A STUDY OF THE EFFECT OF VARIABIE
CLEARANCES ON THE BOLT LOAD
DISTRIEUTION IN A MULII-
FASTENER LAP JOINT

By<br>WARREN LEE GILMOUTR<br>$\because$<br>Bachelor of Science<br>Oklahoma State University Stillwater, Oklahoma

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## TABLE OF CONTENTS

Chapter Page
I. INTRODUCTION ..... 1
II. DERIVATION ..... 3
III. EXPERIMENTAL VERIFICATION OF PREDICTED CLEARANCES. 10
Test Model ..... 10
Testing Procedure ..... 13
IV. RESULTS AND CONCLUSIONS. ..... 18
Result ..... 18
Conclusions ..... 19
BIBLIOGRAPHY. ..... 26
APPENDIX A. ..... 27
APPENDIX B. ..... 28

## IIST OF TABL巴S

Table Page
I. Strain Readings in Microinches. ..... 21
II. Individual Bolt Loads ..... 24
LIST OF IILUSTRATIONS
Plate Page
I. Test Model ..... 11
II. Equipment Arrangement ..... 17
III. One Bolt Test Specimen and Test Set-Up. ..... 30
Figure ..... Page

1. Portion of a Five Bolt Lap Joint Showing ThreeBolts . . . . . . . . . . . . . . . . . . 6
2. Lap Joint Showing the Loads in Segments BetweenBolts7
3. Test Specimen ..... 15
4. Bolt Load Distribution at Various Joint Loadings. ..... 25
5. Load-Deflection Curves for 0.250" Diameter Boltwith Various Clearances . . . . . . . . . . . . 31

## CHAPTER I

## INTRODUCTION

Joint design in recent years has become very important, especially in the aircraft industry. The increase in aircraft weight is probably on the order of ten percent due to the additional material and fasteners required for the joint. Thus, any significant savings in joint weight would result in considerable decrease in weight of the entire aircraft. With the recent increase in airplane production costs, any savings in weight results in a substantial saving in costs, therefore, it becomes paramount that all the joining devices in aircraft be as light as possible.

Joint design in earlier times was, and still is rather inexact. The first approach which was used assumed that each bolt carried an equal amount of load. Later it was suspected that this was not true and actually the bolts at the edges of a lap joint carried more load than the interior bolts. Recently, this suspicion has been substantiated and the variation has been shown to be, in some instances, (end bolt of a three bolt joint) approximately fifteen percent. (1). Currently, joints must be designed such that the extreme bolts will carry this
additional fifteen percent load and, as is usual in joint design at present, all of the bolts are made the same size. Consequently, the interior bolts are not loaded to their full capacity and thus result in excess weight.

It is possible that equal loading of the bolts, or at least full loading of each bolt, could be accomplished by varying the clearances across the lap joint. This wold allow smaller bolts (thus a decrease in weight) to be used, since each fastener would be loaded to its full capacity.

It is the purpose of this report to arrive at a means of predicting the clearances necessary for equal bolt load distribution and to present the results of an experimental check of this prediction. A relationship between necessary clearances, the number of bolts in a joint, the bolt spacing, the properties of the plate material, and the joint load is derived. The clearances predicted by this relation were experimentally checked for a specific joint configuration and the results are presented.

## DERIVATION

In order to arrive at the relationship for predicting clearances, certain simplifying assumptions must be made to overcome inherent indeterminancies. The assumptions made are as follows:
(1) The stress strain relationship for the material is linear.
(2) The load-deflection characteristic of the bolts is linear and is independent of clearances.
(3) The relative motion of the plate and straps may be defined in terms of bolt deflection, hole clearances, and strap strain.
(4) Stress in a strap and plate can be approximated by an average stress $\frac{P}{A}$.
(5) That the load carried by friction between the plates and the straps is negligible.

The first assumption is necessary because some means must be available for determining the total strain in the straps between two adjacent bolts. The strain relationship for Young's modulus holds only when this assumption is made.

The second assumption of linear bolt deflection characteristic has been shown by other investigators to be substantially true under certain circumstances. (1). These
include a loading below the yield point of the bolt material, zero clearances, and considering the bolt as a beam with clamped ends. Some of these conditions are not satisfied in the present study. Consequently, the behavior of the loaddeflection characteristic of a bolt under a loading similar to that of the present study was determined. Joints similar to the one in the present study except having only one bolt per lap and having various clearances were studied in a preliminary investigation. Deflections were measured directly by mechanical strain gages and the load-deflection curves are presented in Appendix $B$. The results show that with considerable clearance the bolt load-deflection characteristic is not linear and that with clearances on the order of three percent of the bolt diameter, bolts show an increased change in deflection with load under higher loadings; however, the increase is rather small and it is believed that with a normal working load for a joint the non-linearity would be insignificant. The third assumption takes care of the difficulty in determining or describing the bearing action of the bolt on the plate and straps.

The bearing action is very complex. Little work has been done to determine what actual deflections take place due to compression in the plate and bolt itself. Actually the third assumption implies that there is no compression of the bolt or plate, and that all relative motion between adjacent bolts is the sum of the total strain of the material between the bolts (as obtained from Young's modulus and an average stress
mid-way between the bolts) and the clearances between the bolts and holes. Thus, the assumption absorbs the bearing action problem.

The fourth assumption, while not absolutely true as indicated by other investigations, can again be considered sufficiently accurate for this investigation. (1).

Tate and Rosenfield (I) indicate that assumption five is substantially correct though many other investigations have indicated that it plays a significant part in the load carrying capacity of many lap joints. However, experience gained during the tests of Appendix B indicates that the assumption is correct, especially when the materials have high hardness. The test specimens described in Appendix B, being made of $7075-\mathrm{T} 6$ aluminum, could not be gripped in the jaws of the testing machine, apparently because of their extreme hardness. To stop the slippage, extensions of ClOlO steel were attached to the ends of the specimens and the load applied through these extensions. Thus, it appears that a normal force (clamping action) of several times the joint load would be necessary to produce a friction force capable of carrying a significant load. Toward this end the bolts on installation were tightened snuggly with a wrench, loosened, and then retightened by hand.

Based on these five assumptions, a derivation of the proposed relationship for predicting clearances can be made. From the second assumption it is seen that in order to have equal distribution along the joint, the deflection of each
bolt must be the same. Thus in Figure $1, d_{1}=d_{2}=d_{3}$, and the center to center distances of the ends of two adjacent bolts must be equal.


P = Joint load.
C (Clearance) $=$ Diameter of hole - Diameter of bolt.
d = Deflection of bolt.
$m=C e n t e r$ to center distance of holes at zero load. a = Elongation of section between bolts due to load.

Figure 1. Portion of a Five Bolt Lap Joint Showing Three Bolts
The equality of distances requires that

$$
a_{23}^{\prime}+m=a_{23}+m-\frac{C_{2}}{2}-d_{2}+d_{3}
$$

$$
\begin{equation*}
\text { or } \left.c_{2}=2\left(a_{23}-a_{23}\right)^{\prime}\right) \tag{1}
\end{equation*}
$$

Between bolts 1 and 2, the relation is:

$$
a_{12}+m=a_{12}+m-\frac{C_{1}}{2}+\frac{C_{2}}{2}+d_{2}-d_{1}
$$

or $C_{1}=C_{2}+2\left(a_{12}-a_{12}\right)$.
Eq. (2)
The elongation of the strap segment between bolts is obtained by observing the relation between the elongation of the strap and plate between the same two bolts. This relation depends on the loads in the plate and strap segments. These loads are shown in Figure 2 in terms of the total joint load P.


Figure 2. Lap Joint Showing the Loads in Segments Between Bolts

From Young's modulus, $a_{i j}=\frac{F M}{A E}$, where $j=1+1$
and both are bolt locations; $F$ is the load in the section between $i$ and $j ; A$ is the area of the section and $E$ is the modulus of elasticity. The force corresponding to

$$
\begin{array}{ll}
a_{12} \text { is, } & F=P-\frac{P}{N} ; \\
a_{23} \text { is, } & F=P-\frac{2 P}{N} ;
\end{array}
$$

and to

$$
a_{i j}, \quad F=P-\frac{i P}{\mathbb{N}}
$$

It follows that

$$
\begin{equation*}
a_{i j}=\frac{(P-i P / N) m}{A E}=\frac{P m}{A E}(1-i / \mathbb{N}) \tag{3}
\end{equation*}
$$

and similarly, $\quad a_{i j}{ }^{\dagger}=\frac{\frac{i P m}{N}}{A E}$.
Division of the last two equations yields,

$$
\begin{equation*}
\frac{a_{i j}}{a_{i j}}=\frac{\frac{P m}{A E}(1-i / \mathbb{N})}{\frac{\mathbb{P m}}{\overline{A E}}(i / \mathbb{N})}=\frac{i}{i} \tag{5}
\end{equation*}
$$

Substituting for $a_{i, j}{ }^{\prime}$ in Eqs. (1) and (2) gives:

$$
\begin{equation*}
c_{2}=2\left(a_{23}-2 \frac{a 23}{N-2}\right)=2 a_{23}\left(1-\frac{2}{N-2}\right)=2 a_{23}\left(\frac{N-4}{N-2}\right) \tag{Ia}
\end{equation*}
$$

$$
\begin{align*}
c_{1} & =c_{2}+2\left(a_{12}-\frac{a_{12}}{\mathbb{N}-1}\right)=c_{2}+2 a_{12}\left(\frac{\mathbb{N}-2}{\mathbb{N}-1}\right) .  \tag{2a}\\
\text { or } c_{1} & =2 a_{12}\left(\frac{\mathbb{N}-2}{\mathbb{N}-1}\right)+2 a_{23}\left(\frac{\mathbb{N}-4}{\mathbb{N}-2}\right) .
\end{align*}
$$

In general induction leads to

$$
c_{i}=\sum_{i}^{f(\mathbb{N})} 2 a_{i j}\left(\frac{\mathbb{N}-2 i}{\mathbb{N}-i}\right),
$$

where $f(\mathbb{N})=\frac{\mathbb{N}-1}{2}$ for odd values of $N$, and $f(\mathbb{N})=\frac{\mathbb{N}-2}{2}$ for even values of N. Since,

$$
2 a_{i j}\left(\frac{\mathbb{N}-2 i}{\mathbb{N}-i}\right)=\frac{2 P m}{A E}(I-i / \mathbb{N})\left(\frac{\mathbb{N}-2 i}{\mathbb{N}-i}\right)=\frac{2 \operatorname{Pm}(\mathbb{N}-2 i)}{A E},
$$

it follows that

$$
\begin{equation*}
c_{i}=\frac{2 P \mathrm{Pm}}{\mathbb{N A E}} \sum_{i}^{\mathrm{f}(\mathbb{N})}(\mathbb{N}-2 i) \tag{6}
\end{equation*}
$$

Equation (6) is the proposed relation for predicting the necessary clearances for equal bolt load distribution. It is based on a joint having an odd number of bolts, the center bolt having zero clearances in both plate and strap and the remaining bolts having zero clearances in one and the predicted clearance in the other. All clearances may be increased by an equal amount without disturbing the bolt load distribution. Also, since " $\mathrm{m}^{\prime}$ may be inside the summation, it could be varied to provide some flexibility in joint configuration. The relationship can be applied to a joint with an even number of bolts by considering the two center bolts as one and calculating the clearances using a value for "N" of one less than the actual number of bolts. The predicted clearances are then applied to the remaining bolts.

The relationship is limited to the range of loadings that stress the bolts and plates to a value below their proportional limits. Beyond the load corresponding to the proportional limits of either or both, it has been found that yielding of one or the other, or both, tend to equalize the bolt load distribution. (1). In a joint designed for equal bolt load distribution with a given maximum load, the joint can be subjected to higher loadings and still maintain essentially an equal bolt load distribution, although local yielding would take place with such loadings. Also, the relationship is limited to joints with bolts made of the same material and having like diameters. Under a condition of loading with a fraction of the design load, the bolt loading is unequal, the bulk of the load being carried by the interior bolts. Intermediate bolt load distributions are shown in Figure 4.

EXPERIMENTAL VERIFICATION OF PREDICTED CLEARANCES

The lap joint used in the test was designed so that maximum deflection of the bolts and strain of the plate material would occur under a load that would not cause stresses above the proportional limits. Also, an attempt was made to duplicate the materials and configurations Used in present day aircraft construction, in order that the results might be more easily applied to design in the aircraft industry.

Test Model

The test model consisted of two double lap joints fastened by five fasteners each (Figure 3). The joint labeled "A" has clearances for equal bolt loading at a joint load of 23,000 pounds. The joint labeled "B" has the necessary clearances predicted for a 46,000 pound load. The two configurations were used in order to determine the bolt load distribution at loads above and below the design joint load.

The joints were doubled in order to avoid the bending monent inherent in a single lap joint due to eccentricity of load applications. The bending moment in the single lap

PIATE I
TEST MODEL

joint produced "waves" along the joint such that any strain measurement taken on the surface of one strap between two adjacent bolts would be considerably influenced. By doubling the joint, bending moments of opposite sign are introduced in the central plate and they cancel. Some "wave" shape is still present in the straps because of the bending moment introduced by the deflection of the bolts. However, no method was found for determining this effect. It appears that the amount of distortion in strain readings would be proportional to the load in the section. The actual bolt loads would then be proportional to the calculated loads. Thus, the bolt loads presented in the results need to be corrected by some small percentage. The lack of the correction does not, however, change the relative magnitudes of the bolt loads. Tate and Rosenfield (1) attempted to make this correction and found that at higher loadings, (near the yield point of the materials) the effect was considerable, as indicated by separation of the straps from the plate. In the present study no such separation was detected and it is concluded that the loadings were low enough that the bending effect was negligible.

The sizes of the straps and bolts were dictated by the availability of material, capacity of testing machine, and fabrication methods available. The straps were 0.250 inches thick by 1.750 inches in width. The plates were 0.500 inches thick by 1.750 inches in width. The bolts used were 0.250 inches in diameter by 2 inches in length. The bolts were
threaded on both ends so that both ends would present the same deflection characteristics. A collar 3/8" long made of 1/4" black pipe was placed under each nut in order that sufficient threading was available for the nuts and that no threads would. be in bearing contact with the straps.

The material of the plate and strap was $7075-\mathrm{T} 6$ rolled aluminum plate. The specimens were cut from the plate so that the direction of the grain coincided with the load ap. plication. The edges of the straps and plates were milled to assure uniform width and straightness. The bolts were fabricated from commercial carbon steel of one percent carbon content. The bolts were then heat treated to gain hardness and strength. The heat treatment consisted of heating the bolts to $1440^{\circ} \mathrm{F} .$, quenching in 0il, and tempering at $400^{\circ} \mathrm{F}$. The heat treatment resulted in an average Rockwell hardness of 38 .

All holes were drilled and all holes except those with 17 thousandths clearance were reamed to size. No reamer was available in the size necessary for the 17 thousandths clearances. In most cases, holes of the same size were aligned and finish reamed with one operation to assure aniformity.

## Testing: Procedure

In order to verify the predicted clearances, the bolt load distribution was determined. The load in the strap between adjacent bolts was deternined by means of strain
measurements and the load on each bolt was assumed to be the difference of the loads in the straps on either side of the bolt. The load in the free end of the strap was assumed to be zero and the load between the two joints was assumed to be the joint load.

Strain measurements were taken by means of electrical strain gages. Three gages were placed, as shown in Figure: 3, half way between each pair of adjacent bolts. The gages were spaced at equal intervals across the plate. An attempt was made to determine the most advantageous placement of the gages a line along which the three indicated strains would be nearly the same. Two tests were made on a steel lap joint similar to the test model, in which the strap surface stress levels and distribution was to be determined by brittle stress coating. The results were inconclusive; consequently, the placement used by Tate and Rosenfield (1) was used. They indicate that while this is not the best placement, the strains obtained should not vary more than twenty percent among the three gages. With variations in load of this amount or less, an average of the three loads (strains) should be representative of the section load.

The SR-4 strain gages were type $A-5,1 / 2^{\prime \prime}$ in length, and were applied according to manufacturers specifications.

An SR-4 bridge circuit was used in conjunction with a switching circuit to take the strain readings. The system indicates strain in microinches directly and from this and Young's modulus, the load in the section can be determined.


Figure 3. Test Specimen

The load was applied to the joint in a Baldwin Southwark hydraulic testing machine of 60,000 pounds capacity. The machine was calibrated in June, 1959 and the maximum error found was 0.38 percent. Plate II shows the test arrangement.

The load was applied in increments of 2,000 pounds over a range of from zero to 14,000 on the first two runs and from zero to 23,000 pounds on the last run. Subsequently, the specimen was loaded to failure at approximately 32,000 pounds. Measurements during the test consisted solely of the strain readings at various loadings.

PIATE II
EQUIPMENT ARRANGEMENT


## RESULTS AND CONCLUSIONS

## Results

The load distribution, as indicated in Figure 4, did not become equal at the design load in either lap joint. One bolt in each joint carried considerably more than the others. In joint "A" at the design load, bolt 4 carried a load fourty percent greater than the design load.

On the four remaining bolts in joint "A", the greatest percentage deviation was approximately eighteen percent. This occurred on bolts 1 and 5 and was below the design load. Bolts 2 and 3 were loaded to within five percent of the design load.

The distribution in joint "B" was similar to that in "A" except that the deviations were more pronounced. Since the design loading was not reached, no comparison can be given concerning the accuracy of the predicted clearances. However, at intermediate loads, the deviation from an average load (joint load divided by number of bolts) was as much as sixty percent. This was above the average load. The deviation below average was considerably less - on the order of thirty percent.

The results of the continuation of the third run were somewhat erratic. The specimen ruptured at approxinately 32,000 pounds. Bolt 4 failed at that loading and subsequently all four remaining bolts failed, some in shear, some in bending and some in tension.

## Conclusions

Zero or equal clearance along a miti-fastener lap joint require greatest load on the outer bolts and least load on the center bolt. From the results of this study it can be concluded that the loads on the bolts can be equalized by varying the clearances along the joint. The derived relationship however, over-corrects for the inequality. One possible reason for this is the dependence of the slope of the bolt load-deflection characteristic on clearance.

The curves in Figure 5, Appendix B show that while the characteristic is primarily linear, its slope depends on clearance. The greater the clearance the greater deflection and the greater the apparent yield under a given load. Thus, bolts with the greater clearance (as predicted by the presented relationship) must be deflected a greater amount to carry the same load. The modification of the relationship to include this effect could be a subject for further study. The unusually high loading on bolts 4 and 9 suggest that some fabrieation inequalities are present on the fasteners. To check this, the holes were inspected and
reneasured to see if the correct clearance had been applied. Discrepancies of less than eight ten-thomsandths were noted in all cases. In addition bolt diameters were rechecked and the Rockwell "C" hardness of each bolt was determined to insure that no extraneous bolts had been used. The checks uncovered no discrepancies. The possibility of misaligned holes remains as the only possible explanation. No means was available for checking the hole alignment.

It can be concluded from the preceding discmssion that the load distribution is very sensitive to slight discrepancies in fabrication. This, plus the indication that correct clearances for equal load distribution must be even smaller than those used in this test, indicates that the usefulness of this method of load distribution control is small, except for joints under high loads with five or more fasteners.

STRAIN READINGS IN MICROINCHES

| Joint | Gage Numbers |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 2 |
| Rtan 1 |  |  |  |  |  |  |  |  |  |
| 0 | 5920 | 6910 | 6290 | 6850 | 7000 | 6300 | 6740 | 7270 | 7810 |
| 2,000 | 5970 | 6900 | 6300 | 6920 | 7050 | 6350 | 6850 | 7340 | 7780 |
| 4,000 | 6030 | 6950 | 6370 | 7030 | 7130 | 6470 | 7010 | 7480 | 7930 |
| 6,000 | 6060 | 6960 | 6390 | 7110 | 7190 | 6530 | 7120 | 7580 | 8040 |
| 8,000 | 6080 | 6940 | 6380 | 7140 | 7200 | 6550 | 7220 | 7640 | 8160 |
| 10,000 | 6170 | 6990 | 6440 | 7230 | 7290 | 6630 | 7350 | 7750 | 8300 |
| 12,000 | 6210 | 7030 | 6490 | 7320 | 7380 | 6740 | 7480 | 7890 | 8430 |
| 14,000 | 6250 | 7040 | 6530 | 7370 | 7420 | 6810 | 7580 | 7970 | 8520 |


| Run ${ }^{2}$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 5960 | 6930 | 6290 | 6890 | 7050 | 6330 | 6790 | 7270 | 7710 |
| 2,000 | 5940 | 6890 | 6260 | 6920 | 7040 | 6350 | 6860 | 7330 | 7730 |
| 4,000 | 5970 | 6910 | 6330 | 7020 | 7110 | 6440 | 7000 | 7430 | 7870 |
| 6,000 | 6080 | 6940 | 6370 | 7110 | 7160 | 6500 | 7090 | 7540 | 8000 |
| 8,000 | 6090 | 6970 | 6400 | 7170 | 7210 | 6560 | 7240 | 7640 | 8110 |
| 10,000 | 6180 | 6990 | 6430 | 7240 | 7280 | 6640 | 7350 | 7730 | 8240 |
| 12,000 | 6200 | 7020 | 6490 | 7320 | 7350 | 6720 | 7500 | 7850 | 8340 |
| 14,000 | 6240 | 7050 | 6550 | 7390 | 7420 | 6810 | 7580 | 7960 | 8460 |


| Run 3 |  |  |  |  |  |  |  |  |  |
| ---: | ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 5940 | 6920 | 6280 | 6860 | 7000 | 6310 | 6780 | 7240 | 7640 |
| 2,000 | 5970 | 6900 | 6270 | 6930 | 7050 | 6350 | 6850 | 7310 | 7700 |
| 4,000 | 5980 | 6900 | 6310 | 7010 | 7080 | 6410 | 7010 | 7410 | 7820 |
| 6,000 | 6050 | 6930 | 6350 | 7080 | 7160 | 6480 | 7100 | 7510 | 7930 |
| 8,000 | 6110 | 6960 | 6390 | 7160 | 7210 | 6540 | 7220 | 7620 | 8050 |
| 10,000 | 6140 | 6990 | 6450 | 7250 | 7280 | 6620 | 7340 | 7740 | 8170 |
| 12,000 | 6180 | 7030 | 6510 | 7330 | 7360 | 6720 | 7490 | 7850 | 8350 |
| 14,000 | 6220 | 7050 | 6540 | 7380 | 7420 | 6800 | 7580 | 7940 | 8450 |
| 16,000 | 6260 | 7100 | 6590 | 7480 | 7500 | 6890 | 7700 | 8060 | 8600 |
| 18,000 | 6330 | 7130 | 6640 | 7550 | 7580 | 6990 | 7820 | 8170 | 8710 |
| 20,000 | 6370 | 7160 | 6680 | 7650 | 7660 | 7110 | 8000 | 8310 | 8890 |
| 23,000 | 6440 | 7200 | 6730 | 7800 | 7780 | 7250 | 8200 | 8500 | 9150 |


| Run 4 |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 5980 | 6960 | 6300 | 6900 | 7030 | 6310 | 6970 | 7330 | 7820 |
| 24,500 | 6380 | 7250 | 6750 | 7910 | 7960 | 7430 | 8460 | 8650 | 9330 |
| 25,500 | $64 \cdot 20$ | 7230 | 6790 | 7980 | 7990 | 7450 | 8600 | 8720 | 9450 |
| 30,000 | 6480 | 7290 | 6800 | 8200 | 8220 | 7700 | 8900 | 9060 | 9770 |

TABLE I (Continued)

| Joint |  | Gage Numbers |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Load | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| Run 1 1-13 - 12 |  |  |  |  |  |  |  |  |  |
| 0 | 7650 | 8130 | 7130 | 5840 | 6200 | 5820 | 6960 | 7760 | 8060 |
| 2,000 | 7870 | 8300 | 7350 | 5980 | 6450 | 6050 | 7130 | 7960 | 8200 |
| 4,000 | 8010 | 8520 | 7570 | 6200 | 6660 | 6290 | 7290 | 8100 | 8320 |
| 6,000 | 8300 | 8700 | 7770 | 6380 | 6840 | 6480 | 7460 | 8250 | 8490 |
| 8,000 | 8460 | 8840 | 7920 | 6600 | 7020 | 6650 | 7600 | 8400 | 8640 |
| 10,000 | 8650 | 9020 | 8120 | 6770 | 7200 | 6850 | 7740 | 8540 | 8760 |
| 12,000 | 8850 | 9200 | 8270 | 7000 | 7400 | 7010 | 7890 | 8700 | 8910 |
| 14,000 | 9100 | 9330 | 8450 | 7200 | 7520 | 7240 | 8030 | 8770 | 8990 |


| Run 2 |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 7650 | 8130 | 7200 | 5730 | 6270 | 5890 | 7020 | 7820 | 8080 |
| 2,000 | 7870 | 8310 | 7350 | 5990 | 6490 | 6100 | 7190 | 8010 | 8230 |
| 4,000 | 8070 | 8490 | 7530 | 6200 | 6700 | 6280 | 7350 | 8150 | 8410 |
| 6,000 | 8290 | 8700 | 7740 | 6400 | 6860 | 6480 | 7510 | 8320 | 8570 |
| 8,000 | 8480 | 8860 | 7950 | 6600 | 7000 | 6630 | 7640 | 8430 | 8720 |
| 10,000 | 8660 | 9030 | 8110 | 6800 | 7230 | 6820 | 7780 | 8570 | 8810 |
| 12,000 | 8840 | 9200 | 8280 | 7020 | 7330 | 7020 | 7950 | 8700 | 8920 |
| 14,000 | 9030 | 9350 | 8500 | 7160 | 7570 | 7200 | 8070 | 8820 | 9060 |


| Rin 3 3 |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 7620 | 8090 | 7130 | 5790 | 6250 | 5850 | 7010 | 7830 | 8080 |
| 2,000 | 7890 | 8310 | 7330 | 6020 | 6480 | 6080 | 7200 | 8020 | 8250 |
| 4,000 | 8070 | 8480 | 7530 | 6290 | 6650 | 6280 | 7380 | 8170 | 8390 |
| 6,000 | 8290 | 8690 | 7750 | 6430 | 6880 | 6470 | 7550 | 8330 | 8580 |
| 8,000 | 8480 | 8830 | 7930 | 6630 | 7020 | 6620 | 7680 | 8490 | 8690 |
| 10,000 | 8660 | 9020 | 8100 | 6850 | 7180 | 6790 | 7820 | 8570 | 8840 |
| 12,000 | 8850 | 9190 | 8310 | 7030 | 7350 | 6990 | 7970 | 8700 | 8910 |
| 14,000 | 9030 | 9330 | 8460 | 7160 | 7520 | 7170 | 8100 | 8840 | 9070 |
| 16,000 | 9200 | 9500 | 8650 | 7380 | 7680 | 7350 | 8210 | 8970 | 9200 |
| 18,000 | 9400 | 9660 | 8850 | 7550 | 7830 | 7510 | 8350 | 9070 | 9320 |
| 20,000 | 9520 | 9830 | 9050 | 7720 | 8000 | 7700 | 8470 | 9190 | 9490 |
| 23,000 | 9870 | 10070 | 9260 | 8000 | 8230 | 7960 | 8670 | 9380 | 9600 |


| Run 4 |  |  |  |  |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 7690 | 8160 | 7240 | 5560 | 6450 | 6030 | 7190 | 7970 | 8230 |
| 24,500 | 10100 | 9840 | 9580 | 8320 | 8580 | 8350 | 8960 | 9610 | 9890 |
| 25,500 | 10180 | 10350 | 9670 | 8490 | 8640 | 8330 | 9000 | 9610 | 9900 |
| 30,000 | 10630 | 10670 | 10020 | 8850 | 8940 | 8740 | 9260 | 9880 | 10160 |

TABLE I (continued)

| Joint | Gage Numbers |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Load | 19 | 20 | 21 | 22 | 23 | 24 |
| Run 1 |  |  |  |  |  |  |
| 0 | 6230 | 5650 | 6210 | 5230 | 3910 | 5000 |
| 2,000 | 6300 | 5760 | 6240 | 5250 | 3940 | 4850 |
| 4,000 | 6500 | 5780 | 6330 | 5240 | 3930 | 4850 |
| 6,000 | 6610 | 5880 | 6440 | 5270 | 3930 | 4900 |
| 8,000 | 6730 | 5930 | 6530 | 5310 | 3980 | 4870 |
| 10,000 | 6850 | 6000 | 6580 | 5340 | 3960 | 4930 |
| 12,000 | 6930 | 6100 | 6670 | 5380 | 3960 | 4970 |
| 14,000 | 7030 | 6180 | 6700 | 5430 | 4010 | 4960 |
| $\operatorname{Ran} 2$ |  |  |  |  |  |  |
| 0 | 6290 | 5660 | 6150 | 5250 | 3950 | 5060 |
| 2,000 | 6390 | 5730 | 6240 | 5260 | 3950 | 4910 |
| 4,000 | 6530 | 5800 | 6350 | 5260 | 3930 | 4880 |
| 6,000 | 6640 | 5890 | 6430 | 5270 | 3920 | 4950 |
| 8,000 | 6720 | 5960 | 6530 | 5300 | 3930 | 4920 |
| 10,000 | 6850 | 6030 | 6580 | 5330 | 3950 | 4960 |
| 12,000 | 6980 | 6120 | 6630 | 5400 | 3980 | 5000 |
| 14,000 | 7070 | 6200 | 6750 | 5430 | 4000 | 5030 |


| Run 3 |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 6280 | 5680 | 6130 | 5250 | 3950 | 4890 |
| 2,000 | 6400 | 5740 | 6230 | 5260 | 3950 | 4900 |
| 4,000 | 6550 | 5820 | 6330 | 5250 | 3940 | 4940 |
| 6,000 | 6650 | 5910 | 6440 | 5290 | 3930 | 4980 |
| 8,000 | 6770 | 5990 | 6540 | 5320 | 3950 | 4920 |
| 10,000 | 6850 | 6040 | 6570 | 5350 | 3960 | 4980 |
| 12,000 | 6960 | 6120 | 6650 | 5390 | 3970 | 4990 |
| 14,000 | 7070 | 6200 | 6730 | 5430 | 3990 | 5040 |
| 16,000 | 7190 | 6330 | 6860 | 5490 | 4030 | 5030 |
| 18,000 | 7280 | 6390 | 6930 | 5540 | 4070 | 5160 |
| 20,000 | 7390 | 6480 | 7000 | 5610 | 4120 | 5180 |
| 23,000 | 7550 | 6610 | 7150 | 5660 | 4160 | 5250 |


| Run 4 |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 6450 | 5860 | 6280 | 5420 | 4130 | 5320 |
| 24,500 | 7770 | 6890 | 7370 | 5950 | 4460 | 5790 |
| 25,500 | 7760 | 6840 | 7330 | 5950 | 4420 | 5740 |
| 30,000 | 7970 | 7020 | 7520 | 6040 | 4500 | 5800 |

TABLE II
INDIVIDUAL BOLT LOADS

| Joint | : $\quad$ Bolt Locations |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Load | $: 1$ | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| Run 1 |  |  |  |  |  |  |  |  |  |  |
| 2,000 | 154 | 55 | 309 | 1338 | 144 | 117 | 336 | 910 | 937 | -300 |
| 4,000 | 700 | 446 | 737 | 1729 | 388 | 90 | 1089 | 1247 | 1938 | -364 |
| 6,000 | 882 | 874 | 1101 | 2785 | 368 | 422 | 1274 | 1756 | 2757 | -209 |
| 8,000 | 846 | 1098 | 1765 | 3304 | 993 | 693 | 1665 | 2312 | 3267 | 63 |
| 10,000 | 1456 | 1274 | 2129 | 3877 | 1264 | 1019 | 2129 | 2794 | 3785 | 273 |
| 12,000 | 2093 | 1510 | 2466 | 4277 | 1654 | 1235 | 2512 | 3376 | 4359 | 518 |
| 14,000 | 2111 | 1984 | 2793 | 51.60 | 1952 | 1561 | 3312 | 3613 | 4723 | 791 |
| Run 2 |  |  |  |  |  |  |  |  |  |  |
| 2,000 | -336 | 372 | 419 | 1210 | 335 | -93 | 546 | 728 | 1246 | -427 |
| 4,000 | 91 | 819 | 700 | 1757 | 633 | 87 | 910 | 1183 | 2393 | -573 |
| 6,000 | 637 | 882 | 1092 | 2694 | 695 | 390 | 1124 | 1847 | 3003 | -364 |
| 8,000 | 846 | 1192 | 1665 | 3304 | 993 | 902 | 1429 | 2275 | 3758 | -364 |
| 10,000 | 1327 | 1374 | 2002 | 3850 | 1446 | 1019 | 2193 | 2639 | 4231 | -82 |
| 12,000 | 1665 | 1738 | 2421 | 4304 | 1872 | 1472 | 2493 | 3067 | 4604 | 364 |
| 14,000 | 2056 | 2039 | 2675 | 5060 | 2170 | 1743 | 3066 | 3340 | 5242 | 609 |
| Run 3 |  |  |  |  |  |  |  |  |  |  |
| 2,000 | 0 | 492 | 118 | 1390 | 0 | -100 | 430 | 820 | 795 | 55 |
| 4,000 | 155 | 845 | 760 | 2000 | 240 | -50 | 900 | 1250 | 1730 | 120 |
| 6,000 | 480 | 1200 | 700 | 3370 | 250 | 250 | 1070 | 1920 | 2332 | 328 |
| 8,000 | 975 | 1275 | 1490 | 3560 | 700 | 780 | 1320 | 2220 | 3380 | 300 |
| 10,000 | 1300 | 1680 | 1850 | 3990 | 1180 | 1100 | 1880 | 2860 | 3560 | 600 |
| 12,000 | 1760 | 2020 | 2400 | 4520 | 1300 | 1400 | 2500 | 3110 | 4105 | 785 |
| 14,000 | 2030 | 2301 | 2680 | 4980 | 2000 | 2000 | 2620 | 3580 | 4680 | 1120 |
| 16,000 | 2460 | 2800 | 2940 | 5600 | 2200 | 2300 | 3200 | 3050 | 5550 | 1400 |
| 18,000 | 2920 | 2990 | 3290 | 6200 | 2600 | 2800 | 3600 | 4210 | 5310 | 2080 |
| 20,000 | 3270 | 3570 | 4260 | 5600 | 3200 | 3200 | 3950 | 4400 | 5960 | 2490 |
| 23,000 | 3740 | 4360 | 4700 | 6500 | 3700 | 3850 | 4650 | 4700 | 7130 | 2670 |
| $\begin{aligned} & \text { Run }{ }^{4} 4,500 \end{aligned}$ | 3460 | 4990 | 4650 | 6500 | 4900 | 2600 | 6400 | 5050 | 6450 | 4000 |
| 25,500 | 3640 | 5180 | 5280 | 7700 | 3700 | 2900 | 7000 | 5400 | 6480 | 3720 |
| 30,000 | 4000 | 6800 | 6200 | 8000 | 5000 | 4300 | 7700 | 6100 | 7450 | 4450 |



Figure 4. Bolt Load Distribution at Varioús Joint Loadings

1. Tate, Manford B., and Samuel J. Rosenfield, "Preliminary Investigation of the Loads Carried by Individual Bolts in Bolted Joints" National Advisory Committee on Aeronautics, Technical Note 1051, May, 1946
2. Jenkin, E.S., "Rational Design of Fastenings," Society of Automotive Engineers Journal, Volume 52, No. 9 , September, 1944, pp. 421-429

APPENDIX A

## SAMPLE CALCULATION OF CLEARANCES

Given: 1. Joint load $P=23,000$ pounds.
2. Stress area $A=(1.75) "(0.501)^{\prime \prime}=0.876$ sq. in.
3. Bolt spacing $m=2$ in.
4. Number of bolts $N=5$.
5. Modulus of elasticity $E=10.4 \times 10^{6}$

$$
C_{i}=\frac{2 P m}{N A H} \sum_{i}^{\frac{-N-1}{2}}(N-2 i) \quad \frac{N-1}{2}=\frac{5-1}{2}=.2
$$

Substitution of given values yields

$$
c_{i}=\frac{(2)(23.000)(2)}{(5)(0.876)\left(10.4 \times 10^{6}\right)} \sum_{i}^{2}(5-2 i)
$$

Bol
1
2

3
1
$5-2 i$
$\sum_{\substack{i \\ 4 \\ i}}^{2}(5-2 i)$
$C_{i}$
0.00808
0.00202

## APPETVIX B

## DETERMINATION OF BOLT LOAD-DEFLECTIOF CHARACTERISTIC WITH CLEARANCE

To determine the effect of clearance on the bolt loaddeflection characteristic, one bolt, butt joints were tested with various clearances. The clearances used were $0.0046^{\prime \prime}$, 0.018", and "infinite". The "infinite" clearance hole was obtained, by removing material from the hole wall opposite the side in bearing contact. This allows unrestrained deflection of the bolt.

The configuration of the test models and the instrumentation of the test set-up is shown in Plate III. The models were made of 7075-T6 rolled aluminum plate and the bolts were fabricated from carbon steel drill rod and heat treated. The heat treatment consisted of heating to $1440^{\circ} \mathrm{F}$. , quenching in oil, and tempering at $400^{\circ} \mathrm{F}$. The resulting Rockwell C hardness was approximately 38. The holes were drilled and the $0.0046^{\prime \prime}$ clearance hole was finish reamed. On assembly, $3 / 8^{\prime \prime}$ thick collars were placed under each nut to dupiicate the boit end action of an ordinary installation without collar, and allow the threaded portion of the bolt to be kept clear of the bearing area of the bolt.

Slipping of the specimen in the jaws of the testing machine occurred during the first tests. Because of the
method of measuring, absolutely no slippage between the specimen and the lower jaw could be allowed. Therefore, extensions of cloio commercial steel were attached to the ends of the specimen to provide a soft and positive gripping surface. The deflections were measured directly with mechanical strain gages. Pins $3 / 32^{\prime \prime}$ in diameter were inserted in grooves in the straps and a hole in the plate in such a manner that they rested against the bolt. They were free to move so that any motion of the bolt would be transmitted through the pin to its free end. The strain gages were placed so as to indicate the axial movement of these pins. Caliper and dial gages as shown in Plate III were used. They were clamped to supports which were, in turn, clamped to the stationary bolster of the testing machine. Thus, the motion indicated by the gages was the motion of the three points on the bolt with respect to a common point - the bolster. By averaging the two bolt end movements and subtracting the bolt center movement, the deflection of the ends of the bolt with respect to the center was obtained.

Three runs were made on each specimen and the averaged results are shown in Figure 5.: The load was applied in increments of 200 pounds over a range of 200 pounds to 3000 pounds. Readings at a load of 150 pounds were also taken and used as a zero reference since loadings of less than this allowed slippage of the specimen with resulting disruption of strain readings.

PIATE III
ONE BOLT TEST SPECINEN AND TEST SET-UP



Figure 5. Load-Deflection Curves for $0.250^{\prime \prime}$ Dianeter Bolt with Various Clearances

VITA
Warren Lee Gilmour
Candidate for the Degree of
Master of Science

Thesis: A STUDY OF THE EFFECT OF VARIABLE CLEARANCES ON THE BOLT LOAD DISTRIBUTION IN A MULTI-FASTENER LAP JOINT

Major Field: Mechanical Engineering
Biographical:
Personal Data: Born in Kingfisher, Oklahoma, November 30, 1932, the son of Glenn and Elizabeth Irene Gilmour.

Education: Attended grade school in Kingfisher, Oklahoma; graduated from Kingfisher High School in 1950; received the Bachelor of Science degree from Oklahoma state University, with a major in Mechanical Engineering in May, 1958; completed requirements for the Master of Science degree in August, 1959.

Experience: Served with the United States Navy from January, 1951 until September, 1954; during summers of 1955 , 1956, and 1957 worked for Bradley Mechanical Contracting in Stillwater, Oklahoma, and during summer of 1958 worked for Douglas Aircraft Company in Tulsa, Oklahoma.

Professional Organizations: Member of the Institute of Aeronautical Sciences.

