09	181	0.104D 09	182	0.104D 09	183	0.104D 09	184	0.104D 09
184	0.104D 09	185	0.104D 09	186	0.104D 09	187	0.104D 09	188	0.104D 09	189	0.104D 09	190	0.104D 09
190	0.104D 09	191	0.104D 09	192	0.104D 09	193	0.104D 09	194	0.104D 09	195	0.104D 09	196	0.104D 09
196	0.104D 09	197	0.104D 09	198	0.104D 09	199	0.104D 09	200	0.104D 09	201	0.104D 09	202	0.104D 09
202	0.104D 09	203	0.104D 09	204	0.104D 09	205	0.104D 09	206	0.104D 09	207	0.104D 09	208	0.104D 09
208	0.104D 09	209	0.104D 09	210	0.104D 09	211	0.104D 09	212	0.104D 09	213	0.104D 09	214	0.104D 09
214	0.104D 09	215	0.104D 09	216	0.104D 09	217	0.104D 09	218	0.104D 09	219	0.104D 09	220	0.104D 09
220	0.104D 09	221	0.104D 09	222	0.104D 09	223	0.104D 09	224	0.104D 09	225	0.104D 09	226	0.104D 09
226	0.104D 09	227	0.104D 09	228	0.104D 09	229	0.104D 09	230	0.104D 09	231	0.104D 09	232	0.104D 09
232	0.104D 09	233	0.104D 09	234	0.104D 09	235	0.104D 09	236	0.104D 09	237	0.104D 09	238	0.104D 09
238	0.104D 09	239	0.104D 09	240	0.104D 09	241	0.104D 09	242	0.104D 09	243	0.104D 09	244	0.104D 09
244	0.104D 09	245	0.104D 09	246	0.104D 09	247	0.104D 09	248	0.104D 09	249	0.104D 09	250	0.104D 09
250	0.104D 09	251	0.104D 09	252	0.104D 09	253	0.104D 09	254	0.104D 09	255	0.104D 09	256	0.104D 09
256	0.104D 09	257	0.104D 09	258	0.104D 09	259	0.104D 09	260	0.104D 09	261	0.104D 09	262	0.104D 09
262	0.104D 09	263	0.104D 09	264	0.104D 09	265	0.104D 09	266	0.104D 09	267	0.104D 09	268	0.104D 09
268	0.104D 09	269	0.104D 09	270	0.104D 09	271	0.104D 09	272	0.104D 09	273	0.104D 09	274	0.104D 09
274	0.104D 09	275	0.104D 09	276	0.104D 09	277	0.104D 09	278	0.104D 09	279	0.104D 09	280	0.104D 09
280	0.104D 09	281	0.104D 09	282	0.104D 09	283	0.104D 09	284	0.104D 09	285	0.104D 09	286	0.104D 09
286	0.104D 09	287	0.104D 09	288	0.104D 09	289	0.104D 09	290	0.104D 09	291	0.104D 09	292	0.104D 09
292	0.104D 09	293	0.104D 09	294	0.104D 09	295	0.104D 09	296	0.104D 09	297	0.104D 09	298	0.104D 09
298	0.104D 09	299	0.104D 09	300	0.104D 09	301	0.104D 09	302	0.104D 09	303	0.104D 09	304	0.104D 09
304	0.104D 09	305	0.104D 09	306	0.104D 09	307	0.104D 09	308	0.104D 09	309	0.104D 09	310	0.104D 09
310	0.104D 09	311	0.104D 09	312	0.104D 09	313	0.104D 09	314	0.104D 09	315	0.104D 09	316	0.104D 09
316	0.104D 09	317	0.104D 09	318	0.104D 09	319	0.104D 09	320	0.104D 09	321	0.104D 09	322	0.104D 09
322	0.104D 09	323	0.104D 09	324	0.104D 09	325	0.104D 09	326	0.104D 09	327	0.104D 09	328	0.104D 09
328	0.104D 09	329	0.104D 09	330	0.104D 09	331	0.104D 09	332	0.104D 09	333	0.104D 09	334	0.104D 09
334	0.104D 09	335	0.104D 09	336	0.104D 09	337	0.104D 09	338	0.104D 09	339	0.104D 09	340	0.104D 09
340	0.104D 09	341	0.104D 09	342	0.104D 09	343	0.104D 09	344	0.104D 09	345	0.104D 09	346	0.104D 09
346	0.104D 09	347	0.104D 09	348	0.104D 09	349	0.104D 09	350	0.104D 09	351	0.104D 09	352	0.104D 09
352	0.104D 09	353	0.104D 09	354	0.104D 09	355	0.104D 09	356	0.104D 09	357	0.104D 09	358	0.104D 09
358	0.104D 09	359	0.104D 09	360	0.104D 09	361	0.104D 09	362	0.104D 09	363	0.104D 09	364	0.104D 09
364	0.104D 09	365	0.104D 09	366	0.104D 09	367	0.104D 09	368	0.104D 09	369	0.104D 09	370	0.104D 09
370	0.104D 09	371	0.104D 09	372	0.104D 09	373	0.104D 09	374	0.104D 09	375	0.104D 09	376	0.104D 09
376	0.104D 09	377	0.104D 09	378	0.104D 09	379	0.104D 09	380	0.104D 09	381	0.104D 09	382	0.104D 09
382	0.104D 09	383	0.104D 09	384	0.104D 09	385	0.104D 09	386	0.104D 09	387	0.104D 09	388	0.104D 09
388	0.104D 09	389	0.104D 09	390	0.104D 09	391	0.104D 09	392	0.104D 09	393	0.104D 09	394	0.104D 09
394	0.104D 09	395	0.104D 09	396	0.104D 09	397	0.104D 09	398	0.104D 09	399	0.104D 09	400	0.104D 09

CONCENTRATION DISTRIBUTION AT TIME =1200.000 HOURS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.331D 00	2	0.484D 03	3	0.687D 05	4	0.854D 03	5	0.895D 00				
6	0.144D 00	7	0.253D 00	8	0.397D 03	9	0.524D 06	10	0.392D 03				
11	0.379D 00	12	0.110D 00	13	0.790D 01	14	0.138D 03	15	0.165D 05				
16	0.128D 03	17	0.120D 00	18	0.240D 01	19	0.130D 01	20	0.217D 02				
21	0.216D 04	22	0.217D 02	23	0.153D 01	24	0.416D 02	25	0.879D 03				
26	0.147D 01	27	0.122D 03	28	0.147D 01	29	0.859D 03	30	0.218D 03				
31	0.141D 04	32	0.447D 01	33	0.298D 01	34	0.447D 01	35	0.211D 04				
36	0.483D 05	37	0.168D 04	38	0.608D 03	39	0.318D 01	40	0.808D 03				
41	0.228D 04	42	0.467D 07	43	0.248D 00	44	0.435D 03	45	0.763D 05				
46	0.425D 03	47	0.433D 00	48	0.195D 00	49	0.266D 00	50	0.344D 03				
51	0.574D 05	52	0.344D 03	53	0.251D 00	54	0.146D 00	55	0.816D 01				
56	0.120D 03	57	0.174D 08	58	0.252D 03	59	0.104D 00	60	0.433D 01				
61	0.105D 01	62	0.184D 03	63	0.222D 04	64	0.184D 02	65	0.134D 01				
66	0.511D 02	67	0.870D 03	68	0.130D 01	69	0.120D 03	70	0.130D 01				
71	0.757D 03	72	0.251D 03	73	0.134D 04	74	0.335D 01	75	0.274D 01				
76	0.325D 01	77	0.185D 04	78	0.917D 08	79	0.148D 06	80	0.498D 03				
81	0.285D 01	82	0.498D 03	83	0.197D 08	84	0.487D 07	85	0.185D 00				
86	0.323D 03	87	0.476D 03	88	0.223D 03	89	0.276D 00	90	0.784D 01				
91	0.142D 00	92	0.250D 03	93	0.360D 03	94	0.250D 03	95	0.211D 00				
96	0.589D 01	97	0.445D 01	98	0.890D 02	99	0.111D 05	100	0.890D 02				
101	0.656D 01	102	0.182D 01	103	0.888D 02	104	0.137D 02	105	0.140D 04				
106	0.137D 02	107	0.888D 02	108	0.231D 02	109	0.339D 03	110	0.940D 00				
111	0.778D 02	112	0.840D 00	113	0.511D 03	114	0.123D 03	115	0.860D 05				
116	0.293D 01	117	0.187D 01	118	0.293D 01	119	0.149D 04	120	0.279D 05				
121	0.100D 06	122	0.282D 03	123	0.200D 01	124	0.389D 03	125	0.149D 06				
126	0.279D 07	127	0.211D 01	128	0.930D 02	129	0.515D 04	130	0.930D 02				
131	0.386D 01	132	0.300D 01	133	0.166D 01	134	0.740D 02	135	0.423D 04				
136	0.740D 02	137	0.866D 02	138	0.556D 02	139	0.565D 02	140	0.259D 02				
141	0.142D 04	142	0.205D 02	143	0.101D 02	144	0.176D 02	145	0.850D 03				
146	0.403D 01	147	0.298D 03	148	0.403D 01	149	0.149D 02	150	0.251D 03				
151	0.567D 04	152	0.282D 00	153	0.131D 02	154	0.262D 00	155	0.980D 04				
156	0.152D 04	157	0.169D 03	158	0.888D 02	159	0.367D 00	160	0.885D 02				
161	0.288D 05	162	0.402D 06	163	0.226D 07	164	0.123D 03	165	0.456D 02				
166	0.122D 03	167	0.344D 07	168	0.462D 08								

APPENDIX F

INPUT/OUTPUT OF FIELD APPLICATION PROBLEM

INPUT DATA FOR THREE-DIMENSIONAL

GROUNDWATER DISP BY FINITE ELEMENT METHOD

TOTAL NO OF ELEMENTS * 154
TOTAL NO OF NODES * 360
MAXIMUM NO OF NODES PER ELEMENT * 8
TOTAL NO. OF MATERIALS * 1
NUMBER OF PUMPING WELLS * 0
NUMBER OF CONCS TO BE ESTIMATED * 360

NUMBER OF PUMPING PERIODS * 0
TOTAL SIMULATION PERIODS * 16
FACTOR MULTIPLYING COMPUTED CONCS * 1 00000

STEP SIZE * 24 00000
STATE OF PROBLEM * 1
NO OF SPECIFIED CONDITIONS * 100

NODES	X(I)	Y(I)	Z(I)	CINT(I)
1	0.000 00	0.000 00	0.100 02	0.000 00
2	0.000 00	0.110 04	0.100 02	0.000 00
3	0.000 00	0.150 04	0.100 02	0.000 00
4	0.000 00	0.180 04	0.100 02	0.000 00
5	0.000 00	0.200 04	0.100 02	0.000 00
6	0.000 00	0.210 04	0.100 02	0.000 00
7	0.000 00	0.210 04	0.100 02	0.000 00
8	0.000 00	0.240 04	0.100 02	0.000 00
9	0.000 00	0.250 04	0.100 02	0.000 00
10	0.000 00	0.270 04	0.100 02	0.000 00
11	0.000 00	0.300 04	0.100 02	0.000 00
12	0.000 00	0.320 04	0.100 02	0.000 00
13	0.000 00	0.350 04	0.100 02	0.000 00
14	0.000 00	0.370 04	0.100 02	0.000 00
15	0.000 00	0.400 04	0.100 02	0.000 00
16	0.000 00	0.450 04	0.100 02	0.000 00
17	0.120 04	0.000 00	0.100 02	0.000 00
18	0.120 04	0.110 04	0.100 02	0.000 00
19	0.120 04	0.150 04	0.100 02	0.000 00
20	0.120 04	0.200 04	0.100 02	0.000 00
21	0.120 04	0.210 04	0.100 02	0.000 00
22	0.120 04	0.240 04	0.100 02	0.000 00
23	0.120 04	0.250 04	0.100 02	0.000 00
24	0.120 04	0.270 04	0.100 02	0.000 00
25	0.120 04	0.300 04	0.100 02	0.000 00
26	0.120 04	0.350 04	0.100 02	0.000 00
27	0.120 04	0.370 04	0.100 02	0.000 00
28	0.120 04	0.400 04	0.100 02	0.000 00
29	0.120 04	0.450 04	0.100 02	0.000 00
30	0.230 04	0.000 00	0.100 02	0.000 00
31	0.230 04	0.110 04	0.100 02	0.000 00
32	0.230 04	0.150 04	0.100 02	0.000 00
33	0.230 04	0.200 04	0.100 02	0.000 00
34	0.230 04	0.210 04	0.100 02	0.000 00
35	0.230 04	0.240 04	0.100 02	0.000 00
36	0.230 04	0.250 04	0.100 02	0.000 00
37	0.230 04	0.270 04	0.100 02	0.000 00
38	0.230 04	0.300 04	0.100 02	0.000 00
39	0.230 04	0.320 04	0.100 02	0.000 00
40	0.230 04	0.350 04	0.100 02	0.000 00
41	0.230 04	0.370 04	0.100 02	0.000 00
42	0.230 04	0.400 04	0.100 02	0.000 00
43	0.230 04	0.450 04	0.100 02	0.000 00
44	0.230 04	0.450 04	0.100 02	0.000 00
45	0.230 04	0.570 04	0.100 02	0.000 00
46	0.350 04	0.000 00	0.100 02	0.000 00
47	0.350 04	0.110 04	0.100 02	0.000 00
48	0.350 04	0.150 04	0.100 02	0.000 00
49	0.350 04	0.200 04	0.100 02	0.000 00
50	0.350 04	0.210 04	0.100 02	0.000 00
51	0.350 04	0.240 04	0.100 02	0.000 00
52	0.350 04	0.250 04	0.100 02	0.000 00
53	0.350 04	0.270 04	0.100 02	0.000 00
54	0.350 04	0.300 04	0.100 02	0.000 00
55	0.350 04	0.320 04	0.100 02	0.000 00
56	0.350 04	0.350 04	0.100 02	0.000 00
57	0.350 04	0.370 04	0.100 02	0.000 00
58	0.350 04	0.400 04	0.100 02	0.000 00
59	0.350 04	0.450 04	0.100 02	0.000 00
60	0.460 04	0.000 00	0.100 02	0.000 00
61	0.460 04	0.110 04	0.100 02	0.000 00
62	0.460 04	0.150 04	0.100 02	0.000 00
63	0.460 04	0.200 04	0.100 02	0.000 00
64	0.460 04	0.210 04	0.100 02	0.000 00
65	0.460 04	0.240 04	0.100 02	0.000 00
66	0.460 04	0.250 04	0.100 02	0.000 00
67	0.460 04	0.270 04	0.100 02	0.000 00
68	0.460 04	0.300 04	0.100 02	0.000 00
69	0.460 04	0.320 04	0.100 02	0.000 00
70	0.460 04	0.350 04	0.100 02	0.000 00
71	0.460 04	0.370 04	0.100 02	0.000 00
72	0.460 04	0.400 04	0.100 02	0.000 00
73	0.460 04	0.450 04	0.100 02	0.000 00
74	0.460 04	0.450 04	0.100 02	0.000 00
75	0.460 04	0.570 04	0.100 02	0.000 00
76	0.580 04	0.000 00	0.100 02	0.000 00
77	0.580 04	0.110 04	0.100 02	0.000 00
78	0.580 04	0.150 04	0.100 02	0.000 00
79	0.580 04	0.200 04	0.100 02	0.000 00
80	0.580 04	0.210 04	0.100 02	0.000 00
81	0.580 04	0.240 04	0.100 02	0.000 00
82	0.580 04	0.250 04	0.100 02	0.000 00
83	0.580 04	0.270 04	0.100 02	0.000 00
84	0.580 04	0.300 04	0.100 02	0.000 00
85	0.580 04	0.320 04	0.100 02	0.000 00
86	0.580 04	0.350 04	0.100 02	0.000 00
87	0.580 04	0.370 04	0.100 02	0.000 00
88	0.580 04	0.400 04	0.100 02	0.000 00
89	0.580 04	0.450 04	0.100 02	0.000 00
90	0.580 04	0.450 04	0.100 02	0.000 00
91	0.580 04	0.570 04	0.100 02	0.000 00
92	0.690 04	0.000 00	0.100 02	0.000 00
93	0.690 04	0.110 04	0.100 02	0.000 00
94	0.690 04	0.150 04	0.100 02	0.000 00
95	0.690 04	0.200 04	0.100 02	0.000 00
96	0.690 04	0.210 04	0.100 02	0.000 00
97	0.690 04	0.240 04	0.100 02	0.000 00
98	0.690 04	0.250 04	0.100 02	0.000 00
99	0.690 04	0.270 04	0.100 02	0.000 00
100	0.690 04	0.300 04	0.100 02	0.000 00
101	0.690 04	0.320 04	0.100 02	0.000 00
102	0.690 04	0.350 04	0.100 02	0.000 00
103	0.690 04	0.370 04	0.100 02	0.000 00
104	0.690 04	0.400 04	0.100 02	0.000 00
105	0.690 04	0.450 04	0.100 02	0.000 00
106	0.810 04	0.000 00	0.100 02	0.000 00
107	0.810 04	0.110 04	0.100 02	0.000 00

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ELEM5	NODE-ELEMENT RELATIONSHIP							
	N1	N2	N3	N4	N5	N6	N7	N8
1	1	3	16	17	181	182	187	186
2	2	4	17	18	182	183	188	187
3	3	5	18	19	182	184	188	188
4	4	6	19	20	184	185	200	189
5	5	7	20	21	185	186	200	200
6	6	8	21	22	186	187	202	201
7	7	9	22	23	187	188	203	202
8	8	10	23	24	188	189	204	203
9	9	11	24	25	189	190	205	204
10	10	12	25	26	190	191	206	205
11	11	13	26	27	191	192	207	206
12	12	14	27	28	192	193	208	207
13	13	15	28	29	193	194	209	208
14	14	16	29	30	194	195	210	209
15	15	17	30	31	195	196	211	210
16	16	18	31	32	196	197	212	211
17	17	19	32	33	197	198	213	212
18	18	20	33	34	198	199	214	213
19	19	21	34	35	199	200	215	214
20	20	22	35	36	200	201	216	215
21	21	23	36	37	201	202	217	216
22	22	24	37	38	202	203	218	217
23	23	25	38	39	203	204	219	218
24	24	26	39	40	204	205	220	219
25	25	27	40	41	205	206	221	220
26	26	28	41	42	206	207	222	221
27	27	29	42	43	207	208	223	222
28	28	30	43	44	208	209	224	223
29	29	31	44	45	209	210	225	224
30	30	32	45	46	210	211	226	225
31	31	33	46	47	211	212	227	226
32	32	34	47	48	212	213	228	227
33	33	35	48	49	213	214	229	228
34	34	36	49	50	214	215	230	229
35	35	37	50	51	215	216	231	230
36	36	38	51	52	216	217	232	231
37	37	39	52	53	217	218	233	232
38	38	40	53	54	218	219	234	233
39	39	41	54	55	219	220	235	234
40	40	42	55	56	220	221	236	235
41	41	43	56	57	221	222	237	236
42	42	44	57	58	222	223	238	237
43	43	45	58	59	223	224	239	238
44	44	46	59	60	224	225	240	239
45	45	47	60	61	225	226	241	240
46	46	48	61	62	226	227	242	241
47	47	49	62	63	227	228	243	242
48	48	50	63	64	228	229	244	243
49	49	50	64	64	229	230	245	244

47	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171	172	173	174	175	176	177	178	179	180	181	182	183	184	185	186	187	188	189	190	191	192	193	194	195	196	197	198	199	200	201	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218	219	220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400
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107 114 115 130 129 294 295 310 309
 108 116 117 131 130 295 296 311 310
 109 118 119 132 131 296 297 312 311
 110 118 119 133 132 297 298 313 312
 111 118 119 134 133 298 299 314 313
 112 119 120 135 134 299 300 315 314
 113 121 122 137 136 301 302 317 316
 114 122 123 138 137 302 303 318 317
 115 123 124 139 138 303 304 319 318
 116 124 125 140 139 304 305 320 319
 117 125 126 141 140 305 306 321 320
 118 126 127 142 141 306 307 322 321
 119 127 128 143 142 307 308 323 322
 120 128 129 144 143 308 309 324 323
 121 129 130 145 144 309 310 325 324
 122 130 131 146 145 310 311 326 325
 123 131 132 147 146 311 312 327 326
 124 132 133 148 147 312 313 328 327
 125 133 134 148 148 313 314 329 328
 126 134 135 149 149 314 315 330 329
 127 136 137 150 150 316 317 331 331
 128 137 138 151 151 317 318 332 332
 129 138 139 152 152 318 319 333 333
 130 139 140 153 153 319 320 334 334
 131 140 141 154 154 320 321 335 335
 132 141 142 155 155 321 322 336 336
 133 142 143 156 156 322 323 337 337
 134 143 144 157 157 323 324 338 338
 135 144 145 158 158 324 325 339 339
 136 145 146 159 159 325 326 340 340
 137 146 147 160 160 326 327 341 341
 138 147 148 161 161 327 328 342 342
 139 148 149 162 162 328 329 343 343
 140 149 150 163 163 329 330 344 344
 141 151 152 164 164 331 332 345 346
 142 152 153 165 165 332 333 346 347
 143 153 154 166 166 333 334 347 348
 144 154 155 167 167 334 335 348 349
 145 155 156 168 168 335 336 349 350
 146 156 157 169 169 336 337 350 351
 147 157 158 170 170 337 338 351 352
 148 158 159 171 171 338 339 352 353
 149 159 160 172 172 339 340 353 354
 150 160 161 173 173 340 341 354 355
 151 161 162 174 174 341 342 355 356
 152 162 163 175 175 342 343 356 357
 153 163 164 176 176 343 344 357 358
 154 164 165 177 177 344 345 358 359

FIXED BOUNDARY CONDITIONS

NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID	NODE	ID
1	0	3	0	4	0	5	0	6	0	7	0
6	0	8	0	9	0	10	0	11	0	12	0
11	0	13	0	14	0	15	0	16	0	17	0
16	0	21	0	25	0	28	0	31	0	30	0
60	0	31	0	45	0	46	0	61	0	60	0
91	0	72	0	76	0	90	0	91	0	105	0
135	0	106	0	120	0	121	0	135	0	136	0
166	0	150	0	151	0	165	0	166	0	167	0
171	0	168	0	169	0	170	0	171	0	172	0
176	0	172	0	174	0	175	0	176	0	177	0
181	0	178	0	179	0	180	0	181	0	182	0
186	0	182	0	184	0	185	0	186	0	187	0
191	0	188	0	189	0	190	0	191	0	192	0
196	0	193	0	194	0	195	0	196	0	210	0
240	0	211	0	225	0	226	0	240	0	241	0
271	0	215	0	255	0	270	0	271	0	285	0
315	0	286	0	300	0	301	0	315	0	316	0
346	0	320	0	331	0	345	0	346	0	347	0
351	0	328	0	349	0	350	0	351	0	352	0
356	0	353	0	354	0	355	0	356	0	357	0
		358	0	359	0	360	0				

MAXIMUM BANDWIDTH = 230 ON ROW NO. 13

OUTPUT FOR THREE-DIMENSIONAL
GROUNDWATER DISP BY FINITE ELEMENTS METHOD

INITIAL CONC DISTRIBUTION AT TIME = 0.000 DAYS											
NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000 00	2	0.0000 00	3	0.0000 00	4	0.0000 00	5	0.0000 00	6	0.0000 00
6	0.0000 00	7	0.0000 00	8	0.0000 00	9	0.0000 00	10	0.0000 00	11	0.0000 00
11	0.0000 00	12	0.0000 00	13	0.0000 00	14	0.0000 00	15	0.0000 00	16	0.0000 00
16	0.0000 00	17	0.0000 00	18	0.0000 00	19	0.0000 00	20	0.0000 00	21	0.0000 00
21	0.0000 00	22	0.0000 00	23	0.0000 00	24	0.0000 00	25	0.0000 00	26	0.0000 00
26	0.0000 00	27	0.0000 00	28	0.0000 00	29	0.0000 00	30	0.0000 00	31	0.0000 00
31	0.0000 00	32	0.0000 00	33	0.0000 00	34	0.0000 00	35	0.0000 00	36	0.0000 00
36	0.0000 00	37	0.0000 00	38	0.0000 00	39	0.0000 00	40	0.0000 00	41	0.0000 00
41	0.0000 00	42	0.0000 00	43	0.0000 00	44	0.0000 00	45	0.0000 00	46	0.0000 00
46	0.0000 00	47	0.0000 00	48	0.0000 00	49	0.0000 00	50	0.0000 00	51	0.0000 00
51	0.0000 00	52	0.0000 00	53	0.0000 00	54	0.0000 00	55	0.0000 00	56	0.0000 00
56	0.0000 00	57	0.0000 00	58	0.0000 00	59	0.0000 00	60	0.0000 00	61	0.0000 00
61	0.0000 00	62	0.0000 00	63	0.0000 00	64	0.0000 00	65	0.0000 00	66	0.0000 00
66	0.0000 00	67	0.0000 00	68	0.0000 00	69	0.0000 00	70	0.0000 00	71	0.0000 00
71	0.0000 00	72	0.0000 00	73	0.0000 00	74	0.0000 00	75	0.0000 00	76	0.0000 00
76	0.0000 00	77	0.0000 00	78	0.0000 00	79	0.0000 00	80	0.0000 00	81	0.0000 00
81	0.0000 00	82	0.0000 00	83	0.0000 00	84	0.0000 00	85	0.0000 00	86	0.0000 00
86	0.0000 00	87	0.0000 00	88	0.0000 00	89	0.0000 00	90	0.0000 00	91	0.0000 00
91	0.0000 00	92	0.0000 00	93	0.0000 00	94	0.0000 00	95	0.0000 00	96	0.0000 00
96	0.0000 00	97	0.0000 00	98	0.0000 00	99	0.0000 00	100	0.0000 00	101	0.0000 00
101	0.0000 00	102	0.0000 00	103	0.0000 00	104	0.0000 00	105	0.0000 00	106	0.0000 00
106	0.0000 00	107	0.0000 00	108	0.0000 00	109	0.0000 00	110	0.0000 00	111	0.0000 00
111	0.0000 00	112	0.0000 00	113	0.0000 00	114	0.0000 00	115	0.0000 00	116	0.0000 00
116	0.0000 00	117	0.0000 00	118	0.0000 00	119	0.0000 00	120	0.0000 00	121	0.0000 00
121	0.0000 00	122	0.0000 00	123	0.0000 00	124	0.0000 00	125	0.0000 00	126	0.0000 00
126	0.0000 00	127	0.0000 00	128	0.0000 00	129	0.0000 00	130	0.0000 00	131	0.0000 00
131	0.0000 00	132	0.0000 00	133	0.0000 00	134	0.0000 00	135	0.0000 00	136	0.0000 00
136	0.0000 00	137	0.0000 00	138	0.0000 00	139	0.0000 00	140	0.0000 00	141	0.0000 00
141	0.0000 00	142	0.0000 00	143	0.0000 00	144	0.0000 00	145	0.0000 00	146	0.0000 00
146	0.0000 00	147	0.0000 00	148	0.0000 00	149	0.0000 00	150	0.0000 00	151	0.0000 00
151	0.0000 00	152	0.0000 00	153	0.0000 00	154	0.0000 00	155	0.0000 00	156	0.0000 00
156	0.0000 00	157	0.0000 00	158	0.0000 00	159	0.0000 00	160	0.0000 00	161	0.0000 00
161	0.0000 00	162	0.0000 00	163	0.0000 00	164	0.0000 00	165	0.0000 00	166	0.0000 00
166	0.0000 00	167	0.0000 00	168	0.0000 00	169	0.0000 00	170	0.0000 00	171	0.0000 00
171	0.0000 00	172	0.0000 00	173	0.0000 00	174	0.0000 00	175	0.0000 00	176	0.0000 00
176	0.0000 00	177	0.0000 00	178	0.0000 00	179	0.0000 00	180	0.0000 00	181	0.0000 00
181	0.0000 00	182	0.0000 00	183	0.0000 00	184	0.0000 00	185	0.0000 00	186	0.0000 00
186	0.0000 00	187	0.0000 00	188	0.0000 00	189	0.0000 00	190	0.0000 00	191	0.0000 00
191	0.0000 00	192	0.0000 00	193	0.0000 00	194	0.0000 00	195	0.0000 00	196	0.0000 00
196	0.0000 00	197	0.0000 00	198	0.0000 00	199	0.0000 00	200	0.0000 00	201	0.0000 00
201	0.0000 00	202	0.0000 00	203	0.0000 00	204	0.0000 00	205	0.0000 00	206	0.0000 00
206	0.0000 00	207	0.0000 00	208	0.0000 00	209	0.0000 00	210	0.0000 00	211	0.0000 00
211	0.0000 00	212	0.0000 00	213	0.0000 00	214	0.0000 00	215	0.0000 00	216	0.0000 00

216	0.0000	00
271	0.0000	00
226	0.0000	00
231	0.0000	00
236	0.0000	00
241	0.0000	00
246	0.0000	00
251	0.0000	00
256	0.0000	00
261	0.0000	00
266	0.0000	00
271	0.0000	00
276	0.0000	00
281	0.0000	00
286	0.0000	00
291	0.0000	00
296	0.0000	00
301	0.0000	00
306	0.0000	00
311	0.0000	00
316	0.0000	00
321	0.0000	00
326	0.0000	00
331	0.0000	00
336	0.0000	00
341	0.0000	00
346	0.0000	00
351	0.0000	00
356	0.0000	00
217	0.0000	00
222	0.0000	00
227	0.0000	00
232	0.0000	00
237	0.0000	00
242	0.0000	00
247	0.0000	00
252	0.0000	00
257	0.0000	00
262	0.0000	00
267	0.0000	00
272	0.0000	00
277	0.0000	00
282	0.0000	00
287	0.0000	00
292	0.0000	00
297	0.0000	00
302	0.0000	00
307	0.0000	00
312	0.0000	00
317	0.0000	00
322	0.0000	00
327	0.0000	00
332	0.0000	00
337	0.0000	00
342	0.0000	00
347	0.0000	00
352	0.0000	00
357	0.0000	00
218	0.0000	00
223	0.0000	00
228	0.0000	00
233	0.0000	00
238	0.0000	00
243	0.0000	00
248	0.0000	00
253	0.0000	00
258	0.0000	00
263	0.0000	00
268	0.0000	00
273	0.0000	00
278	0.0000	00
283	0.0000	00
288	0.0000	00
293	0.0000	00
298	0.0000	00
303	0.0000	00
308	0.0000	00
313	0.0000	00
318	0.0000	00
323	0.0000	00
328	0.0000	00
333	0.0000	00
338	0.0000	00
343	0.0000	00
348	0.0000	00
353	0.0000	00
358	0.0000	00
219	0.0000	00
224	0.0000	00
229	0.0000	00
234	0.0000	00
239	0.0000	00
244	0.0000	00
249	0.0000	00
254	0.0000	00
259	0.0000	00
264	0.0000	00
269	0.0000	00
274	0.0000	00
279	0.0000	00
284	0.0000	00
289	0.0000	00
294	0.0000	00
299	0.0000	00
304	0.0000	00
309	0.0000	00
314	0.0000	00
319	0.0000	00
324	0.0000	00
329	0.0000	00
334	0.0000	00
339	0.0000	00
344	0.0000	00
349	0.0000	00
354	0.0000	00
359	0.0000	00
220	0.0000	00
225	0.0000	00
230	0.0000	00
235	0.0000	00
240	0.0000	00
245	0.0000	00
250	0.0000	00
255	0.0000	00
260	0.0000	00
265	0.0000	00
270	0.0000	00
275	0.0000	00
280	0.0000	00
285	0.0000	00
290	0.0000	00
295	0.0000	00
300	0.0000	00
305	0.0000	00
310	0.0000	00
315	0.0000	00
320	0.0000	00
325	0.0000	00
330	0.0000	00
335	0.0000	00
340	0.0000	00
345	0.0000	00
350	0.0000	00
355	0.0000	00
360	0.0000	00

CONCENTRATION DISTRIBUTION AT TIME = 216 000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000 00	3	0.2000 00	6	0.0000 03	9	0.0000 00	12	0.4270 02	15	0.1100 03	18	0.9020 02	21	0.0000 00
6	0.1220 03	7	0.0000 00	8	0.1880 03	13	0.5010 02	14	0.0000 00	16	0.1600 03	17	0.9020 02	20	0.0000 00
11	0.7220 02	12	0.5010 02	13	0.0000 00	14	0.0000 00	15	0.0000 00	18	0.3770 02	19	0.9020 02	22	0.0000 00
16	0.0000 00	17	0.0000 00	18	0.0000 00	19	0.0000 00	20	0.1710 03	23	0.1710 03	24	0.1360 03	27	0.0000 00
21	0.1250 03	22	0.1490 03	23	0.5020 02	24	0.1110 03	25	0.0000 00	28	0.0000 00	29	0.0000 00	32	0.0000 00
26	0.8750 02	27	0.5020 02	28	0.0000 00	29	0.0000 00	30	0.0000 00	33	0.0000 00	34	0.0000 00	37	0.0000 00
31	0.0000 00	32	0.0000 00	33	0.0000 00	34	0.0000 00	35	0.0000 00	38	0.2070 02	39	0.7520 02	42	0.1700 03
36	0.1320 03	37	0.1500 03	38	0.1700 03	39	0.0000 00	40	0.2100 03	43	0.0000 00	44	0.0000 00	47	0.0000 00
41	0.1250 03	42	0.6870 02	43	0.0000 00	44	0.0000 00	45	0.0000 00	48	0.0000 00	49	0.0000 00	52	0.0000 00
46	0.0000 00	47	0.0000 00	48	0.0000 00	49	0.0000 00	50	0.0000 00	53	0.2200 03	54	0.9020 02	57	0.0000 00
51	0.1000 03	52	0.1500 03	53	0.1700 03	54	0.0000 00	55	0.0000 00	58	0.0000 00	59	0.0000 00	62	0.0000 00
56	0.1730 03	57	0.8850 02	58	0.8020 02	59	0.0000 00	60	0.0000 00	63	0.0000 00	64	0.0000 00	67	0.0000 00
61	0.0000 00	62	0.0000 00	63	0.0000 00	64	0.0000 00	65	0.0000 00	68	0.0000 00	69	0.0000 00	72	0.0000 00
66	0.7220 02	67	0.1130 03	68	0.1800 03	69	0.8240 02	70	0.1800 03	73	0.0000 00	74	0.0000 00	77	0.0000 00
71	0.1580 03	72	0.1000 03	73	0.0000 00	74	0.0000 00	75	0.0000 00	78	0.0000 00	79	0.0000 00	81	0.0000 00
76	0.0000 00	77	0.0000 00	78	0.0000 00	79	0.0000 00	80	0.0000 00	83	0.1250 03	84	0.4000 02	87	0.0000 00
81	0.6090 02	82	0.7810 02	83	0.1000 03	84	0.0000 00	85	0.0000 00	88	0.0000 00	89	0.0000 00	91	0.0000 00
86	0.9060 02	87	0.6520 02	88	0.0000 00	89	0.0000 00	90	0.0000 00	93	0.0000 00	94	0.0000 00	96	0.0000 00
91	0.0000 00	92	0.0000 00	93	0.0000 00	94	0.0000 00	95	0.0000 00	98	0.1000 03	99	0.8460 02	101	0.5000 02
96	0.6250 02	97	0.8130 02	98	0.0000 00	99	0.0000 00	100	0.0000 00	103	0.0000 00	104	0.0000 00	106	0.6540 02
101	0.5000 02	102	0.0000 00	103	0.0000 00	104	0.0000 00	105	0.0000 00	108	0.0000 00	109	0.4120 02	110	0.0000 00
106	0.0000 00	107	0.0000 00	108	0.0000 00	109	0.0000 00	110	0.0000 00	113	0.7500 02	114	0.6230 02	116	0.5680 02
111	0.6140 02	112	0.6220 02	113	0.0000 00	114	0.0000 00	115	0.0000 00	118	0.0000 00	119	0.0000 00	121	0.0000 00
116	0.0000 00	117	0.0000 00	118	0.0000 00	119	0.0000 00	120	0.0000 00	123	0.3740 02	124	0.5630 02	126	0.6880 02
121	0.0000 00	122	0.0000 00	123	0.0000 00	124	0.0000 00	125	0.0000 00	128	0.9870 02	129	0.0000 00	131	0.0000 00
126	0.7500 02	127	0.6880 02	128	0.0000 00	129	0.0000 00	130	0.0000 00	133	0.0000 00	134	0.0000 00	136	0.0000 00
131	0.0000 00	132	0.0000 00	133	0.0000 00	134	0.0000 00	135	0.0000 00	138	0.8530 02	139	0.8500 02	141	0.0000 00
136	0.0000 00	137	0.0000 00	138	0.0000 00	139	0.0000 00	140	0.0000 00	143	0.0000 00	144	0.0000 00	146	0.5420 02
141	0.5420 02	142	0.4200 02	143	0.0000 00	144	0.0000 00	145	0.0000 00	148	0.0000 00	149	0.0000 00	151	0.0000 00
146	0.0000 00	147	0.0000 00	148	0.0000 00	149	0.0000 00	150	0.0000 00	153	0.0000 00	154	0.5010 02	156	0.0000 00
151	0.0000 00	152	0.0000 00	153	0.0000 00	154	0.0000 00	155	0.0000 00	158	0.0000 00	159	0.0000 00	161	0.0000 00
156	0.0000 00	157	0.0000 00	158	0.0000 00	159	0.0000 00	160	0.0000 00	163	0.0000 00	164	0.0000 00	166	0.0000 00
161	0.0000 00	162	0.0000 00	163	0.0000 00	164	0.0000 00	165	0.0000 00	168	0.0000 00	169	0.0000 00	171	0.0000 00
166	0.0000 00	167	0.0000 00	168	0.0000 00	169	0.0000 00	170	0.0000 00	173	0.0000 00	174	0.0000 00	176	0.0000 00
171	0.0000 00	172	0.0000 00	173	0.0000 00	174	0.0000 00	175	0.0000 00	178	0.0000 00	179	0.0000 00	181	0.0000 00
176	0.0000 00	177	0.0000 00	178	0.0000 00	179	0.0000 00	180	0.0000 00	183	0.0000 00	184	0.0000 00	186	0.0000 00
181	0.0000 00	182	0.0000 00	183	0.0000 00	184	0.0000 00	185	0.0000 00	188	0.1880 03	189	0.8020 02	191	0.1100 03
186	0.1220 03	187	0.2000 03	188	0.0000 00	189	0.0000 00	190	0.1600 03	193	0.0000 00	194	0.8020 02	196	0.0000 00
191	0.1100 03	192	0.5010 02	193	0.0000 00	194	0.0000 00	195	0.0000 00	198	0.0000 00	199	0.3770 02	201	0.0000 00
196	0.0000 00	197	0.0000 00	198	0.0000 00	199	0.0000 00	200	0.0000 00	203	0.1710 03	204	0.0000 00	206	0.1260 03
201	0.0000 00	202	0.1490 03	203	0.1710 03	204	0.0000 00	205	0.0000 00	208	0.0000 00	209	0.0000 00	211	0.0000 00
206	0.1260 03	207	0.5020 02	208	0.0000 00	209	0.0000 00	210	0.0000 00	213	0.2070 02	214	0.0000 00	216	0.1750 02
211	0.0000 00	212	0.8750 02	213	0.0000 00	214	0.0000 00	215	0.0000 00	218	0.3100 03	219	0.0000 00	221	0.1700 03
216	0.1750 02	217	0.1500 03	218	0.0000 00	219	0.0000 00	220	0.0000 00	223	0.0000 00	224	0.0000 00	226	0.0000 00
221	0.1500 03	222	0.6670 02	223	0.0000 00	224	0.0000 00	225	0.0000 00	228	0.0000 00	229	0.0000 00	231	0.0000 00
226	0.0000 00	227	0.0000 00	228	0.0000 00	229	0.0000 00	230	0.0000 00	233	0.2200 03	234	0.0000 00	236	0.0000 00
231	0.0000 00	232	0.1000 03	233	0.1700 03	234	0.0000 00	235	0.0000 00	238	0.0000 00	239	0.0000 00	241	0.0000 00
236	0.0000 00	237	0.1730 03	238	0.8020 02	239	0.0000 00	240	0.0000 00	243	0.0000 00	244	0.0000 00	246	0.0000 00
241	0.0000 00	242	0.0000 00	243	0.0000 00	244	0.0000 00	245	0.0000 00	248	0.0000 00	249	0.0000 00	251	0.0000 00
246	0.0000 00	247	0.1130 03	248	0.0000 00	249	0.0000 00	250	0.1800 03	253	0.0000 00	254	0.0000 00	256	0.0000 00
251	0.7220 02	252	0.1000 03	253	0.1500 03	254	0.0000 00	255	0.0000 00	258	0.0000 00	259	0.0000 00	261	0.0000 00
256	0.0000 00	257	0.0000 00	258	0.0000 00	259	0.0000 00	260	0.0000 00	263	0.1250 03	264	0.0000 00	266	0.0000 00
261	0.6090 02	262	0.7810 02	263	0.1000 03	264	0.0000 00	265	0.0000 00	268	0.0000 00	269	0.0000 00	270	0.0000 00
266	0.9060 02	267	0.6520 02	268	0.0000 00	269	0.0000 00	270	0.0000 00						

271	0.0000 00	273	0.0000 00	274	0.0000 00	275	0.0000 00	0.0000 02
276	0.6250 02	276	0.1000 03	276	0.1000 03	280	0.8460 02	0.8540 02
281	0.5000 02	283	0.0000 00	284	0.0000 00	285	0.0000 00	0.0000 00
286	0.0000 00	288	0.0000 00	288	0.0000 00	290	0.4120 02	0.3680 02
291	0.6100 02	292	0.7500 02	294	0.7500 02	295	0.6230 02	0.5010 02
296	0.0000 00	298	0.0000 00	298	0.0000 00	300	0.0000 00	0.0000 00
301	0.0000 00	303	0.0000 00	304	0.3740 02	305	0.5630 02	0.8880 02
306	0.7500 02	308	0.8470 02	308	0.8470 02	310	0.0000 00	0.0000 00
311	0.0000 00	312	0.0000 00	314	0.0000 00	315	0.0000 00	0.0000 00
316	0.0000 00	318	0.0000 00	318	0.6630 02	320	0.8500 02	0.8250 02
321	0.5420 02	322	0.4200 02	324	0.0000 00	325	0.0000 00	0.0000 00
326	0.0000 00	328	0.0000 00	328	0.0000 00	330	0.0000 00	0.0000 00
331	0.0000 00	332	0.0000 00	334	0.0000 00	335	0.0000 00	0.0000 00
336	0.0000 00	338	0.0000 00	338	0.0000 00	340	0.5010 02	0.0000 00
341	0.0000 00	342	0.0000 00	344	0.0000 00	345	0.0000 00	0.0000 00
346	0.0000 00	348	0.0000 00	348	0.0000 00	350	0.0000 00	0.0000 00
351	0.0000 00	352	0.0000 00	354	0.0000 00	355	0.0000 00	0.0000 00
356	0.0000 00	358	0.0000 00	358	0.0000 00	360	0.0000 00	0.0000 00

CONCENTRATION DISTRIBUTION AT TIME = 396.000 DAYS

NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS	NODES	CONCS
1	0.0000 00	3	0.0000 00	5	0.0000 00	7	0.0000 00	9	0.0000 00
6	0 1000 03	7	0 1600 03	8	0 1500 03	9	0 9640 02	10	0 7500 02
11	0 5630 02	12	0 3830 02	13	0 0000 00	14	0 0000 00	15	0 0000 00
16	0 0000 00	17	0 0000 00	18	0 3010 02	19	0 5000 02	20	0 7480 02
21	0 1230 03	22	0 1500 03	23	0 1630 03	24	0 1500 03	25	0 1100 03
26	0 8330 02	27	0 5000 02	28	0 0000 00	29	0 0000 00	30	0 0000 00
31	0 0000 00	32	0 0000 00	33	0 0000 00	34	0 0000 00	35	0 7220 02
36	0 1470 03	37	0 1560 03	38	0 1720 03	39	0 1830 03	40	0 1410 03
41	0 1050 03	42	0 7510 02	43	0 2010 02	44	0 0000 00	45	0 0000 00
46	0 0000 00	47	0 0000 00	48	0 0000 00	49	0 4000 02	50	0 6250 02
51	0 9850 02	52	0 1500 03	53	0 1620 03	54	0 1740 03	55	0 1800 03
56	0 1640 03	57	0 1000 03	58	0 6630 02	59	0 0000 00	60	0 0000 00
61	0 0000 00	62	0 0000 00	63	0 0000 00	64	0 3010 02	65	0 5000 02
66	0 1000 03	67	0 1200 03	68	0 1400 03	69	0 1700 03	70	0 2010 03
71	0 1720 03	72	0 1270 03	73	0 7530 02	74	0 0000 00	75	0 0000 00
76	0 0000 00	77	0 0000 00	78	0 0000 00	79	0 0000 00	80	0 5000 02
81	0 6880 02	82	0 8130 02	83	0 8380 02	84	0 1130 03	85	0 1500 03
86	0 1200 03	87	0 8750 02	88	0 5940 02	89	0 0000 00	90	0 0000 00
91	0 0000 00	92	0 0000 00	93	0 0000 00	94	0 0000 00	95	0 5000 02
96	0 5630 02	97	0 6010 02	98	0 6320 02	99	0 6620 02	100	0 7210 02
101	0 6430 02	102	0 5820 02	103	0 4000 02	104	0 0000 00	105	0 0000 00
106	0 0000 00	107	0 0000 00	108	0 0000 00	109	0 2010 02	110	0 5010 02
111	0 5720 02	112	0 6190 02	113	0 6660 02	114	0 7380 02	115	0 6430 02
116	0 5480 02	117	0 2130 02	118	0 0000 00	119	0 0000 00	120	0 0000 00
121	0 0000 00	122	0 0000 00	123	0 0000 00	124	0 5010 02	125	0 6630 02
126	0 7000 02	127	0 7030 02	128	0 6020 02	129	0 5000 02	130	0 0000 00
131	0 0000 00	132	0 0000 00	133	0 0000 00	134	0 0000 00	135	0 0000 00
136	0 0000 00	137	0 0000 00	138	0 3000 02	139	0 7510 02	140	0 8750 02
141	0 4360 02	142	0 2020 02	143	0 0000 00	144	0 0000 00	145	0 0000 00
146	0 0000 00	147	0 0000 00	148	0 0000 00	149	0 0000 00	150	0 0000 00
151	0 0000 00	152	0 0000 00	153	0 5000 02	154	0 0000 00	155	0 0000 00
156	0 0000 00	157	0 0000 00	158	0 0000 00	159	0 0000 00	160	0 0000 00
161	0 0000 00	162	0 0000 00	163	0 0000 00	164	0 0000 00	165	0 0000 00
166	0 0000 00	167	0 0000 00	168	0 0000 00	169	0 0000 00	170	0 0000 00
171	0 0000 00	172	0 0000 00	173	0 0000 00	174	0 0000 00	175	0 0000 00
176	0 0000 00	177	0 0000 00	178	0 0000 00	179	0 0000 00	180	0 0000 00
181	0 0000 00	182	0 0000 00	183	0 0000 00	184	0 5000 02	185	0 7500 02
186	0 1000 03	187	0 1600 03	188	0 1500 03	189	0 9640 02	190	0 7520 02
191	0 5630 02	192	0 3830 02	193	0 0000 00	194	0 0000 00	195	0 0000 00
196	0 0000 00	197	0 0000 00	198	0 3010 02	199	0 5000 02	200	0 7480 02
201	0 1230 03	202	0 1500 03	203	0 1630 03	204	0 1500 03	205	0 1100 03
206	0 8330 02	207	0 5000 02	208	0 0000 00	209	0 0000 00	210	0 0000 00
211	0 0000 00	212	0 0000 00	213	0 0000 00	214	0 0000 00	215	0 7220 02
216	0 1470 03	217	0 1560 03	218	0 1720 03	219	0 1830 03	220	0 1410 03
221	0 1050 03	222	0 7510 02	223	0 2010 02	224	0 0000 00	225	0 0000 00
226	0 0000 00	227	0 0000 00	228	0 0000 00	229	0 4000 02	230	0 6250 02
231	0 9850 02	232	0 1500 03	233	0 1620 03	234	0 1740 03	235	0 1800 03
236	0 1640 03	237	0 1000 03	238	0 6630 02	239	0 0000 00	240	0 0000 00
241	0 0000 00	242	0 0000 00	243	0 0000 00	244	0 3010 02	245	0 5000 02
246	0 1000 03	247	0 1200 03	248	0 1400 03	249	0 1700 03	250	0 2010 03
251	0 1720 03	252	0 1270 03	253	0 7530 02	254	0 0000 00	255	0 0000 00
256	0 0000 00	257	0 0000 00	258	0 0000 00	259	0 0000 00	260	0 5000 02
261	0 6880 02	262	0 8130 02	263	0 8380 02	264	0 1130 03	265	0 1500 03
266	0 1200 03	267	0 8750 02	268	0 5940 02	269	0 0000 00	270	0 0000 00

271	0 0000 00	274	0 0000 00	275	0 5000 02
276	0 5630 02	278	0 6320 02	280	0 7210 02
281	0 6430 02	284	0 4000 02	285	0 0000 00
286	0 0000 00	288	0 0000 00	290	0 5010 02
291	0 5720 02	292	0 6180 02	295	0 6430 02
296	0 5480 02	298	0 3130 02	300	0 0000 00
301	0 0000 00	302	0 0000 00	305	0 6630 02
306	0 7000 02	308	0 6070 02	310	0 0000 00
311	0 0000 00	312	0 0000 00	315	0 0000 00
316	0 0000 00	318	0 3000 02	320	0 5750 02
321	0 4360 02	322	0 2020 02	325	0 0000 00
326	0 0000 00	328	0 0000 00	330	0 0000 00
331	0 0000 00	332	0 0000 00	335	0 0000 00
336	0 0000 00	338	0 8000 02	340	0 0000 00
341	0 0000 00	342	0 0000 00	345	0 0000 00
346	0 0000 00	348	0 0000 00	350	0 0000 00
351	0 0000 00	352	0 0000 00	355	0 0000 00
356	0 0000 00	357	0 0000 00	360	0 0000 00
		372	0 0000 00		
		378	0 6010 02		
		382	0 5820 02		
		388	0 0000 00		
		392	0 6180 02		
		398	0 3130 02		
		402	0 0000 00		
		408	0 7030 02		
		412	0 0000 00		
		418	0 0000 00		
		422	0 2020 02		
		428	0 0000 00		
		432	0 0000 00		
		438	0 0000 00		
		442	0 0000 00		
		448	0 0000 00		
		452	0 0000 00		
		458	0 0000 00		
		472	0 0000 00		
		478	0 6320 02		
		482	0 4000 02		
		488	0 0000 00		
		492	0 6560 02		
		498	0 0000 00		
		502	0 0000 00		
		508	0 6070 02		
		512	0 0000 00		
		518	0 3000 02		
		522	0 0000 00		
		528	0 0000 00		
		532	0 8000 02		
		538	0 0000 00		
		542	0 0000 00		
		548	0 0000 00		
		552	0 0000 00		
		558	0 0000 00		

APPENDIX G
ERROR ANALYSIS AT DIFFERENT NODES
AND TIMES

TABLE IV
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 240 HRS., DEPTH: 1 M

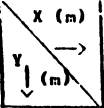
	0	10	20	30	40	50	60
5							
Analytical Solution	0.120×10^4	0.126×10^3	0.193×10^0	0.641×10^{-5}	0.477×10^{-11}	0.803×10^{-19}	0.305×10^{-28}
Model Solution	0.105×10^4	0.111×10^3	0.174×10^0	0.587×10^{-5}	0.441×10^{-11}	0.775×10^{-19}	0.297×10^{-28}
% Error	12.50	11.9	9.84	8.424	7.547	3.487	2.62
10							
Analytical Solution	0.584×10^6	0.534×10^4	0.501×10^1	0.143×10^{-3}	0.945×10^{-10}	0.161×10^{-17}	0.595×10^{-27}
Model Solution		0.469×10^4	0.441×10^1	0.131×10^{-3}	0.945×10^{-10}	0.156×10^{-17}	0.580×10^{-27}
% Error	12.32	12.17	11.97	8.39	4.92	3.11	2.52
20							
Analytical Solution	0.188×10^1	0.380×10^{-1}	0.629×10^{-4}	0.227×10^{-8}	0.160×10^{-14}	0.251×10^{-22}	0.914×10^{-32}
Model Solution	0.170×10^1	0.347×10^{-1}	0.586×10^{-4}	0.259×10^{-8}	0.154×10^{-14}	0.242×10^{-22}	0.893×10^{-32}
% Error	9.57	8.68	6.84	6.50	3.75	3.59	2.30

TABLE V
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 240 HRS., DEPTH: 2 M

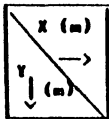
	0	10	20	30	40	50	60
5							
Analytical Solution	0.869×10^3	0.925×10^2	0.144×10^0	0.483×10^{-5}	0.360×10^{-11}	0.608×10^{-19}	0.232×10^{-28}
Model Solution	0.780×10^3	0.834×10^2	0.131×10^0	0.452×10^{-5}	0.346×10^{-11}	0.590×10^{-19}	0.226×10^{-28}
Z Error	10.24	9.84	9.03	6.42	3.90	2.96	2.59
10							
Analytical Solution	0.178×10^6	0.380×10^4	0.372×10^1	0.108×10^{-3}	0.751×10^{-10}	0.122×10^{-17}	0.452×10^{-27}
Model Solution	0.157×10^6	0.338×10^4	0.335×10^1	0.100×10^{-3}	0.715×10^{-10}	0.118×10^{-17}	0.452×10^{-27}
Z Error	11.8	11.05	9.95	7.41	4.79	3.28	2.88
20							
Analytical Solution	0.106×10^1	0.276×10^{-1}	0.472×10^{-4}	0.171×10^{-8}	0.121×10^{-14}	0.190×10^{-22}	0.693×10^{-32}
Model Solution	0.095×10^1	0.249×10^{-1}	0.431×10^{-4}	0.161×10^{-8}	0.116×10^{-14}	0.185×10^{-22}	0.674×10^{-32}
Z Error	10.38	9.78	8.69	5.85	4.13	2.63	2.74

TABLE VI
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 240 HRS., DEPTH: 4 M

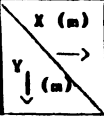
	0	10	20	30	40	50	60
5							
Analytical Solution	0.224×10^3	0.256×10^2	0.430×10^{-1}	0.149×10^{-5}	0.113×10^{-11}	0.194×10^{-19}	0.742×10^{-29}
Model Solution	0.203×10^3	0.232×10^2	0.392×10^{-1}	0.139×10^{-5}	0.109×10^{-11}	0.189×10^{-19}	0.722×10^{-29}
% Error	9.38	9.38	8.84	6.71	3.54	2.58	1.66
10							
Analytical Solution	0.132×10^5	0.907×10^3	0.108×10^1	0.330×10^{-4}	0.235×10^{-10}	0.387×10^{-18}	0.145×10^{-27}
Model Solution	0.119×10^5	0.818×10^3	0.098×10^1	0.308×10^{-4}	0.224×10^{-10}	0.376×10^{-18}	0.141×10^{-27}
% Error	9.85	9.81	9.26	6.67	4.68	2.84	2.76
20							
Analytical Solution	0.897×10^{-1}	0.738×10^{-2}	0.144×10^{-4}	0.528×10^{-9}	0.379×10^{-15}	0.604×10^{-23}	0.222×10^{-32}
Model Solution	0.803×10^{-1}	0.666×10^{-2}	0.132×10^{-4}	0.498×10^{-9}	0.365×10^{-15}	0.588×10^{-23}	0.216×10^{-32}
% Error	10.47	9.76	8.33	5.68	3.69	2.65	2.70

TABLE VII

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 480 HRS., DEPTH: 1 M

<div style="border: 1px solid black; padding: 2px; display: inline-block;"> x (m) \rightarrow y (m) \downarrow </div>	0	10	20	30	40	50	60
5							
Analytical Solution	0.715×10^3	0.316×10^3	0.148×10^2	0.888×10^{-1}	0.738×10^{-4}	0.875×10^{-8}	0.150×10^{-12}
Model Solution	0.712×10^3	0.288×10^3	0.137×10^2	0.830×10^{-1}	0.718×10^{-4}	0.853×10^{-8}	0.148×10^{-12}
Z Error	10.44	8.86	7.43	6.53	2.71	2.51	1.33
10							
Analytical Solution	0.195×10^6	0.484×10^5	0.890×10^3	0.308×10^1	0.202×10^{-2}	0.212×10^{-6}	0.338×10^{-11}
Model Solution	0.173×10^6	0.429×10^5	0.790×10^3	0.284×10^1	0.194×10^{-2}	0.207×10^{-6}	0.333×10^{-11}
Z Error	11.36	11.28	11.2	7.79	3.96	2.36	1.48
20							
Analytical Solution	0.896×10^0	0.255×10^0	0.609×10^{-2}	0.274×10^{-4}	0.236×10^{-7}	0.300×10^{-11}	0.526×10^{-16}
Model Solution	0.822×10^0	0.236×10^0	0.573×10^{-2}	0.259×10^{-4}	0.231×10^{-7}	0.294×10^{-11}	0.517×10^{-16}
Z Error	8.26	7.45	5.91	5.47	2.01	2.0	1.71

TABLE VIII
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 480 HRS., DEPTH: 2 M

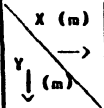
	0	10	20	30	40	50	60
5							
Analytical Solution	0.576×10^3	0.230×10^3	0.108×10^2	0.658×10^{-1}	0.551×10^{-4}	0.657×10^{-8}	0.113×10^{-12}
Model Solution	0.521×10^{-3}	0.209×10^3	0.099×10^2	0.618×10^{-1}	0.534×10^{-4}	0.644×10^{-8}	0.111×10^{-12}
Z Error	9.55	9.13	8.33	6.08	3.09	1.98	1.77
10							
Analytical Solution	0.795×10^5	0.229×10^5	0.569×10^3	0.222×10^1	0.149×10^{-2}	0.159×10^{-6}	0.254×10^{-11}
Model Solution	0.714×10^5	0.206×10^5	0.518×10^3	0.207×10^1	0.143×10^{-2}	0.156×10^{-6}	0.249×10^{-11}
Z Error	10.19	10.04	8.96	6.76	4.03	1.89	1.97
20							
Analytical Solution	0.525×10^0	0.155×10^0	0.416×10^{-2}	0.202×10^{-4}	0.177×10^{-7}	0.225×10^{-11}	0.396×10^{-16}
Model Solution	0.474×10^0	0.141×10^0	0.384×10^{-2}	0.192×10^{-4}	0.114×10^{-7}	0.221×10^{-11}	0.388×10^{-16}
Z Error	9.71	9.03	7.69	4.95	3.56	1.78	1.80

TABLE IX
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 480 HRS., DEPTH: 4 M

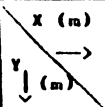
	0	10	20	30	40	50	60
5							
Analytical Solution	0.150×10^3	0.608×10^2	0.296×10^1	0.189×10^{-1}	0.163×10^{-4}	0.199×10^{-8}	0.347×10^{-13}
Model Solution	0.136×10^3	0.554×10^2	0.275×10^1	0.176×10^{-1}	0.158×10^{-4}	0.195×10^{-8}	0.341×10^{-13}
% Error	9.33	8.88	7.72	5.82	3.07	2.01	1.73
10							
Analytical Solution	0.814×10^4	0.296×10^4	0.114×10^3	0.573×10^0	0.425×10^{-3}	0.472×10^{-7}	0.776×10^{-12}
Model Solution	0.73×10^4	0.269×10^4	0.105×10^3	0.540×10^0	0.409×10^{-3}	0.463×10^{-7}	0.763×10^{-12}
% Error	9.83	9.12	7.89	5.76	3.76	1.91	1.68
20							
Analytical Solution	0.555×10^{-1}	0.207×10^{-1}	0.905×10^{-3}	0.575×10^{-5}	0.534×10^{-8}	0.689×10^{-12}	0.122×10^{-16}
Model Solution	0.504×10^{-1}	0.189×10^{-1}	0.835×10^{-3}	0.546×10^{-5}	0.519×10^{-8}	0.678×10^{-12}	0.120×10^{-16}
% Error	9.19	8.70	7.73	4.70	2.81	1.60	1.64

TABLE X
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 720 HRS., DEPTH: 1 M

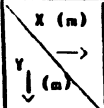
	0	10	20	30	40	50	60
5							
Analytical Solution	0.635×10^3	0.372×10^3	0.539×10^2	0.198×10^1	0.187×10^{-1}	0.471×10^{-4}	0.318×10^{-7}
Model Solution	0.580×10^3	0.343×10^3	0.503×10^2	0.186×10^1	0.182×10^{-1}	0.459×10^{-4}	0.314×10^{-7}
% Error	8.66	7.80	6.68	6.06	2.67	2.55	1.25
10							
Analytical Solution	0.145×10^6	0.717×10^5	0.662×10^4	0.173×10^3	0.813×10^0	0.154×10^{-2}	0.889×10^{-6}
Model Solution	0.129×10^6	0.642×10^5	0.594×10^4	0.160×10^3	0.781×10^0	0.151×10^{-2}	0.876×10^{-6}
% Error	10.75	10.46	10.27	7.51	3.94	1.95	1.46
20							
Analytical Solution	0.679×10^0	0.351×10^0	0.366×10^{-1}	0.894×10^{-3}	0.638×10^{-5}	0.147×10^{-7}	0.102×10^{-10}
Model Solution	0.624×10^0	0.327×10^0	0.348×10^{-1}	0.849×10^{-3}	0.622×10^{-5}	0.143×10^{-7}	0.100×10^{-10}
% Error	8.10	6.72	4.92	5.03	2.51	2.72	1.96

TABLE XI
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 720 HRS., DEPTH: 2 M

<div style="display: inline-block; border: 1px solid black; padding: 2px;"> x (m) \rightarrow y (m) \downarrow </div>	0	10	20	30	40	50	60
5							
Analytical Solution	0.461×10^3	0.270×10^3	0.394×10^2	0.145×10^1	0.138×10^{-1}	0.349×10^{-4}	0.237×10^{-7}
Model Solution	0.421×10^3	0.248×10^3	0.367×10^2	0.137×10^1	0.134×10^{-1}	0.343×10^{-4}	0.233×10^{-7}
Z Error	8.70	8.15	6.85	5.52	2.90	1.72	1.69
10							
Analytical Solution	0.603×10^5	0.314×10^5	0.333×10^4	0.823×10^2	0.558×10^0	0.112×10^{-2}	0.656×10^{-6}
Model Solution	0.544×10^5	0.285×10^5	0.306×10^4	0.709×10^2	0.537×10^0	0.110×10^{-2}	0.645×10^{-6}
Z Error	9.78	9.24	8.11	6.56	3.76	1.79	1.68
20							
Analytical Solution	0.400×10^0	0.290×10^0	0.229×10^{-1}	0.599×10^{-3}	0.457×10^{-5}	0.109×10^{-7}	0.760×10^{-11}
Model Solution	0.365×10^0	0.193×10^0	0.213×10^{-1}	0.570×10^{-3}	0.441×10^{-5}	0.107×10^{-7}	0.748×10^{-11}
Z Error	8.75	8.10	6.99	4.84	3.50	1.83	1.58

TABLE XII
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 720 HRS., DEPTH: 4 M

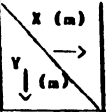
	0	10	20	30	40	50	60
5							
Analytical Solution	0.120×10^3	0.710×10^2	0.105×10^2	0.398×10^0	0.390×10^{-2}	0.101×10^{-4}	0.700×10^{-8}
Model Solution	0.109×10^3	0.654×10^2	0.099×10^2	0.374×10^0	0.379×10^{-2}	0.099×10^{-4}	0.689×10^{-8}
% Error	8.80	7.89	6.67	6.03	2.82	1.98	1.57
10							
Analytical Solution	0.641×10^4	0.362×10^4	0.478×10^3	0.155×10^2	0.130×10^0	0.295×10^{-3}	0.185×10^{-6}
Model Solution	0.584×10^4	0.333×10^4	0.445×10^3	0.146×10^2	0.125×10^0	0.290×10^{-3}	0.182×10^{-6}
% Error	8.89	8.10	6.90	5.81	3.85	1.69	1.62
20							
Analytical Solution	0.438×10^{-1}	0.251×10^{-1}	0.346×10^{-2}	0.123×10^{-3}	0.118×10^{-5}	0.315×10^{-8}	0.228×10^{-11}
Model Solution	0.399×10^{-1}	0.231×10^{-1}	0.323×10^{-2}	0.117×10^{-3}	0.115×10^{-5}	0.390×10^{-8}	0.225×10^{-11}
% Error	8.90	7.97	6.65	4.88	2.54	1.59	1.32

TABLE XIII
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 960 HRS., DEPTH: 1 M

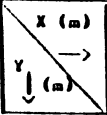
	0	10	20	30	40	50	60
5							
Analytical Solution	0.543×10^3	0.382×10^3	0.959×10^2	0.862×10^1	0.280×10^0	0.333×10^{-2}	0.164×10^{-4}
Model Solution	0.502×10^3	0.356×10^3	0.903×10^2	0.819×10^1	0.275×10^1	0.325×10^{-2}	0.144×10^{-4}
Z Error	7.55	6.80	5.80	5.75	2.48	2.40	1.37
10							
Analytical Solution	0.120×10^6	0.777×10^5	0.153×10^5	0.956×10^3	0.206×10^2	0.168×10^0	0.558×10^{-3}
Model Solution	0.108×10^6	0.702×10^5	0.139×10^5	0.887×10^3	0.198×10^2	0.164×10^0	0.550×10^{-3}
Z Error	1.00	9.65	8.80	7.22	3.88	2.38	1.43
20							
Analytical Solution	0.567×10^0	0.375×10^0	0.786×10^{-1}	0.542×10^{-2}	0.132×10^{-3}	0.124×10^{-5}	0.476×10^{-8}
Model Solution	0.513×10^0	0.353×10^0	0.747×10^{-1}	0.519×10^{-2}	0.128×10^{-3}	0.121×10^{-5}	0.470×10^{-8}
Z Error	9.52	5.87	4.98	4.07	3.00	2.42	1.26

TABLE XIV

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 960 HRS., DEPTH: 2 M

<div style="border: 1px solid black; padding: 2px; display: inline-block;"> X (m) → Y (m) ↓ </div>	0	10	20	30	40	50	60
5							
Analytical Solution	0.394×10^3	0.278×10^3	0.698×10^3	0.630×10^1	0.206×10^0	0.245×10^{-2}	0.108×10^{-4}
Model Solution	0.361×10^3	0.258×10^3	0.656×10^2	0.596×10^0	0.200×10^0	0.241×10^{-2}	0.106×10^{-4}
Z Error	8.40	7.19	6.02	5.40	2.91	1.63	1.85
10							
Analytical Solution	0.504×10^5	0.334×10^5	0.706×10^4	0.493×10^3	0.121×10^2	0.110×10^0	0.392×10^{-3}
Model Solution	0.460×10^5	0.306×10^5	0.656×10^3	0.461×10^3	0.116×10^2	0.108×10^0	0.386×10^{-3}
Z Error	8.73	8.38	7.08	6.49	4.13	1.82	1.53
20							
Analytical Solution	0.335×10^0	0.223×10^0	0.478×10^{-1}	0.342×10^{-2}	0.876×10^{-4}	0.866×10^{-6}	0.346×10^{-8}
Model Solution	0.308×10^0	0.207×10^0	0.450×10^{-1}	0.326×10^{-2}	0.852×10^{-4}	0.852×10^{-6}	0.341×10^{-8}
Z Error	8.06	7.17	5.86	4.12	2.74	1.62	1.45

TABLE XV

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 960 HRS., DEPTH: 4 M

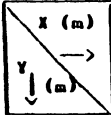
	0	10	20	30	40	50	60
5							
Analytical Solution	0.103×10^3	0.729×10^2	0.185×10^2	0.170×10^1	0.564×10^{-1}	0.686×10^{-3}	0.308×10^{-5}
Model Solution	0.095×10^3	0.678×10^2	0.174×10^2	0.160×10^1	0.549×10^{-1}	0.675×10^{-3}	0.303×10^{-5}
Z Error	7.77	7.00	5.95	5.88	2.66	1.60	1.62
10							
Analytical Solution	0.544×10^4	0.376×10^4	0.895×10^3	0.744×10^2	0.221×10^1	0.239×10^{-1}	0.963×10^{-4}
Model Solution	0.503×10^4	0.349×10^4	0.842×10^3	0.703×10^2	0.213×10^1	0.235×10^{-1}	0.949×10^{-4}
Z Error	7.54	7.18	5.92	5.51	3.62	1.67	1.45
20							
Analytical Solution	0.373×10^{-1}	0.260×10^{-1}	0.632×10^{-2}	0.549×10^{-3}	0.175×10^{-4}	0.209×10^{-6}	0.944×10^{-9}
Model Solution	0.345×10^{-1}	0.242×10^{-1}	0.595×10^{-2}	0.524×10^{-3}	0.170×10^{-4}	0.206×10^{-6}	0.931×10^{-9}
Z Error	7.51	6.92	5.85	4.55	2.86	1.44	1.38

TABLE XVI

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 1. TIME: 1200 HRS., DEPTH: 1 M

<div style="border: 1px solid black; padding: 2px; display: inline-block;"> $X \rightarrow$ (m) $Y \downarrow$ (m) </div>	0	10	20	30	40	50	60
5							
Analytical Solution	0.481×10^3	0.377×10^3	0.131×10^3	0.200×10^2	0.136×10^1	0.410×10^{-1}	0.557×10^{-3}
Model Solution	0.448×10^3	0.353×10^3	0.125×10^3	0.195×10^2	0.133×10^1	0.405×10^{-1}	0.551×10^{-3}
Z Error	6.65	6.37	4.58	2.50	2.21	1.22	1.08
10							
Analytical Solution	0.105×10^6	0.708×10^5	0.232×10^5	0.281×10^4	0.142×10^3	0.311×10^1	0.311×10^{-1}
Model Solution	0.095×10^6	0.707×10^5	0.212×10^5	0.251×10^4	0.136×10^3	0.304×10^1	0.307×10^{-1}
Z Error	9.52	9.36	8.62	8.54	4.22	2.25	1.29
20							
Analytical Solution	0.490×10^0	0.375×10^0	0.116×10^0	0.149×10^{-1}	0.816×10^{-3}	0.197×10^{-2}	0.220×10^{-6}
Model Solution	0.464×10^0	0.356×10^0	0.112×10^0	0.144×10^{-1}	0.804×10^{-3}	0.194×10^{-2}	0.217×10^{-6}
Z Error	6.45	5.07	3.45	3.35	1.47	1.52	1.37

TABLE XVII

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
 CASE 1. TIME: 1200 HRS., DEPTH: 2 M

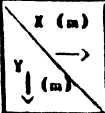
	0	10	20	30	40	50	60
5							
Analytical Solution	0.349×10^3	0.274×10^3	0.949×10^2	0.146×10^2	0.991×10^0	0.301×10^{-1}	0.410×10^{-3}
Model Solution	0.321×10^3	0.25×10^3	0.894×10^2	0.131×10^2	0.963×10^0	0.295×10^{-1}	0.403×10^{-3}
% Error	8.02	7.21	5.78	5.11	2.83	1.99	1.71
10							
Analytical Solution	0.442×10^5	0.334×10^5	0.104×10^5	0.134×10^4	0.743×10^2	0.180×10^1	0.198×10^{-1}
Model Solution	0.409×10^5	0.309×10^5	0.097×10^5	0.125×10^4	0.716×10^2	0.177×10^1	0.195×10^{-1}
% Error	7.47	7.27	6.73	6.72	3.63	1.67	1.52
20							
Analytical Solution	0.294×10^0	0.223×10^0	0.698×10^{-1}	0.918×10^{-2}	0.519×10^{-3}	0.131×10^{-4}	0.152×10^{-6}
Model Solution	0.273×10^0	0.209×10^0	0.660×10^{-1}	0.881×10^{-2}	0.505×10^{-3}	0.129×10^{-4}	0.150×10^{-6}
% Error	7.14	6.28	5.44	4.00	2.70	1.52	1.32

TABLE XVIII

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
 CASE 1. TIME: 1200 HRS., DEPTH: 4 M

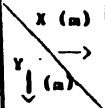
	0	10	20	30	40	50	60
5							
Analytical Solution	0.914×10^2	0.718×10^2	0.251×10^2	0.388×10^1	0.268×10^0	0.826×10^{-2}	0.114×10^{-3}
Model Solution	0.805×10^2	0.670×10^2	0.236×10^2	0.365×10^1	0.261×10^0	0.813×10^{-2}	0.112×10^{-3}
Z Error	7.00	6.68	5.98	5.92	2.61	1.57	1.75
10							
Analytical Solution	0.481×10^4	0.373×10^4	0.125×10^4	0.181×10^3	0.115×10^2	0.324×10^0	0.409×10^{-2}
Model Solution	0.447×10^4	0.348×10^4	0.118×10^4	0.171×10^3	0.111×10^2	0.319×10^0	0.404×10^{-2}
Z Error	7.07	6.70	5.61	5.52	3.48	1.54	1.22
20							
Analytical Solution	0.330×10^{-1}	0.257×10^{-1}	0.871×10^{-2}	0.130×10^{-2}	0.860×10^{-4}	0.257×10^{-5}	0.347×10^{-7}
Model Solution	0.306×10^{-1}	0.240×10^{-1}	0.820×10^{-2}	0.124×10^{-2}	0.838×10^{-4}	0.253×10^{-5}	0.344×10^{-7}
Z Error	7.27	6.61	5.86	4.62	2.56	1.56	1.43

TABLE XIX
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 2. TIME: 240 HRS., DEPTH: 1 M

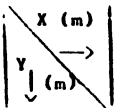
	0	10	20	30	40	50	60
5							
Analytical Solution	0.117×10^4	0.122×10^3	0.168×10^0	0.625×10^{-5}	0.465×10^{-11}	0.783×10^{-19}	0.297×10^{-28}
Model Solution	0.103×10^4	0.108×10^3	0.170×10^0	0.573×10^{-5}	0.449×10^{-11}	0.756×10^{-19}	0.287×10^{-28}
% Error	11.96	11.48	9.57	8.32	3.45	3.44	3.37
10							
Analytical Solution	0.425×10^6	0.518×10^4	0.488×10^1	0.139×10^{-3}	0.969×10^{-10}	0.157×10^{-17}	0.581×10^{-27}
Model Solution	0.373×10^6	0.455×10^4	0.430×10^1	0.127×10^{-3}	0.922×10^{-10}	0.152×10^{-17}	0.562×10^{-27}
% Error	12.24	12.16	11.88	8.63	4.85	3.18	3.27
20							
Analytical Solution	0.174×10^1	0.369×10^{-1}	0.613×10^{-4}	0.222×10^{-8}	0.156×10^{-14}	0.245×10^{-22}	0.891×10^{-32}
Model Solution	0.158×10^1	0.337×10^{-1}	0.571×10^{-4}	0.209×10^{-8}	0.151×10^{-14}	0.237×10^{-22}	0.871×10^{-32}
% Error	9.20	8.67	6.85	6.31	3.21	3.27	2.24

TABLE XX

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 2. TIME: 240 HRS., DEPTH: 2 M

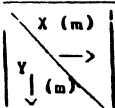
	0	10	20	30	40	50	60
5							
Analytical Solution	0.864×10^3	0.917×10^2	0.143×10^0	0.478×10^{-5}	0.357×10^{-11}	0.603×10^{-19}	0.229×10^{-28}
Model Solution	0.776×10^3	0.825×10^2	0.131×10^0	0.446×10^{-5}	0.334×10^{-11}	0.580×10^{-19}	0.223×10^{-28}
% Error	10.88	10.03	8.39	6.69	6.44	2.82	2.62
10							
Analytical Solution	0.244×10^6	0.377×10^4	0.369×10^1	0.107×10^{-3}	0.744×10^{-10}	0.121×10^{-17}	0.445×10^{-27}
Model Solution	0.217×10^6	0.330×10^4	0.333×10^1	0.100×10^{-3}	0.709×10^{-10}	0.115×10^{-17}	0.435×10^{-27}
% Error	11.00	10.88	9.76	6.54	4.70	2.48	2.68
20							
Analytical Solution	0.109×10^1	0.274×10^{-1}	0.468×10^{-4}	0.170×10^{-8}	0.120×10^{-14}	0.188×10^{-22}	0.687×10^{-32}
Model Solution	0.095×10^1	0.247×10^{-1}	0.428×10^{-4}	0.160×10^{-8}	0.117×10^{-14}	0.183×10^{-22}	0.669×10^{-32}
% Error	10.09	9.85	8.55	5.88	2.66	2.66	2.62

TABLE XXI

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 2. TIME: 240 HRS., DEPTH: 4 M

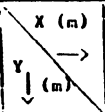
	0	10	20	30	40	50	60
5							
Analytical Solution	0.246×10^3	0.278×10^2	0.461×10^{-1}	0.159×10^{-5}	0.121×10^{-11}	0.206×10^{-19}	0.788×10^{-29}
Model Solution	0.221×10^3	0.251×10^2	0.421×10^1	0.148×10^{-5}	0.116×10^{-11}	0.200×10^{-19}	0.768×10^{-29}
% Error	10.16	9.71	8.68	6.92	4.13	2.91	2.54
10							
Analytical Solution	0.169×10^5	0.101×10^4	0.117×10^1	0.353×10^{-4}	0.251×10^{-10}	0.411×10^{-18}	0.154×10^{-27}
Model Solution	0.151×10^5	0.091×10^4	0.107×10^1	0.330×10^{-4}	0.239×10^{-10}	0.400×10^{-18}	0.150×10^{-27}
% Error	10.65	9.90	8.55	6.52	4.78	2.68	2.60
20							
Analytical Solution	0.118×10^0	0.805×10^{-2}	0.154×10^{-4}	0.564×10^{-9}	0.404×10^{-15}	0.624×10^{-23}	0.236×10^{-32}
Model Solution	0.106×10^0	0.727×10^{-2}	0.141×10^{-4}	0.533×10^{-9}	0.389×10^{-15}	0.626×10^{-23}	0.230×10^{-32}
% Error	10.16	9.09	8.44	5.50	3.71	2.54	2.49

TABLE XXII
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 2. TIME: 480 HRS., DEPTH: 1 M

<div style="display: inline-block; border: 1px solid black; padding: 2px;"> $X (m)$ \rightarrow Y \downarrow (m) </div>	0	10	20	30	40	50	60
5							
Analytical Solution	0.772×10^3	0.307×10^3	0.144×10^2	-0.865×10^{-1}	0.719×10^{-4}	0.853×10^{-8}	0.146×10^{-12}
Model Solution	0.702×10^3	0.282×10^3	0.133×10^2	0.812×10^{-1}	0.703×10^{-4}	0.836×10^{-8}	0.143×10^{-12}
% Error	9.07	8.14	7.64	6.13	2.23	1.99	2.05
10							
Analytical Solution	0.156×10^6	0.407×10^5	0.833×10^3	0.299×10^1	0.196×10^{-2}	0.207×10^{-6}	0.330×10^{-11}
Model Solution	0.138×10^6	0.362×10^5	0.742×10^3	0.277×10^1	0.189×10^{-2}	0.203×10^{-6}	0.325×10^{-11}
% Error	11.54	11.06	10.92	7.36	3.57	1.93	1.52
20							
Analytical Solution	0.835×10^0	0.240×10^0	0.585×10^{-2}	0.266×10^{-4}	0.230×10^{-7}	0.292×10^{-11}	0.513×10^{-16}
Model Solution	0.766×10^0	0.223×10^0	0.553×10^{-2}	0.252×10^{-4}	0.225×10^{-7}	0.286×10^{-11}	0.504×10^{-16}
% Error	8.26	7.08	5.47	5.26	2.17	2.05	1.75

TABLE XXIII

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 2. TIME: 480 HRS., DEPTH: 2 M

<div style="display: inline-block; border-right: 1px solid black; border-bottom: 1px solid black; padding: 2px;"> X (m) → Y (m) ↓ </div>	0	10	20	30	40	50	60
5							
Analytical Solution	0.572×10^3	0.228×10^3	0.107×10^2	0.652×10^{-1}	0.546×10^{-4}	0.651×10^{-8}	0.112×10^{-12}
Model Solution	0.517×10^3	0.208×10^3	0.099×10^2	0.609×10^{-1}	0.515×10^{-4}	0.634×10^{-8}	0.109×10^{-12}
% Error	9.61	8.77	7.48	6.59	5.67	2.61	2.50
10							
Analytical Solution	0.946×10^5	0.257×10^5	0.579×10^3	0.221×10^1	0.148×10^{-2}	0.157×10^{-6}	0.252×10^{-11}
Model Solution	0.848×10^5	0.231×10^5	0.528×10^3	0.207×10^1	0.142×10^{-2}	0.154×10^{-6}	0.248×10^{-11}
% Error	10.36	10.12	8.81	6.33	4.05	1.91	1.59
20							
Analytical Solution	0.534×10^0	0.157×10^0	0.415×10^{-2}	0.200×10^{-4}	0.175×10^{-7}	0.233×10^{-4}	0.393×10^{-16}
Model Solution	0.484×10^0	0.143×10^0	0.383×10^{-2}	0.190×10^{-4}	0.171×10^{-7}	0.219×10^{-11}	0.386×10^{-16}
% Error	9.36	8.92	7.71	5.00	2.29	1.79	1.78

TABLE XXIV
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 2. TIME: 480 HRS., DEPTH: 4 M

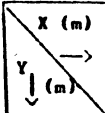
	0	10	20	30	40	50	60
5							
Analytical Solution	0.164×10^3	0.664×10^2	0.324×10^1	0.204×10^{-1}	0.175×10^{-4}	0.213×10^{-8}	0.371×10^{-13}
Model Solution	0.149×10^3	0.605×10^2	0.299×10^1	0.192×10^{-1}	0.168×10^{-4}	0.209×10^{-8}	0.365×10^{-13}
% Error	9.15	8.89	7.72	5.88	4.00	1.88	1.62
10							
Analytical Solution	0.101×10^5	0.355×10^4	0.129×10^3	0.628×10^0	0.460×10^{-3}	0.507×10^{-7}	0.830×10^{-12}
Model Solution	0.091×10^5	0.324×10^4	0.119×10^3	0.594×10^0	0.442×10^{-3}	0.497×10^{-7}	0.814×10^{-12}
% Error	9.90	8.73	7.75	5.41	3.91	1.97	1.92
20							
Analytical Solution	0.699×10^{-1}	0.250×10^{-1}	0.101×10^{-2}	0.621×10^{-5}	0.572×10^{-8}	0.737×10^{-12}	0.130×10^{-16}
Model Solution	0.632×10^{-1}	0.228×10^{-1}	0.093×10^{-2}	0.592×10^{-5}	0.556×10^{-8}	0.725×10^{-12}	0.128×10^{-16}
% Error	9.59	8.8	7.92	4.67	2.88	1.63	1.54

TABLE XXV

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 2. TIME: 720 HRS., DEPTH: 1 M

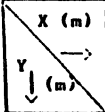
	0	10	20	30	40	50	60
5							
Analytical Solution	0.617×10^3	0.361×10^3	0.524×10^2	0.192×10^1	0.182×10^{-1}	0.458×10^{-4}	0.190×10^{-7}
Model Solution	0.565×10^3	0.333×10^3	0.490×10^2	0.181×10^1	0.178×10^{-1}	0.447×10^{-4}	0.304×10^{-7}
% Error	8.42	7.61	6.49	5.73	2.20	2.40	1.99
10							
Analytical Solution	0.117×10^6	0.587×10^5	0.568×10^4	0.125×10^3	0.777×10^0	0.150×10^{-2}	0.865×10^{-6}
Model Solution	0.105×10^6	0.526×10^5	0.510×10^4	0.116×10^3	0.747×10^0	0.147×10^{-2}	0.854×10^{-6}
% Error	10.26	10.39	10.21	7.2	3.86	2.00	1.27
20							
Analytical Solution	0.633×10^0	0.329×10^0	0.346×10^{-1}	0.856×10^{-3}	0.618×10^{-5}	0.143×10^{-7}	0.989×10^{-11}
Model Solution	0.585×10^0	0.307×10^0	0.329×10^{-1}	0.817×10^{-3}	0.603×10^{-5}	0.140×10^{-7}	0.977×10^{-11}
% Error	7.58	6.69	4.91	4.56	2.43	2.10	1.21

TABLE XXVI
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 2. TIME: 720 HRS., DEPTH: 2 M

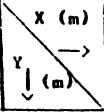
	0	10	20	30	40	50	60
5							
Analytical Solution	0.457×10^3	0.268×10^3	0.390×10^2	0.144×10^1	0.137×10^{-1}	0.346×10^{-4}	0.235×10^{-7}
Model Solution	0.418×10^3	0.247×10^3	0.363×10^2	0.135×10^1	0.129×10^{-1}	0.337×10^{-4}	0.230×10^{-7}
% Error	8.53	7.84	6.92	6.25	5.83	2.60	2.12
10							
Analytical Solution	0.710×10^5	0.362×10^5	0.365×10^4	0.852×10^2	0.559×10^0	0.111×10^{-2}	0.650×10^{-6}
Model Solution	0.610×10^5	0.329×10^5	0.336×10^4	0.797×10^2	0.539×10^0	0.109×10^{-2}	0.639×10^{-6}
% Error	9.86	9.12	7.95	6.46	3.58	1.80	1.69
20							
Analytical Solution	0.406×10^0	0.293×10^0	0.230×10^{-1}	0.599×10^{-3}	0.454×10^{-5}	0.108×10^{-7}	0.753×10^{-11}
Model Solution	0.373×10^0	0.197×10^0	0.215×10^{-1}	0.571×10^{-3}	0.442×10^{-5}	0.906×10^{-7}	0.744×10^{-11}
% Error	8.12	7.51	6.52	4.67	2.54	1.85	1.46

TABLE XXVII

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
 CASE 2. TIME: 720 HRS., DEPTH: 4 M

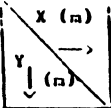
	0	10	20	30	40	50	60
5							
Analytical Solution	0.132×10^3	0.777×10^2	0.115×10^2	0.433×10^0	0.422×10^{-2}	0.109×10^{-4}	0.753×10^{-8}
Model Solution	0.121×10^3	0.716×10^2	0.107×10^2	0.406×10^0	0.406×10^{-2}	0.107×10^{-4}	0.742×10^{-8}
% Error	8.33	7.85	6.96	5.77	3.79	1.83	1.46
10							
Analytical Solution	0.789×10^4	0.441×10^4	0.565×10^3	0.177×10^2	0.144×10^0	0.322×10^{-3}	0.200×10^{-6}
Model Solution	0.722×10^4	0.405×10^4	0.527×10^3	0.167×10^2	0.139×10^0	0.317×10^{-3}	0.197×10^{-6}
% Error	8.49	7.94	6.73	5.65	3.47	1.55	1.5
20							
Analytical Solution	0.548×10^{-1}	0.308×10^{-1}	0.406×10^{-2}	0.135×10^{-3}	0.129×10^{-5}	0.339×10^{-8}	0.245×10^{-11}
Model Solution	0.500×10^{-1}	0.284×10^{-1}	0.381×10^{-2}	0.132×10^{-3}	0.126×10^{-5}	0.334×10^{-8}	0.242×10^{-11}
% Error	8.76	7.79	6.62	4.35	2.33	1.47	1.22

TABLE XXVIII

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
 CASE 2. TIME: 960 HRS., DEPTH: 1 M

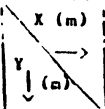
	0	10	20	30	40	50	60
5							
Analytical Solution	0.528×10^3	0.372×10^3	0.932×10^2	0.839×10^1	0.273×10^0	0.324×10^{-2}	0.142×10^{-4}
Model Solution	0.491×10^3	0.348×10^3	0.883×10^2	0.795×10^1	0.268×10^0	0.318×10^{-2}	0.140×10^{-4}
% Error	7.00	6.45	5.26	5.24	1.83	1.85	1.41
10							
Analytical Solution	0.969×10^5	0.632×10^5	0.127×10^5	0.827×10^3	0.186×10^2	0.158×10^0	0.537×10^{-3}
Model Solution	0.874×10^5	0.574×10^5	0.110×10^5	0.771×10^3	0.180×10^2	0.155×10^0	0.529×10^{-3}
% Error	9.80	9.15	8.66	6.77	3.23	1.90	1.49
20							
Analytical Solution	0.530×10^0	0.351×10^0	0.736×10^{-1}	0.513×10^{-2}	0.126×10^{-3}	0.119×10^{-5}	0.461×10^{-8}
Model Solution	0.495×10^0	0.332×10^0	0.705×10^{-1}	0.490×10^{-2}	0.123×10^{-3}	0.117×10^{-5}	0.453×10^{-8}
% Error	6.60	5.41	4.47	4.48	2.38	1.74	1.68

TABLE XXIX

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
 CASE 2. TIME: 960 HRS., DEPTH: 2 M

$\begin{array}{c} X \text{ (m)} \\ \swarrow \quad \searrow \\ \downarrow \quad \rightarrow \\ Y \text{ (m)} \end{array}$	0	10	20	30	40	50	60
5							
Analytical Solution	0.391×10^3	0.276×10^3	0.693×10^2	0.625×10^1	0.204×10^0	0.243×10^{-2}	0.107×10^{-4}
Model Solution	0.362×10^3	0.252×10^3	0.651×10^2	0.585×10^1	0.193×10^0	0.235×10^{-2}	0.105×10^{-4}
% Error	7.41	6.52	6.06	5.76	5.39	2.06	1.97
10							
Analytical Solution	0.592×10^5	0.389×10^5	0.799×10^4	0.536×10^3	0.126×10^2	0.112×10^0	0.391×10^{-3}
Model Solution	0.545×10^5	0.359×10^5	0.743×10^4	0.504×10^3	0.122×10^2	0.111×10^0	0.387×10^{-3}
% Error	7.94	7.71	7.01	5.97	3.17	1.0	0.69
20							
Analytical Solution	0.340×10^0	0.226×10^0	0.493×10^{-1}	0.344×10^{-2}	0.877×10^{-4}	0.862×10^{-6}	0.343×10^{-8}
Model Solution	0.314×10^0	0.211×10^0	0.454×10^{-1}	0.328×10^{-2}	0.859×10^{-4}	0.846×10^{-6}	0.337×10^{-8}
% Error	7.64	6.64	6.0	4.65	2.05	1.86	1.75

TABLE XXX

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 2. TIME: 960 HRS., DEPTH: 4 M

<div style="display: inline-block; border: 1px solid black; padding: 2px;"> X (m) → Y (m) ↓ </div>	0	10	20	30	40	50	60
5							
Analytical Solution	0.113×10^3	0.798×10^2	0.202×10^2	0.185×10^1	0.613×10^{-1}	0.744×10^{-3}	0.333×10^{-5}
Model Solution	0.105×10^3	0.746×10^2	0.190×10^2	0.175×10^1	0.591×10^{-1}	0.730×10^{-3}	0.327×10^{-5}
% Error	7.08	6.52	5.94	5.41	3.59	1.88	1.80
10							
Analytical Solution	0.669×10^4	0.459×10^4	0.108×10^4	0.874×10^2	0.253×10^1	0.268×10^{-1}	0.106×10^{-3}
Model Solution	0.617×10^4	0.425×10^4	0.101×10^4	0.826×10^2	0.244×10^1	0.264×10^{-1}	0.105×10^{-3}
% Error	7.77	7.40	6.48	5.49	3.56	1.49	0.9
20							
Analytical Solution	0.465×10^{-1}	0.321×10^{-1}	0.762×10^{-2}	0.641×10^{-3}	0.198×10^{-4}	0.230×10^{-6}	0.102×10^{-8}
Model Solution	0.431×10^{-1}	0.300×10^{-1}	0.728×10^{-2}	0.612×10^{-3}	0.193×10^{-4}	0.226×10^{-6}	0.101×10^{-8}
% Error	7.31	6.54	5.46	4.52	2.53	1.24	0.98

TABLE XXXI

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
 CASE 2. TIME: 1200 HRS., DEPTH: 1 M

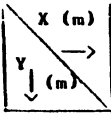
	0	10	20	30	40	50	60
5							
Analytical Solution	0.468×10^3	0.367×10^3	0.127×10^3	0.194×10^2	0.132×10^1	0.399×10^{-1}	0.524×10^{-3}
Model Solution	0.435×10^3	0.344×10^3	0.120×10^3	0.184×10^2	0.136×10^1	0.335×10^{-1}	0.499×10^{-3}
% Error	7.05	6.27	5.51	5.15	1.75	1.70	1.62
10							
Analytical Solution	0.846×10^5	0.633×10^5	0.191×10^5	0.237×10^4	0.123×10^3	0.280×10^1	0.290×10^{-1}
Model Solution	0.763×10^5	0.574×10^5	0.174×10^5	0.222×10^4	0.120×10^3	0.274×10^1	0.285×10^{-1}
% Error	9.81	9.32	8.71	6.33	2.44	2.14	1.72
20							
Analytical Solution	0.464×10^0	0.350×10^0	0.109×10^0	0.140×10^{-1}	0.773×10^{-3}	0.188×10^{-4}	0.292×10^{-6}
Model Solution	0.433×10^0	0.331×10^0	0.104×10^0	0.134×10^{-1}	0.757×10^{-3}	0.195×10^{-4}	0.197×10^{-6}
% Error	6.68	5.43	4.59	4.29	2.07	1.60	1.41

TABLE XXXII

ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
 CASE 2. TIME: 1200 HRS., DEPTH: 2 M

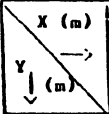
	0	10	20	30	40	50	60
5							
Analytical Solution	0.347×10^3	0.272×10^3	0.942×10^2	0.144×10^2	0.983×10^0	0.299×10^{-1}	0.407×10^{-3}
Model Solution	0.323×10^3	0.	0.890×10^2	0.137×10^2	0.940×10^0	0.293×10^{-1}	0.399×10^{-3}
Z Error	6.92	6.25	5.52	4.86	4.37	2.00	1.96
10							
Analytical Solution	0.518×10^5	0.389×10^5	0.119×10^5	0.150×10^4	0.804×10^2	0.189×10^1	0.202×10^{-1}
Model Solution	0.476×10^5	0.360×10^5	0.111×10^5	0.140×10^4	0.779×10^2	0.187×10^1	0.200×10^{-1}
Z Error	8.11	7.46	6.73	6.66	3.11	1.06	1.0
20							
Analytical Solution	0.298×10^0	0.226×10^0	0.706×10^{-1}	0.926×10^{-2}	0.522×10^{-3}	0.131×10^{-4}	0.151×10^{-6}
Model Solution	0.276×10^0	0.211×10^0	0.666×10^{-1}	0.889×10^{-2}	0.511×10^{-3}	0.129×10^{-4}	0.149×10^{-5}
Z Error	7.38	6.63	5.69	4.06	2.10	1.53	1.32

TABLE XXXIII
ERROR ANALYSIS AT DIFFERENT NODES AND TIMES
CASE 2. TIME: 1200 HRS., DEPTH: 4 M

<div style="display: inline-block; border: 1px solid black; padding: 2px;"> $X (m)$ \rightarrow $Y (m)$ \downarrow </div>	0	10	20	30	40	50	60
5							
Analytical Solution	0.100×10^3	0.787×10^2	0.274×10^2	0.424×10^1	0.292×10^0	0.898×10^{-2}	0.124×10^{-3}
Model Solution	0.093×10^3	0.740×10^2	0.259×10^2	0.403×10^1	0.282×10^0	0.885×10^{-2}	0.122×10^{-3}
% Error	7.00	6.00	5.47	5.00	3.42	1.61	1.45
10							
Analytical Solution	0.590×10^4	0.456×10^4	0.151×10^4	0.216×10^3	0.135×10^2	0.372×10^0	0.461×10^{-2}
Model Solution	0.545×10^4	0.423×10^4	0.142×10^4	0.205×10^3	0.131×10^2	0.367×10^0	0.456×10^{-2}
% Error	7.62	7.24	6.60	5.10	3.00	1.34	1.08
20							
Analytical Solution	0.410×10^{-1}	0.318×10^{-1}	0.106×10^{-1}	0.155×10^{-2}	0.100×10^{-3}	0.291×10^{-5}	0.387×10^{-7}
Model Solution	0.386×10^{-1}	0.300×10^{-1}	0.101×10^{-1}	0.149×10^{-2}	$0. \quad \quad \quad -3$	0.288×10^{-5}	0.344×10^{-7}
% Error	5.85	5.66	4.71	3.87	2.00	1.03	1.03

2

VITA

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