

A REPORT GENERATING LINEAR PROGRAMMING MODEL
FOR SCHEDULING THE ISSUANCE OF LARGE
CERTIFICATES OF DEPOSIT

By

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Bachelor of Science

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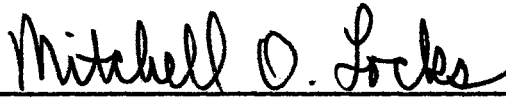
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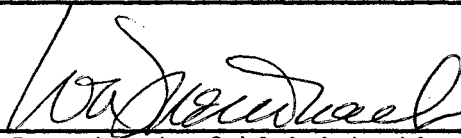
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Report Approved:



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Title of Study: A REPORT GENERATING LINEAR PROGRAMMING MODEL FOR
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Candidate for Degree of Master
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Scope of Study: This study concerns a linear programming model which schedules the issuance of large (\$100,000 or over) Certificates of Deposit (CD's) by a commercial bank. The objective of the study is to construct a model that will generate management reports based on the solution of the linear programming model. The solution of the linear programming problem represents a minimization of the total interest cost for all Certificates of Deposit to be issued during a 13-month period, based on an interest rate forecast supplied by the Chase Econometric Institute, subject to constraints which reflect management policy with respect to growth, turnover, and liquidity of the CD portfolio and the types of markets serviced by these instruments. The management reports prepared by the model are a summary of the linear program solution based on statistics of sales, outstanding amounts, and weighted average interest rates per type of instrument.

Findings and Conclusions: The model predicts an optimal CD sales schedule for thirteen months while minimizing the total interest cost of the sales over the planning period and generates four management reports based on the sales schedule predicted. However, the model involves only one type of liability of the bank and assumes certainty in predicting the CD sales schedule. The results of this study suggest that further research concerning the inclusion of risk constraints, more comprehensive management policy considerations, and economic considerations into the model is needed to make the model a more effective management decision making tool.

ADVISOR'S APPROVAL

Mitchell O. Locke

PREFACE

This study is concerned with the modification of an existing Certificates of Deposit scheduling model of a commercial bank. The primary objective is to construct a model that will generate various management reports based on the solution of the linear programming model that minimizes the total cost of the issuance of the Certificates of Deposit over a thirteen-month period.

The author wishes to express his appreciation to his major advisor, Dr. Mitchell O. Locks, for his guidance and assistance throughout this study. Appreciation is also expressed to Mr. James Bruce of the Liberty National Bank in Oklahoma City, Oklahoma, for his assistance in the preparation of the relevant banking information used in this study.

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CHAPTER I

INTRODUCTION

This paper concerns a linear programming (LP) model which schedules the issuance of large (\$100,000 or over) Certificates of Deposit (CD's) by a commercial bank. The original version of this model, which was prepared by Lester R. Harris [17] as an MBA Research Report at Oklahoma State University, schedules CD's for the fixed 13-month period June, 1974 to June, 1975, inclusive, using IBM's Mathematical Programming System Extended (MPSX). This paper reports on a modification of that model which generates a management report by editing and summarizing the LP output; the model also has a "rolling" feature which makes it possible to prepare this report for any consecutive 13-month period, as well as, a graphical summarization of the output which is prepared on a CALCOMP plotter.

The model is an application of an LP problem designed to minimize an objective function subject to a number of constraining equations. The solution is a set of variables, each variable representing the amount of a type of CD issued during a particular month for a specified maturity. This solution represents a minimization of the total interest cost for all CD's to be issued during the 13-month period, based upon an interest rate forecast supplied by the Chase Econometric Institute, subject to constraints which express management policy with respect to growth, turnover, and liquidity of the CD portfolios, and the types of markets serviced by these instruments.¹

The management report prepared by the model is a summary of the LP solution based upon statistics of sales, outstanding amounts, and weighted average interest rates per type of instruments. There are three basic types of CD's, each representing a different market: local (type-0), national (type-6), and special (type-8).

In preparing this study, a feature of MPSX known as "READCOMM" [26] was used which enables the programmer to write a FORTRAN program to modify the LP output in any way which is convenient for his purposes. Variables are selected from the solution set of the LP program, temporarily stored, and used to provide the management report output.²

Lastly, recommendations and suggestions are provided concerning further improvements in the model.

FOOTNOTES

¹The interested reader should refer to Appendix A for the description and an abbreviated example of the LP model.

²See Appendix B for a description of the programs written for this model. Also, see references [25] and [26] for a description of the MPSX and READCOMM.

CHAPTER II

REVIEW OF THE LITERATURE

Introduction

A review of the current literature reveals a growing awareness of the applicability of modeling techniques as an analytical tool to the management of bank assets, liabilities, and investments. The present chapter discusses some early approaches to financial management and concludes by discussing an inter-temporal, dynamic model for bond portfolio management which provided some suggestions for improvement in the model discussed by this report.

Portfolio Management

The Problem. The essence of the management problem of portfolio selection is the need to achieve a proper balance between income, adequate liquidity to meet loan demand and deposit withdrawals, and the risk of default when considering the total of a bank's financial position. Portfolio decisions made at any time directly affect a bank's current, as well as future, income and profits. Since the selection of different alternatives invariably represent a trade-off between profits, liquidity, and risk, the management is presented with a perplexing problem. The evaluating and weighing of the factors involved in making the decision between alternatives have caused managers to seek improved approaches to portfolio management.

Early Approaches. Two basic approaches enumerated in the literature to provide an assist for bank management are the "pooled-funds" approach and the "asset allocation" approach (see Broaddus, reference [6]). Under the pooled-funds concept, bank management arbitrarily defines a fixed liquidity standard and each dollar attracted is allocated in identical proportion among its various categories of assets. A major fault of this procedure is its failure to consider variations in liquidity needs that arise from variations in the structure of liability and loan accounts.

Another portfolio management technique is the asset allocation approach. This technique recognizes the variations in liquidity needs and allocates funds obtained from rapidly turned-over liabilities to relatively short maturity assets, and vice versa. In Broaddus's opinion the asset allocation approach is an improvement over the pooled-funds approach, however, the technique possesses some fundamental weaknesses. First, turnover rate is a poor guide to liquidity requirements since the turnover rate does not consider account stability, that is, the net daily variation of an account's total balance. Second, the technique is arbitrary and inflexible, since the technique has neither a clearly-defined bank goal which guides the determination of the various fund allocation procedures, nor a systematic procedure for changing the allocation process as changing external conditions, such as asset yields, dictate. Some of the more recent modeling techniques described below avoid these difficulties.

Simulation. Perhaps the earliest modeling technique was the application of simulation for financial management. Markowitz [27] used this technique in employing quadratic programming as an illustration

of solving the problems of portfolio selection. This method consists of a blending of mathematical and statistical techniques to assist persons skilled in investment management. However, as with the techniques mentioned previously, Markowitz's technique does not consider some of the important interactions between income, liquidity, and risk. More recently, developments in applying the techniques of mathematics and economics by means of computers have enhanced the modeling of the financial decision process.

Linear Programming (LP). By use of the techniques of linear programming, it is possible to formulate a model which is a more factual representation of the banking environment to help management in its decision process. One application of an LP model was developed by Weingartner [32] for the financial planning problem of "capital budgeting under capital rationing". Other models for financial planning have also been developed by Baumol and Quandt [1] and Carleton [7].

In the area of portfolio management the first model was developed by Chambers and Charnes [9]. Their model is a comprehensive attempt at determining an optimal portfolio for an individual bank over several time periods in considering reserve requirements and a "balanced" portfolio. The reserve requirements state that part of the bank's assets must be held in cash or deposited with the Federal Reserve. The balanced portfolio restriction was a set of measures used by the bank examiners of the Federal Reserve System.

Another application of an LP model for portfolio management was developed at the Banker's Trust Company and is described in papers by Cohen and Hammer [12] and Cohen, Hammer, and Schneider [13]. The

objective of their model is to maximize net income while "(1) maintaining both a safe and an adequately liquid portfolio, and (2) assuring that neither the bank's short-run nor long-run flexibility will be impaired".

The model starts from the bank's initial position and works with management's best estimates of future interest rates in order to determine the ideal posture of the bank's portfolio. The model determines an optimal sequence of balance-sheet positions over the several planning periods that lie between the current date and the planning horizon. However, as with the aforementioned models, the Cohen and Hammer model is limited in that the model does not consider either the dynamic structure of the portfolio management problem or the uncertainty of future events. In an attempt to overcome these problems a dynamic model for bond portfolio management was developed by Bradley and Crane [5] which could have applications to other aspects of bank portfolio management.

The Bradley and Crane model is an LP model which includes both asset and liability positions of the bank, takes into account the uncertainty of future events, and considers the dynamic structure of the portfolio management problem. The model incorporates three decision variables, buy, sell, and hold, for each asset and liability, and forecasts the values of these variables over a specified multiperiod planning horizon. The model also facilitates the specification of variable-length periods for the planning horizon. It also considers the dynamic interactions between the various assets and liabilities and the probability of random events in predicting the decision variables over the planning horizon.

Finally, because the portfolio management problem can tend to become large and difficult to solve, Bradley and Crain discuss the decomposition algorithm of mathematical programming¹ in solving the overall portfolio management model.

Summary

Any review of the current literature will reveal that modeling techniques are currently being applied to many areas of financial and bank management problems. This chapter has provided a brief discussion of the development of some analytical models, such as LP models, in the area of financial and bank management. The remainder of this study is concerned with a model for scheduling the issuance of large Certificates of Deposit for a commercial bank.

FOOTNOTE

¹In the decomposition procedure some of the constraining equations are treated implicitly as subproblems of the original LP. Solutions to the subproblems are then used in obtaining the solution to the master program. This technique permits the model to be large enough to solve any realistic description of the portfolio management problem, while cutting computing time and cost substantially. For a detailed explanation of the decomposition procedure see references, Dantzig and Wolfe [14] and [15], Gass [17], Himmelblau [23], and Zionts [33].

CHAPTER III

A REPORT GENERATING LINEAR PROGRAMMING MODEL FOR SCHEDULING THE ISSUANCE OF LARGE CERTIFICATES OF DEPOSIT

Introduction

The report generating model generates four different customized management reports which summarize the LP program solution:

- (1) Maturity Date Analysis by Type of Certificates of Deposit
- (2) Predicted Certificates of Deposit Sales by Maturity Period
- (3) Summary Totals by Month
- (4) Graphical Summary.

Maturity Date Analysis Report

Within this report information predicted by the LP program is summarized for the three CD markets serviced, local (type-0), national (type-6), and special (type-8), for each of the thirteen months of the planning horizon. This report presents the amounts of CD's maturing in future periods, the percent of the total amount outstanding that that amount represents, and an associated weighted average interest rate for the outstanding amount of all instruments of a given type.

This maturity date analysis report provides a "picture" of the

bank's CD liability requirements for each of the thirteen planning periods by type of CD. Additionally, the report provides information for computing interest cost figures associated with the maturing CD amounts.

Figure 1 is the maturity date report for the 13-month period June, 1974 to June, 1975, coinciding with the fixed period covered by the model described in reference [20].

Predicted Sales Report

This report represents a summarization of the predicted sales amounts for the planning periods by type of CD and maturity period. For each type CD within a certain maturity period the beginning balance, current predicted sales, forecasted interest rate, and the net amount outstanding are reported.

Figure 2 gives the predicted sales report for the planning period June, 1974 to June, 1975.

Summary Report

This section (Figure 3) contains the summary totals of monthly sales, monthly payout of CD principles, and the total net amounts outstanding for each of the 13-months of the planning period.

Graphical Report

The graphical report (Figure 4) is divided into three sections: sales totals, summary totals, and cost. The sales totals section is a graphical representation of the total sales of each type of CD for each of the next thirteen months, plus the total of all sales for each month.

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

***** TYPE 0 *****			***** TYPE 6 *****			***** TYPE 8 *****		
CERT AMTS	PCT OF	WGHTD AVG	CERT AMTS	PCT OF	WGHTD AVG	CERT AMTS	PCT OF	WGHTD AV
MATURING	TOT AMT	INTST RATE	MATURING	TOT AMT	INTST RATE	MATURING	TOT AMT	INTST RA
JLA 1974								

\$ 28412.00	24.91	9.7163	\$ 2000.00	4.90	10.8746	\$ 350.00	16.44	7.995
38534.99	33.75	9.8680	12363.54	30.26	10.9999	1444.00	67.83	8.501
16344.00	14.33	10.2200	8885.44	21.75	9.5801	0.0	0.0	0.0
5410.63	4.74	8.2565	5920.00	14.49	10.3670	185.00	8.69	9.000
3169.70	2.78	10.0001	1685.44	4.13	10.6799	0.0	0.0	0.0
22174.00	19.44	8.9571	10000.00	24.48	9.4000	150.00	7.05	6.000
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
\$ 114045.31		9.6308	\$ 40854.42		10.1884	\$ 2129.00		8.286
JUL 1974								

\$ 38534.99	32.02	9.8680	\$ 12363.54	25.25	10.9999	\$ 1444.00	81.17	8.501
38092.91	31.65	10.0713	18994.55	38.79	10.2930	0.0	0.0	0.0
17893.18	14.87	9.4238	5920.00	12.09	10.3670	185.00	10.40	9.000
3169.70	2.63	10.0001	1685.44	3.44	10.6799	0.0	0.0	0.0
22174.00	18.42	8.9571	10000.00	20.42	9.4000	150.00	8.43	6.000
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
487.20	0.40	9.5101	0.0	0.0	0.0	0.0	0.0	0.0
\$ 120351.57		9.7005	\$ 48963.53		10.3114	\$ 1779.00		8.342
JLG 1974								

\$ 38092.91	31.40	10.0713	\$ 18994.55	33.80	10.2930	\$ 0.0	0.0	0.0
41001.32	33.80	9.2808	20800.00	37.01	10.0756	185.00	55.22	9.000
3169.70	2.61	10.0001	6400.00	11.39	10.1274	0.0	0.0	0.0
34257.91	28.24	8.9757	10000.00	17.80	9.4000	150.00	44.78	6.000
4300.85	3.55	8.8500	0.0	0.0	0.0	0.0	0.0	0.0
487.20	0.40	9.5101	0.0	0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
\$ 121309.89		9.4473	\$ 56194.54		10.0347	\$ 335.00		7.656

Figure 1. Maturity Date Report

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

TYPE 0			TYPE 6			TYPE 8			
CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD INTST	
SEP 1974									
4	\$ 41001.32	32.59	9.2808	\$ 20800.00	35.49	10.0756	\$ 185.00	55.22	9.0
4	27149.60	21.58	8.4019	19630.00	33.50	9.4083	0.0	0.0	0.0
4	46578.21	37.34	8.7549	12295.44	20.98	9.3309	150.00	44.78	6.0
4	4937.23	3.92	8.7443	3780.00	6.45	8.8999	0.0	0.0	0.0
5	5736.95	4.56	8.0093	2094.56	3.57	8.7399	0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	\$ 125803.31		8.8157	\$ 58599.99		9.5722	\$ 335.00		7.0
CCT 1974									
4	\$ 27149.60	23.95	8.4019	\$ 19630.00	33.83	9.4083	\$ 0.0	0.0	0.0
4	63923.30	56.39	8.4805	19779.99	34.09	8.9975	150.00	100.00	6.0
4	5147.23	4.54	8.7013	7244.56	12.48	8.6704	0.0	0.0	0.0
5	13751.75	12.13	7.7474	7710.00	13.29	8.4122	0.0	0.0	0.0
5	3379.70	2.98	7.4001	3665.44	6.32	8.1301	0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	\$ 113351.58		8.3505	\$ 58029.99		8.9631	\$ 150.00		6.0
NOV 1974									
4	\$ 63923.30	42.14	8.4805	\$ 19779.99	37.37	8.9975	\$ 150.00	100.00	6.0
4	26055.80	17.18	7.5690	13539.11	25.58	8.3817	0.0	0.0	0.0
5	27097.59	17.87	7.5073	10095.44	19.07	8.3196	0.0	0.0	0.0
5	8527.70	5.62	7.2371	3665.44	6.93	8.1301	0.0	0.0	0.0
5	13395.30	8.83	6.9700	5850.00	11.05	7.7301	0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	12675.60	8.36	6.8401	0.0	0.0	0.0	0.0	0.0	0.0
	\$ 151675.29		7.8096	\$ 52929.99		8.5105	\$ 150.00		6.0

Figure 1. (Continued)

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

***** TYPE 0 *****			***** TYPE 6 *****			***** TYPE 8 *****			
CERT AMTS	PCT OF	WGHTD AVG	CERT AMTS	PCT OF	WGHTD AVG	CERT AMTS	PCT OF	WGHTD	
MATURING	TOT AMT	INTST RATE	MATURING	TOT AMT	INTST RATE	MATURING	TOT AMT	INTST	
CEC 1974									
4	\$ 26055.80	22.89	7.5650	\$ 13539.11	25.77	8.3817	\$ 0.0	0.0	0.0
5	40260.39	35.38	7.4232	19935.44	37.94	8.1124	0.0	0.0	0.0
5	21420.70	18.82	7.2266	7130.00	13.57	8.0037	0.0	0.0	0.0
5	13395.30	11.77	6.9700	6084.56	11.58	7.7305	0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	12675.60	11.14	6.8401	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0	0.0	0.0	5850.00	11.13	7.5999	0.0	0.0	0.0
	\$ 113807.78		7.3013	\$ 52539.11		8.0657	\$ 0.0		0.0
JAN 1975									
5	\$ 40260.39	31.45	7.4232	\$ 19935.44	37.55	8.1124	\$ 0.0	0.0	0.0
5	34583.49	27.02	7.1576	12980.00	24.45	7.9388	0.0	0.0	0.0
5	13665.10	10.67	6.9729	8470.00	15.96	7.7585	0.0	0.0	0.0
5	13177.80	10.29	6.9902	5850.00	11.02	7.6999	0.0	0.0	0.0
5	12675.60	9.90	6.8401	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0	0.0	0.0	5850.00	11.02	7.5999	0.0	0.0	0.0
5	13650.00	10.66	6.7000	0.0	0.0	0.0	0.0	0.0	0.0
	\$ 128012.38		7.1348	\$ 53085.44		7.9115	\$ 0.0		0.0
FEB 1975									
i	\$ 34583.49	28.27	7.1576	\$ 12980.00	24.97	7.9388	\$ 0.0	0.0	0.0
i	35355.59	28.90	6.9892	17985.44	34.60	7.6852	0.0	0.0	0.0
i	26070.80	21.31	6.9803	9314.56	17.92	7.6591	0.0	0.0	0.0
i	12675.60	10.36	6.8401	0.0	0.0	0.0	0.0	0.0	0.0
i	0.0	0.0	0.0	5850.00	11.25	7.5999	0.0	0.0	0.0
i	13650.00	11.16	6.7000	0.0	0.0	0.0	0.0	0.0	0.0
i	0.0	0.0	0.0	5850.00	11.25	7.4099	0.0	0.0	0.0
	\$ 122335.48		6.9985	\$ 51980.00		7.7033	\$ 0.0		0.0

Figure 1. (Continued)

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

TYPE 0			TYPE 6			TYPE 8		
CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD INTST
MAR 1975								
\$ 35355.55	28.70	6.9892	\$ 17985.44	31.56	7.6852	\$ 0.0	0.0	0.0
\$ 39248.59	31.86	7.0137	\$ 15164.56	26.61	7.6323	\$ 0.0	0.0	0.0
\$ 13432.60	10.90	6.8519	\$ 2385.44	4.19	7.5598	\$ 0.0	0.0	0.0
\$ 0.0	0.0	0.0	\$ 5850.00	10.27	7.5999	\$ 0.0	0.0	0.0
\$ 35170.80	28.55	6.7368	\$ 9750.00	17.11	7.2699	\$ 0.0	0.0	0.0
\$ 0.0	0.0	0.0	\$ 5850.00	10.27	7.4099	\$ 0.0	0.0	0.0
\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0
\$ 123207.56		6.9100	\$ 56985.44		7.5578	\$ 0.0		0.0
APR 1975								
\$ 39248.59	30.88	7.0137	\$ 15164.56	28.00	7.6323	\$ 0.0	0.0	0.0
\$ 26610.39	20.94	6.9557	\$ 8235.44	15.20	7.6881	\$ 0.0	0.0	0.0
\$ 12420.80	9.77	7.1199	\$ 9314.56	17.20	7.6409	\$ 0.0	0.0	0.0
\$ 46820.80	38.41	6.8076	\$ 15600.00	28.80	7.3861	\$ 0.0	0.0	0.0
\$ 0.0	0.0	0.0	\$ 5850.00	10.80	7.4099	\$ 0.0	0.0	0.0
\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0
\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0
\$ 127100.58		6.9420	\$ 54164.55		7.5473	\$ 0.0		0.0
MAY 1975								
\$ 26610.39	22.63	6.9557	\$ 8235.44	15.51	7.6881	\$ 0.0	0.0	0.0
\$ 27300.00	23.21	7.1856	\$ 15164.56	28.57	7.7332	\$ 0.0	0.0	0.0
\$ 62700.00	54.16	6.9016	\$ 23835.44	44.90	7.5464	\$ 0.0	0.0	0.0
\$ 0.0	0.0	0.0	\$ 5850.00	11.02	7.4099	\$ 0.0	0.0	0.0
\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0
\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0
\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0	\$ 0.0	0.0	0.0
\$ 117610.39		6.9897	\$ 53085.44		7.6067	\$ 0.0		0.0

Figure 1. (Continued)

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

***** TYPE 0 *****			***** TYPE 6 *****			***** TYPE 8 *****				
CERT AMTS	PCT OF	WGHTD AVG	CERT AMTS	PCT OF	WGHTD AVG	CERT AMTS	PCT OF	WGHTD		
MATURING	TOT AMT	INTST RATE	MATURING	TOT AMT	INTST RATE	MATURING	TOT AMT	INTST		
JUN 1975										

5	\$ 27300.00	23.08	7.1856	\$ 15164.56	28.00	7.7332	\$	0.0	0.0	0.0
5	91000.00	76.92	7.0302	33149.99	61.20	7.6990		0.0	0.0	0.0
5	0.0	0.0	0.0	5850.00	10.80	7.4099		0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0
	\$ 118299.99		7.0661	\$ 54164.55		7.6774	\$	0.0		0.0

Figure 1. (Continued)

LIBERTY NATIONAL BANK

PREDICTED CERTIFICATES OF DEPOSIT SALES BY MATURITY PERIOD

30 DAY MATURITY

(DOLLAR AMOUNTS IN THOUSANDS)

	TYPE 0			TYPE 6			TYPE 8		
	*****			*****			*****		
	BEGINNING BALANCE		\$	BEGINNING BALANCE		\$	BEGINNING BALANCE		\$
	28412.00			2000.00			350.00		
MONTH	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING
JUN 74	\$ 12845.00	10.320	\$ 12845.00	\$ 12363.54	11.000	\$ 12363.54	\$ 0.0	11.000	\$ 0.0
JUL 74	21748.91	9.960	21748.91	10109.11	10.920	10109.11	0.0	10.920	0.0
AUG 74	23108.15	9.170	23108.15	14880.00	9.960	14880.00	0.0	9.960	0.0
SEP 74	23979.90	8.191	23979.90	13230.00	9.061	13230.00	0.0	9.061	0.0
OCT 74	16945.10	7.720	16945.10	7484.55	8.450	7484.55	0.0	8.450	0.0
NOV 74	20908.57	7.290	20908.57	6294.55	8.049	6294.55	0.0	8.049	0.0
DEC 74	13162.80	7.250	13162.80	9840.00	7.900	9840.00	0.0	7.900	0.0
JAN 75	13162.80	7.150	13162.80	5850.00	7.860	5850.00	0.0	7.860	0.0
FEB 75	21690.50	6.999	21690.50	9515.44	7.620	9515.44	0.0	7.620	0.0
MAR 75	13177.80	7.080	13177.80	5850.00	7.590	5850.00	0.0	7.590	0.0
APR 75	13177.80	7.150	13177.80	5850.00	7.740	5850.00	0.0	7.740	0.0
MAY 75	14879.20	7.240	14879.20	5850.00	7.880	5850.00	0.0	7.880	0.0
JUN 75	27300.00	7.330	27300.00	9314.55	8.090	9314.55	0.0	8.090	0.0
	<u>223606.50</u>			<u>116431.75</u>			<u>0.0</u>		

Figure 2. Predicted Sales Report

LIBERTY NATIONAL BANK

PREDICTED CERTIFICATES OF DEPOSIT SALES BY MATURITY PERIOD

60 DAY MATURITY

(DOLLAR AMOUNTS IN THOUSANDS)

	TYPE 0			TYPE 6			TYPE 8		
	*****			*****			*****		
	BEGINNING BALANCE	\$	25690.00	BEGINNING BALANCE	\$	0.0	BEGINNING BALANCE	\$	1444.00
MONTH	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING
JUN 74	\$ 0.0	10.290	\$ 25690.00	\$ 3885.44	10.970	\$ 3885.44	\$ 0.0	10.970	\$ 1444.00
JUL 74	12482.55	9.930	12482.55	0.0	10.890	3885.44	0.0	10.890	0.0
AUG 74	0.0	9.140	12482.55	4714.55	9.930	4714.55	0.0	9.930	0.0
SEP 74	12720.30	8.160	12720.30	2295.44	9.030	7010.00	0.0	9.030	0.0
OCT 74	210.00	7.690	12530.30	3464.56	8.420	5760.00	0.0	8.420	0.0
NOV 74	13345.85	7.260	13555.85	2385.44	8.020	5850.00	0.0	8.020	0.0
DEC 74	12853.00	7.220	26238.85	3464.56	7.870	5850.00	0.0	7.870	0.0
JAN 75	269.80	7.120	13162.80	2385.44	7.830	5850.00	0.0	7.830	0.0
FEB 75	12853.00	6.970	13162.80	3464.56	7.590	5850.00	0.0	7.590	0.0
MAR 75	757.00	7.050	13650.00	2385.44	7.560	5850.00	0.0	7.560	0.0
APR 75	12420.80	7.120	13177.80	3464.56	7.710	5850.00	0.0	7.710	0.0
MAY 75	14879.20	7.210	27300.00	8235.44	7.850	11700.00	0.0	7.850	0.0
JUN 75	0.0	7.300	14879.20	0.0	8.060	8235.44	0.0	8.060	0.0
	-----			-----			-----		
	\$ 92871.49			\$ 40145.44			\$ 0.0		

Figure 2. (Continued)

LIBERTY NATIONAL BANK

PREDICTED CERTIFICATES OF DEPOSIT SALES BY MATURITY PERIOD

90 DAY MATURITY

(DOLLAR AMOUNTS IN THOUSANDS)

	TYPE 0			TYPE 6			TYPE 8		
	*****			*****			*****		
	BEGINNING BALANCE		\$	BEGINNING BALANCE		\$	BEGINNING BALANCE		\$
	16344.00			5000.00			0.0		
MONTH	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING
JUN 74	\$ 398.63	10.160	\$ 16742.63	\$ 3720.00	10.840	\$ 8720.00	\$ 0.0	10.840	\$ 0.0
JUL 74	0.0	9.800	16742.63	0.0	10.760	8720.00	0.0	10.760	0.0
AUG 74	12083.91	9.010	12482.55	0.0	9.800	3720.00	0.0	9.800	0.0
SEP 74	636.38	8.030	12720.30	3780.00	8.900	3780.00	0.0	8.900	0.0
OCT 74	8014.80	7.560	20735.10	5615.44	8.290	9395.44	0.0	8.290	0.0
NOV 74	5148.00	7.130	13795.18	0.0	7.890	9395.44	0.0	7.890	0.0
DEC 74	0.0	7.090	13162.80	234.56	7.740	5850.00	0.0	7.740	0.0
JAN 75	13177.80	6.990	18325.80	5850.00	7.700	6084.55	0.0	7.700	0.0
FEB 75	0.0	6.840	13177.80	0.0	7.460	6084.55	0.0	7.460	0.0
MAR 75	0.0	6.920	13177.80	0.0	7.430	5850.00	0.0	7.430	0.0
APR 75	13650.00	6.990	13650.00	5850.00	7.580	5850.00	0.0	7.580	0.0
MAY 75	0.0	7.080	13650.00	0.0	7.720	5850.00	0.0	7.720	0.0
JUN 75	0.0	7.170	13650.00	0.0	7.930	5850.00	0.0	7.930	0.0
	<u>\$ 53109.52</u>			<u>\$ 25050.00</u>			<u>\$ 0.0</u>		

Figure 2. (Continued)

LIBERTY NATIONAL BANK

PREDICTED CERTIFICATES OF DEPOSIT SALES BY MATURITY PERIOD

120 DAY MATURITY

(DOLLAR AMOUNTS IN THOUSANDS)

	TYPE 0			TYPE 6			TYPE 8		
	*****			*****			*****		
	BEGINNING BALANCE	\$	5012.00	BEGINNING BALANCE	\$	2200.00	BEGINNING BALANCE	\$	185.00
MONTH	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING
JUN 74	\$ 3169.70	10.000	\$ 8181.70	\$ 1685.44	10.680	\$ 3885.44	\$ 0.0	10.680	\$ 185.00
JUL 74	0.0	9.640	8181.70	0.0	10.600	3885.44	0.0	10.600	185.00
AUG 74	4300.85	8.850	12482.55	0.0	9.640	3885.44	0.0	9.640	185.00
SEP 74	5249.75	7.870	12720.30	2094.56	8.740	3780.00	0.0	8.740	0.0
OCT 74	3379.70	7.400	12930.30	3665.44	8.130	5760.00	0.0	8.130	0.0
NOV 74	13395.30	6.970	26325.60	5850.00	7.730	11610.00	0.0	7.730	0.0
DEC 74	0.0	6.930	22024.75	0.0	7.580	11610.00	0.0	7.580	0.0
JAN 75	0.0	6.830	16775.00	0.0	7.540	9515.44	0.0	7.540	0.0
FEB 75	0.0	6.680	13395.30	0.0	7.300	5850.00	0.0	7.300	0.0
MAR 75	21520.80	6.760	21520.80	9750.00	7.270	9750.00	0.0	7.270	0.0
APR 75	0.0	6.830	21520.80	0.0	7.420	9750.00	0.0	7.420	0.0
MAY 75	0.0	6.920	21520.80	0.0	7.560	9750.00	0.0	7.560	0.0
JUN 75	0.0	7.010	21520.80	0.0	7.770	9750.00	0.0	7.770	0.0
	<u>\$ 51016.09</u>			<u>\$ 23045.44</u>			<u>\$ 0.0</u>		

Figure 2. (Continued)

LIBERTY NATIONAL BANK

PREDICTED CERTIFICATES OF DEPOSIT SALES BY MATURITY PERIOD

180 DAY MATURITY

(DOLLAR AMOUNTS IN THOUSANDS)

	TYPE 0			TYPE 6			TYPE 8		
	*****			*****			*****		
	BEGINNING BALANCE		\$ 22179.00	BEGINNING BALANCE		\$ 10000.00	BEGINNING BALANCE		\$ 150.00
MONTH	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING
JUN 74	\$ 0.0	9.870	\$ 22174.00	\$ 0.0	10.550	\$ 10000.00	\$ 0.0	10.550	\$ 150.00
JUL 74	487.20	9.510	22661.20	0.0	10.470	10000.00	0.0	10.470	150.00
AUG 74	0.0	8.720	22661.20	0.0	9.510	10000.00	0.0	9.510	150.00
SEP 74	0.0	7.740	22661.20	0.0	8.610	10000.00	0.0	8.610	150.00
OCT 74	0.0	7.270	22661.20	0.0	8.000	10000.00	0.0	8.000	150.00
NOV 74	12675.60	6.840	13162.80	5850.00	7.600	5850.00	0.0	7.600	0.0
DEC 74	0.0	6.800	13162.80	0.0	7.450	5850.00	0.0	7.450	0.0
JAN 75	13650.00	6.700	26325.60	5850.00	7.410	11700.00	0.0	7.410	0.0
FEB 75	0.0	6.550	26325.60	0.0	7.170	11700.00	0.0	7.170	0.0
MAR 75	0.0	6.630	26325.60	0.0	7.140	11700.00	0.0	7.140	0.0
APR 75	0.0	6.700	26325.60	0.0	7.290	11700.00	0.0	7.290	0.0
MAY 75	0.0	6.790	13650.00	0.0	7.430	5850.00	0.0	7.430	0.0
JUN 75	0.0	6.880	13650.00	0.0	7.640	5850.00	0.0	7.640	0.0
	<u>\$ 26812.80</u>			<u>\$ 11700.00</u>			<u>\$ 0.0</u>		

Figure 2. (Continued)

LIBERTY NATIONAL BANK

SUMMARY TOTALS BY MONTH

(DOLLAR AMOUNTS IN THOUSANDS)

MONTH	MONTHLY SALES	MONTHLY PAYOUT	NET AMOUNT OUTSTANDING
JUN 74	\$ 38067.76	\$ 30762.00	\$129514.75
JUL 74	44827.78	52342.54	121999.94
AUG 74	59087.47	57087.47	123999.94
SEP 74	63986.33	61966.33	125999.94
OCT 74	48779.60	46779.60	127999.94
NOV 74	85853.31	83853.31	129999.94
DEC 74	39594.91	39594.91	125999.94
JAN 75	60195.84	60195.84	129999.94
FEB 75	47563.50	47563.50	129999.94
MAR 75	53441.04	53441.04	125999.94
APR 75	54413.16	54413.16	129999.94
MAY 75	43843.84	43843.84	129999.94
JUN 75	36614.55	36614.55	129999.94

Figure 3. Summary Report

This graph provides an illustration for comparing the future sales of CD's in each of the markets being serviced.

The second section is of the summary totals of the LP program and represents the same information of the summary totals report.

The last section of the graphical report is the cost graph. This graph depicts the total amount paid out in interest for all CD's for each month of the 13-month planning period.

Although the graphical report can only be interpreted with approximate values, the report is useful as a pictorial representation of the LP solution. Thus, management is provided with a ready reference of the growth pattern and the approximate cost of the CD portfolio over the planning horizon.

"Rolling Feature"

As mentioned earlier in this study, the model is designed to be general in that any 13-month period can be represented. This "rolling feature" provides management with the four reports described above for any, or all, of the months of the planning period. Figure 5 is an example of this feature for the 13-month period of December, 1974 to December, 1975, inclusive.

Summary

The model generates four management reports based on the solution of the LP problem. These reports provide management with analytical tools to be used in planning a balanced liability portfolio.

SALES TOTALS

LEGEND

- + TYPE 0 SALES
- * TYPE 6 SALES
- o TOTAL SALES

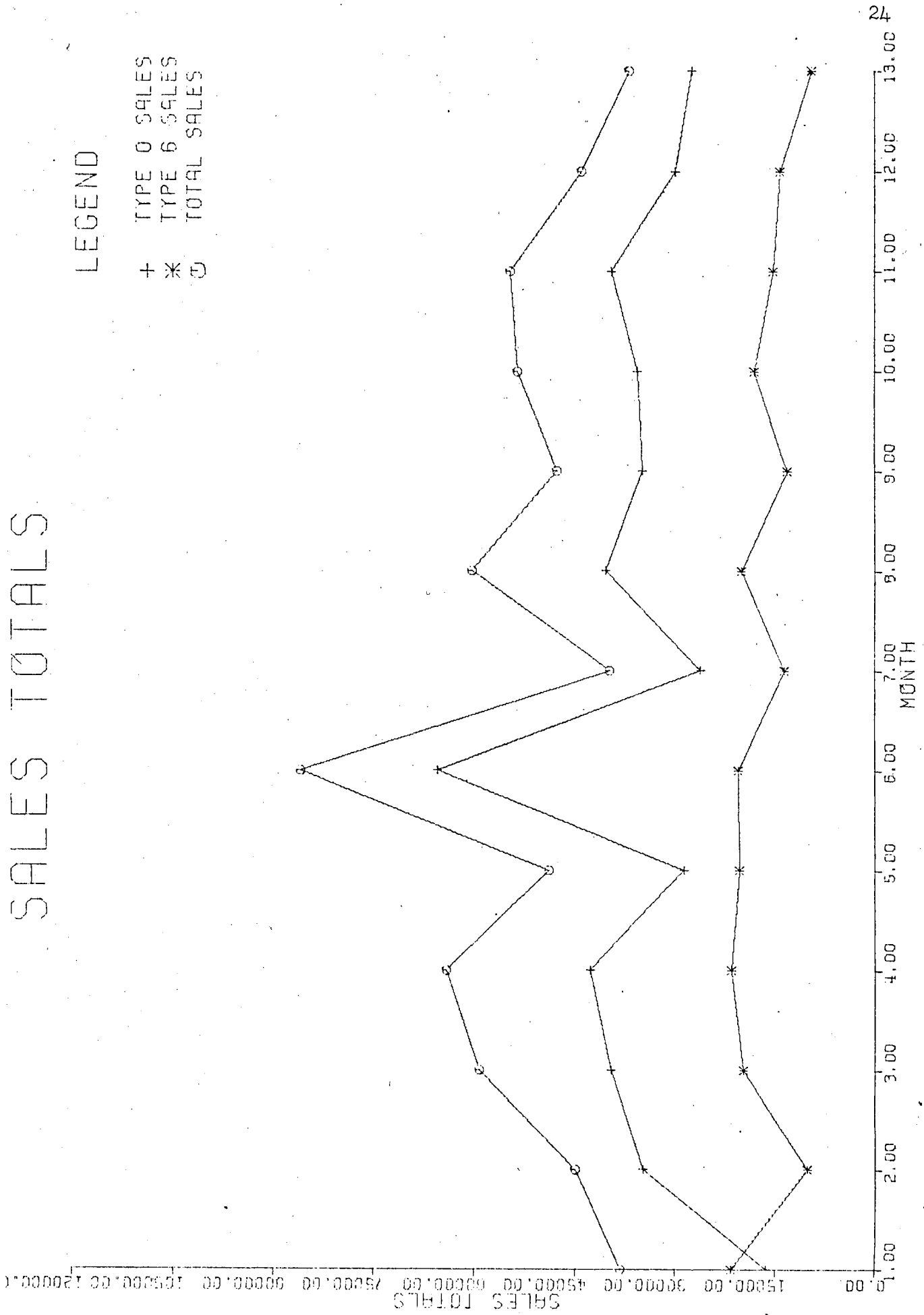
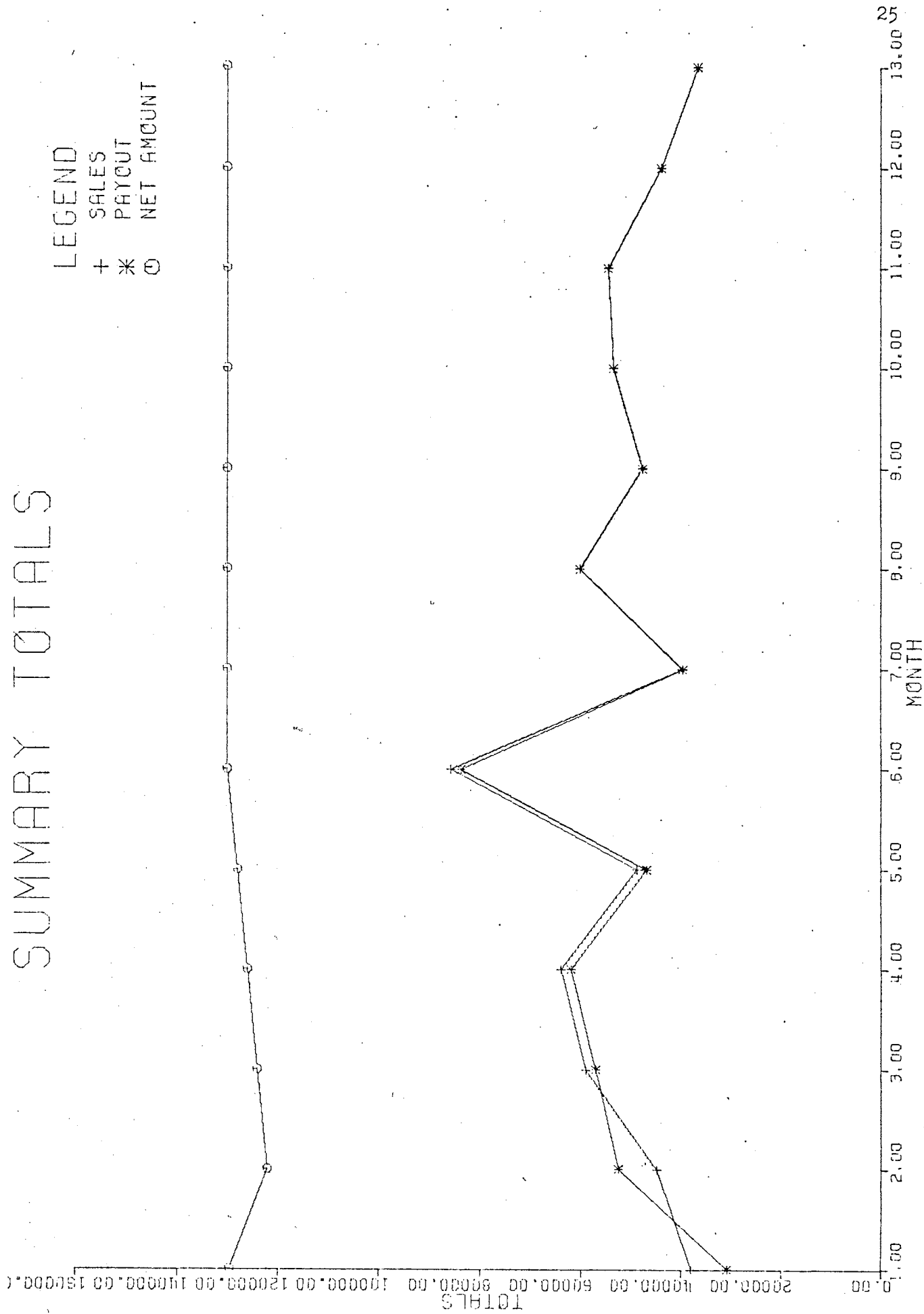


Figure 4. Graphical Report.

SUMMARY TOTALS

LEGEND

- + SALES
- * PAYOUT
- ⊖ NET AMOUNT



(Continued)

COST TOTALS

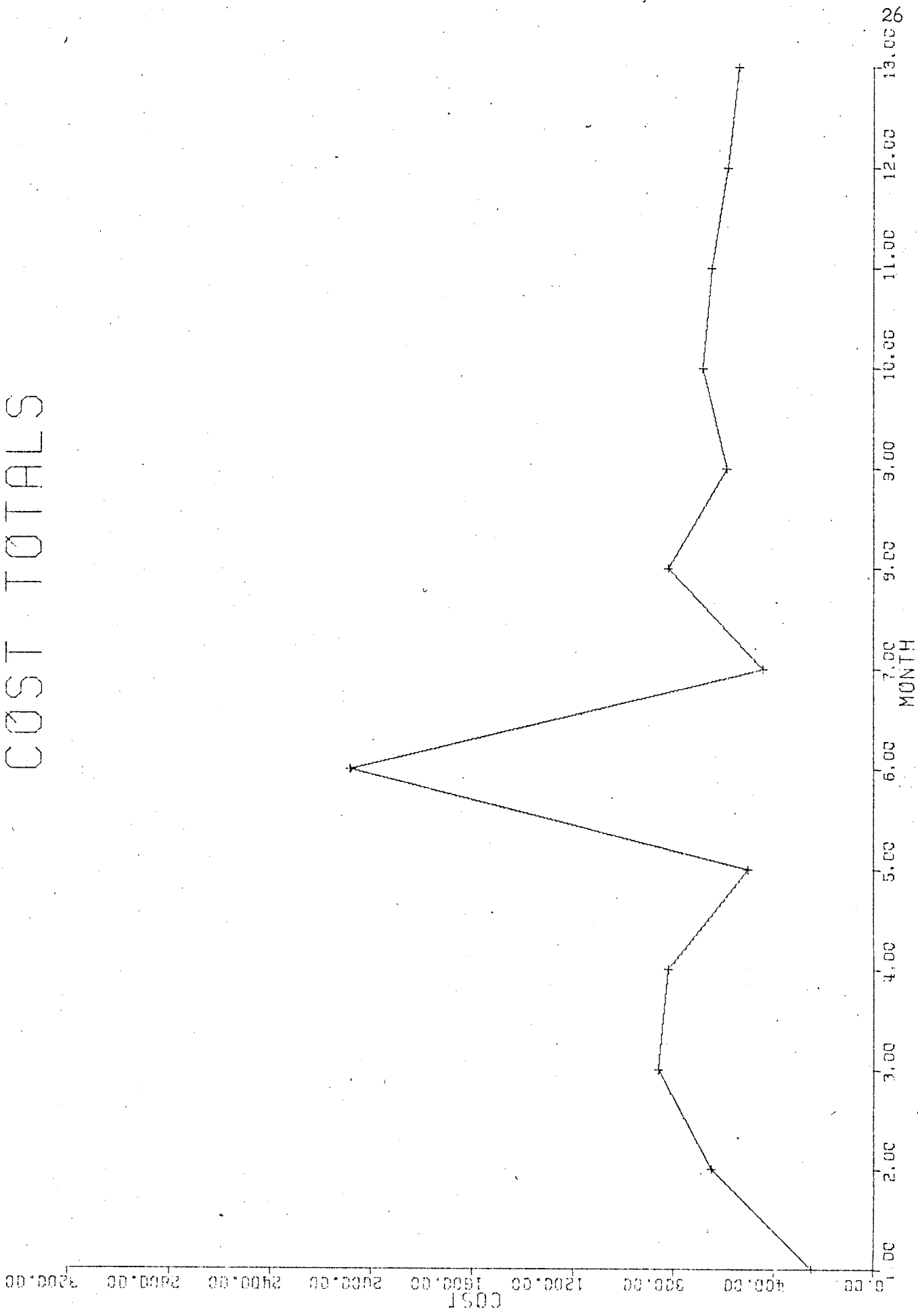


Figure 4. (Continued)

LIBERTY NATIONAL BANK

SUMMARY TOTALS BY MONTH

(DOLLAR AMOUNTS IN THOUSANDS)

MONTH	MONTHLY SALES	MONTHLY PAYOUT	NET AMOUNT OUTSTANDING
DEC 74	\$ 88837.88	\$ 15770.10	\$129999.94
JAN 75	88837.88	15770.10	129999.94
FEB 75	56767.52	56767.52	129999.94
MAR 75	55330.76	55330.76	129999.94
APR 75	89050.00	89050.00	129999.94
MAY 75	64350.00	64350.00	129999.94
JUN 75	61947.84	61947.84	129999.94
JUL 75	53102.16	53102.16	129999.94
AUG 75	72602.13	72602.13	129999.94
SEP 75	31397.84	31397.84	129999.94
OCT 75	70002.13	70002.13	129999.94
NOV 75	42447.84	42447.84	129999.94
DEC 75	39000.00	39000.00	129999.94

Figure 5. Example of "Rolling Feature"

CHAPTER IV

IMPLEMENTATION AND IMPLICATIONS

The model predicts an optimal CD sales schedule for thirteen months while minimizing the total interest costs of the sales over the planning period. The optimal solution is subject to constraints reflecting bank management policy with respect to growth objectives, balance amounts outstanding, minimum sales, and prevention of rapid turnover of certain types of CD's. However, the model's use as an effective liability management model is limited. As discussed in Chapter II, an effective portfolio management model must assist bank management in achieving a proper balance between income, liquidity, and risk. The model considered in this study involves only one type of liability, Certificates of Deposit, and assumes certainty. Thus, the study implies certain improvements are available to make this model a more effective analytical tool for management.

Perhaps the most important improvement suggested deals with the decision variables. In order to achieve a balance between income, liquidity, and risk, other details of the bank's balance sheet should be included as decision variables or as constraining equations. The interrelationships between a bank's assets and liabilities, liquidity position, and Federal Reserve minimum deposit regulations necessitate the inclusion of these additional variables.

A second important consideration for improvement of the model is

the forecasts of future interest rates, loan demand, and future levels of deposits within the planning period. These forecasts must be made while considering the various types and maturities of relevant assets, liabilities, and capital items of the balance sheet. The method used in forecasting should be able to incorporate conditions of uncertainty and variations in economic conditions. These interrelationships must be realistically included in the forecasts if the model is to produce useable management results.

Another implication of the study is the structure and number of the constraints of the model. A linear programming model can accommodate as many constraints as bank managers consider relevant to the portfolio decision process. Detailed and realistic sets of liquidity constraints should be built into the model reflecting liability and capital structures, cash flow patterns, and miscellaneous restrictions imposed by management on the basis of experience. Other constraints are also conceivable, reflecting legal reserve requirements and the use of certain assets as collateral to support government deposits. Moreover, the linear programming model must include constraints reflecting well defined bank goals and management policies.

Another implication discussed in Cohen and Hammer [12] concerns the use of the dual variables that are a product of the LP solution. The dual solution indicates the incremental benefits associated with a marginal increase, or decrease, of any of the model's constraints. Thus, the model can provide information useful in determining the marginal rate of return on capital, the maximum interest rate to pay for additional CD's and opportunity costs associated with various management policies.

Similarly, the MPSX procedure includes features for sensitivity analysis of the model's variables. The RANGE function causes the program to automatically determine an upper and lower bound on the variables of the model in order that the solution remain optimal. MPSX also includes a feature that allows the programmer to define certain bounds for the coefficients of the variables and have the program increment those coefficients until the solution is no longer optimal. These features allow the programmer considerable latitude in simulating varying economic conditions and management policies.

In summary, the LP model should include comprehensive risk constraints, policy considerations, and economic and institutional considerations which must be evaluated in order to make relevant portfolio management decisions.

CHAPTER V

SUMMARY AND RECOMMENDATIONS

The application of linear programming to bank management appears to be one of the more important recent developments in banking. The current study has dealt with one such LP model; a report generating LP model for scheduling the issuance of large CD's.

The objective of the study has been to construct a model to provide an output of selected LP solution data in a management type of report form. This was accomplished by using a special feature of the MPS called READCOMM. READCOMM allows the LP program to access an external program to report selected MPSX solution data.

As a result of the research for this study several areas for improvement have been uncovered. Basically, these improvements are indicated in the areas of the constraints and the variables included in the model.

In conclusion, there are two areas that could justify further research concerning this model. The decomposition procedure mentioned in Chapter II is the first one of these areas. Bradley and Crane [5] briefly discuss this technique for solving LP problems. The simplifying and time-saving aspects of the decomposition technique seem to be especially applicable to this model. Lastly, research into the area of direct-access systems is needed. A direct-access application would greatly simplify the changing and updating of the model. One such

system is discussed in an article by Thomas P. Gerrity, Jr. [18]. Before implementation of the model as a portfolio management tool, research in these areas should be conducted.

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APPENDIXES

APPENDIX A

THE MODEL

Purpose

The objective of the model is to minimize the total interest cost for a thirteen-month period subject to constraining equations which express management policy with respect to growth, turnover, and liquidity of the CD portfolio. The variables of the model are dollar amounts of CD sales for each instrument-maturity-month. The constraints are linear equations of these variables.

Structual Variables

The model contains a separate variable for each of the thirteen-months, type of CD, and maturity period, in addition to variables representing the beginning balances for each type of CD and maturity period. These variables comprise the objective function and the constraints of the model.

Constraints

Seventy Percent Rule. These constraints reflect management policy that sales in any period plus the previous month's balance must be greater than or equal to seventy percent of the total dollars transacted in that period.

Thirty Percent Rule. These constraint equations assure that management's policy of maintaining at least thirty percent of all instruments issued as national market instruments (type-6) is achieved in the model's solution.

Balanced Distribution. Management would like to have a more even distribution of maturity instruments for each type in the future periods of the planning horizon. This policy is reflected in constraints that restrict the amounts outstanding in each maturity period for a particular month from being less than or exceeding certain percentages of the total amount outstanding during that month.

Accumulators

The model also contains equations which provide the total sales for each month, total sales for each instrument sold during each month, the total payout of maturing instruments during each month, and the total net amount outstanding during any month. These accumulators are included for use in constructing the constraints discussed above and certain bounds on the variables of the model.

Bounds on Variables

In order to reflect management's policies of growth in amounts of instruments issued and restrictions concerning certain maturity periods of some instruments, upper and lower bounds were included for some of the variables of the model. First, a lower bound of \$130 million was placed on the total net amount outstanding during any month. This reflects management policy concerning the growth of the CD portfolio. Lastly, management stated that during the planning horizon no special

market (type-8) instruments would be issued. Therefore, the variables representing sales of type-8 CD's were set equal to zero.

Interest Costs

Interest costs were computed for each of the structural variables by multiplying the forecasted annual interest rate by a factor representing the fraction of 365 days for which interest is paid on the instrument. These interest costs were then used as the coefficients of the decision variables in the objective function of the LP problem. The model minimizes the total of these interest costs over the planning horizon.

Abbreviated Example

Because of the large number of variables (567) included in the model, only an illustrative example will be presented here.

$$\text{Minimize Cost} = .10(x) + .05(y)$$

$$\begin{aligned} \text{Subject to: } & x+y \leq 100 \text{ million} \\ & y \geq .33(x) \\ & x \geq 30 \text{ million} \end{aligned}$$

APPENDIX B

All of the modifications to the Harris model presented in the paper were programmed and solved for use with the IBM Mathematical Programming System Extended (MPSX) on the IBM Model 360/65 computer located at Oklahoma State University. If the resulting model is to be used on another model computer or at another installation, some control cards may have to be changed.

Also, the changes made to the model make use of a feature of MPSX known as READCOMM. This feature allows the programmer to augment the MPSX procedure with a FORTRAN program to output selected data of the MPSX solution in different types of formats. (It should also be noted that other features utilizing programming languages other than FORTRAN might have also been used¹.) The use of the special features of MPSX necessitates certain changes in the MPSX Control Program and the addition of a program to the model. These changes will be discussed in the sections that follow.

Control Program

The MPSX Control Program (Exhibit I) provides the initialization and setup of the data storage areas to be used in solving the LP problem. Also, the control program inputs the data, calls for a solution routine, and provides various output listings as requested by the programmer. Two changes were necessary in this program to facilitate the use of the READCOMM feature.

PROGRAM('ND')

40

TITLE ('LIBERTY NATIONAL BANK CERTIFICATES OF DEPOSIT')

INITIALIZE ALL INPUT FILES

INITIALZ

SETUP WORK FILES FOR INPUT OF DATA

MOVE(XDATA,'CDEZZ')
MOVE(XPBNAME,'PBFILE')

SETUP READCOMM FILE FOR USE WITH FORTRAN PROGRAM

ASSIGN('COMMFMT','FT04F001','COMM')
PREPOUT('COMMFMT')

CONVERT INPUT DATA TO INTERNAL STORAGE FORMAT

CONVERT('SUMMARY')
SETUP('BOUNDS','DOLRS')
MOVE(XOBJ,'COST')
MOVE(XRHS,'RHS')
LIST INPUT DATA
TITLE ('LIBERTY NATIONAL BANK -- INPUT DATA')

BCDOUT

TITLE ('LIBERTY NATIONAL BANK -- SOLUTION')

SOLVE PROBLEM USING THE DUAL SOLUTION METHOD

DUAL
SOLUTION

SETUP EDITED DATA FOR READCOMM FILE

SOLUTION('FILE','COMMFMT','RSECTION','2','CSECTION','2/4/5', 1
RMASKS',' ','CMASKS','***A','***B','***C','***D','***E','**PD', 2
ANET','BNET','***CNET','***DNET','***ENET','BAL*A','BAL*B', 3
BAL*C','BAL*D','BAL*E','**SAL','**NET',' ')

DETERMINE RANGES FOR VARIABLES FOR SOLUTION TO REMAIN OPTIMAL
TITLE ('LIBERTY NATIONAL BANK -- VARIABLE RANGES')
RANGE

BEGIN EDITING OF SOLUTION

FREECORE
MGMTFORM
EXIT
PEND

The first change is the addition of the ASSIGN statement. This statement prepares an additional storage area to be used by the READCOMM routine. The storage area is a file used to store the selected MPSX solution variables until the FORTRAN program is executed.

Second, an additional SOLUTION statement was added. Within this statement a selection list causes the applicable variables of the MPSX solution set to be stored in the READCOMM file discussed above. After execution of the MPSX program, the FORTRAN program accesses the READCOMM file for use in obtaining the desired output format.

Output FORTRAN Program

This section of the model contains the program written to output the MPSX variables in the management report form. Exhibit II is the FORTRAN program used in the report generating model.

MANAGEMENT OUTPUT FORM

PURPOSE:

THIS PROGRAM IS DESIGNED TO EDIT AND OUTPUT SELECTED INFORMATION FROM THE COMPUTED SOLUTION OF THE CERTIFICATE OF DEPOSIT PREDICTION MODEL WRITTEN BY LESTER HARRIS, GRADUATE OF OKLAHOMA STATE UNIVERSITY. THE HARRIS MODEL PREDICTS THE OPTIMAL AMOUNTS OF THREE TYPES OF SHORT-TERM CERTIFICATES OF DEPOSIT SALES FOR THE NEXT THIRTEEN MONTHS. THREE FORMATS ARE USED TO EDIT THE MODEL SOLUTION:

- (1) MATURITY DATE ANALYSIS - FOR EACH MONTH PREDICTED BY THE MODEL, THE AMOUNTS OF CERTIFICATES MATURING IN THE FUTURE MONTHS ARE PROVIDED
- (2) PREDICTED SALES - THIS SECTION PROVIDES THE MODEL PREDICTED SALES FOR THE NEXT THIRTEEN MONTHS BY MATURITY PERIOD
- (3) SUMMARY TOTALS - THIS SECTION PROVIDES THE TOTAL MONTHLY SALES, MONTHLY PAYOUT, AND THE NET AMOUNT OUTSTANDING FOR THE PREDICTED MONTHS.

THE PROGRAM IS DESIGNED TO BE GENERAL IN NATURE TO FACILITATE ITS USE ANY THIRTEEN MONTH PERIOD WITH A MINIMUM OF VARIABLE CHANGES. THE REQUIRED CHANGES ARE NOTED BY ** IN THE VARIABLE DEFINITION SECTION WHICH FOLLOWS.

VARIABLE DEFINITION:

ACCO -- ACCUMULATED INTEREST PAID EACH MONTH ON TYPE 0 CD'S.
 ACC6 -- ACCUMULATED INTEREST PAID EACH MONTH ON TYPE 6 CD'S.
 ACC8 -- ACCUMULATED INTEREST PAID EACH MONTH ON TYPE 8 CD'S.
 AMTNET -- TOTAL NET AMOUNT OUTSTANDING EACH MONTH.
 ATOTAL -- TOTAL OF ACCUMULATED INTEREST PAID FOR EACH TYPE CD.
 BAL -- BEGINNING BALANCES FOR EACH TYPE CD AND MATURITY PERIOD.
 ** BEGIN -- THE NAME OF THE BEGINNING MONTH OF THE MODEL.
 COL -- USED TO STORE THE COLUMN NAME OF THE MODEL SOLUTION.
 COST -- INTEREST COST PER MONTH.
 DAYS -- MATURITY PERIOD.
 ** ENDING -- THE NAME OF THE ENDING MONTH OF THE MODEL.
 FILE -- FILE DESIGNATOR OF THE STORED SOLUTION.
 HEAD1, HEAD2, HEAD3, HEAD4 -- OUTPUT HEADINGS.
 INDIC -- INDICATOR OF END OF THE FILE USED FOR OUTPUT.
 INDICES: PROGRAM COUNTERS
 I, IEND, IJ, INDX, IROW, IX, IY, JK, KOUNT1, LL, LOOP, LP, LINX
 ** KNT -- NUMBER OF THE BEGINNING MONTH OF THE MODEL.
 MONTH -- THE CURRENT MONTH BEING PREDICTED.
 NAME -- THE NAME OF EACH SOLUTION STORED ON THE FILE.
 PAYOUT -- TOTAL AMOUNT PAID OUT EACH MONTH.
 SALES -- TOTAL SALES EACH MONTH.
 SUM -- SUMMARY TOTAL SALES, PAYOUT, AND NET AMOUNT OUTSTANDING.

TOTAL -- ACCUMULATED SALES FOR EACH OF THE THIRTEEN MONTHS. 43
 TYOMAT -- MATURITY DATA FOR TYPE 0 CD'S.
 TY6MAT -- MATURITY DATA FOR TYPE 6 CD'S.
 TY8MAT -- MATURITY DATA FOR TYPE 8 CD'S.
 TYPE0 -- PLOT DATA OF TYPE 0 SALES.
 TYPE6 -- PLOT DATA OF TYPE 6 SALES.
 TYPE8 -- PLOT DATA OF TYPE 8 SALES.
 VAL -- PREDICTED DATA FOR EACH MONTH BY MATURITY PERIOD.
 VALUES -- FILED SOLUTION VALUES.
 WAIR -- WEIGHTED AVERAGE INTEREST RATE.
 XDATA -- PLOT DATA FOR EACH MONTH.
 YR -- YEAR OR YEARS INCLUDED IN THE MODEL PREDICTIONS.

SETUP DATA STORAGE AREA TO BE USED BY PROGRAM

INTEGER HEAD1(12),HEAD2(12),HEAD3(12),HEAD4(6),BEGIN(4),ENDING(4)
 INTEGER DAYS,FILE,MONTH(30),YR(30)
 DOUBLE PRECISION NAME,COL(10),VALUES(3)
 DOUBLE PRECISION VAL(65,9),BAL(15),SUM(13,3),TOTAL(3),FACTOR(5)
 DOUBLE PRECISION TYOMAT(19,3),TY6MAT(19,3),TY8MAT(19,3)
 DOUBLE PRECISION ACC0(19),ACC6(19),ACC8(19),ATOTAL(3),WAIR(3)
 DIMENSION TYPE0(15),TYPE6(15),TYPE8(15),COST(15),XDATA(15)
 DIMENSION XPLOT(4),SALES(15),PAYOUT(15),AMTNET(15)

DATA INITIALIZATION

DATA HEAD1/11*4H****,4H* /, IOUT/6/, FILE/4/,
 A HEAD2/2*4H****,4H** ,4HLIBE,4HRTY ,4HNATI,4HOVAL,4H BAN,
 B 4HK *,2*4H****,4H* /,
 C HEAD3/4H****,4H* C,4HERTI,4HFICA,4HTE O,4HF DE,4HPOSI,4HT SC,
 D 4HHEDU,4HLE ,4H****,4H* /,
 E HEAD4/6*4H****/,
 H BEGIN/4H DE,4HCEMB,4HER ,4H1974/,
 I ENDING/4H DEC,4HEMBE,4HR 19,4H75 /,
 J TYPE0/15*0.0/, TYPE6/15*0.0/, TYPE8/15*0.0/,KOUNT1/0/,
 K XDATA/1.0,2.0,3.0,4.0,5.0,6.0,7.0,8.0,9.0,10.0,11.0,12.0,13.0,
 L 14.0,15.0/, COST/15*0.0/

DATA MONTH/4H JAN,4H FEB,4H MAR,4H APR,4H MAY,4H JUN,4H JUL,
 1 4H AUG,4H SEP,4H OCT,4H NOV,4H DEC,4H JAN,4H FEB,4H MAR,4H APR,
 2 4H MAY,4H JUN,4H JUL,4H AUG,4H SEP,4H OCT,4H NOV,4H DEC,4H JAN,
 3 4H FEB,4H MAR,4H APR,4H MAY,4H JUN/

DATA YR/12*74,12*75,6*76/,ATOTAL/3*0.0/

DATA ACCO/19*0.0/,ACC6/19*0.0/,ACC8/19*0.0/

44

DATA TYOMAT/57*0.0/,TY6MAT/57*0.0/,TY8MAT/57*0.0/

FACTOR(1) = 365./30.
FACTOR(2) = 365./60.
FACTOR(3) = 365./90.
FACTOR(4) = 365./120.
FACTOR(5) = 365./180.

MAIN HEADINGS

WRITE (IDOUT,100) HEAD1,HEAD2,HEAD3,BEGIN,ENDING,HEAD1

OBTAIN INPUT DATA FROM 'READCOMM'

POSITION FILE TO THE BEGINNING

CALL POSITN (FILE,INDIC)
CALL ARRAY (FILE,INDIC,NAME,NRCOL)

POSITION TO THE COLUMN SECTION OF THE FILE

10 CALL ARRAY (FILE,INDIC,NAME,NRCOL)
IF (INDIC - 1) 90,90,11

INPUT THE BEGINNING BALANCES FOR EACH TYPE CD AND MATURITY
PERIOD AND COMPUTE THE ASSOCIATED COST AND MATURITY DATE

11 DO 20 LL = 1,15
CALL VECTOR (FILE,INDIC,VALUES)
IF (INDIC - 1) 10,10,12
12 GO TO (13,13,13,13,14,15,15,15,15,16,17,17,17,17,18),LL
13 TYOMAT(LL,1) = TYOMAT(LL,1) + VALUES(2)
ACCO(LL) = ACCO(LL) + VALUES(2)*VALUES(3)*FACTOR(LL)
COST(LL) = COST(LL) + VALUES(2) * VALUES(3)
GO TO 19
14 TYOMAT(LL+1,1) = TYOMAT(LL+1,1) + VALUES(2)
ACCO(LL+1) = ACCO(LL+1) + VALUES(2)*VALUES(3)*FACTOR(LL)
COST(LL+1) = COST(LL+1) + VALUES(2) * VALUES(3)
GO TO 19
15 TY6MAT(LL-5,1) = TY6MAT(LL-5,1) + VALUES(2)
ACC6(LL-5) = ACC6(LL-5) + VALUES(2)*VALUES(3)*FACTOR(LL-5)
COST(LL-5) = COST(LL-5) + VALUES(2) * VALUES(3)
GO TO 19
16 TY6MAT(LL-4,1) = TY6MAT(LL-4,1) + VALUES(2)
ACC6(LL-4) = ACC6(LL-4) + VALUES(3)*VALUES(2)*FACTOR(LL-5)
COST(LL-4) = COST(LL-4) + VALUES(2) * VALUES(3)
GO TO 19
17 TY8MAT(LL-10,1) = TY8MAT(LL-10,1) + VALUES(2)
ACC8(LL-10) = ACC8(LL-10)+VALUES(2)*VALUES(3)*FACTOR(LL-10)
COST(LL-10) = COST(LL-10) + VALUES(2) * VALUES(3)
GO TO 19
18 TY8MAT(LL-9,1) = TY8MAT(LL-9,1) + VALUES(2)
ACC8(LL-9) = ACC8(LL-9) + VALUES(2)*VALUES(3)*FACTOR(LL-10)

```

COST(LL-9) = COST(LL-9) + VALUES(3) * VALUES(2)
19 BAL(LL) = VALUES(2)
20 CONTINUE

DO 7000 I = 1,13

  SETUP COUNTERS TO BEGIN INPUT OF MONTHLY DATA

  IROW = KOUNT1 + 1
  IEND = KOUNT1 + 53
  LP = 0
  JK = I

  DO 3000 LOOP = IROW,IEND,13
    LP = LP + 1
    JK = JK + 1

  INPUT MONTHLY DATA AND COMPUTE THE ASSOCIATED COST AND MATURITY
  DATE

    DO 2000 INDX = 1,7,3
      CALL VECTOR (FILE,INDIC,VALUES)
      IF (INDIC - 1) 10,10,30
30 IF (LP .EQ. 5) JK=JK+1
      IF (INDX - 4) 31,32,33
31 TYPE0(I) = TYPE0(I) + VALUES(2)
      TYOMAT(JK,1) = TYOMAT(JK,1) + VALUES(2)
      ACC0(JK) = ACC0(JK) + VALUES(2)*VALUES(3)*FACTOR(LP)
      GO TO 34
32 TYPE6(I) = TYPE6(I) + VALUES(2)
      TY6MAT(JK,1) = TY6MAT(JK,1) + VALUES(2)
      ACC6(JK) = ACC6(JK) + VALUES(2)*VALUES(3)*FACTOR(LP)
      GO TO 34
33 TYPE8(I) = TYPE8(I) + VALUES(2)
      TY8MAT(JK,1) = TY8MAT(JK,1) + VALUES(2)
      ACC8(JK) = ACC8(JK) + VALUES(2)*VALUES(3)*FACTOR(LP)
34 VAL(LOOP,INDX) = VALUES(2)
      VAL(LOOP,INDX+1) = VALUES(3) * FACTOR(LP) * 100.0
      COST(JK) = COST(JK) + VALUES(2) * VALUES(3)
2000 CONTINUE
3000 CONTINUE

  INPUT SUMMARY TOTALS FOR EACH MONTH

  DO 4000 LP = 1,3
    CALL VECTOR (FILE,INDIC,VALUES)
    IF (INDIC - 1) 10,10,35
35 SUM(I,LP) = VALUES(2)
4000 CONTINUE

  INPUT THE NET AMOUNT OUTSTANDING FOR EACH MONTH

  DO 6000 LOOP = 3,9,3
    DO 5000 INDX = IROW,IEND,13
      CALL VECTOR (FILE,INDIC,VALUES)
      IF (INDIC - 1) 10,10,36
36 VAL(INDX,LOOP) = VALUES(2)
5000 CONTINUE

```

6000 CONTINUE
KOUNT1 = KOUNT1 + 1

46

RE-INITIALIZE THE TOTALS STORAGE AREAS

DO 8025 IY= 1,3
TOTAL(IY) = 0.0
ATOTAL(IY) = 0.0

8025 CONTINUE
GO TO (47,48,47,48,47,48,47,48,47,48,47,48,47), I

WRITE HEADINGS FOR THE MATURITY DATE OUTPUT SECTION

47 WRITE (IOUT,111)
WRITE (IOUT,112)
48 KNT = I + 11
WRITE (IOUT,116) MONTH(KNT),YR(KNT),HEAD4
IX = I
ND = IX + 6
LINX = 1

ACCUMULATE THE TOTALS FOR THE MATURITY DATE OUTPUT

DO 8050 IY = IX,ND
TOTAL(1) = TOTAL(1) + TYOMAT(IY,1)
TOTAL(2) = TOTAL(2) + TY6MAT(IY,1)
TOTAL(3) = TOTAL(3) + TY8MAT(IY,1)
ATOTAL(1) = ATOTAL(1) + ACCO(IY)
ATOTAL(2) = ATOTAL(2) + ACC6(IY)
ATOTAL(3) = ATOTAL(3) + ACC8(IY)
8050 CONTINUE

COMPUTE THE WEIGHTED AVERAGE INTEREST RATE FOR THE TOTALS OUTPUT

DO 8075 IY = 1,3
IF (TOTAL(IY) .LE. 1.0) GO TO 88
WAIR(IY) = ATOTAL(IY) / TOTAL(IY) * 100.0
GO TO 8075
88 WAIR(IY) = 0.0
8075 CONTINUE

COMPUTE THE PERCENT OF TOTAL AMOUNT AND THE WEIGHTED AVERAGE INTEREST RATE FOR EACH MONTH

DO 6075 IJ = IX,ND
IF (TOTAL(1) .LE. 1.0) GO TO 54
TYOMAT(IJ,2) = TYOMAT(IJ,1) / TOTAL(1) * 100.0
49 IF (TOTAL(2) .LE. 1.0) GO TO 55
TY6MAT(IJ,2) = TY6MAT(IJ,1) / TOTAL(2) * 100.0
50 IF (TOTAL(3) .LE. 1.0) GO TO 56
TY8MAT(IJ,2) = TY8MAT(IJ,1) / TOTAL(3) * 100.0
51 IF (TYOMAT(IJ,1) .LE. 1.0) GO TO 57
TYOMAT(IJ,3) = ACCO(IJ) / TYOMAT(IJ,1) * 100.0
52 IF (TY6MAT(IJ,1) .LE. 1.0) GO TO 58
TY6MAT(IJ,3) = ACC6(IJ) / TY6MAT(IJ,1) * 100.0
53 IF (TY8MAT(IJ,1) .LE. 1.0) GO TO 59
TY8MAT(IJ,3) = ACC8(IJ) / TY8MAT(IJ,1) * 100.0
GO TO 60

Exhibit II. (Continued)

```

54 TYOMAT(IJ,2) = 0.0
GO TO 49
55 TY6MAT(IJ,2) = 0.0
GO TO 50
56 TY8MAT(IJ,2) = 0.0
GO TO 51
57 TYOMAT(IJ,3) = 0.0
GO TO 52
58 TY6MAT(IJ,3) = 0.0
GO TO 53
59 TY8MAT(IJ,3) = 0.0
60 IF (LINX - 1) 61,61,62

WRITE THE MONTHLY MATURITY DATE FIGURES

61 WRITE (IOUT,113) MONTH(KNT), YR(KNT), (TYOMAT(IJ,J), J=1,3),
1 (TY6MAT(IJ,J), J=1,3), (TY8MAT(IJ,J), J=1,3)
GO TO 63
62 WRITE (IOUT,114) MONTH(KNT), YR(KNT), (TYOMAT(IJ,J), J=1,3),
1 (TY6MAT(IJ,J), J=1,3), (TY8MAT(IJ,J), J=1,3)
63 KNT = KNT + 1
LINX = 2
6075 CONTINUE

WRITE THE TOTAL FIGURES FOR THE MATURITY DATE OUTPUT

WRITE (IOUT,115) (TOTAL(IY), WAIR(IY), IY=1,3)
7000 CONTINUE

INCREMENT THE COUNTERS

IROW = 1
IEND = 13
DAYS = 30
DO 8000 INDX = 1,5
IF (INDX .EQ. 5) DAYS = 180

WRITE THE HEADINGS FOR THE PREDICTED MONTHLY SALES OUTPUT

WRITE (IOUT,101) HEAD4, DAYS, HEAD4
WRITE (IOUT,102)
WRITE (IOUT,103) BAL(INDX), BAL(INDX+5), BAL(INDX+10)
WRITE (IOUT,104)
DO 7025 LOOP = 1,3
TOTAL(LOOP) = 0.0
7025 CONTINUE
KNT = 12
LINX = 1
DO 7050 LOOP = IROW, IEND
IF (LINX - 1) 37,37,38

WRITE THE MONTHLY FIGURES, ACCUMULATE THE TOTALS, AND INCREMENT
THE COUNTERS

37 WRITE (IOUT,105) MONTH(KNT), YR(KNT), (VAL(LOOP, II), II=1,9)
GO TO 39
38 WRITE (IOUT,106) MONTH(KNT), YR(KNT), (VAL(LOOP, II), II=1,9)
39 TOTAL(1) = TOTAL(1) + VAL(LOOP,1)

```

```

TOTAL(2) = TOTAL(2) + VAL(LOOP,4)
TOTAL(3) = TOTAL(3) + VAL(LOOP,7)
LINX = LINX + 1
KNT = KNT + 1
7050 CONTINUE

      OUTPUT TOTALS

      WRITE (IOUT,107) TOTAL
      DAYS = DAYS + 30
      IROW = IROW + 13
      IEND = IEND + 13
3000 CONTINUE

      WRITE THE SUMMARY TOTALS FOR THE MODEL

      KNT = 12
      WRITE (IOUT,108)
      WRITE (IOUT,109) MONTH(KNT),YR(KNT),(SUM(I,I),I=1,3)
      WRITE(IOUT,110)(MONTH(KNT+I),YR(KNT+I),(SUM(I,J),J=1,3),I=1,12)

      SET UP THE PLOT DATA FOR THE SUMMARY TOTALS

      CALL PLOTS
      CALL PLOT(0.,-11.0,-3)
      CALL SCALE (XDATA,12.0,13,1)

      DO 9025 KK = 1,13
      SALES(KK) = SUM(KK,1)
      PAYOUT(KK) = SUM(KK,2)
      AMTNET(KK) = SUM(KK,3)
9025 CONTINUE

      XPLOT(1) = AMIN1(SALES,PAYOUT,AMTNET)
      XPLOT(2) = AMAX1(SALES,PAYOUT,AMTNET)

      CALL PLOT(0.0,1.5,-3)
      CALL SCALE (XPLT,8.0,2,1)

      SALES(14) = XPLOT(3)
      PAYOUT(14) = XPLOT(3)
      AMTNET(14) = XPLOT(3)
      SALES(15) = XPLOT(4)
      PAYOUT(15) = XPLOT(4)
      AMTNET(15) = XPLOT(4)

      CALL AXIS(0.0,0.0,'MONTH',-5,12.0,0.0,XDATA(14),XDATA(15))
      CALL AXIS(0.0,0.0,'TOTALS',6,8.0,90.0,SALES(14),SALES(15))

      CALL LINE (XDATA,SALES,13,1,1,3)
      CALL LINE (XDATA,PAYOUT,13,1,1,11)
      CALL LINE (XDATA,AMTNET,13,1,1,1)

      CALL SYMBOL(3.0,8.25,.35,'SUMMARY TOTALS',0.0,14)
      CALL SYMBOL(10.0,8.0,.21,'LEGEND',0.0,6)
      CALL SYMBOL(10.0,7.75,.14,3,0.0,-1)

```

```

CALL SYMBOL(999.0,999.0,.14,' SALES',0.0,7)
CALL SYMBOL(10.0,7.5 ,.14,11,0.0,-1)
CALL SYMBOL(999.0,999.0,.14,' PAYOUT',0.0,8)
CALL SYMBOL(10.0,7.25,.14,1,0.0,-1)
CALL SYMBOL(999.0,999.0,.14,' NET AMOUNT',0.0,12)

```

SET UP THE PLOT DATA FOR THE PROJECTED SALES

```

TYPE0(14) = 0.0
TYPE0(15) = 15000.0
TYPE6(14) = 0.0
TYPE6(15) = 15000.0
SALES(14) = 0.0
SALES(15) = 15000.0

```

```

CALL PLOT (15.0,0.0,-3)
CALL AXIS (0.0,0.0,'MONTH',-5,12.0,0.0,XDATA(14),XDATA(15))
CALL AXIS(0.0,0.0,'SALES TOTALS',12,8.0,90.0,TYPE0(14),TYPE0(15))

```

```

CALL LINE (XDATA,TYPE0,13,1,1,3)
CALL LINE (XDATA,TYPE6,13,1,1,1)
CALL LINE (XDATA,SALES,13,1,1,1)

```

```

CALL SYMBOL(3.5,8.25,.35,'SALES TOTALS',0.0,12)
CALL SYMBOL(10.0,7.75,.21,'LEGEND',0.0,6)
CALL SYMBOL(10.0,7.25,.14,3,0.0,-1)
CALL SYMBOL(999.0,999.0,.14,' TYPE 0 SALES',0.0,14)
CALL SYMBOL(10.0,7.0 ,.14,11,0.0,-1)
CALL SYMBOL(999.0,999.0,.14,' TYPE 6 SALES',0.0,14)
CALL SYMBOL(10.0,6.75,.14,1,0.0,-1)
CALL SYMBOL(999.0,999.0,.14,' TOTAL SALES',0.0,13)

```

SET UP THE DATA FOR THE COST TOTALS PLOT

```

CALL PLOT (15.0,0.0,-3)
CALL SCALE (COST, 8.0,13,1)

```

```

CALL AXIS( 0.0,0.0,'MONTH',-5,12.0,0.0,XDATA(14),XDATA(15))
CALL AXIS(0.0,0.0,'COST',4, 8.0,90.0,COST(14),COST(15))

```

```

CALL LINE (XDATA,COST ,13,1,1,3)

```

```

CALL SYMBOL(5.0,8.25,.35,'COST TOTALS',0.0,11)
CALL PLOT (15.0,0.0,-3)

```

OUTPUT FORMATS

```

100 FORMAT (1H1/1H0/1H0/1H0/1H0/1H0/1H0/1H0/1H0/1H0/1H0/1H0/1H0/,
1 44X,12A4/1H0,43X,12A4/1H0,43X,12A4/1H0,
2 43X,'**',4A4,' THROUGH ',4A4,'**'/1H0,43X,12A4)

```

```

101 FORMAT(1H1,56X,'LIBERTY NATIONAL BANK'//1H0,37X,'PREDICTED CERTIFI
1CATES OF DEPOSIT SALES BY MATURITY PERIOD'/1H0,54X,6A4/1H0,58X,13,
2' DAY MATURITY'/1H0,54X,6A4)

```

```

102 FORMAT(1H0,53X,'(DOLLAR AMOUNTS IN THOUSANDS)'/1H0/1H0,27X,

```



```

1 'TYPE 0',36X,'TYPE 6',36X,'TYPE 8'/1H0,13X,
2 '*****',8X,
3 '*****',8X,
4 '*****')

```

```

103 FORMAT (1H ,15X,'BEGINNING BALANCE $',F10.2,12X,
1 'BEGINNING BALANCE $',F10.2,12X,'BEGINNING BALANCE $',F10.2)

```

```

104 FORMAT(1H0/1H ,15X,'CURRENT',5X,'INTST',5X,'NET AMOUNT',10X,
1 'CURRENT',5X,'INTST',5X,'NET AMOUNT',10X,'CURRENT',5X,'INTST',
2 5X,'NET AMOUNT'/1H , ' MONTH',10X,'SALES',7X,'RATE',4X,
3 'OUTSTANDING',11X,'SALES',7X,'RATE',4X,'OUTSTANDING',11X,'SALES',
4 7X,'RATE',4X,'OUTSTANDING'/1H+, ' _____',10X,' _____',6X,' _____',
5 4X,' _____',11X,' _____',6X,' _____',4X,' _____',11X,
6 ' _____',6X,' _____',4X,' _____')

```

```

105 FORMAT (1H0,A4,I3,6X,'$',F9.2,3X,F6.3,5X,'$',F9.2,8X,'$',F9.2,3X,
1 F6.3,5X,'$',F9.2,8X,'$',F9.2,3X,F6.3,5X,'$',F9.2)

```

```

106 FORMAT (1H0,A4,I3,7X,F9.2,3X,F6.3,6X,F9.2,9X,F9.2,3X,F6.3,6X,
4 F9.2,9X,F9.2,3X,F6.3,6X,F9.2)

```

```

107 FORMAT (1H ,13X,'-----',32X,'-----',32X,'-----',
1 /1H 13X,'$',F9.2,32X,'$',F9.2,32X,'$',F9.2)

```

```

108 FORMAT(1H1,56X,'LIBERTY NATIONAL BANK'//1H0,55X,'SUMMARY TOTALS BY
1 MONTH'//1H0,52X,'(DOLLAR AMOUNTS IN THOUSANDS)'//1H0,95X,
2 'NET AMOUNT'/1H ,25X,'MONTH',15X,'MONTHLY SALES',11X,
3 'MONTHLY PAYOUT',11X,'OUTSTANDING'/1H+,25X,' _____',15X,
4 ' _____',11X,' _____',11X,' _____')

```

```

109 FORMAT(1H0,23X,A4,I3,16X,'$',F9.2,15X,'$',F9.2,13X,'$',F9.2)

```

```

110 FORMAT(1H0,23X,A4,I3,17X,F9.2,16X,F9.2,14X,F9.2)

```

```

111 FORMAT(1H1,56X,'LIBERTY NATIONAL BANK'//1H0,38X,'MATURITY DATE ANA
1 LYSIS BY TYPE OF CERTIFICATES OF DEPOSIT' /1H ,52X,'(DOLLAR AMOUNT
2 S IN THOUSANDS)'//1H0,27X,'TYPE 0',36X,'TYPE 6',36X,'TYPE 8',/1H ,
3 13X,'*****',8X,'*****'
4 '*****',8X,'*****')

```

```

112 FORMAT(1H ,14X,'CERT AMTS PCT OF WGH TD AVG',10X,
1 'CERT AMTS PCT OF WGH TD AVG',10X,'CERT AMTS PCT OF WGH
2 TD AVG'/1H , ' MONTH',8X,'MATURING TOT AMT INTST RATE',9X,
3 'MATURING TOT AMT INTST RATE',9X,'MATURING TOT AMT INT
4 ST RATE')

```

```

113 FORMAT(1H0,A4,I3,6X,'$',F10.2,4X,F6.2,4X,F8.4,9X,'$',F10.2,4X,
1 F6.2,4X,F8.4,9X,'$',F10.2,4X,F6.2,4X,F8.4)

```

```

114 FORMAT(1H0,A4,I3,7X,F10.2,4X,F6.2,4X,F8.4,10X,F10.2,4X,F6.2,4X,
1 F8.4,10X,F10.2,4X,F6.2,4X,F8.4)

```

```

115 FORMAT(1H0/1H0,'TOTALS',6X,'$',F11.2,15X,F7.4,8X,'$',F11.2,15X,
1 F7.4,8X,'$',F11.2,15X,F7.4)

```

```

116 FORMAT(1H0/1H0, 7X,A4, ' 19',I2/1H ,6A4)
90 RETURN

```

FOOTNOTE

¹MPS also allows the solution to be stored in STANDARD FORMAT for use with the Programming Language 1 (PL/1) or Common Business Oriented Language (COBOL). However, these languages were unfamiliar to the programmer. Also, the STANDARD FORMAT feature is not as versatile as the READCOMM feature in that editing of the solution is not permitted. (See the IBM MPS/360, Linear and Separable Programming-User's Manual, reference [25].)

APPENDIX C

REPORTS FOR THE PERIOD

DECEMBER, 1974 to DECEMBER, 1975

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

MONTH	TYPE 0			TYPE 6			TYPE 8		
	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE
***** DEC 1974 *****									
DEC 74	\$ 13770.10	13.14	10.6714	\$ 2000.00	5.39	11.8503	\$ 0.0	0.0	0.0
JAN 75	39217.52	37.43	10.3660	17549.99	47.30	11.2315	0.0	0.0	0.0
FEB 75	10832.48	10.34	10.8285	3900.00	10.51	10.9701	0.0	0.0	0.0
MAR 75	20230.76	19.31	10.4795	9750.00	25.23	10.8401	0.0	0.0	0.0
APR 75	7069.24	6.75	10.0001	3900.00	10.51	10.6799	0.0	0.0	0.0
MAY 75	3447.84	3.29	10.0566	0.0	0.0	0.0	0.0	0.0	0.0
JUN 75	10202.16	9.74	9.8700	0.0	0.0	0.0	0.0	0.0	0.0
TOTALS	\$ 104770.09		10.3927	\$ 37099.99		11.0765	\$ 0.0		0.0
***** JAN 1975 *****									
JAN 75	\$ 39217.52	30.12	10.3660	\$ 17549.99	31.03	11.2315	\$ 0.0	0.0	0.0
FEB 75	33880.75	26.02	10.2374	21450.00	37.93	10.9288	0.0	0.0	0.0
MAR 75	36400.00	27.95	10.2353	9750.00	17.24	10.8401	0.0	0.0	0.0
APR 75	7069.24	5.43	10.0001	3900.00	6.90	10.6799	0.0	0.0	0.0
MAY 75	3447.84	2.65	10.0566	0.0	0.0	0.0	0.0	0.0	0.0
JUN 75	10202.16	7.83	9.8700	0.0	0.0	0.0	0.0	0.0	0.0
JUL 75	0.0	0.0	0.0	3900.00	6.90	10.5499	0.0	0.0	0.0
TOTALS	\$ 130217.50		10.2291	\$ 56549.99		10.9641	\$ 0.0		0.0

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

MONTH	TYPE 0 *****			TYPE 6 *****			TYPE 8 *****		
	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE
FEB 1975 *****									
FEB 75	\$ 33880.75	27.13	10.2374	\$ 21450.00	35.48	10.9288	\$ 0.0	0.0	0.0
MAR 75	63700.00	51.01	9.7788	25350.00	41.94	10.2983	0.0	0.0	0.0
APR 75	13650.00	10.93	9.5855	9750.00	16.13	10.2299	0.0	0.0	0.0
MAY 75	3447.84	2.76	10.0566	0.0	0.0	0.0	0.0	0.0	0.0
JUN 75	10202.16	8.17	9.8700	0.0	0.0	0.0	0.0	0.0	0.0
JUL 75	0.0	0.0	0.0	3900.00	6.45	10.5499	0.0	0.0	0.0
AUG 75	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
TOTALS	\$ 124880.74		9.8972	\$ 60449.99		10.5272	\$ 0.0		0.0
MAR 1975 *****									
MAR 75	\$ 63700.00	41.18	9.7788	\$ 25350.00	39.39	10.2983	\$ 0.0	0.0	0.0
APR 75	40950.00	26.47	8.6556	23400.00	36.36	9.5477	0.0	0.0	0.0
MAY 75	17097.84	11.05	8.5426	5850.00	9.09	9.0301	0.0	0.0	0.0
JUN 75	23852.16	15.42	8.8170	3900.00	6.06	8.8999	0.0	0.0	0.0
JUL 75	9100.00	5.88	7.8700	5850.00	9.09	9.9466	0.0	0.0	0.0
AUG 75	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
SEP 75	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
TOTALS	\$ 154699.99		9.0843	\$ 64350.00		9.7933	\$ 0.0		0.0

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

MONTH	TYPE 0			TYPE 6			TYPE 8		
	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE
APR 1975									
APR 75	\$ 40950.00	31.03	8.6556	\$ 23400.00	38.71	9.5477	\$ 0.0	0.0	0.0
MAY 75	44397.84	33.65	8.0366	17550.00	29.03	8.6432	0.0	0.0	0.0
JUN 75	23852.16	18.08	8.8170	5850.00	9.68	8.7399	0.0	0.0	0.0
JUL 75	18200.00	13.79	7.7150	9750.00	16.13	9.2839	0.0	0.0	0.0
AUG 75	4550.00	3.45	7.4001	3900.00	6.45	8.1301	0.0	0.0	0.0
SEP 75	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
OCT 75	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
TOTALS	\$ 131949.98		8.3035	\$ 60450.00		9.0729	\$ 0.0		0.0
MAY 1975									
MAY 75	\$ 44397.84	32.79	8.0366	\$ 17550.00	31.03	8.6432	\$ 0.0	0.0	0.0
JUN 75	37502.16	27.70	8.2613	11700.00	20.69	8.3947	0.0	0.0	0.0
JUL 75	31850.00	23.52	7.5199	15600.00	27.59	8.8101	0.0	0.0	0.0
AUG 75	4550.00	3.36	7.4001	3900.00	6.45	8.1301	0.0	0.0	0.0
SEP 75	13650.00	10.08	6.9700	5850.00	10.34	7.7301	0.0	0.0	0.0
OCT 75	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
NOV 75	3447.84	2.55	6.8401	1950.00	3.45	8.0000	0.0	0.0	0.0
TOTALS	\$ 135397.83		7.8179	\$ 56550.00		8.4858	\$ 0.0		0.0

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

MONTH	TYPE 0			TYPE 6			TYPE 8		
	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE
***** JUN 1975 *****									
JUN 75	\$ 37502.16	29.18	8.2613	\$ 11700.00	23.08	8.3947	\$ 0.0	0.0	0.0
JUL 75	51152.15	39.81	7.4181	25350.00	50.00	8.4600	0.0	0.0	0.0
AUG 75	7997.84	6.22	7.3223	3900.00	7.69	8.1301	0.0	0.0	0.0
SEP 75	18200.00	14.16	7.0000	7800.00	15.38	7.7326	0.0	0.0	0.0
OCT 75	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
NOV 75	3447.84	2.68	6.8401	1950.00	3.85	8.0000	0.0	0.0	0.0
DEC 75	10202.16	7.94	6.7999	0.0	0.0	0.0	0.0	0.0	0.0
TOTALS	\$ 128502.14		7.5344	\$ 50700.00		8.2899	\$ 0.0		0.0
***** JUL 1975 *****									
JUL 75	\$ 51152.15	35.98	7.4181	\$ 25350.00	43.33	8.4600	\$ 0.0	0.0	0.0
AUG 75	21647.84	15.23	7.2139	9750.00	16.67	7.9678	0.0	0.0	0.0
SEP 75	28402.16	19.98	7.0431	13650.00	23.33	7.7743	0.0	0.0	0.0
OCT 75	13650.00	9.60	6.9902	3900.00	5.67	7.6999	0.0	0.0	0.0
NOV 75	3447.84	2.43	6.8401	1950.00	3.33	8.0000	0.0	0.0	0.0
DEC 75	10202.16	7.18	6.7999	0.0	0.0	0.0	0.0	0.0	0.0
JAN 76	13650.00	9.60	6.7000	3900.00	6.67	7.4501	0.0	0.0	0.0
TOTALS	\$ 142152.14		7.1436	\$ 58500.00		8.0846	\$ 0.0		0.0

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

MONTH	TYPE 0 *****			TYPE 6 *****			TYPE 8 *****		
	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE
AUG 1975 *****									
AUG 75	\$ 21647.84	19.22	7.2139	\$ 9750.00	20.00	7.9678	\$ 0.0	0.0	0.0
SEP 75	46602.15	41.37	7.0260	23400.00	48.00	7.7100	0.0	0.0	0.0
OCT 75	17097.84	15.18	6.9861	3900.00	8.00	7.6999	0.0	0.0	0.0
NOV 75	3447.84	3.06	6.8401	1950.00	4.00	8.0000	0.0	0.0	0.0
DEC 75	10202.16	9.06	6.7999	0.0	0.0	0.0	0.0	0.0	0.0
JAN 76	13650.00	12.12	6.7000	3900.00	8.00	7.4501	0.0	0.0	0.0
FEB 76	0.0	0.0	0.0	5850.00	12.00	7.4099	0.0	0.0	0.0
TOTALS	\$ 112647.82		6.9904	\$ 48750.00		7.7155	\$ 0.0		0.0
SEP 1975 *****									
SEP 75	\$ 46602.15	33.87	7.0260	\$ 23400.00	37.50	7.7100	\$ 0.0	0.0	0.0
OCT 75	30747.84	22.35	7.0277	9750.00	15.63	7.6337	0.0	0.0	0.0
NOV 75	13650.00	9.92	6.9970	7800.00	12.50	7.6698	0.0	0.0	0.0
DEC 75	10202.16	7.41	6.7999	1950.00	3.13	7.4302	0.0	0.0	0.0
JAN 76	36400.00	26.45	6.7376	13650.00	21.87	7.3214	0.0	0.0	0.0
FEB 76	0.0	0.0	0.0	5850.00	9.38	7.4099	0.0	0.0	0.0
MAR 76	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
TOTALS	\$ 137602.14		6.9305	\$ 62399.99		7.5712	\$ 0.0		0.0

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

MONTH	TYPE 0 *****			TYPE 6 *****			TYPE 8 *****		
	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE
OCT 1975 *****									
OCT 75	\$ 30747.84	25.26	7.0277	\$ 9750.00	19.23	7.6337	\$ 0.0	0.0	0.0
NOV 75	27300.00	22.42	7.0737	13650.00	26.92	7.7001	0.0	0.0	0.0
DEC 75	13650.00	11.21	6.8808	1950.00	3.85	7.4302	0.0	0.0	0.0
JAN 76	50050.00	41.11	6.8064	19500.00	38.46	7.3989	0.0	0.0	0.0
FEB 76	0.0	0.0	0.0	5850.00	11.54	7.4099	0.0	0.0	0.0
MAR 76	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
APR 76	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
TOTALS	\$ 121747.83		6.9306	\$ 50700.00		7.5276	\$ 0.0		0.0
NOV 1975 *****									
NOV 75	\$ 27300.00	23.08	7.0737	\$ 13650.00	25.93	7.7001	\$ 0.0	0.0	0.0
DEC 75	27300.00	23.08	7.0606	7800.00	14.81	7.7678	0.0	0.0	0.0
JAN 76	63699.99	53.85	6.8929	25350.00	48.15	7.5030	0.0	0.0	0.0
FEB 76	0.0	0.0	0.0	5850.00	11.11	7.4099	0.0	0.0	0.0
MAR 76	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
APR 76	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
MAY 76	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
TOTALS	\$ 118299.98		6.9733	\$ 52650.00		7.5830	\$ 0.0		0.0

LIBERTY NATIONAL BANK

MATURITY DATE ANALYSIS BY TYPE OF CERTIFICATES OF DEPOSIT
(DOLLAR AMOUNTS IN THOUSANDS)

MONTH	TYPE 0 *****			TYPE 6 *****			TYPE 8 *****		
	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE	CERT AMTS MATURING	PCT OF TOT AMT	WGHTD AVG INTST RATE
***** DEC 1975 *****									
DEC 75	\$ 27300.00	23.08	7.0606	\$ 7800.00	15.38	7.7678	\$ 0.0	0.0	0.0
JAN 76	90999.99	76.92	7.0242	37050.00	73.08	7.6882	0.0	0.0	0.0
FEB 76	0.0	0.0	0.0	5850.00	11.54	7.4099	0.0	0.0	0.0
MAR 76	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
APR 76	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
MAY 76	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
JUN 76	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
TOTALS	\$ 118299.99		7.0326	\$ 50700.00		7.6684	\$ 0.0		0.0

LIBERTY NATIONAL BANK

PREDICTED CERTIFICATES OF DEPOSIT SALES BY MATURITY PERIOD

30 DAY MATURITY

(DOLLAR AMOUNTS IN THOUSANDS)

	TYPE 0			TYPE 6			TYPE 8		
	*****			*****			*****		
	BEGINNING BALANCE	\$	13770.10	BEGINNING BALANCE	\$	2000.00	BEGINNING BALANCE	\$	0.0
MONTH	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING
DEC 74	\$ 27300.00	10.320	\$ 27300.00	\$ 4675.00	11.000	\$ 4675.00	\$ 0.0	11.000	\$ 0.0
JAN 75	23048.28	9.960	23048.28	17550.00	10.920	17550.00	0.0	10.920	0.0
FEB 75	27300.00	9.170	27300.00	15600.00	9.960	15600.00	0.0	9.960	0.0
MAR 75	27300.00	8.191	27300.00	13650.00	9.061	13650.00	0.0	9.061	0.0
APR 75	27300.00	7.720	27300.00	11700.00	8.450	11700.00	0.0	8.450	0.0
MAY 75	13650.00	7.290	13650.00	5850.00	8.049	5850.00	0.0	8.049	0.0
JUN 75	19302.16	7.250	19302.16	9750.00	7.900	9750.00	0.0	7.900	0.0
JUL 75	13650.00	7.150	13650.00	5850.00	7.860	5850.00	0.0	7.860	0.0
AUG 75	18200.00	6.999	18200.00	9750.00	7.620	9750.00	0.0	7.620	0.0
SEP 75	13650.00	7.080	13650.00	5850.00	7.590	5850.00	0.0	7.590	0.0
OCT 75	13650.00	7.150	13650.00	5850.00	7.740	5850.00	0.0	7.740	0.0
NOV 75	13650.00	7.240	13650.00	5850.00	7.880	5850.00	0.0	7.880	0.0
DEC 75	27300.00	7.330	27300.00	11700.00	8.090	11700.00	0.0	8.090	0.0
	<u>265300.43</u>			<u>123624.98</u>			<u>0.0</u>		

LIBERTY NATIONAL BANK

PREDICTED CERTIFICATES OF DEPOSIT SALES BY MATURITY PERIOD

60 DAY MATURITY

(DOLLAR AMOUNTS IN THOUSANDS)

	TYPE 0			TYPE 6			TYPE 8		
	*****			*****			*****		
	BEGINNING BALANCE		\$	BEGINNING BALANCE		\$	BEGINNING BALANCE		\$
MONTH	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING
			\$ 11917.52			\$ 12875.00			\$ 0.0
DEC 74	\$ 4491.49	10.290	\$ 16409.01	\$ 3900.00	10.970	\$ 16775.00	\$ 0.0	10.970	\$ 0.0
JAN 75	16169.24	9.930	20660.73	0.0	10.890	3900.00	0.0	10.890	0.0
FEB 75	6580.76	9.140	22750.00	5850.00	9.930	5850.00	0.0	9.930	0.0
MAR 75	13650.00	8.160	20230.76	5850.00	9.030	11700.00	0.0	9.030	0.0
APR 75	0.0	7.690	13650.00	1950.00	8.420	7800.00	0.0	8.420	0.0
MAY 75	13650.00	7.260	13650.00	5850.00	8.020	7900.00	0.0	8.020	0.0
JUN 75	3447.84	7.220	17097.84	0.0	7.870	5850.00	0.0	7.870	0.0
JUL 75	10202.16	7.120	13650.00	5850.00	7.830	5850.00	0.0	7.830	0.0
AUG 75	3447.84	6.970	13650.00	0.0	7.590	5950.00	0.0	7.590	0.0
SEP 75	10202.16	7.050	13650.00	5850.00	7.560	5850.00	0.0	7.560	0.0
OCT 75	3447.84	7.120	13650.00	0.0	7.710	5850.00	0.0	7.710	0.0
NOV 75	13650.00	7.210	17097.84	5850.00	7.850	5850.00	0.0	7.850	0.0
DEC 75	0.0	7.300	13650.00	0.0	8.060	5850.00	0.0	8.060	0.0
	<u>98939.31</u>			<u>40950.00</u>			<u>0.0</u>		

LIBERTY NATIONAL BANK

PREDICTED CERTIFICATES OF DEPOSIT SALES BY MATURITY PERIOD

90 DAY MATURITY

(DOLLAR AMOUNTS IN THOUSANDS)

	TYPE 0			TYPE 6			TYPE 8		
	*****			*****			*****		
	BEGINNING BALANCE	\$	6340.99	BEGINNING BALANCE	\$	0.0	BEGINNING BALANCE	\$	0.0
MONTH	CURRENT SALES	INTST RATE	NET AMOUNT QUISHANDING	CURRENT SALES	INTST RATE	NET AMOUNT QUISHANDING	CURRENT SALES	INTST RATE	NET AMOUNT QUISHANDING
DEC 74	\$ 13650.00	10.160	\$ 19990.99	\$ 9750.00	10.840	\$ 9750.00	\$ 0.0	10.840	\$ 0.0
JAN 75	0.0	9.800	19990.99	0.0	10.760	9750.00	0.0	10.760	0.0
FEB 75	0.0	9.010	13650.00	0.0	9.800	9750.00	0.0	9.800	0.0
MAR 75	13650.00	8.030	13650.00	3900.00	8.900	3900.00	0.0	8.900	0.0
APR 75	9100.00	7.560	22750.00	3900.00	8.290	7800.00	0.0	8.290	0.0
MAY 75	0.0	7.130	22750.00	0.0	7.890	7800.00	0.0	7.890	0.0
JUN 75	4550.00	7.090	13650.00	1950.00	7.740	5850.00	0.0	7.740	0.0
JUL 75	13650.00	6.990	18200.00	3900.00	7.700	5850.00	0.0	7.700	0.0
AUG 75	0.0	6.840	18200.00	0.0	7.460	5850.00	0.0	7.460	0.0
SEP 75	0.0	6.920	13650.00	1950.00	7.430	5850.00	0.0	7.430	0.0
OCT 75	13650.00	6.990	13650.00	5850.00	7.580	7800.00	0.0	7.580	0.0
NOV 75	0.0	7.080	13650.00	0.0	7.720	7800.00	0.0	7.720	0.0
DEC 75	0.0	7.170	13650.00	0.0	7.930	5850.00	0.0	7.930	0.0
	<u>\$ 68250.00</u>			<u>\$ 31200.00</u>			<u>\$ 0.0</u>		

LIBERTY NATIONAL BANK

PREDICTED CERTIFICATES OF DEPOSIT SALES BY MATURITY PERIOD

120 DAY MATURITY

(DOLLAR AMOUNTS IN THOUSANDS)

	TYPE 0			TYPE 6			TYPE 8		
	*****			*****			*****		
	BEGINNING	BALANCE	\$	BEGINNING	BALANCE	\$	BEGINNING	BALANCE	\$
	6580.76			0.0			0.0		
MONTH	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST RATE	NET AMOUNT OUTSTANDING
DEC 74	\$ 7069.24	10.000	\$ 13650.00	\$ 3900.00	10.680	\$ 3900.00	\$ 0.0	10.680	\$ 0.0
JAN 75	0.0	9.640	13650.00	0.0	10.600	3900.00	0.0	10.600	0.0
FEB 75	0.0	8.850	13650.00	0.0	9.640	3900.00	0.0	9.640	0.0
MAR 75	9100.00	7.870	16169.24	1950.00	8.740	5850.00	0.0	8.740	0.0
APR 75	4550.00	7.400	13650.00	3900.00	8.130	5850.00	0.0	8.130	0.0
MAY 75	13650.00	6.970	27300.00	5850.00	7.730	11700.00	0.0	7.730	0.0
JUN 75	0.0	6.930	27300.00	0.0	7.580	11700.00	0.0	7.580	0.0
JUL 75	0.0	6.830	18200.00	0.0	7.540	9750.00	0.0	7.540	0.0
AUG 75	0.0	6.680	13650.00	0.0	7.300	5850.00	0.0	7.300	0.0
SEP 75	22750.00	6.760	22750.00	9750.00	7.270	9750.00	0.0	7.270	0.0
OCT 75	0.0	6.830	22750.00	0.0	7.420	9750.00	0.0	7.420	0.0
NOV 75	0.0	6.920	22750.00	0.0	7.560	9750.00	0.0	7.560	0.0
DEC 75	0.0	7.010	22750.00	0.0	7.770	9750.00	0.0	7.770	0.0
	<u>\$ 57119.23</u>			<u>\$ 25350.00</u>			<u>\$ 0.0</u>		

LIBERTY NATIONAL BANK

PREDICTED CERTIFICATES OF DEPOSIT SALES BY MATURITY PERIOD

180 DAY MATURITY

(DOLLAR AMOUNTS IN THOUSANDS)

	TYPE 0			TYPE 6			TYPE 8		
	*****			*****			*****		
	BEGINNING BALANCE	\$	3447.84	BEGINNING BALANCE	\$	0.0	BEGINNING BALANCE	\$	0.0
MONTH	CURRENT SALES	INTST. RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST. RATE	NET AMOUNT OUTSTANDING	CURRENT SALES	INTST. RATE	NET AMOUNT OUTSTANDING
DEC 74	\$ 10202.16	9.870	\$ 13650.00	\$ 3900.00	10.550	\$ 3900.00	\$ 0.0	10.550	\$ 0.0
JAN 75	0.0	9.510	13650.00	0.0	10.470	3900.00	0.0	10.470	0.0
FEB 75	0.0	8.720	13650.00	0.0	9.510	3900.00	0.0	9.510	0.0
MAR 75	0.0	7.740	13650.00	0.0	8.610	3900.00	0.0	8.610	0.0
APR 75	0.0	7.270	13650.00	1950.00	8.000	5850.00	0.0	8.000	0.0
MAY 75	3447.84	6.840	13650.00	0.0	7.600	5850.00	0.0	7.600	0.0
JUN 75	10202.16	6.800	13650.00	3900.00	7.450	5850.00	0.0	7.450	0.0
JUL 75	13650.00	6.700	27300.00	5850.00	7.410	11700.00	0.0	7.410	0.0
AUG 75	0.0	6.550	27300.00	0.0	7.170	11700.00	0.0	7.170	0.0
SEP 75	0.0	6.630	27300.00	0.0	7.140	11700.00	0.0	7.140	0.0
OCT 75	0.0	6.700	27300.00	0.0	7.290	9750.00	0.0	7.290	0.0
NOV 75	0.0	6.790	23852.16	0.0	7.430	9750.00	0.0	7.430	0.0
DEC 75	0.0	6.880	13650.00	0.0	7.640	5850.00	0.0	7.640	0.0
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	\$ 37502.15			\$ 15600.00			\$ 0.0		

LIBERTY NATIONAL BANK

SUMMARY TOTALS BY MONTH

(DOLLAR AMOUNTS IN THOUSANDS)

MONTH	MONTHLY SALES	MONTHLY PAYOUT	NET AMOUNT OUTSTANDING
DEC 74	\$ 88837.88	\$ 15770.10	\$129999.94
JAN 75	88837.88	15770.10	129999.94
FEB 75	56767.52	56767.52	129999.94
MAR 75	55330.76	55330.76	129999.94
APR 75	89050.00	89050.00	129999.94
MAY 75	64350.00	64350.00	129999.94
JUN 75	61947.84	61947.84	129999.94
JUL 75	53102.16	53102.16	129999.94
AUG 75	72602.13	72602.13	129999.94
SEP 75	31397.84	31397.84	129999.94
OCT 75	70002.13	70002.13	129999.94
NOV 75	42447.84	42447.84	129999.94
DEC 75	39000.00	39000.00	129999.94