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THE SIMULATION OF TRAFFIC TO EVALUATE THE EFFICIENCY OF THE INTERSECTION

## CONTROL SYSTEM

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## CHAPTER I

## INTRODUCTION

One important test in the development of new traffic control methods is an evaluation of proposed alternates. It is impractical to test every alternate on a real time basis, and it is not wise to choose an alternate without comparison testing. With the rapid development of high speed computers, simulation of traffic under the various alternatives has proved to be a valuable means of providing effective comparisons at reasonable cost.

Simulation is a technique which enables the study of a complex traffic system in the laboratory rather than in the field. It is usually faster and less expensive than the testing of a real system. In many cases, it enables study of system characteristics prior to construction of the facility. The modern digital electronic computer presently provides the high speed of computation and the logic capabilities that enables it to react in a manner analogous to vehicles traveling on a roadway (4). By proper programming, the behavior of each vehicle represented within the computer may be calculated by following predetermined patterns, derived from the observation of real vehicles or established mathematical theory. By this method, the precise control of the dynamic traffic process can be maintained and many unnecessary variables eliminated (4).

In considering changing an intersection control system, either providing a separate lane for turning traffic or changing the signal phases, the question usually is to determine which change is the most effective and advantageous. Since the traffic characteristics vary considerably at different locations, the correct answer is not easily obtained by simply applying traffic theories. The direct way would be to make actual changes and evaluate the results for comparison. However, this method is impractical because it is time consuming and expensive. Another way is to solve the problem using a computer simulation model.

This research concerns a computer simulation program that will be used to evaluate the single intersection controlled by traffic signal. The intersection considered has one or two lanes on each approach, and may have separate turning lanes. A traffic signal is used to control traffic in all directions.

The first part of the research is the development of the computer simulation program, written in GPSS (General Purpose Simulation System), and run on the IBM $360 / 65$ computer. The output of the program is a table indicating the traveling times required by vehicles on each approaching lane to cross the intersection, and the queue length of stopped vehicles. The reason for using "delay" or "traveling time" rather than "load factor" as the measuring parameter is because it is more realistic from the street user's standpoint. This parameter is the value that will be used as a measure of comparison when any changes occur.

The second part of the research is field observation. Traffic data and statistics are observed from a selected intersection for use as the input information of the computer program. The time-lapse photography
method, in addition to stop watches, was used to record the flow of traffic. The data from this method can be analyzed conveniently by replaying in a single-frame movie projector.

The third and last part is the analysis and comparison of the results. Evaluation of program accuracy and further research needed are discussed.

## Development of Previous Traffic Simulation Using the Computer

Since World War II; there has been an increasing use of computers to speed and simplify the mathematical processes involved in simulation. These computers are of two general types: analog (continuous variable) and digital (discrete-variable) (31). Both types have been used for traffic simulation; however, analog simulation has some disadvantages because the vehicle is represented as a passive element completely controlled by external factors. Digital simulation, on the other hand, offers tremendous possibilities in this area by handling elements of the simulation in successive steps (36). Although traffic engineers realize that the digital computer permits bringing the traffic facility into the laboratory with unlimited control conditions, nevertheless, there has been comparatively little work done in this area.

In 1956, there were three digital computer simulations reported in the traffic engineering field. Gerlough simulated freeway traffic on a general-purpose computer (37). Goode et al. developed a model of a signalized intersection using the MIDAC digital computer (38). Wong's paper (39) described the simulation of a portion of a multilane boulevard.

In 1959, Gerlough presented another paper (40) describing computer inputs which may be used to represent the operation of traffic streams. The statistical distributions he mentioned are: Poisson, exponential, shifted exponential, and composite exponential. Lewis (41) and Benhard (42) simulated the intersection of two two-lane streets with actuated signal control. Perchonek and Levy (43), and Wohl (44) applied the digital computer to study the problem of freeway on-ramp operations. Glickstein and associates (45) applied computer simulation techniques to the interchange design problem.

Kell presented two subsequent papers $(46,47)$ on obtaining vehicle delays at intersections by the application of computer simulation. His studies compared orthogonal intersections of two two-lane, two-way streets, having traffic signal control (fixed time, semi-actuated, or full actuated) with intersections having cross street stop sign control.

Since 1962 Lewis has presented two papers describing the basic theory of simulation techniques at intersections. His first paper (4) details his simulation model and its application to determine the vehicular delays at the intersection of a four-lane major street with a twolane minor street. The computer output (the delays) was used to determine volume warrants for different types of intersection control. In the second paper (48), Lewis proposed an improved headway distribution which consists of a modified binomial distribution, using two different levels of probability, for use in simulation studies.

In 1966, Dart (1) studied the problems of left-turn traffic at signalized intersections on four-lane arterial streets. He applied the computer simulation technique to obtain the left-turn characteristics.

The delay data was used to observe the factual warrants for left-turn channelization.

In recent years, due to the faster and more efficient generation of computer machines, simulations on computer have been widely employed by traffic engineers. The research in this field has been considerably increased. Separate studies of Beilby (49) and Story (50) used similar techniques to simulate traffic flow by digital computer. Klijnhout (51) simulated a single intersection with traffic signal, his program being written in PL1 language for the third generation IBM 360/65 computer. Rumsey and Hartley (33) simulated a model of traffic flow between two adjacent intersections. Their model emphasized the behavior of platoons created by vehicles leaving one signalized intersection toward the neighboring intersection.

Simulation models for large scale street networks have also been developed in the past few years. Davies et a1. (11) wrote a street network mode1 using FORTRAN IV to operate on the CDC 6500 computer. Other large scale models which are well-known at the present time include:

1. TRANS model developed by P1anning Research Corporation (52).
2. DYNAMO model developed by MIT (53).
3. UNIST simulator developed by the University of Manchester Institute of Science and Technology (54, 55).

As computer speeds have increased and the complexity of simulations have grown, special-purpose computer languages have been developed to aid in the development and debugging of simulation programs. One of the most widely used of these languages now is GPSS (56). To publicize how a substantial reduction in the programming effort can be accomplished
by using the simulator, Blum $(57,58)$ developed a traffic simulation program written in GPSS II and FAP languages for the IBM 7090/94 systems. His program dealt with traffic flow at various types of intersections and was later adapted for large-scale street networks.

## Traffic Behavior at Signalized Intersections

When a vehicle, approaching an intersection, reaches the point where the stream of traffic is influenced by the signal at the intersection, the pattern of flow is changed, depending on vehicle interactions and driver responses. The general description of the nature of traffic at four-lane intersections, illustrated in Figure 1, follows the idea of intersection characteristics described by Dart (1).*

In the case of an isolated intersection, before the vehicles reach the intersection, usually several hundred feet in advance, their characteristics are not yet affected by the intersection congestion. Their arrival times will generally be considered random, making the distribution of successive time spacing between vehicles (inter-arrival time) an exponential relationship.

When passing point $A$ in Figure 1 (the reference point for this model), drivers will notice the changing pattern of the preceding vehicles (the build-up of a queue of stopped vehicles or the slowing of vehicles ahead). When the signal phase is yellow or red, the first independent vehicle in that cycle will not begin to decelerate until about half-way or more from point $A$ to the stop line, designated as

[^0]

Figure 1. Illustration of Traffic Behaviors at a Typical Signalized Intersection (1)
zone $C$. This is the zone where the driver, realizing the stop condition ahead, will likely decelerate at a comfortable rate. This zone is also the general area where approaching drivers may suddenly encounter a yellow phase and must quickly decide whether to decelerate at an uncomfortable rate or to continue through the intersection (D, Figure 1). Due to vehicle interaction, the trailing vehicle of a platoon will begin to slow soon after passing point $A$, usually at the location of point $B$, between point $A$ and zone $C$.

There can be interaction between successive vehicles in a traffic lane at any point on the approach between point $A$ and the intersection proper, because of the different speeds of these vehicles. The driver of a faster trailing vehicle will adjust his speed according to the speed differential and headway between the two vehicles. If the driver of the faster vehicle is planning to turn and is already in the proper lane for the turn, then he will likely slow down and follow the slower vehicle in this lane. The driver of a nonturning vehicle in the same situation may not be willing to slow down. When there is a large enough gap in another lane, he may attempt to improve his position by passing the slower vehicle through a lane change maneuver.

If there is no separate left-turn signal phase, the driver of a left-turning vehicle near the intersection in the inside lane must evaluate the opposing traffic streams. Generally, he requires a gap size in the opposing traffic, $G$, that is large enough for his turning maneuver. He may find such a gap in advance without stopping and make his turn immediately, or he may have to stop near point $E$ and wait for a suitable gap. Under heavy traffic conditions, he may have to wait to turn until after the yellow phase has displayed and all opposing traffic has stopped.

The following vehicle, meanwhile, if it is not a left-turner, may not want to be delayed waiting for the turning vehicle to move and may try to change to the adjacent outside lane, as at point $F$, if there is a large enough gap for a lane change maneuver.

In the case where there is heavy pedestrian movement crossing the side street, the right-turn vehicle from the outside 1 ane may have to wait until all pedestrians have passed. In this case a build-up of stopped vehicles may occur during the green signal phase, and one or more of the following vehicles, if not turning, may try to make a lane change in the same manner as in the case of the left turn. Still another case may occur where right-turning is allowed during the red signal phase. The first vehicle in the outside lane may turn right after accepting a gap from the cross-street traffic stream.

When the signal changes to green, there is usually a short starting delay before the first vehicle in a queue begins to move into the intersection proper. This delay is the perception and reaction time required for the driver of the first vehicle. Succeeding vehicles will follow with progressively smaller headway until some relatively constant value is reached for the last few vehicles in the queue.

## CHAPTER II

## VEHICLE BEHAVIOR ASSOCIATED WITH

## SIGNALIZED INTERSECTIONS

It is obvious that the delay is a most important factor in the determination of intersection efficiency, and thus its causes and characteristics should be studied. Previous studies have indicated that the delay deals primarily with vehicle behavior responding to the intersection control devices. To study the traffic simulation model, it is necessary to realize all of the statistics and characteristics of vehicles associated with the intersection control devices.

## Traffic Distribution

There are many variables associated with a traffic system. These concern the characteristics of vehicles, roadway, and drivers. Most of them are of a statistical nature. Due to a lack of knowledge of the distributions and laws of interaction of traffic system components at the present time, the traffic engineer usually fits the distributions to observations of the overall system. The variables usually observed are: flow (rate), inter-arrival times, and speeds. If given the distribution of one variable, it is sometimes possible (when the relationships between variables are known to some extent) to determine the distribution of another through simulation (31).

Greenshields et al. (5) have shown that the vehicle arrivals, with low to moderate flow and with a sufficient number of lanes so that vehicles can pass at will, generally follow the Poisson distribution. Thus, inter-arrival times follow the exponential distribution (as shown in Figure 2). This distribution of arrival times has been extensively employed in many theories concerning vehicular traffic, following Greenshields.

The Poisson theory is based on the random placement of discrete points on a line. A vehicle, however, occupies a finite length of roadway. Thus, the actual characteristics and behavior of vehicles vary considerably from the theoretical at higher traffic volumes. At capacity, arrivals may approach a uniform spacing and the theory is not suitable.

The exponential distribution is continuous as is the physical phenomenon it represents. If vehicles are constrained so that they cannot pass, there will be some minimum nonzero gaps (headways) which can exist between successive vehicles. Gerlough (32) has proposed the shifted exponential distribution (as shown in Figure 3). The idea of this distribution is to translate a small distance, $\tau$, away from the origin along the time axis.

At high traffic volumes, vehicles are not free to select their own positions in the roadways. The distribution existing under this constraint is called platoon behavior. Platoon behavior also occurs at an intersection within a network of a sequence of intersections. Vehicle arrivals are no longer random, but are dependent on the departure pattern from the adjacent intersection. It is observed in practice (33) that vehicles leave a signalized intersection in the form of platoons which


Figure 2. Exponential Distribution of Gaps (Inter-Arrival Times, Where $\bar{h}$ is the Mean of the Gaps) (32)


Figure 3. Exponential Distribution of Gaps Shifted From Origin (2)
spread out as the vehicles travel toward the neighboring intersection. Work by Damson and Chimini (34) in fitting the hyperlang probability distribution (a linear combination of the translated [shifted] exponential and the translated erlang distributions) to intervehicular headway, indicates a minimum headway, $\tau$, of 0.75 seconds for unconstrained vehicles. For the constrained vehicles, this parameter varies down to 0.55 seconds, which is indicative of an intervehicular spacing of only 7 or 8 feet. This value is the absolute minimum spacing that can occur in the traffic stream.

Schuh1 (35) pointed out that a traffic stream may be regarded as a mixture of free-moving and constrained vehicles, each of which conforms to a Poisson-like behavior. Free-moving vehicles can be represented by an exponential through the origin; constrained vehicles, by a shifted exponential. The composite exponential (32) is the sum of these two exponentials (as shown in Figure 4 (a)). This exponential has compared favorably with data from field observations (Figure 4(b)).

## Car-Following Behavior

In the absence of other interfering vehicles, a driver will attempt to keep the speed of his vehicle fairly constant at his desired speed in order to minimize trip duration and maximize safety. When following other vehicles whose speed is within the range of his speed, the driver introduces a new consideration, the intervehicular spacing, the magnitude of which depends on his speed. According to the general rule, the safe spacing is the length of a vehicle (about 15 feet) for every 10 miles per hour of traveling speed.


Figure 4. Composite Exponential Curve for InterArrival Times (32)

The car-following theory developed by Herman et al. $(8,9)$ is based on the role and interaction of the three components of the traffic stream: road topology (number of lanes, nature of intersection, signals, warning signs, etc.), vehicle characteristics (speed, acceleration and deceleration, vehicle signaling, vision, etc.), and driver behavior (range of perception, lags between perception and response, etc.).

Since the full spectrum of behavior at an intersection involves a tracking or following process, the car-following theory may be used to describe certain patterns of intersection performance. This relationship was applied directly to the problem of processing vehicles in a simulation model developed by Davies et al. (11). The car-following theory, as simplified for use in Davies' model, may be expressed in the general form:

$$
\text { response }=\text { sensitivity } x \text { stimulus. }
$$

This can be expressed in the form,

$$
\begin{equation*}
A_{t+T}=a_{0}\left[\frac{V_{t}^{\prime}-V_{t}}{X_{t}^{1}-X_{t}}\right] \tag{2.1}
\end{equation*}
$$

where

$$
\begin{aligned}
& A_{t+T}=\text { acceleration of the follower initiated at time }(t+T) ; \\
& T=\text { time lag of the driver-vehicle system; } \\
& V_{t}^{\prime}, V_{t}=\text { velocities of the leader and follower, initiated at time } t ; \\
& X_{t}^{\prime}, X_{t}=\text { positions of the leader and follower initiated at time } t ; \\
& a_{0}=\text { characteristic speed. } \\
& \text { Drew (10) has developed Equation (2.1) and expressed it in the }
\end{aligned}
$$ form:

$$
\begin{equation*}
A_{t+T}=a_{0}\left[\frac{V_{t}^{\prime}-V_{t}}{\left(x_{t}^{\prime}-x_{t}\right)^{m}}\right] \tag{2.2}
\end{equation*}
$$

From his analysis Drew suggested various values of $m$; for general cases where $m=1$, Equation (2.2) converts back to Equation (2.1), which indicated that $a_{0}=U_{m}$, the optimum car speed. If $m=2$, then $a_{0}=U_{f} / k_{j}$, where $U_{f}$ is the free speed and $k_{j}$ is the jam concentration (speed is down to zero in the latter case.

The behavior of the leading vehicle of a queue being discharged from a signal differs from that of a follower. This case was described by Davies et al. (11) as free behavior and may be expressed as:

$$
\begin{equation*}
A_{t+T}^{\prime}=K\left[T V^{\prime}-V_{t}^{\prime}\right] \tag{2.3}
\end{equation*}
$$

where

$$
\begin{aligned}
A_{t+T}^{\prime} & =\text { acceleration of vehicle initiated at time } t+T ; \\
K & =\text { proportionality coefficient; } \\
T V^{\prime} & =\text { target velocity of vehicle; } \\
V_{t}^{\prime} & =\text { velocity of vehicle at time } t . \\
& \text { Derivation of the Spacing Equation }
\end{aligned}
$$

In his simulation model Lewis (4) considered the above discussion as concerned with the capacity or near-capacity situation. He believed that to get relatively realistic results, as far as the traffic simulation is concerned, a car-following model should also be applicable for a wide range of traffic volumes including those that are well below a capacity situation. His derivation of this relationship is based on the premise that vehicles do not collide and are operated in a safe manner. He then developed the equations to calculate space limitations or margin for safety.

The spacing, including the vehicle length and a clear space (between successive vehicles) of vehicles stopped in a queue averages about 22 to 25 feet ( 12,13 ). When vehicles are moving at the same speed the spacing is greater to ensure safety, and may be expressed as (4):

$$
\begin{equation*}
S \geq P+1.09 v \tag{2.4}
\end{equation*}
$$

where
$S=\underset{\text { front of adjacent vehicles; }}{\operatorname{minimum}}$ desiret, measured from front to
$P=$ minimum stopped vehicle spacing;
$V=$ velocity in ft/sec.
This equation includes the product of brake reaction time and velocity, plus a few feet for safety clearance. It is substantiated by the practical consideration of braking behavior and is approximated by:

$$
\begin{equation*}
s \geq p+v \tag{2.5}
\end{equation*}
$$

In general traffic flow, vehicles will not be likely to travel at the same speed. If the following vehicle is traveling at a higher speed than the lead vehicle, then the former has to reduce its speed to provide minimum spacing. The relationship, analyzed by Lewis (4), is shown diagrammatically in Figure 5.

If the lead vehicle maintains a constant speed throughout the maneuver, $\left(V_{j}^{\prime}=V_{2}^{\prime}\right)$, then:

$$
\begin{equation*}
s_{1}=p+v_{1}^{1}+\frac{1}{2 D}\left(v_{1}-v_{1}\right)^{2} \tag{2.6}
\end{equation*}
$$

where

$$
\begin{aligned}
S_{1} & =\text { minimum spacing } \\
V_{1} & =\text { velocity of lead vehicle; } \\
V_{1} & =\text { velocity of following vehicle } ; \\
D & =\text { rate of deceleration. }
\end{aligned}
$$



$$
v_{1}>v_{1}^{\prime}>v_{2}^{\prime}
$$

Figure 5. Factors Involved in the Spacing Relationship (4)

If the situation occurs that the lead vehicle decelerates to stop $\left(V_{2}^{\prime}=0\right)$, then the relation is:

$$
\begin{equation*}
S_{1}=P+\frac{1}{2 D}\left(v_{1}^{2}-v_{1}^{2}\right) \tag{2.7}
\end{equation*}
$$

## Starting Headways for Vehicles in a Stopped Queue

This is a short delay between the onset of a green signal phase and the actual movement of a vehicle into an intersection, involving both perception and response. The delay time from the beginning of green phase until the first vehicle in a queue moves into the intersection (rear wheels beyond cross-street curb line) may be assigned the term "starting headway." The study of Greenshields et al. (5), which is still considered applicable by Pignataro (19), showed that the average stārting headway is 3.8 seconds. The average headway between successive pairs of vehicles is shown in Table I.

TABLE I
TIME INTERVALS BETWEEN VEHICLES ENTERING A SIGNALIZED INTERSECTION (5)

| Vehicle <br> Number | Interval Between <br> Vehicles (sec) | Entrance Time <br> $(\mathrm{sec})$ |
| :---: | :---: | :---: |
| 1 | -- | 3.8 |
| 2 | 3.1 | 6.9 |
| 3 | 2.7 | 9.6 |
| 4 | 2.4 | 12.0 |
| 5 | 2.2 | 14.2 |
| 6 | 2.1 | 16.3 |
| 7 | 2.1 | 18.4 |
| 8 | 2.1 | 20.5 |
| 9 | 2.1 | 22.6 |
| 10 | 2.1 | 24.7 |

Bartle et al. (20) studied the starting delay of vehicles at 13 signalized intersections. They observed that mean starting delays range from 2.91 seconds to 4.40 seconds with an average of 3.83 seconds. They considered the remaining vehicles in the queue as a single platoon. The average time spacing, dividing the time for platoon movement by one less than the number of vehicles entering during that time, ranged from 0.95 to 1.63 seconds.

Capelle and Pinnell (21) studied the headways for queues entering signalized intersections at diamond interchanges. They found that the headways decrease rapidly for the first two vehicles in line with a lesser decrease for each succeeding vehicle. They then concluded that instead of using the ordinarily accepted general definition, starting
delay of a line of stopped vehicles can best be attributed to the reaction time and starting performance of the first two vehicles in line (as illustrated in Figure 6). Their observations yield a starting delay (for the first two vehicles) of 5.9 seconds and an average headway of 2.2 seconds.

Berry and Gandhi (17) studied the headways of compact platoon vehicles during peak hours. Their observation indicated significantly decreased values for both starting delay and headway during peak hours. The field data showed that starting delay ranges from 2.37 to 2.76 seconds and headway of the platoon ranges from 1.07 to 1.31 seconds. Analysis also indicated that the adverse weather significantly increased headways.

## Consideration of the Yellow Phase of a Traffic Signal

When the vehicle is approaching the signalized intersection, in some cases the driver may have difficulty in making a decision. If the green phase is displayed, he will proceed at about the same speed; if it is red, then he will have to decelerate and prepare to stop. However, if the signal indication is turning yellow, then he must decide whether to continue through the intersection or to stop. Gazis, Herman and Maradudin (18) described this zone on an approach to the intersection as a "dilemma zone." It is the zone in which the driver either has to speed up to clear the intersection on the yellow phase or decelerate at an uncomfortable rate to stop at the stop line. Field observation by Dart (1), as summarized in Table II, indicates that the driver's

TABLE II
A STUDY OF DRIVER RESPONSE TO YELLOW PHASE OF SIGNAL (1)

| Distance From <br> Intersection When <br> Yellow Phase, Starts | Approaching Venicles |  |  | Indicated <br> Probability |
| :---: | :---: | :---: | :---: | :---: |
|  | Number <br> That Stop | Percent <br> Stopping | Stopping |  |
| $0-40^{\prime}$ | 18 | 1 | $5.6 \%$ | 0.056 |
| $50-80^{\prime}$ | 17 | 5 | 29.4 | 0.294 |
| $90-120^{\prime}$ | 21 | 17 | 80.9 | 0.809 |
| $130-160^{\prime}$ | 21 | 19 | 90.5 | 0.905 |
| $180+$ | 41 | 41 | 100.0 | 1.000 |
| Totals | 118 | 83 | . |  |

HEADWAYS BETWEEN VEHICLES ENTERING INTERSECTION


Figure 6. Time-Headways Between Successive Passenger Vehicles (21)
decision depends on the distance between his car and the intersection proper when the yellow phase starts.

During peak hours, Berry and Gandhi (17) observed that about half of the yellow phase length is utilized by traffic. They termed this portion of the yellow phase as the "effective yellow."

## Acceleration and Deceleration Characteristics

The laws of motion can be applied to evaluate the relationship of vehicular operating characteristics including speeds, spacings, acceleration, deceleration, and stopping distances (3). For the vehicles moving straight, the formula of straight line motion is applied as follows:

Uniform motion, velocity constant:

$$
\begin{equation*}
S=V t \tag{2.8}
\end{equation*}
$$

Uniform accelerated motion:

$$
\begin{align*}
& V=V_{0}+a t  \tag{2.9}\\
& S=V_{0} t+\frac{1}{2} a t^{2}  \tag{2.10}\\
& V=V_{0}+\sqrt{2 a s} \tag{2.11}
\end{align*}
$$

where

$$
\begin{aligned}
& V_{0}=\text { initial velocity }, \mathrm{ft} / \mathrm{sec} ; \\
& V=\text { final velocity, ft/sec; } \\
& S=\text { distance in feet; } \\
& t=\text { time in seconds; } \\
& a=\text { acceleration, ft/sec }{ }^{2}
\end{aligned}
$$

A uniform rate of speed change is generally assumed under free flowing conditions. Although observed rates of acceleration are not
quite uniform, the uniform case was used in Lewis' simulation model and was considered to supply an adequate approximation of the real case. Greenshields (5) classified the different forms of speed change from his study of intersection performance. Lewis (4, p. 12) has simplified and summarized this study as follows:

1. A chronotropic acceleration is one where delay is independent of the time lost in speed change, such as a vehicle stopping for a red signal. Regardless of the time lost in stopping, the vehicle is still delayed until the signal turns green.
2. Functional speed change occurs when the loss of time is dependent on the rate of speed change, such as a bus stopping to discharge passengers.
Lewis (4) assumed an acceleration rate of $3 \mathrm{ft} / \mathrm{sec}^{2}$, while an average velocity of 30 miles per hour or $44 \mathrm{ft} / \mathrm{sec}$ was selected in his simulation model. This value is functional and used for the free-flow acceleration. When vehicles are under the pressure of traffic flows, higher rates of acceleration are used. For the case of vehicles accelerating from a stopped or near-stopped condition at stop signs or signals, and also the case of left turn maneuvers, these vehicles must accelerate rapidly to take advantage of available gaps in the traffic stream. For these cases accelerations of 6,5 and $4 \mathrm{ft} / \mathrm{sec}^{2}$ were assumed for the first three queued vehicles, respectively. The freeflow acceleration of $3 \mathrm{ft} / \mathrm{sec}^{2}$ was applied thereafter.

One study of vehicle acceleration (60) indicated that maximum accelerations up to $14.67 \mathrm{ft} / \mathrm{sec}^{2}$ ( $10.0 \mathrm{mi} / \mathrm{hr} / \mathrm{sec}$ ) were obtained from the field. It is believed that about $10 \mathrm{ft} / \mathrm{sec}^{2}$ is the limiting value for comfort if maintained for any length of time, and that at least one-half second should be used to change from zero acceleration to $10 \mathrm{ft} / \mathrm{sec}^{2}$ (6).

For vehicles decelerating to a stop, previous studies have shown that the maximum deceleration rate of vehicles varies from 20.2 to 28.9 $\mathrm{ft} / \mathrm{sec}^{2}(3)$. These figures are much higher than any observed under ordinary conditions and those used in mos.t simulation models.

The deceleration rates should not be determined by the vehicle itself, but by passenger reaction. Deceleration rates greater than those now practically applied are very probably not desirable because of human limitations and response. The limitation is the length of time required by an individual to adjust himself to externally applied forces. The National Safety Council has adopted a deceleration rate of $17 \mathrm{ft} / \mathrm{sec}^{2}$ as the maximum for comfort (7). It is found that practical values of deceleration used in every day traffic conditions range from 4.84 to $7.77 \mathrm{ft} / \mathrm{sec}^{2}(60)$. Wilson's studies (6) showed an average deceleration rate of passenger vehicles with relatively unimpaired comfort for their passengers to be $8.55 \mathrm{ft} / \mathrm{sec}^{2}$. Additional values of deceleration rates cited by Baerwald (3, p. 26-27) are:

1. $11 \mathrm{ft} / \mathrm{sec}^{2}$--considered undesirable but not alarming to passengers.
2. $14 \mathrm{ft} / \mathrm{sec}^{2}$--packages may slide off the seat, and the occupants of the vehicles find this rate uncomfortable.
3. above
$20 \mathrm{ft} / \mathrm{sec}^{2}$--the occupants must brace themselves firmly to avoid being thrown off the seat, will be used only in emergency situations.

## Stopping Performance

There are two types of stops that occur at the intersection, stoppint first in line at the intersection and stopping behind another stopped vehicle. It is accepted in practice that the use of a constant
deceleration stopping model is realistic. When they have the choice, drivers tend to decelerate at an approximately constant rate throughout the duration of their stops (11). Based on the motion equations with uniform deceleration, Equation (2.11) can be expressed for each time increment as (4):

$$
\begin{equation*}
v_{t}^{2}=2 D(X-Z D) \tag{2.12}
\end{equation*}
$$

where

$$
\left.\begin{array}{rl}
V_{t} & =\text { velocity at time } t ; \\
D & =\text { deceleration rate; } \\
X & =\text { the distance between the vehicle at time } t-1 \text { and the } \\
& \text { stopping point; }
\end{array}\right] \begin{aligned}
& Z D=\text { the distance traveled during one time increment. } \\
& \text { Equation (2.12) has been further analyzed by Lewis (4) to obtain }
\end{aligned}
$$ the stopping restriction related to the velocity of vehicle at time $t-1$, when the vehicle starts to decelerate. Finally, the relationship becomes:

$$
\begin{equation*}
Z D=\frac{1}{2} v_{t-1}-\frac{D}{4}+\left[\frac{D^{2}}{16}-\frac{D}{4} v_{t-1}+\frac{D}{2} x\right]^{1 / 2} \tag{2.13}
\end{equation*}
$$

where

$$
V_{t-1}=\text { velocity at time } t-1
$$

## Turning Performance

Vehicles that desire to turn left or right at an intersection at some point must abandon free-flow operating and accept the turning schedule. They should not be operated in excess of a maximum safe speed during the turn. Maximum turning velocity is related to turning radius and side friction by the equation:

$$
\begin{equation*}
V_{\max }=\sqrt{f g r} \tag{2.14}
\end{equation*}
$$

where
$V_{\text {max }}=$ maximum turning velocity, $\mathrm{ft} / \mathrm{sec}$;
$\mathrm{f}=$ coefficient of friction;
$r=$ turning radius;
$\mathrm{g}=$ acceleration of gravity.
During this maneuver it is assumed that a free-flowing vehicle will decelerate uniformly up to a point during the turn which is called "turn point" (4). Once past the turn point the vehicle is free to accelerate normally. Vehicles having a high initial speed start decelerating at some point prior to turning and start to accelerate at some point during the turn, while the vehicles with low speed may accelerate throughout the entire turning maneuver.

It has been observed from previous field observations (14, 15, 16) that the maximum velocity at the turning point is about $15 \mathrm{ft} / \mathrm{sec}$. Since turning speeds depend on the turning radius, there is a tendency to use a slower turning speed for right turns than for left turns due to the shorter turning radius available. In the case of lack of interference for right turns, the opposite may occasionally be true.

## Gap Acceptance for Left Turn Maneuver

When approaching a signalized intersection without a separate left-turn phase, the left-turning driver has to evaluate the gap sizes in the opposing traffic stream and select an opening that is large enough to cross through safely. Acceptance of a gap suitable for attempting the left-turn maneuver depends on the characteristics of
driver, intersection, and traffic situation (22), so that accepted gaps will not be the same size.

The waiting driver considers each gap, $h$, in the opposing traffic stream. He will either cross (accepts the gap if $h \geq \tau$ ) or wait (rejects the gap if $h<\tau$ ). The value of $\tau$, the critical gap, was assumed to be a single constant value by early theorists (23).

Kaiser (24), from a study at an unsignalized intersection, found that the smallest gap accepted was 3.75 seconds and the largest gap rejected was 4.75 seconds. Noblitt (25) showed that acceptable gaps for left-turn truck combinations were 1.4 to 1.8 times as large as the required gap for passenger cars, and 1.2 to 1.5 times as large as the required gap for single-unit trucks. Kell (26) summarized the data from 500 field observations on two-land two-way streets. His left-turn gap acceptance distribution is shown in Table III.

TABLE III
GAP ACCEPTANCES BY LEFT-TURN VEHICLES, TWO-LANE, TWO-WAY STREETS AFTER KELL (26)

| Gap Size | Cumulative <br> Percent Accepting | Gap Size | Cumulative <br> Percent Accepting |
| :--- | :---: | :---: | :---: |
| $<1.0 \mathrm{sec}$ | 0 | $\leq 5.0 \mathrm{sec}$ | 94.7 |
| $\leq 1.5$ | 1.4 | $\leq 5.5$ | 96.4 |
| $\leq 2.0$ | 10.2 | $\leq 6.0$ | 97.9 |
| $\leq 2.5$ | 18.3 | $\leq 6.5$ | 98.2 |
| $\leq 3.0$ | 31.3 | $\leq 7.0$ | 98.5 |
| $\leq 3.5$ | 50.0 | $\leq 7.5$ | 99.3 |
| $\leq 4.0$ | 64.6 | $\leq 8.0$ | 99.4 |
| $\leq 4.5$ | 85.3 | $>8.0$ | 100.0 |

Solberg and Oppenlander (27) studied the lag and gap acceptances for drivers entering and crossing a major roadway from a stopped position. They observed that the overall median acceptance time for leftturn movements was 7.82 seconds. The distribution of this study is illustrated in Figure 7.

At signalized intersections, the left-turn critical gaps, as shown by Behnam (22), are depicted in Figure 8. The point of intersection of the two curves in this picture represents the average critical gap, which is 4.5 seconds.

The speed of vehicles is an important factor in considering the gaps to be acceptable for a driver. In all cases, the driver of a stopped vehicle will require a larger size of gap than the driver of a moving vehicle. Figure 9 (23) illustrates the results of data gathered by Texas Transportation Institute on several Texas freeways to analyze gap acceptances for moving and stopped vehicles merging at the freeway entrance ramp.

Weiss and Maradudin (28) developed a method of treating gap acceptance delay which accounts for driver impatience. They believed that the size of acceptable gap is reduced as delay increases. Instead of a constant size of acceptable gap, $\tau$, originally desired by the drivers, they will probably accept a shorter gap. The probability of a driver accepting a gap of size $H$ after the $i$ th vehicle has passed is $F_{i}(H)$, or

$$
F_{0}(H) \leq F_{1}(H) \leq \cdot \cdots F_{i}(H) .
$$

Wagner (29) studied the gaps and lags that were accepted by the driver of a side-street vehicle stopped at the stop sign, waiting to enter the intersection. He compared the gap acceptance distribution


Figure 7. Distribution of Accepted and
Rejected Lags and Gaps at Intersection Left Turns
(27)


Figure 8. Cumulative Distribution of Accepted and Rejected Gaps at Signalized Intersections (22)


Figure 9. Gap Acceptance of Merging Vehicles (23)
for right-turn, straight,, and left-turn vehicles, as shown in Figure 10. This analysis indicated no significantly different results among these maneuvers.

Dart (30) collected his field data about various types of gap acceptances, as shown in Figure 11, on four-lane approach signalized intersections. He indicated the relationships as shown in Figure 12. This research also indicated that there is the probability of 0.145 or $14.5 \%$ that the first vehicles of the left turn channelization queue will make the turn before the opposing traffic enters the intersection when the signal turns green. This action is termed "jump-the-gun."


Figure 10. Effect of Direction of Side Street Vehicle Movement on Gap Acceptance Distribution (29)


Figure 11. Opposing Traffic Stream Gap Types
Confronting Left-Turn Vehicles
(30)


Figure 12. Probability of Left-Turn Vehicle Accepting Gap From Stopped Position at Signalized Four-Way Intersections (30)

## CHAPTER III

## INTERSECTION FIELD STUDIES

## Objectives of the Studies

The prime purpose of this simulation program is to represent the real traffic condition for any street intersection having one or two lane approaches at right angles to each other. Although the computer program may be operated with artificial input traffic data, actual field data, if available, is more authentic and leads to more realistic results. Previous field observation studies have indicated that it is not unusual to find that the data from field observations may be far different than the theoretical traffic distributions appearing in the traffic literature. In any simulation model, the first thing one must do to get correct and accurate results is to supply the right input data. It is therefore important for this model that all traffic characteristics of the intersection under consideration agree with the actual conditions there. In addition to the data collected for input of the program, field observations also supply statistical data such as queue length and delay time distributions, used to check output results.

Most former researchers who have employed traffic intersection simulation $(38,42,46)$ have obtained the vehicle delay as their principal "figure-of-merit." Only two have actually compared simulation output with actual field studies. Lewis (4) observed data from actual
intersections and tried to compare his simulation results with the actual field delays, but found that it was impossible to correlate conditions. Dart (1) measured delays in field studies at several intersections in Texas. These delays were then compared with delays obtained from simulation studies. He reported that correlation was obtained in roughly one-half of the intersections.

Field observations yield the following data:

1. Beginning of the green signal phase.
2. Length of the cycle.
3. Time each vehicle enters the system.
4. Type of vehicle: passenger car, single unit truck, etc.
5. Speed of those vehicles, passing through the intersection without delay.
6. Whether the vehicle was stopped by the signal.
7. Starting delay after the start of green signal phase, and headway of the following vehicles.
8. Number of stopped vehicles in the queue for each signal cycle.
9. Percent of turning vehicles.
10. Total time each vehicle appears in the system: including the stopped delay, delays during acceleration and deceleration, and the traveling time.
11. Total vehicles in each lane during period being studied.

Study Method Selection

Based on experience from field studies, Dart (1) believed that the most satisfactory and economical study procedure, from both field study and data analysis time standpoints, was the time-lapse photography
technique. Cribbins and associates (59), who conducted urban traffic control studies in North Carolina, also found that time-lapse equipment provided the ability to record on film a very precise, quantitative account of specific traffic variables, such as speed, volume, density, headway, merging, and weaving. With limited amount of funds and time for the research, the time-lapse photography technique is considered the most suitable to collect all necessary data. Most of the field data therefore were collected via this procedure.

In addition to the above method, stop watches also can be used to get data from which more precise and accurate results are needed, such as starting delay and traveling time across the intersection proper. While the time-lapse photography method with frames exposed at 1 second intervals provides an accuracy of $\pm 0.5$ second, a stop watch, on the other hand, can be read to 0.01 second.

## Equipment and Time-Lapse Procedure

A Nizo S-80 Schneider Verigon time-lapse camera was used to collect most data. This camera uses Super-8 film cartridges and is powered by six 1.5 volt batteries. The camera can take automatically exposed pictures at rates of one frame per minute to 54 frames per second. The appearance of the camera is illustrated in Figure 13 (a).

The time-lapse controller dial that is used for setting the filming rate is not accurately calibrated from the factory, so it is left to the operator to check with a stop watch prior to the operation. This is a disadvantage of using the camera in this research. Since it is very difficult to set the film rate exactly as desired, calibration required

(a) Nizo S80 Camera

(b) Kodak Stop-Action Projector

Figure 13. Time-Lapse Photography Equipment
extra time for summarizing the data. Once the framing rate is set, filming will continue without variation.

Kodak Kodachrome II film in Super-8 cartridges was used in all filming. Color film enables the viewers to more readily identify the phase and cycle changes of traffic signals and to recognize the moving vehicles more easily.

Data from the color films were projected manually by means of a Kodak Ektagraphic MFS-8 projector, as illustrated in Figure 13 (b). This projector can be operated at various speeds or in the still mode for a single frame analysis. The latter is the one used in this research. The projector lamp, with average life of 12 hours, is air cooled and film can be viewed indefinitely in the still mode without burning.

During the filming process, the camera was set up on a tower of a church within 500 feet of the intersection being studied. The single frame button on the camera was set at about 1 second intervals. A clock was included in the field of view to establish time of the day and provide a check on the frame interval obtained.

This technique provides time measurements to an accuracy of $\pm 0.5$ second after calibration. One advantage of the method is that the traffic data from the intersection is permanently available and complete analysis of a situation can be obtained by running and rerunning the film through a projector.

## Use of Stop-Watches

While observing the field data by means of stop-watches, three observers in a parked car at a corner of the intersection near the traffic lane being studied were used to observe data from individual
vehicles. Each observer simultaneously studied different vehicles for the same variable, such as the starting delay of the first vehicles in queue, etc. When the signal phase turned green, a stop-watch was started counting and was stopped when the rear wheel of the first vehicle in that queue crossed the stop line and entered the intersection proper. The time recorded was the starting delay. Similarly, the headway of the following vehicles, according to their positions in the queue, was considered as the interval of time between successive vehicle crossings of the stop line.

The stop lines on each lane of the pavement are also used as reference points in observing the traveling time across the intersection for through, right-turn, and left-túrn vehicles. Despite the different lengths of vehicles, the position of the rear wheels was always used to represent the position of that vehicle.

## CHAPTER IV

## RESULTS OF FIELD STUDIES

The intersection at W. Sixth Avenue and S. Duck Street in Stillwater, Oklahoma was the selected site for field observations. This intersection is a typical one, similar to that shown in Figure 1, with two lanes in each approach and additional left-turn lanes. The field data were observed between 4:30 p.m. and 5:30 p.m. in April, 1975. There is a small percentage of trucks that may increase the delay during this period and were ignored in this study. It was also observed that there is no pedestrian interruption affecting the right-turn vehicles.

The approximate width of each approaching lane is about 11 feet, while the length of the separate left-turn lane is about 100 feet. Parking is prohibited on all approaches. The stop-lines for vehicles are about 5 feet back from the pedestrian crosswalk, but the obscure markings tended to lead first vehicles in the queues to stop at the crosswalk lines.

Because of limited observation sites for taking the time-lapse movies, traffic in each direction was taken on different days. The sites for the camera setting were two church towers about 300 feet away from the intersection. The reference lines, for the entry of the vehicles, were set at different distances from the intersection to best fit the capability of the camera angle. Since there is more traffic on W. Sixth Avenue, these reference lines were set at 300 feet from the
stop lines on each approach. They are 100 feet and 175 feet on S. Duck Street for southbound and northbound traffic, respectively.

The fixed-cycle traffic control system has traffic-actuated left turn phases. Alternative cycle lengths are 60 and 80 seconds, with equal time for each street. There is a separate left-turn phase after the through traffic signal, but it is automatically omitted if there is no vehicle on left-turn lane by the time the left-turn phase should turn green.

## Starting Delay and Headways

According to the summarized data in Appendix A, the average starting delay of the first vehicles in a queue is observed to be 3.26 seconds for the straight-through vehicles, and 3.58 seconds for the left-turn vehicles. These figures are assumed to be applicable to all approaches since their geometrics are identical.

The headways of the following vehicles are listed:

| Position of Vehicles <br> in Queue | Through and Right-Turn <br> Vehicles (Seconds) | Left-Turn Vehicles <br> (Seconds) |
| :---: | :---: | :---: |
| 2nd | 2.55 | 2.49 |
| 3rd | 2.39 | 2.20 |
| 4th | 2.19 | 2.07 |
| 5th | 2.23 | 1.92 |

As compared to the critical headway of 1 second, the above figures show that the drivers here are not in a hurry, probably because there are not too many vehicles in queues. The headways are decreased successively because of increasing speed, and believed to be constant after the 5 th vehicle. Decreasing headway in left-turn lane is sharper because of the short time phase of signal for these vehicles.

## Traveling Time Across the Intersection

One purpose of the study is to observe the actual time required for the vehicles to pass the 55-60 feet width of the intersection proper. The details of results from each approach are shown in Appendix B, from which the average values are shown in Table IV.

TABLE IV
AVERAGE TRAVELING TIME FOR VEHICLES TO CROSS THE INTERSECTION PROPER

|  | Position of Vehicles in Queue |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Types of <br> Vehicles | Non- <br> Stop | 1st | 2nd | 3rd | 4th | 5th |
| Right-turn | 1.70 | 1.92 | 1.98 | 1.32 | 1.65 | 1.25 |
| Through | 2.13 | 2.80 | 3.21 | 2.99 | 2.86 | 3.03 |
| Left-turn | 2.80 | 2.80 | 3.05 | 3.19 | 3.05 | -- |

It is apparent from Table IV that there is not much difference for right-turn vehicles in any position in the queue since they have to slow down before making the turn, as is also the case for left-turn vehicles. After starting delay of about 3.26 seconds, the first straight-through vehicle in the queue can pass the intersection more quickly than the following cars because there are not any obstacles in sight. The driver can accelerate his vehicle at will up to the desired speed, while the speeds of the following vehicles are constrained by
preceding ones, and may have to decrease speed if the preceding car makes a right turn.

The non-stop vehicle is one that arrives at the intersection during a green signal phase and can go on without stop.

## Turning Traffic

Table $V$ summarizes results of field observations of turning traffic in each approaching lane. There are high percentages of turning vehicles in most approaching lanes.

TABLE V
PERCENTAGE OF TURNING VEHICLES

| Direction <br> of Traffic | Lanes | Total <br> Vehicles | Right-Turn <br> Vehicles | Left-Turn <br> Vehicles | Percentage |
| :--- | :--- | :--- | :---: | :---: | :---: |
| Southbound | outside <br> inside | 175 | 65 | -- | 37.1 |
|  | outside | 321 | -- | 119 | 37.1 |
|  | inside | 275 | 121 | -- | 36.7 |
| Northbound | outside | 234 | -- | 28 | 10.2 |
|  | inside | 334 | -- | -- | 12.0 |
| Eastbound | outside | 443 | 116 | -- | 39.8 |
|  | inside | 413 | -- | 124 | 26.2 |

## Traveling Time of Vehicles From Reference Lines Until Leaving the System

The traveling time of each individual vehicle, starting when it passes the reference line until it moves past the intersection proper, was observed by analyzing the recorded movies frame by frame. These results are calculated separately for vehicles moving through, making a left turn, or making a right turn. The purpose is to provide field data to compare with the results of the computer simulation program. Differences in traveling time are affected by the characteristics of the vehicles, starting delay, stopping delay, and also the position of vehicle in the stopped queue when the signal phase turns green (Appendix D).

## Vehicle Arrival Time*

Arrival time at the reference line for each individual vehicle is recorded by using the single frame movie photographic method of about 1 second per frame. The distributions of the arrival time fit very well with the shifted exponential distribution. This agrees with previous work (2) using this method, with the physical length of cars and minimum following distance by drivers being considered.

As previously mentioned, many traffic engineers in the past have concluded that general traffic flow patterns are likely to follow some type of Poisson distribution which may be generally expressed as:

[^1]\[

$$
\begin{equation*}
P(x)=\frac{m^{x} e^{-m}}{x!} \tag{4.1}
\end{equation*}
$$

\]

where

$$
\begin{aligned}
m & =\text { mean of observed data; } \\
x & =\text { number of successes; } \\
P(x) & =\text { the probability of exactly } x \text { successes } .
\end{aligned}
$$

Since the arrival rate of vehicles deals with counting distributions for discrete events (arrivals of vehicles) within a given time interval, the distribution of gaps (time spacing) between vehicles is a continuous variable and is treated by means of interval distributions. Of possible distributions, the best known is the (negative) exponential distribution (2). The value of $m$ in the Poisson distribution is replaced here as follows:

$$
\begin{equation*}
m=\frac{V t}{3600} \tag{4.2}
\end{equation*}
$$

where

$$
V=\text { hourly volume; }
$$

$\mathrm{t}=$ length of each observation in seconds.
Thus,

$$
\begin{align*}
& P(x)=\left(\frac{V t}{3600}\right)^{x} e^{-\frac{V t}{3600}} \\
& P(0)=e^{-\frac{V t}{3600}} \tag{4.3}
\end{align*}
$$

If there are no vehicles in a particular interval of length $t$, then there will be a gap of at least $t$ seconds between the last previous vehicle and the next vehicle. This means that $P(0)$ is also the probability of a gap equal to or greater than $t$ seconds, which may be expressed as:

$$
\begin{equation*}
P(g \geq t)=e^{-\frac{V t}{3600}} \tag{4.4}
\end{equation*}
$$

where

$$
m=\frac{V t}{3600}
$$

is the mean of the arrival (counting) probability distribution.
It may be seen, from this relationship, that the number of gaps greater than any given value will be distributed according to an exponential curve.

Now, if we set

$$
\begin{equation*}
m=\frac{t}{T} \tag{4.5}
\end{equation*}
$$

then
$\mathrm{T}=$ the mean of the interval (gap) probability distribution.
Thus, the probability of a gap equal to or greater than $t$ may be written:

$$
\begin{equation*}
P(g \geq t)=e^{-t / T} \tag{4.6}
\end{equation*}
$$

or in reverse probability as:

$$
\begin{equation*}
P(g<t)=1-e^{-t / T} \tag{4.7}
\end{equation*}
$$

If we include gaps of size smaller than some value, say $\tau$, this situation can be represented by shifting the exponential distribution by an amount of $\tau$. The equation now becomes

$$
\begin{equation*}
P(g<t)=1-e^{-(t-\tau) /(T-\tau)} \tag{4.8}
\end{equation*}
$$

The minimum arrival time observed in the field is about 1 second, and thus $\tau=1$ is used in the above equation to evaluate the interval probability distribution in this study. All results are summarized in Appendix C.

## Vehicle Speed

The speeds of the free flowing vehicles, without any interruptions while moving in the system, were observed by playing and replaying the individual frames of the time-lapse movie. The total time of each vehicle, as determined by the number of frames in which it appears in the movie, divided by the distance, results in vehicle speed. Cumulative speed distribution for each approaching lane is shown in Appendix E. Most of the distributions, except the observed speeds of the southbound vehicles, have a median value between 32.5 and $40 \mathrm{ft} / \mathrm{sec}$ and have distribution shapes similar to that used in Dart's model (1). The southbound vehicles showed considerably slower speed with the median of about $25 \mathrm{ft} / \mathrm{sec}$, while the design speed for all approaches is $41 \mathrm{ft} /$ $\sec (28 \mathrm{mi} / \mathrm{hr})$. There is no obvious reason to explain slower speed in this direction.

## CHAPTER V

## THE SIMULATION MODEL

The purpose of the traffic simulation model is to produce realistic results economically. The movement of traffic in and near a signalized intersection is a very complex operation, which tends to be oversimplified if this operation is represented mathematically. The use of simulation techniques, however, permits the analyst to build any degree of realism that he wishes into the intersection model. However, in developing a simulation model, it is unwise to build a perfect representation of the real intersection. Not only is such perfection difficult and time-consuming to obtain but the resulting model will likely be very inefficient (4). Therefore, a simulation model should be employed which will adequately represent the most important operating characteristics and ignore the unusual or insignificant events.

Since the primary objective of this research is to study the delays caused by traffic congestion and signalization, the simulation model will not represent realistically those characteristics of vehicles and drivers which do not significantly affect the delays. GPSS language is chosen because, in the writer's opinion, its program statements are powerful. In other words, one statement in GPSS can represent many things at the same time. Furthermore, this language provides some built-in statistical parameters which adequately fit the traffic data requirement. It
therefore results in simpler and more efficient programs in terms of computer time to real time ratio.

## Mode of Representation

There are certain specific block types in GPSS language that are analogous to the pattern of traffic flow in the roadway. The general representations can be briefly described as follows:

The "generate" blocks are used to represent the arrival of vehicles at the entrance to the system. Vehicles are "created" and sent into the system at the precalculated intervals. Many "function" blocks are used to meter the vehicle arrivals, usually in the form of statistical distributions.

Each vehicle is represented by a "transaction" created from the generate blocks. Once leaving the generate block, a transaction will be assigned its own behavior, such as speed, turning maneuver, marked time when entering the system, etc. This transaction will try to move as far as possible without violating physical constraints, similar to a real vehicle on the roadway, until it passes through the intersection and leaves the system. Along each approaching lane to the intersection, a transaction may be interrupted by preceding slower transaction, by the traffic signal, represented by "logic" blocks, and by the queue of stopped transaction which are represented by a "user chain." The traveling times of vehicles having assigned speeds, acceleration and deceleration, turning speeds, etc., are supplied by "variable" blocks according to the immediate condition a vehicle is dealing with. These traveling times are controlled by the use of "advance" blocks. "Group" blocks are used
along with the user chains to determine the queue length in each cycle of the signal.

By this means, each transaction in the model will act analogously to the average driver-operated vehicle. It may be noted that in actuality, not all drivers are average, but will make driving decisions based on many individual characteristics and state of mind. However, the computer transactions always act in an identical manner.

## The Basic Form of the Model

The simulation model used in this research represents the traffic operation at a single signalized intersection. The model admits one or two approach lanes plus one additional left-turn lane, where desired. The computer program is separated into two parts: the traffic control program and the traffic flow program.

1. Traffic control program. This program simulates the traffic signal in all four directions. For easier handling and adjustment when signal complexity increases, each signal direction is separately represented. This permits the user to trace the signal simulation in one direction in the same way the drivers observe the signal. The control system can employ two-phase or three-phase signals, or may be adjusted to any type of signal that is possible to be installed at the studied intersection.
2. Traffic flow program. This program simulates the vehicular traffic from all approaching lanes (maximum of eight lanes). Traffic is represented for a distance back from each approach stop line. This distance is the length along the approach lane sufficient to permit an entering vehicle to stabilize its behavior before reaching any of the
critical points in the lane. In addition, this length is necessary to provide storage room when demand volumes increase and the queuing has been built up. This section of roadway may be called "zone of influence," since vehicles in the zone are influenced by any intersection congestion. It is bounded by the "reference line" and the "stop line" (see Figure 14).

A vehicle enters the system when it crosses the reference line (or entrance), triggering the travel timer for this vehicle. If this vehicle is not in a platoon, affected by the previous signalized intersection, it may move at its desired constant speed. When there is a preceding slower vehicle, the following one must decelerate and join the platoonlike stream. The arriving vehicle will slow down to join the line when there is a queue of vehicles waiting for the green signal. If there is no queue, the arriving vehicle will check the signal and will enter the intersection at the same speed during a green signal, or decelerate to stop at the stop line during the red phase of the signal, to be the first vehicle in the queue. If the vehicle is making a right turn it will check the acceptable gap for a right turn on red, or it may wait for the next green phase. Once a vehicle has entered the intersection and reached the second stop line, on the leaving lane, it is considered out of the system and no longer has any effect on other vehicles still in the system.

## Assigned Intersection System Geometry

The principal geometrics of the intersection system, where separate left-turn lanes are provided, are shown in Figure 14. Key points for


Figure 14. An Intersection Module and Vehicle Paths
approaching vehicles are located by the reference lines and stop lines. The system consists of the two elements:

1. Intersection cells. The intersection is divided into a "checkerboard" arrangement of cells of similar size, with the exception of separate left-turn lanes which are considered as special and extra cells. The boundaries of each of these cells are determined by the region formed by pairs of intersecting lanes in the intersection. In the special case where there is a separate left-turn lane, two additional cells, for example $\mathrm{C}_{27}$ and $\mathrm{C}_{28}$ in Figure 14, are included and utilized by left-turn vehicles only. For other than left-turning vehicles these two cells are considered as parts of cells in the inner lane: cells $\mathrm{C}_{14}$ and $\mathrm{C}_{15}$.
2. Lanes. Each approaching lane is assigned a different number to go with the symbol of the lane, $\mathrm{L}_{11}, \mathrm{~L}_{12}$, etc., denoting the different lanes. For the case where only one lane exists in any direction, the inner lane is used and vehicles can make the right turn from this lane.

## Simulation of Signal Control

Traffic in the system is controlled primarily by the settings of the signal control box dials. Usually, variation in signal settings include:

Signal Cycle Length--total time for a single sequence of red, yellow and green lights.

Splits--percentage of signal cycle length for the red, yellow and green periods.

Offsets--percentage of cycle length for initial synchronization of consecutive traffic signals to maintain an uninterrupted flow.

In the simulator signal, control for each direction of traffic is accomplished by a signal control loop (as shown in Figure 15). An independent program generates a signal "regulator" for each traffic phase in each direction. The regulators circulate in the signal control loop, turning the signals on and off at fixed or calculated intervals. Vehicles arriving or waiting at the intersection must test a red signal associated with the phase; they cannot enter the cells until the signal has turned green. There is one exception: the right turn is permitted on red phase with an acceptable gap. Yellow signal time is included in the total green time.

## Simulation of Vehicles

Inter-arrival times for vehicles entering the system are generated by a shifted exponential distribution (based on Poisson arrivals). The assumption of Poisson arrivals has been found to be reasonably representative of actual traffic conditions when traffic is light and when the effect of a previous signal is negligible. In heavy traffic and/or where a prior signal is of considerable consequence (vehicles usually arrive in platoons at an almost uniform rate), observed arrival distributions may be substituted for the assumed distribution. Different "function" blocks were formed to represent the inter-arrival times for each lane of traffic.

For realistic simulation of the traffic stream, traffic in each lane was programmed independently. Vehicles in different lanes have different paths and appear in different places in the program. This allows the standard statistical outputs to be examined and traced individually for each lane. Characteristics of vehicles on inside lane and


Figure 15. Signal Control Loop (3 Phase Cycle)
outside lane were programmed a little differently, as shown by flow charts in Figures 16 and 17. The difference concerns the turning maneuver and checking for the left-turn lane.

Upon entering the network, a number of operating characteristics are assigned to individual vehicles in the system, velocity from observed distribution is assigned to the vehicle until the vehicle's free flow is inhibited by a preceding vehicle or signal light. If the vehicle overtakes a preceding one, it assumes the slower vehicle's speed. Changing lanes near the intersection rarely occurs, except when blocked by a vehicle waiting for a left-turn opportunity. This will be ignored in the program. The decision of the driver to go straight through or make a turn is also assigned to the vehicles.


Figure 16. Outside Lane Vehicle Flow


Figure 17. Inside or Single Lane Traffic Flow

## CHAPTER VI

## SIMULATION RESULTS

The principal purpose of the simulation model is to provide output consisting of mean queue lengths and mean traveling times for traffic from each approaching lane of the studied intersection, using any particular set of input data. It requires several sets of results for comparison and evaluation in order to determine the best possible choice of signal cycle phase lengths. The first run usually employs actual signal times currently in use at the intersection. The output thus shows the efficiency of present traffic situations and control signals. Succeeding sets of data, in the direction of possibly decreasing the mean traveling times and/or mean queue lengths, may be programmed to run separately or, by the use of reset procedures, may provide a series of solutions.

The simulation model also tabulates data, for checking purposes, on the arrival time and speed distributions of traffic from each approaching lane. Likewise, the accuracy of the program in representing turning data may be traced from the block statistics, supplied as the standard output for GPSS (as demonstrated in Appendix F).

## Typical Simulation Output

All the computer outputs are in the form of statistical distributions which include the mean values and standard deviations, separately
determined for each lane of traffic. The results include the distributions of queue length, traveling time, speed, and arrival times of vehicles. Appendices $G$ through $L$ contain sample computer output sheets. Also included are examples of the built-in standard statistical output associated with clock and block entities as shown in Appendix F. These are useful for the purposes of tracing each step of the program and also checking certain parameters, such as the percentage of turning vehicles.

## Validation of Simulation Model

In writing this computer program, the writer tried to formulate a model which would reflect all of the important traffic parameters of a signalized intersection, as well as take cognizance of those minor parameters which may not significantly affect the final results. Previous investigators using nominal input (e.g., 10 percent turning volume) for their models $(1,4)$, have found that their results were hardly comparable to the field observations. This was because their models permitted only a few input data values, and depended on assumptions to fill in the remaining parameters. The intersection traffic was therefore not adequately represented. The writer believes that any specific intersection will have unique conditions and characteristics of its own. The model used to evaluate a specific intersection should be able to represent these characteristics.

For reality in evaluating the selected intersection, all characteristics and statistics collected from the field were used as the input of the program. These values appeared in the INITIAL, VARIABLE, and FUNCTION cards in the first part of the source program.

## Check of Random Distributions

The first part of the checking procedure deals with the goodness and accuracy of random numbers generated by the GENERATE blocks in the model. Since these numbers are important to represent the correct statistical input, different sets of random numbers may have to be used for groups of data.

Appendix $C$ contains comparisons between computer generated and observed arrival-time distributions. Results show that the distributions from field observations, theoretical shifted-exponential distribution, and the values supplied by the model all agree very well.

In Appendix E, the distributions of vehicle speeds, observed from the field, are compared with those generated in the model. Even though in most lanes the generated values in the model are somewhat higher than those observed, they may be considered as being in good agreement.

Percentage of turning vehicles is the last test of the accuracy that the model GENERATE blocks can supply in accordance with a set of input data. Table VI shows the comparison of percentage of turning traffic between the observed values which are used as input data, and the values generated in the model. The greatest deviation is $+4.8 \%$ for the southbound, right-turn traffic, while the smallest deviation is $-0.4 \%$ for the westbound, right-turn traffic. The comparisons here also indicate reasonable agreement.

## Tests of Output Results

The queue length and traveling time are the most important outputs that derive from the model. These values were thus compared with field

## TABLE VI <br> COMPARISON OF TURNING VEHICLES BETWEEN FIELD dATA AND THE SIMULATED VALUES

|  |  | Percent Turning Vehicles |  |  |
| :--- | :--- | :---: | :---: | :---: |
| Direction | Type of Turn | Observed | Simulated | Differences |
| Southbound | Right-turn | 37 | 41.8 | +4.8 |
|  | Left-turn | 37 | 35.0 | -2.0 |
| Westbound | Right-turn | 36 | 35.6 | -0.4 |
|  | Left-turn | 10 | 9.0 | -7.0 |
| Northbound | Right-turn | 12 | 15.5 | +3.5 |
|  | Left-turn | 40 | 37.6 | -2.4 |
| Eastbound | Right-turn | 26 | 27.3 | +7.3 |
|  | Left-turn | 30 | 27.5 | -2.5 |

observations under similar conditions. For the northbound traffic, the comparison was made for a signal cycle of 80 seconds, while other approaches were compared when the signal cycle was 60 seconds.

Table VII gives the values of average queue length and also the standard deviation for each traffic approach. It is noted that, for each approach, the simulated queue length is a little smaller than that observed in the field. Because of light traffic at the selected intersection and the resulting short queues, the percentage differences are magnified while the absolute differences are very small.

Like the queue lengths, the mean traveling times as shown in Table VIII generally indicated smaller simulation values than the observed values, the differences averaging 10 percent. Standard deviations were in somewhat closer agreement. This amount of difference between actual and simulated values is not unexpected when dealing with phenomena as variable as traffic.

TABLE VII
COMPARISON OF MEAN QUEUE LENGTHS

| Direction | Lanes | Nean Queue Lensth |  | Differences | Standard Deviation |  | Differences |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Observed | Simulated |  | Observed | Simulated |  |
| Southhound ${ }^{\text {l }}$ | Outside Inside Left-turn | $\begin{aligned} & 1.84 \\ & 2.40 \\ & 2.34 \end{aligned}$ | $\begin{aligned} & 1.81 \\ & 2.00 \\ & 1.80 \end{aligned}$ | $\begin{aligned} & -0.03 \\ & -0.40 \\ & -0.54 \end{aligned}$ | 1.23 1.24 1.43 | 1.29 1.59 1.45 | $\begin{aligned} & +0.06 \\ & +0.35 \\ & +0.02 \end{aligned}$ |
| We stbound ${ }^{1}$ | Outside <br> Inside <br> Left-turn | $\begin{aligned} & 4.37 \\ & 2.72 \\ & 0.46 \end{aligned}$ | $\begin{aligned} & 3.41 \\ & 2.44 \\ & 0.40 \end{aligned}$ | $\begin{aligned} & -0.96 \\ & -0.28 \\ & -0.06 \end{aligned}$ | 2.13 1.61 0.71 | $\begin{aligned} & 2.00 \\ & 1.38 \\ & 0.64 \end{aligned}$ | $\begin{aligned} & -0.13 \\ & =0.23 \\ & =0.07 \end{aligned}$ |
| Northbound ${ }^{2}$ | Outside Inside Left-turn | $\begin{aligned} & 2.94 \\ & 2.75 \\ & 2.16 \end{aligned}$ | 2.70 2.41 1.98 | $\begin{aligned} & -0.24 \\ & -0.35 \\ & -0.18 \end{aligned}$ | 1.63 1.40 1.43 | $\begin{aligned} & 1.41 \\ & 1.51 \\ & 1.68 \end{aligned}$ | $\begin{aligned} & -0.21 \\ & +0.11 \\ & +0.25 \end{aligned}$ |
| Eastbound ${ }^{\text {l }}$ | Outside <br> Inside <br> Left-turn | $\begin{aligned} & 3.14 \\ & 1.79 \\ & 1.83 \end{aligned}$ | 2.81 2.12 1.37 | $\begin{aligned} & -0.33 \\ & +0.33 \\ & -0.46 \end{aligned}$ | $\begin{aligned} & 2.20 \\ & 1.33 \\ & 1.27 \end{aligned}$ | $\begin{aligned} & 1.64 \\ & 1.50 \\ & 1.08 \end{aligned}$ | $\begin{aligned} & -0.56 \\ & +0.17 \\ & -0.19 \end{aligned}$ |

[^2]TABLE VIII
COMPARISON OF TRAVELING TIME

| Direction | Lane | $\begin{gathered} \text { Tean Iravelling Time } \\ \text { (seconds) } \end{gathered}$ |  | Differences | Standard Deviation |  | Difierences |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Observed | Simulated |  | Observed | Simulated |  |
| Southbound ${ }^{\text {l }}$ | ```Outside (Th)}\mp@subsup{}{}{3 Outside(R) Inside Left-turn``` | $\begin{aligned} & 22.50 \\ & 22.32 \\ & 22.59 \\ & 40.70 \end{aligned}$ | $\begin{array}{r} 19.96 \\ 20.01 \\ \because 22.21 \\ 37.50 \end{array}$ | $\begin{aligned} & -2.54 \\ & -2.31 \\ & -0.28 \\ & -3.20 \end{aligned}$ | $\begin{aligned} & 16.17 \\ & 17.00 \\ & 15.73 \\ & 25.44 \end{aligned}$ | $\begin{aligned} & 12.85 \\ & 13.09 \\ & 14.56 \\ & 17.31 \end{aligned}$ | $\begin{aligned} & -3.32 \\ & -3.91 \\ & -1.17 \\ & -8.13 \end{aligned}$ |
| Westbound' | ```Outside (mh) Outside(R) Inside Left-turn``` | $\begin{aligned} & 34.69 \\ & 30.44 \\ & 24.51 \\ & 37.17 \end{aligned}$ | $\begin{aligned} & 27.25 \\ & 28.60 \\ & 26.80 \\ & 39.56 \end{aligned}$ | $\begin{aligned} & -7.44 \\ & -1.84 \\ & +2.29 \\ & +2.39 \end{aligned}$ | $\begin{aligned} & 20.67 \\ & 18.28 \\ & 14.53 \\ & 15.94 \end{aligned}$ | $\begin{aligned} & 13.73 \\ & 13.28 \\ & 13.69 \\ & 21.61 \end{aligned}$ | $\begin{aligned} & -6.94 \\ & -5.00 \\ & -0.84 \\ & +5.67 \end{aligned}$ |
| Northbound ${ }^{2}$ | $\begin{aligned} & \text { Outside (Th) } \\ & \text { Outside (R) } \\ & \text { Inside } \\ & \text { Ieft-turn } \end{aligned}$ | $\begin{aligned} & 31.95 \\ & 35.00 \\ & 33.48 \\ & 37.94 \end{aligned}$ | $\begin{aligned} & 31.00 \\ & 23.41 \\ & 28.61 \\ & 42.74 \end{aligned}$ | $\begin{aligned} & -0.95 \\ & -6.59 \\ & -4.87 \\ & +4.80 \end{aligned}$ | $\begin{aligned} & 21.07 \\ & 21.87 \\ & 22.02 \\ & 22.82 \end{aligned}$ | $\begin{aligned} & 19.23 \\ & 21.16 \\ & 19.03 \\ & 22.02 \end{aligned}$ | $\begin{aligned} & -1.84 \\ & -0.71 \\ & -2.99 \\ & -0.80 \end{aligned}$ |
| Eastbound ${ }^{\text {l }}$ | ```Outside(Th) Outside(R) Inside Left-turn``` | $\begin{aligned} & 26.40 \\ & 26.31 \\ & 22.06 \\ & 40.72 \end{aligned}$ | $\begin{aligned} & 24.02 \\ & 22.66 \\ & 24.76 \\ & 38.70 \end{aligned}$ | $\begin{aligned} & -2.38 \\ & -3.65 \\ & +2.70 \\ & -2.02 \end{aligned}$ | $\begin{aligned} & 15.35 \\ & 14.24 \\ & 14.66 \\ & 21.62 \end{aligned}$ | $\begin{aligned} & 12.49 \\ & 11.76 \\ & 13.39 \\ & 16.74 \end{aligned}$ | $\begin{aligned} & -2.86 \\ & -2.48 \\ & +1.27 \\ & -4.88 \end{aligned}$ |

$\frac{1}{2}$ Signal cycle $=60$ seconds
3 Signal cycle $=80$ seconds
4 Straight through vehicles
4 Right-turning vehicles

CHAPTER VII

## INTERSECTION ANALYSIS

The purpose of this chapter is to consider the selection of the most effective traffic control system providing minimum delay for vehicles entering the intersection. Measures to be considered may include changing of traffic signal phasing as well as proposed additional lanes for left-turn and right-turn traffic, wherever it seems to be desirable and applicable. The studied intersection already has a separate left-turn lane on all four approaches; this type of geometric development is therefore not a possibility. The primary consideration here is the intersection control signal.

As previously mentioned, the first trial computer run is usually based on the constraints of the present signal control system. The results may be used as an indicator of how effective the signal phasing is: whether the proportion of total green time allotted to an approach conforms to its ratio of volume, whether the turning vehicles can continue without too much delay, etc. If the results indicate that the signal phasing should be rearranged to be more appropriate, then changes can be made and the results compared.

In the trial computer runs to observe the effects of signal cycle changes, the entering traffic behavior and characteristics are maintained exactly the same for each trial run. Only the signal phasing and cycle lengths are changed.

It should be noted that the yellow signal phase is combined with the green, resulting in what has been termed an "effective green" time. This procedure not only simplifies calculations somewhat, but also corresponds to observed driver behavior, and has been used similarly by other investigators.

The parameters used to evaluate and to compare intersection efficiencies are the mean queue length and mean traveling time. Traveling time is chosen instead of delay time because, in the opinion of the writer, it has broader application when comparisons are made involving vehicles traveling at different speeds.

## Comparison of Traffic Signal Phasing

There are six alternatives of signal phasing considered in this analysis. They may be classified as follows:*

1. A 60 -second cycle with 20 seconds of green for through traffic and 10 seconds (optional**) for left-turn phasing on each approach (2010, 20-10). This is the present signal phasing at this intersection, except for the period from 4:00 p.m. to 6:00 p.m., for which the signal changes to an 80-second cycle.
2. An 80 -second cycle with phasing of 24 seconds green for through traffic and 18 seconds (optional) for left-turn on northbound and southbound, while phasing for eastbound and westbound traffic is 22 seconds

[^3]and 16 seconds for through and left-turn traffic, respectively (24-18, 22-16). This is the typical signal phasing being operated during the period from 4:00 p.m. to 6:00 p.m. on weekdays.
3. A 70 -second cycle with phasing of 25 seconds and 10 seconds for all approaches (25-10, 25-10).
4. A 50 -second cycle with phasing of 15 seconds and 10 seconds for all approaches (15-10, 15-10).
5. An 80 -second cycle with phasing of 25 seconds and 15 seconds for all approaches (25-15, 25-10).
6. A 60-second cycle with phasing times proportioned approximately to the volumes of traffic on each approach. The green times are 17 seconds and 10 seconds for northbound and southbound, 25 seconds and 8 seconds for eastbound and westbound traffic.

Table IX shows the comparison of mean queue values for the above alternatives. The results indicate that the 50 -second cycle (No. 4) provides the smallest queue for northbound and southbound traffic, while the 60 -second cycle (No. 6) is the best for eastbound and westbound traffic (except for the left-turn traffic eastbound).

The results indicate the same conclusion when considering the mean traveling times, in Table $X$. Therefore, either the 50 -second cycle (No. 4) or 60-second cycle (No. 6) should be the choice for this intersection.

It should be noted, however, that the left-turn phase of 8 seconds for eastbound and westbound traffic (60-second cycle, No. 6) provides insufficient time for the left-turners of eastbound traffic (30\% leftturn). Both east and westbound left-turners show increased travel time over similar traffic in trial No. 4, because a phasing of 8 seconds

TABLE IX
MEAN QUEUE LENGTH ANALYSIS

| Direction | Lanes | Lfean Queue length (Vehicles/cycle) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $60 \mathrm{sec} .^{1}$ | $80 \mathrm{sec} .^{2}$ | 70 sec. ${ }^{3}$ | $50 \mathrm{sec} .^{4}$ | 80 sec .5 | $60 \mathrm{sec}{ }^{6}$ |
| Southbound | Outside <br> Inside <br> Left-turn | $\begin{aligned} & 1.81 \\ & 2.00 \\ & 1.80 \end{aligned}$ | $\begin{aligned} & 2.79 \\ & 2.90 \\ & 1.86 \end{aligned}$ | $\begin{aligned} & 2.33 \\ & 2.51 \\ & 2.06 \end{aligned}$ | $\begin{aligned} & 1.50 \\ & 1.77 \\ & 1.39 \end{aligned}$ | $\begin{aligned} & 2.82 \\ & 2.91 \\ & 2.02 \end{aligned}$ | $\begin{aligned} & 2.03 \\ & 2.15 \\ & 1.73 \end{aligned}$ |
| Westbound | Outside Inside Left-turn | $\begin{aligned} & 3.41 \\ & 2.44 \\ & 0.40 \end{aligned}$ | 5.59 3.63 0.51 | $\begin{aligned} & 3.62 \\ & 2.58 \\ & 0.47 \end{aligned}$ | $\begin{aligned} & 3.14 \\ & 2.12 \\ & 0.33 \end{aligned}$ | $\begin{aligned} & 4.95 \\ & 3.39 \\ & 0.51 \end{aligned}$ | $\begin{aligned} & 2.86 \\ & 2.17 \\ & 0.31 \end{aligned}$ |
| Northbound | Outside Inside Left-turn | $\begin{aligned} & 1.91 \\ & 1.62 \\ & 1.53 \end{aligned}$ | $\begin{aligned} & 2.70 \\ & 2.41 \\ & 1.98 \end{aligned}$ | $\begin{aligned} & 2.02 \\ & 1.98 \\ & 1.94 \end{aligned}$ | $\begin{aligned} & 1.35 \\ & 1.42 \\ & 1.33 \end{aligned}$ | $\begin{aligned} & 2.68 \\ & 2.43 \\ & 2.00 \end{aligned}$ | $\begin{aligned} & 2.05 \\ & 1.78 \\ & 1.58 \end{aligned}$ |
| Eastbound | Outside Inside Left-turn | $\begin{aligned} & 2.81 \\ & 2.12 \\ & 1.37 \end{aligned}$ | 4.75 3.16 1.80 | 3.56 2.65 1.65 | $\begin{aligned} & 2.56 \\ & 1.73 \\ & 1.15 \end{aligned}$ | $\begin{aligned} & 4.36 \\ & 2.91 \\ & 1.78 \end{aligned}$ | $\begin{aligned} & 1.72 \\ & 1.18 \\ & 1.42 \end{aligned}$ |

```
\(160 \mathrm{sec} .-\left(20-10^{*}, 20-10^{* *}\right)\).
\(280 \mathrm{sec} .-(24-18,22-16)\).
\(370 \mathrm{sec} .-(25-10,25-10)\).
450 sec. - (15-10, 15-10) :
\(580 \mathrm{sec} .-(25-15,25-15)\).
60 sec. - (17-10, 25-8).
* Signal phases for northbound and southbound traffic.
*** Signal phases for eastbound and westbound traffic.
```

TABLE X
MEAN TRAVELING TIME ANALYSIS

| Direction | Lanes | Tlean Travelline Times (sec.) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $60 \mathrm{sec}^{1}{ }^{1}$ | $80 \mathrm{sec}^{2}$ | $70 \mathrm{sec} .^{3}$ | $50 \mathrm{sec} .^{4}$ | 80 sec .5 | $60 \mathrm{sec}^{6}$ |
| $\begin{aligned} & \text { Southbound } \\ & (98 \mathrm{ft} .)^{*} \end{aligned}$ | ```Outside(Th) Outside(R) Inside Left-turn``` | $\begin{aligned} & 19.96 \\ & 20.01 \\ & 22.21 \\ & 37.50 \end{aligned}$ | $\begin{aligned} & 26.84 \\ & 25.36 \\ & 27.59 \\ & 36.87 \end{aligned}$ | $\begin{aligned} & 25.31 \\ & 22.00 \\ & 22.87 \\ & 40.99 \end{aligned}$ | $\begin{aligned} & 18.19 \\ & 18.37 \\ & 20.22 \\ & 28.31 \end{aligned}$ | $\begin{aligned} & 26.98 \\ & 25.14 \\ & 27.87 \\ & 40.50 \end{aligned}$ | $\begin{aligned} & 21.69 \\ & 22.20 \\ & 24.37 \\ & 34.94 \end{aligned}$ |
| $\begin{aligned} & \text { Westbound } \\ & (300 \mathrm{ft} .) \end{aligned}$ | Outside (Th) Outside (R) Inside <br> Left-turn | $\begin{aligned} & 27.25 \\ & 28.60 \\ & 26.80 \\ & 39.56 \end{aligned}$ | $\begin{aligned} & 32.71 \\ & 42.01 \\ & 35.09 \\ & 45.52 \end{aligned}$ | $\begin{aligned} & \begin{array}{l} 27.24 \\ 26.73 \\ 27.31 \\ 45.56 \end{array} \end{aligned}$ | $\begin{aligned} & 26.98 \\ & 27.98 \\ & 25.84 \\ & 38.68 \end{aligned}$ | $\begin{aligned} & 33.48 \\ & 34.46 \\ & 31.89 \\ & 45.16 \end{aligned}$ | $\begin{aligned} & 22.70 \\ & 22.88 \\ & 22.80 \\ & 36.80 \end{aligned}$ |
| Northbound (198 ft.) | ```Outside (Th) Outside(R) Inside Left-turn``` | $\begin{aligned} & 22.10 \\ & 23.93 \\ & 21.45 \\ & 35.96 \end{aligned}$ | $\begin{aligned} & 31.00 \\ & 28.41 \\ & 28.61 \\ & 42.74 \end{aligned}$ | $\begin{aligned} & 23.01 \\ & 20.00 \\ & 22.91 \\ & 45.16 \end{aligned}$ | $\begin{aligned} & 19.50 \\ & 19.93 \\ & 20.55 \\ & 33.90 \end{aligned}$ | $\begin{aligned} & 29.47 \\ & 31.64 \\ & 28.02 \\ & 43.85 \end{aligned}$ | $\begin{aligned} & 24.12 \\ & 27.28 \\ & 23.81 \\ & 36.92 \end{aligned}$ |
| $\begin{aligned} & \text { Eastbound } \\ & (300 \mathrm{ft} .) \end{aligned}$ | Outside(Th) <br> Outside (R) <br> Inside <br> Left-turn | $\begin{aligned} & 24.02 \\ & 22.66 \\ & 24.76 \\ & 38.70 \end{aligned}$ | $\begin{array}{r} 31.92 \\ 31.93 \\ 31.26 \\ 43.23 \\ \hline \end{array}$ | $\begin{aligned} & 25.15 \\ & 26.53 \\ & 26.56 \\ & 43.83 \\ & \hline \end{aligned}$ | $\begin{aligned} & 23.11 \\ & 22.52 \\ & 22.23 \\ & 32.81 . \end{aligned}$ | $\begin{aligned} & 28.63 \\ & 29.68: \\ & 28.41 \\ & 43.68 \end{aligned}$ | $\begin{aligned} & 18.24 \\ & 15.61 \\ & 16.80 \\ & 40.30 \end{aligned}$ |

[^4]allows only two stopped vehicles to pass through, in comparison with three vehicles in a 10 -second phase. The third vehicle in the 8 -second phase must wait for the next signal cycle.

Some traffic engineers may prefer to have the same amount of delay for vehicles in each approach. Delay times may be computed by subtracting from traveling times the amount of travel time that would be required for an undelayed vehicle. By this measure the 50-second cycle (No. 4) would be the best of the six alternatives.

Other Considerations in Intersection
Analysis

There are several parameters which may be used to evaluate the intersection efficiency in simulation. The term "load factor"* has lost its popularity and now is rarely mentioned. The new terms introduced to this field are "queue length," "mean delay," and "total delays," etc. These parameters are perhaps not as significant for a single approach as they are when there are several approaches to be compared, especially when they have different traffic volumes.

Delay may be the most preferable and understandable parameter. Mean delay is generally used. This parameter carries considerable meaning as far as delay of an individual vehicle is concerned. However, in some cases it may not be suitable when evaluating the entire intersection system, especially if traffic volume from the cross street is much different than the main street. In this case a moderate mean delay may

[^5]result in a large total delay for the street with heavy traffic. For this situation the total delay, either the total delay of each street or total delay of the intersection, may be more appropriate. Furthermore, equal values of delay time will be more meaningful for a faster vehicle than a slower one. The true efficiency of an intersection may thus be obscured if the measure of efficiency is not carefully chosen.

## CHAPTER VIII

## CONCLUSIONS AND RECOMMENDATIONS

## Conclusions

This research has been concerned with the utilization of the GPSS language in traffic simulation. It has shown that, by proper programming, GPSS may be one of the most advantageous languages in simulation of dynamic traffic characteristics, since it provides easier and shorter programming efforts, as well as more understandable concepts which can be followed without much difficulty. The model itself provides built-in useful statistical supplementary data which results in shorter programs, less memory storage required, and less computer time.

Based on this simulation, the following conclusions should be briefly mentioned.

1. Field observation studies of traffic characteristics and statistics are usually difficult and time consuming. A time-lapse photography technique with a one-second exposure interval seems to be a most satisfactory and economical method for observing the inter-arrival times, speeds, and turning percentages of vehicles approaching an intersection. The stop watch, on the other hand, is still useful for more precise parameters. However, the new electrical timer, such as the one built into the Hewlett-Packard calculator HP-55, should be introduced to this
field, since it has the capability of 10 stop-watches operating simultaneously.
2. The simulation results of the selected intersection agree well with the field observations. Even though they are based on only one intersection, the different signal cycles observed provide numerous checks of model validity. By comparing results from different sets of data, a traffic engineer can choose the most effective alternate for a particular intersection.

## Recommendations

The simulation model, in its present form, is capable of evaluating other types of intersections than the four-lane street crossing a fourlane street selected for this study. The following are some of commonly found intersections which would be worthy candidates for investigation in order to extend the scope of application of this model:

1. An intersection of a four-lane street crossing a four-lane street without separate turning lanes.
2. An intersection of a four-lane major street crossing a two-lane minor street.
3. An intersection of a two-lane street crossing a two-lane street.

In addition to the above traffic signal controlled intersections, the computer program could also be modified to evaluate intersections having two-way or four-way stop-sign control.

As far as the concepts of developing a computer simulation is concerned, the most important single parameter affecting the delay time is the inter-arrival time between each approaching vehicle. This is unfortunate, because each individual intersection has a different pattern of
inter-arrival times. Some of them exemplify platoon behavior, especially when strongly influenced by a preceding signalized intersection. Some more nearly represent random behavior, for which the shiftedexponential distribution is appropriate. Most consist of some combination of the two, making the simulation accuracy dependent on collected inter-arrival field data. There is a great need for better understanding of dynamic traffic elements to achieve more adequate mathematical models of intersections.

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## APPENDIX A

STARTING DELAY AND HEADWAY OBSERVATION DATA

STARTING DELAY, FIRST VEHICLE IN QUEUE

| $\begin{gathered} \text { Direction } \\ \text { of } \\ \text { Traffic } \end{gathered}$ | Janes | No. of Vehicles Observed | Avcrage time in seconds |
| :---: | :---: | :---: | :---: |
| Southbound | outside | 9 | 2.93 |
|  | inside | 10 | 3.23 |
|  | left-turn | 24 | 3.90 |
| Westbound | outside | 13 | 3.25 |
|  | inside | 15 | 3.46 |
|  | left-turn | 9 | 3.30 |
| Northbound | outside | 19 | 3.30 |
|  | inșide | 8 | 3.78 |
|  | Ieft-turn | 22 | 3.79 |
| Eastbound | outside | 10 | 2.89 |
|  | inside | 12 | 3.34 |
|  | left-turn | 21 | 3.33 |

NUMBERS OF VEHICLE HEADWAYS OBSERVED

| $\begin{gathered} \text { Direction } \\ \text { of } \\ \text { Traffic } \end{gathered}$ | Lanes | $\begin{gathered} 2^{\text {nd }} \\ \text { Vehicles } \end{gathered}$ | $\begin{gathered} 3^{\text {rd }} \\ \text { vehicles } \end{gathered}$ | $\begin{gathered} 4^{\text {th }} \\ \text { Vehicles } \end{gathered}$ | $5_{\text {vehicles }}^{\text {th }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Southbound | outside | 7 | 6 | 4 | 7 |
|  | inside | 8 | 8 | 9 | 10 |
|  | left-turn | 9 | 11 | 12 | 8 |
| :iestbound | outside | 7 | 10 | 6 | 7 |
|  | inside | 8 | 6 | 9 | 8 |
|  | left-turn | 2 | - | - | - |
| Northbound | outside | 7 | 8 | 5 | 5 |
|  | inside | 4 | 6 | 5 | 4 |
|  | left-turn | 6 | 3 | 7 | 2 |
| Easthound | outside | 8 | 13 | 14 | 7 |
|  | inside | 2 | 4 | - | 3 |
|  | left-turn | 5 | 6 | 10 | 4 |

## HEADWAYS OF OBSERVED VEHICLES IN QUEUES

| $\begin{gathered} \text { Direction } \\ \text { of } \\ \text { Traffic } \end{gathered}$ | Lanes | $2^{\text {nd }}$ <br> Vehicles <br> in Queue | $\begin{gathered} 3^{\text {rd }} \\ \text { vehicles } \\ \text { in Queue } \end{gathered}$ | $\begin{aligned} & 4^{\text {th }} \\ & \text { Vehicles } \\ & \text { in Queue } \end{aligned}$ | $\begin{aligned} & 5^{\text {th }} \\ & \text { Vohicles } \\ & \text { in Queue } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Southbound | outside <br> insj.de <br> left-turn | $\begin{aligned} & 2.32 \\ & 2.53 \\ & 2.66 \end{aligned}$ | $\begin{aligned} & 2.40 \\ & 2.40 \\ & 2.09 \end{aligned}$ | $\begin{aligned} & 2.25 \\ & 2.22 \\ & 2.18 \end{aligned}$ | $\begin{aligned} & 2.04 \\ & 2.01 \end{aligned}$ |
| Westiound | outside <br> inside <br> leitt-turn | $\begin{aligned} & 3.11 \\ & 2.42 \\ & 3.20 \end{aligned}$ | $\begin{aligned} & 2.71 \\ & 2.45 \end{aligned}$ | $2.23$ | $2.29$ |
| Forthuound | outside <br> ingide <br> left-turn | $\begin{aligned} & 3.05 \\ & 2.35 \\ & 2.43 \end{aligned}$ | $\begin{aligned} & 2.58 \\ & 2.25 \\ & 2.00 \end{aligned}$ | $\begin{aligned} & 2.21 \\ & 2.10 \end{aligned}$ | $\begin{aligned} & 2.31 \\ & 1.80 \end{aligned}$ |
| Pestbound | outside <br> inside <br> left-turn | $\begin{aligned} & 2.25 \\ & 2.40 \\ & 2.40 \end{aligned}$ | $\begin{aligned} & 2.23 \\ & 2.17 \\ & 2.31 \end{aligned}$ | $\begin{gathered} 2.06 \\ - \\ 1.94 \end{gathered}$ | $\begin{aligned} & 2.14 \\ & 1.83 \end{aligned}$ |

STARTING DELAY OF QUEUED VEHICLES

| Types of Traffic | ```Starting Lelzy Ist Vehicles``` | Headvays |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{gathered} 2^{\text {nd }} \\ \text { Vehicles } \end{gathered}$ | $\begin{gathered} 3^{\text {rd }} \\ \text { Vehicles } \end{gathered}$ | $\begin{gathered} 4^{\text {th }} \\ \text { Vehicles } \end{gathered}$ | $\begin{gathered} 5^{\text {th }} \\ \text { vehicles } \end{gathered}$ |
| Through \& Risht-turn Vehicles | 3.26 | 2.55 | 2.39 | 2.19 | 2.23 |
| $\begin{aligned} & \text { Ieft-turn } \\ & \text { Venicles } \end{aligned}$ | 3.58 | 2.49 | 2.20 | 2.07 | 1.92 |

## APPENDIX B

## A STUDY OF TRAVELING TIME ACROSS INTERSECTION PROPER

NUMBER OF VEHICLES FOR WHICH INTERSECTION
TRAVELING TIME WAS MANUALLY OBSERVED

| $\begin{gathered} \text { Direction } \\ \text { of } \\ \text { jraffic } \end{gathered}$ | Lanes | Non-stop <br> Vehicles | $\begin{gathered} 1^{s t} \\ \text { Vohicles } \end{gathered}$ | $\begin{gathered} 2^{\text {nd }} \\ \text { vehicles } \end{gathered}$ | $\begin{gathered} 3^{\text {rd }} \\ \text { vehicles } \end{gathered}$ | $\begin{gathered} 4_{4}^{\text {th }} \\ \text { Vehicles } \end{gathered}$ | $5_{\text {th }}^{\text {th }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Southbound | $\begin{aligned} & \text { outsjode }(\mathrm{Th} .)^{1} \\ & \\ & (\mathrm{R})^{2} \\ & \text { inside } \\ & \text { left-turn } \end{aligned}$ | $\begin{array}{r} 3 \\ 5 \\ 3 \\ 8 \end{array}$ | $\begin{array}{r} 3 \\ 6 \\ 4 \\ 10 \end{array}$ | $\begin{array}{r} 3 \\ 2 \\ 9 \\ 11 \end{array}$ | $\begin{array}{r} 1 \\ 1 \\ 13 \\ 13 \end{array}$ | $\begin{array}{r} 2 \\ 4 \\ 5 \\ 10 \end{array}$ | $\begin{aligned} & 2 \\ & 1 \\ & 6 \\ & - \end{aligned}$ |
| Westbound | outside (Th) <br> (R) <br> jnside <br> left-turn | 4 2 9 4 | $\begin{array}{r} 4 \\ 1 \\ 15 \\ 14 \end{array}$ | $\begin{aligned} & 3 \\ & 4 \\ & 7 \\ & 2 \end{aligned}$ | $\begin{aligned} & 5 \\ & 3 \\ & 4 \end{aligned}$ | $\begin{aligned} & 7 \\ & 1 \\ & 6 \\ & - \end{aligned}$ | $\begin{aligned} & 4 \\ & 5 \\ & 2 \end{aligned}$ |
| Northbound | ```outside (Th) (R) inside lect-turn``` | 6 - 4 2 | $\begin{aligned} & 2 \\ & 2 \\ & 1 \\ & 1 \end{aligned}$ | $\begin{array}{r} 7 \\ 1 \\ 8 \\ 10 \end{array}$ | $\begin{aligned} & 6 \\ & - \\ & 6 \\ & 8 \end{aligned}$ | $\begin{aligned} & 6 \\ & 3 \\ & 1 \\ & 1 \end{aligned}$ | $\begin{aligned} & 1 \\ & 2 \\ & 4 \end{aligned}$ |
| Eastbound | ```outside (Th) (R) inside lefi-turn``` | 2 - 4 3 | 2 4 6 6 | $\begin{array}{r} 4 \\ 1 \\ 6 \\ 11 \end{array}$ | 8 3 4 5 | $\begin{aligned} & 7 \\ & 4 \\ & 3 \\ & 2 \end{aligned}$ | $\begin{aligned} & 6 \\ & 4 \\ & 7 \end{aligned}$ |

${ }^{1}$ Straight through vehicles
${ }^{2}$ Right turning vehicles

OBSERVED INTERSECTION TRAVELING TIMES

|  | - Imanes | fion-stop <br> Vehicles | $\frac{I^{\text {st }}}{\text { vehicles }}$ | $\left\|\begin{array}{c} 2^{\text {nd }} \\ \text { venicles } \end{array}\right\|$ | $\begin{gathered} 3^{\text {rd }} \\ \text { vehic:les } \end{gathered}$ | $\begin{gathered} 4^{\text {th }} \\ \text { Vehicjes } \end{gathered}$ | $\left\lvert\, \begin{aligned} & 5^{t h} \\ & \text { Vohicles } \end{aligned}\right.$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Southbound | $\begin{aligned} & \text { outside }(\mathrm{Ch})^{1} \\ & \text { outside }(\mathrm{R})^{2} \\ & \text { inside } \\ & \text { left-turn } \end{aligned}$ | $\begin{aligned} & 1.85 \\ & 2.18 \\ & 2.13 \\ & 2.32 \end{aligned}$ | $\begin{aligned} & 2.84 \\ & 2.20 \end{aligned}$ | $\begin{aligned} & 3.56 \\ & 2.15 \\ & 3.17 \\ & 3.16 \end{aligned}$ | $\begin{aligned} & 3.30 \\ & 1.32 \\ & 3.00 \\ & 3.1 .9 \end{aligned}$ | $\begin{aligned} & 3.05 \\ & 1.65 \\ & 2.68 \\ & 2.91 \end{aligned}$ | $\begin{aligned} & 2.70 \\ & 1.2 .5 \\ & 3.15 \end{aligned}$ |
| Westbound | outside (I'h) <br> outside (R) <br> inside <br> left-turn | $\begin{aligned} & 2.45 . \\ & 1.60 \\ & 2.45 \\ & 2.32 \end{aligned}$ | $\begin{gathered} 2.73 \\ - \\ 3.5 \\ 3.6 \end{gathered}$ | $\begin{aligned} & 3.06 \\ & 1.98 \\ & 3.24 \\ & 2.60 \end{aligned}$ | $\begin{aligned} & 2.80 \\ & 1.43 \\ & 2.77 \end{aligned}$ | $\begin{aligned} & 2.82 \\ & 3.50 \\ & 2.55 \end{aligned}$ | $\begin{aligned} & 2.75 \\ & 1.54 \\ & 2.85 \end{aligned}$ |
| Nor thbound | outside ( I h) <br> outside (R) <br> inside <br> left-turn | $\begin{gathered} 2.06 \\ - \\ 2.22 \\ 2.30 \end{gathered}$ | $3.20$ | $\begin{aligned} & 2.77 \\ & 1.70 \\ & 3.26 \\ & 3.00 \end{aligned}$ | $\begin{gathered} 2.96 \\ - \\ 2.91 \\ 3.08 \end{gathered}$ | $\begin{gathered} 2.70 \\ - \\ 2.70 \\ 3.50 \end{gathered}$ | $2.95$ |
| Eastbound | outside (in) <br> outside (R) <br> inside <br> left-turn | $\begin{gathered} 2.07 \\ - \\ 1.98 \\ 2.46 \end{gathered}$ | $\begin{aligned} & 2.9 \\ & 1.3 \\ & 2.7 \\ & 2.9 \end{aligned}$ | $\begin{aligned} & 3.30 \\ & 1.70 \\ & 3.28 \\ & 3.45 \end{aligned}$ | $\begin{aligned} & 3.40 \\ & 1.10 \\ & 3.10 \\ & 3.30 \end{aligned}$ | $\begin{aligned} & 3.40 \\ & 1.33 \\ & 2.86 \\ & 3.20 \end{aligned}$ | $\begin{aligned} & 3.32 \\ & 1.15 \\ & 3.02 \end{aligned}$ |

I Straight through vehicles
${ }^{2}$ Right turning vehicles

AVERAGE INTERSECTION TRAVELING TIMES

| Vehicles | Mon-stop <br> Vehicles | st <br> Vehicles | $2^{\text {nd }}$ <br> Vehicles <br> nid | $3^{\text {rd }}$ <br> Vehicles | $4^{\text {th }}$ <br> Vehicles | $5^{\text {th }}$ <br> Vehicles |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Through | 2.70 | 1.92 | 1.98 | 1.32 | 1.65 | 1.25 |
| Left-turn | 2.80 | 2.80 | 3.21 | 2.99 | 2.86 | 3.03 |

APPENDIX C

INTER-ARRIVAL TIMES OF VEHICLES









## APPENDIX D

## CUMULATIVE PERCENTAGE OF VEHICLE TRAVELING TIMES



traveling time of vehicles in outside lane (westbound)



traveling time of vehicles in inside lane (northbound)




## APPENDIX E

VEHICLE SPEED DISTRIBUTIONS



## APPENDIX F

STANDARD STATISTICAL OUTPUT ASSOCIATED WITH CLOCK AND BLOCK ENTITIES







190

$\qquad$
$\qquad$ +
$\ldots$
$\cdots$




APPENDIX G

OUTPUTS OF TRAFFIC QUEUES



$\qquad$
$\qquad$

$\qquad$

## APPENDIX H

OUTPUTS OF THROUGH TRAFFIC TRAVELING TIME

$\qquad$



_-n $\qquad$

THROUGH TRAFFIC TRAVELLING TIME IN LANE E2


REMAINING FREQUENCIES ARE ALL ZERU

through traffic taavelling. time in lane 43



APPENDIX I

OUTPUTS OF RIGHT TURN TRAFFIC TRAVELING TIME

$\qquad$

$\qquad$


## APPENDIX J <br> OUTPUTS OF LEFT TURN TRAFFIC TRAVELING TIME



LEFT-TURN TRAFFIC TRAVELLiNG TIML FNGM LANE 32

$\qquad$


APPENDIX K

OUTPUTS OF VEHICLE ARRIVAL-TIME DISTRIBUTION

$\qquad$
arrival-time oistaibution fur vehicles in lane 12

$\qquad$


arrival-time distriaution for vehicles if lane 32



APPENDIX L

OUTPUTS OF VEHICLE SPEED DISTRIBUTION



- -...-spem distriuution of vemicles. in lane 21

speed distribution of vehicles in lane 31

soeed otstataution of vehicles in lane 32




# N <br> VITA <br> Vongchai Jarernswan <br> Candidate for the Degree of <br> Doctor of Philosophy 

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[^0]:    *The following explanation is selected and modified from Reference (1).

[^1]:    *The theory and equations cited in this section are from Reference (2).

[^2]:    $1_{\text {Signal cycle }}=60$ seconds
    ${ }^{2}$ Signal cycle $=80$ seconds

[^3]:    *Yellow phase time is considered an extension of green in the following.
    **When there is no left-turn demand, opposing through traffic retains the green signal for the additional indicated amount of time.

[^4]:    $\frac{1}{2} 60 \mathrm{sec} .-\left(20-10^{*}, 20-10^{* *}\right)$.
    $380 \mathrm{sec} .-(24-18,22-10)$.
    $370 \mathrm{sec} .-(25-10,25-10)$.
    $550 \mathrm{sec} .-(15-10,15-10)$.
    580 sec. - $(25-15,25-15)$.
    $60 \mathrm{sec} .-(17-10,25-8)$.
    *

    * Signal phases for northbound and southbound traffic.
    *** Signal phases for eastbound and westbound traffic.
    \#F:r* Distances between reference line and stop line on each approach.

[^5]:    *The ratio of the number of green phases fully utilized by traffic to the total number of cycles.

