# MULTIVARIATE ANALYSIS APPROACH TO SELECTION OF 

 PARENTAL MATERIALS FOR HYBRIDIZATIONIN WINTER WHEAT

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IN WINTER WHEAT

Thesis Approved:


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## CHAPTER I

## INTRODUCTION

In self-pollinated crops, most of the cultivars consist of one or a limited number of related homozygous genotypes. For improving complex quantitative characters such as yield, choice of parents is critical. The conventional approaches are limited since they necessitate a considerable amount of labor and time. A knowledge of genetic diversity present among populations and its quantitative measurement helps a plant breeder in selecting desirable parents for his breeding program.

One of the important aims of plant breeding is to improve yield and quality by developing superior varieties. This is done by altering, to the best advantage, the genetic makeup of the existing cultivars. Such work should be facilitated if the plant breeder is able to classify the varieties broadly on the basis of a given set of genetic characters and further discriminate any two cultivars belonging to the same class or group. The objectives of this study were: (1) to set up a discriminant function for a number of cultivars grown at different areas during three years and use these functions to determine the best two-way and three-way crosses, and (2) to measure the genetic diversity among populations originating from different ecological areas as a basis for selecting parental materials and to see if there is any relationship between geographical distribution and genetic diversity.

## CHAPTER II

## LITERATURE REVIEW

The basic importance of genetic diversity in breeding for high yield has long been recognized. The magnitude of heterosis in wheat has been reported to be dependent on the degree of genetic diversity between parental stocks (20). This may be used as an indicator of the inherent yielding capacity of a cross. The breeder of small grains makes many crosses, each with a definite purpose, but he has no sure way of knowing their comparative value in advance. We know that certain cultivars have a higher value in combining ability than do others. Lindstrom (11) introduced the principle of "top crossing" in 1931 as a valuable technique in maize improvement. Coefficients of correlation for a number of different characters were determined between the mean performance of the single crosses of inbred lines of corn and the performance of these lines in crosses with a commercial variety. From a comparison of these correlations, Jenkins and Brunson (9) concluded that crosses with open-pollinated varieties may be used efficiently in the preliminary testing of new lines. Suneson (21) emphasized the importance of genetic diversity as a protection against plant diseases and insects. He proposed the breeding methods that give multigenic resistance in multiline varieties.

In self-pollinated species, a lack or a limited amount of genetic diversity is present within established cultivars, since most cultivars
consist of one or a limited number of related homozygous genotypes and selection for uniformity is continually practiced. Genetically diverse populations have shown greater stability in performance over a number of environments (1). The productivity of ten lima bean populations representing three levels of genetic diversity was tested at four locations during four years by Allard (1). The purpose of the test was to determine whether productivity and stability of productivity are related to genetic diversity. Order of productivity was bulks $\geq$ pure lines >mixture. Order of stability of production was bulks >mixture > pure lines (1). The adaptation mechanism may be related to the degree of genetic variation for the characters influencing survival. In selfpollinated crops, the selection of parents for hybridization programs is based largely upon wide adaptation, high yield potential, and genetic diversity. Anand and Murty (2) mentioned that adaptation could be due to heterozygosity, genetic diversity of populations, past history of selection, and the degree of general combining ability. Genetic diversity might permit genetic variability which would have a buffering action in new environments. Finlay and Wilkson (6) reported the measurement of yield and stability of its performance in barley. For each variety a linear regression of individual yield on the mean yield of all varieties for each location and each season was computed. They suggested that the stability of productivity in different environments of the segregating generation could be due to the diversity of genotypes. The retention of genetic diversity within a population could be due to the presence of linkage equilibrium in breeding species. The introduction of alien genes from different geographical areas also has added to the genetic diversity (2). The cultivars which give relatively
high yield and show considerable stability of performance over a large number of locations are classified as having good adaptation. Das and Jain (5) studied adaptation with respect to cytology of the plant. They analyzed a number of wheat cultivars with different adaptability for chiasma formation under different agronomic and environmental conditions. Cultivars well adapted in respect to yielding ability showed relative stability of chiasma frequency (5). Experimental findings reported in the literature indicate that crosses of unrelated, inbred lines of corn show greater heterosis than do crosses of related lines. The success of many double-cross hybrids over very wide areas is the result of their genetic diversity combined with their stability and consistency of performance (1, 12).

In spite of the importance of genetic diversity in hybridization, it is difficult to obtain a dependable estimate of such diversity before making crosses. In the past, ecological or geographical diversity has been used as an index of genetic diversity. A number of studies have shown that the divergenre between populations could not be related to their geographical distribution (2, 3, 4). Harrington (8) suggested that bulk $F_{2}$ yield trials may be used to indicate the potential yield possibilities of a cross. He added that $F_{3}$ yield trials are of supplementary value as a support to the $\mathrm{F}_{2}$ conclusions.

One of the statistical approaches for measuring genetic diversity which has been used by many workers is Mahalanobis' generalized distance $\mathrm{D}^{2}(2,3,4,15,20)$. In a few studies, the relative contribution of different yield components to the total divergence showed that yield per se had a low contribution (2, 3, 13, 15). Thus, Sachan and Shorma (17) emphasized the type of component characters of yield that
should be taken into account. These components should have economic importance under crop improvement programs (17). The genetic divergence as measured by the $\mathrm{D}^{2}$ statistic is reflected to some extent in the combining ability effects. The crosses of most divergent varieties have shown larger specific combining ability effects for a majority of characters (14). Populations may be grouped into several clusters depending on their distances measured by average $\mathrm{D}^{2}$. Somayajulu et al. (20) suggested that cultivars which are grouped together come under one or more of the following categories: (1) related by pedigree, (2) originating in the same or similar ecological regions, and (3) similar in characters such as maturity and plant height which are known to contribute to genetic divergence in wheat (20).

Another technique is the use of discriminant function, first developed by Fisher $(7,16)$. Both statistics deal with the problem in ways very closely related to each other (7, 16). Discriminant function was used in wheats for varietal selection (13, 18, 20), and Smith (19) mentioned it as a tool for selecting parents for hybridization.

## CHAPTER III

## MATERIALS AND METHODS

The cultivars used for this study were obtained from wheat architecture nurseries at the Agronomy Research stations, Stillwater and Lahoma, Oklahoma. The cultivars originated from the U.S.A., U.S.S.R., and European countries. The layout was a randomized complete block design as follows:

1. Thirty entries in 1976-77 with three replications at Stillwater.
2. Thirty entries in $1977-78$ with three replications each at Stillwater and Lahoma.
3. Thirty entries in 1978-79 with four replications each at Stillwater and Lahoma (four entries in 1979, Stillwater, were eliminated because of late maturity). The cultivars used for each experiment were different in different years.

Each entry consisted of four 3-meter rows, with the rows being 30 cm apart. Grain yield and the three major components of yield, namely fertile tiller number per unit area, the average number of kernels per spike, and the average kernel weight, were measured as follows:

Tiller Number - Number of seed-bearing tillers along a random section of $900 \mathrm{~cm}^{2}$. Two samples were taken from each entry.

Number of Kernels per Spike - Six randomly selected spikes from each plot were threshed separately and the kernels were counted.

Kernel Weight - The number of kernels obtained from the six spikes above and their weights were used to estimate the average kernel weight, expressed as weight (grams) per 1000 kernels.

Grain Yield - Plants in a $30-\mathrm{cm}$ section at each end of the two center rows were discarded to eliminate possible border effects. The remaining $1.49 \mathrm{M}^{2}$ were harvested.

## Analysis Procedure

An analysis of variance was carried out for yield and the yield components at each location separately. Two different methods of analysis were employed to attempt to identify superior yielding crosses among the cultivars. One method was discriminant analysis and the other was the determination of genetic divergence using Mahalonobis' $D^{2}$ measure. For each location and year, a discriminant analysis was used. The objective of the analysis is to obtain a discriminant function which is a linear combination of the components, to be used for classifying cultivars and their potential crosses into high, medium, or low yield groups. Linear discriminant analysis was developed by Fisher (7) for two-group classification. In such a case, there are two populations or groups and a set of $P$ variables $\left(X_{1}, X_{2}, \ldots, X_{p}\right)$ associated with the individuals in each population. The population discriminant function is a score or index ( $Z$ ) obtained as a linear combination of the variables:

$$
z=a_{1} x_{1}+a_{2} x_{2} \cdot \cdot+a_{p} x_{p}
$$

The a's are determined in order to maximize the probability of correctly identifying the group membership of an individual. When a sample of individuals from each population is available, the a's are estimated by
maximizing $D^{2} / S S_{W}$ where $D$ is the difference between mean $Z$ scores of the samples, and $S S_{w}$ is the pooled within-sample sum of squares of the Z scores.

If more than two populations are considered, the a's are estimated by maximizing $\frac{S S_{a}}{S S_{w}}$ where $S S_{a}$ and $S S_{w}$ are the sum of squares among and within groups, respectively (16).

To employ discriminant analysis, the group of cultivars in each experiment was partitioned into high, medium, and low yield groups based on observed mean yields over replications. Discriminant weights were determined as described above. The resultant discriminant function is represented as

$$
\text { Score }=Z=a_{1}(T L R)+a_{2}\left(\text { kernels/spike) }+a_{3}\right. \text { (Kwt) }
$$

The amount of contribution by each component to the score is represented by the a value. Another factor influencing variation in score is the amount of variability for each single component, more variability indicating more contribution.

Subsequent to the determination of the discriminant function, this function was used to predict the scores of all two-way and threeway crosses among the cultivars. To do this, it was assumed that gene actions of the yield components is additive, i.e., there is no dominance and no epistasis. Thus, the value of a yield component in a twoway cross was taken to be the average of the component values in the two parental cultivars. However, discriminant function was applied to the highest component of either parents to determine the score for that cross. It was assumed that by selecting in the further generations the high value of yield component would be recovered.

There is no assurance that the population discriminant function will result in a more correct classification method than simply using a random allocation method. This was investigated by using Wilks' likelihood ratio test for significance of the discriminant function. The sample discriminant function was applied as described previously only when it was found to be significant.

The second method used is Mahalanobis' generalized distance $\mathrm{D}^{2}$, applied to 1979 experiments only. The application of the $\mathrm{D}^{2}$ statistic is to measure the degree of divergence for individual characters or the pooled effect of several characters. Based on genetic diversity, a crossing program between genotypes may be initiated. The approach is based on the assumption that the best crosses are between parents showing the maximum genetic divergence. Genetic diversity between two genotypes is measured by

$$
D^{2}=\left(U_{1}-U_{2}\right)^{\prime} \Sigma^{-1}\left(U_{1}-U_{2}\right)
$$

where $U_{1}$ is a vector with three elements, each representing the average of one yield component in a cultivar. $U_{2}$ is defined similarly for a second cultivar. $\sum$ is a symetric $3 \times 3$ genotypic variance, covariance matrix. Since the phenotypic variance $\left(\sigma_{p}^{2}\right)$ is made up of genotypic $\left(\sigma_{G}^{2}\right)$ and environmental $\left(\sigma_{E}^{2}\right)$ components, then $\sigma_{P}^{2}=\sigma_{G}^{2}+\sigma_{E}^{2}$ (10). In estimating the variance, covariance components the expected entry mean square and mean products were partitioned as follows:

$$
E[\operatorname{entry} \text { (M.S.) }]=\operatorname{error}(M . S .)+4 \text { entry (M.S.) }=\sigma_{E}^{2}+4 \sigma_{G}^{2}
$$

$E[$ entry (M.P.) $]=\operatorname{error}(M . P)+$.4 entry (M.P.) $=\sigma_{G a G b}+4 \sigma_{G a}^{2}+G b$
where $\sigma_{G a G b}=$ the covariance of two characters, $a$ and $b, \sigma_{G a+G b}^{2}=$ the joint genotypic variance of characters $a$ and $b$. The genetic diversity was measured between any two cultivars by $\mathrm{D}^{2}$, as mentioned above. Cultivars were grouped into a number of clusters, $\mathrm{D}^{2}$ being treated as the square of generalized distance according to the method described by Tocher as cited by Rao (16).

## RESULTS AND DISCUSSION

## Analysis of Variance

The average yield and yield components for different years and locations are shown in Tables $I, I I, I I I, ~ I V, ~ a n d ~ V . ~ B e f o r e ~ u s i n g ~ a n y ~$ of the approaches, it is necessary to first find out if the cultivars differ significantly among themselves with respect to yleld components. The analysis of variance corresponding to each character for all experiments (Table VI) shows significant differences among entries at the 0.01 level of probability.

## Discriminant Function Analysis

Genotypes were classified into high, medium, and low groups on the basis of observed mean yield over replications (Tables $I, I I, I I I$, IV, and V) in order to obtain a discriminant function and evaluate their potential in crosses. The discriminant weights (a-values) were estimated by maximizing $\lambda=\frac{S_{a}}{S S_{W}}$, where $S S_{a}$ and $S S_{w}$ are the sum of squares among and within group (Appendix A). The $\lambda$ value (discriminant criterion) for each experiment is shown in Table VII. The significance of $\lambda$ was tested using Wilks' likelihood ration criterion to determine if it was statistically different from zero. If $\lambda$ is different from zero, it will permit the conclusion that the groups differ
significantly on the basis of linear combination, $Z$, associated with $\lambda$. A V statistic corresponding to each $\lambda$ value was computed according to Appendix A, and V's were treated as $\chi^{2}$ with 6 d.f. The results of this test for all experiments show that the discriminant criterion ( $\lambda$ ) for 1978 Stillwater and 1979 Lahoma are significant (Table VII). Therefore the three groups of high, medium, and low can be differentiated for the two above experiments on the basis of discriminant function. The $\lambda$ values for the rest of the experiments are not sufficient to classify groups significantly. The $\lambda$ value for 1978 Stillwater is 0.8159 (Table VII) while its $V$ value (16.406) is significant at 0.025 level of probability. The discriminant weights (a-values) associated with each discriminant criterion $\lambda$ were computed as explained in Appendix A , and the results are shown in Table VII. The score of Z value may be written as

$$
\text { Score }=Z=0.0292(T L R)+0.0640(\text { seeds } / \text { spike })+0.0546(\text { Kwt })
$$

The contribution of seeds per spike and kernel weight dominate the function, while the tiller number makes a lower contribution. Any cultivar now may be classified to the proper group by computing its score (assuming that it belongs to one of these groups).

For predicting the scores of all the two-way and three-way crosses among the cultivars, the discriminant function was applied to the highest component values of the parent in a cross. Among the 435 possible hybrids involving the 30 cultivars, those with the highest scores belong to the high group and would be promising. The top 30 scores for hybrids are shown in Table VIII. The hybrid obtained by crossing

Lovrin 6 (P16)* and F23-71 (P17) has the highest score. Tab1e III shows that the yield components for the above cultivars are:

| Name | TLR | Seeds/spike | Kwt | Index score |
| :---: | :---: | :---: | :---: | :---: |
| Lovrin 6 | 33 | 27 | 46 | 5.203 |
| F23-71 | 29 | 43 | 31 | 5.291 |

The score for hybrid obtained by these two parents is computed as follows:

$$
\text { Score }=Z=0.0292(33)+0.064(43)+0.0546(46)=6.239
$$

The discriminant weights (a-values) associated with tiller number ( 0.0292 ), seeds per spike ( 0.064 ) and kernel weight ( 0.0546 ) are each multiplied by the highest corresponding component among the two parents. Since it was assumed that the gene action is additive, the discriminant weights should, in fact, be multiplied by the average of component values in the two parental cultivars, but by selecting in the hybrid population, the high value of yield components would be recovered. The hybrid obtained by Lovrin 6 (P16)* X TX71A562-6 (P26) has the second highest score, since the kernel weight of Lovrin 6 and seeds per spike of TX71A562-6 (P26) (Table III) are high. Meanwhile the tiller number of TX71A562-6 (P26) is intermediate and would be partly responsible for the high score. The hybrid score then may be shown as

$$
\text { Score }=Z=0.0292(40)+0.064(39)+0.0546(46)=6.186
$$

Tam W-101 (P2) is relatively high in tiller number (Table III) and

[^0]Intermediate in kernel weight, and F23-71 (P17)* has the highest number of seeds per spike. The hybrid obtained by these two cultivars has the fourth highest score. Lovrin 6 (P16) with the highest kernel weight may combine with parents high in seeds per spike and tiller number such as Vona (P13), Tam W-102 (P21), and WA5829 (P24) to give high scores. Tam W-101 )P2) is relatively high in tiller number and intermediate in kernel weight, but low in number of seeds per spike. The complementary parents are relatively high in number of seeds per spike, such as F23-71 (P17), Gurgas 2 (P11), Tam W-102 (P21), TX71A562-6 (P26), Vona (P13), and WA5829 (P24). Based on discriminant function associated with 1978 Stillwater and Table VIII, parents high in number of seeds per spike and/or kernel weight, such as Lovrin 6 (P16) and F23-71 (P17), would contribute in many of the top crosses.

The three-way crosses for 1978 Stillwater are shown in Table VIII. Lovrin 6 (P16), F23-71 (P17), and Tam W-103 (P27) combine to give the maximum score value. Their yield components are as follows (Table III):

| Parent | TLR |  | Seeds/Spike |  | Kwt |
| :--- | :---: | :---: | :---: | :---: | :---: |$\quad$| Score |
| :--- |
| Lovrin 6 |

The score value is computed as

Score $=Z=0.0292(56)+0.064(43)+0.0546(46)=6.9$

Osage (P1) is second highest in tiller number (Table II) and

[^1]combines with Lovrin 6 (P16* and F23 (P17) to give the second highest score. The next highest score is obtained by combining Lovrin 6 (P16), Plainsman V (P19) and F23-71 (P17), which are high in kernal weight, tiller number and seeds per spike, respectively.

Comparing parents involved in top two-way and three-way crosses (Table VIII), it is realized that cultivars classified as good parents for two-way crosses were also involved in top three-way crosses.

Cultivars used in 1979 Lahoma (Table IV) are not the same as 1978 Stillwater, but several of them occur in both nurseries. Parents 10, 18, $19,20,21,22,23,24,25$, and 30 occur in 1978 Stillwater, but not in 1979 Lahoma. Conversely, parents 31 through 40 occur in 1979 Lahoma, but not in 1978 Stil1water (Tables III and IV).

The $\lambda$ value (Table VII) for 1979 Lahoma ( 0.6739 ) was tested using Wilks' likelihood ratio test criterion (Appendix A). The related V: value (14.326) was treated as $x^{2}$ with 6 d.f. and it was significant at the . 05 level of probability (Table VII). Discriminant weights were computed according to the illustration in Appendix A and

$$
\text { Score }=Z=0.0165(\text { TLR })+0.06104 \text { (seeds/spike) }+0.0239(\text { Kwt })
$$

The contribution of seeds per spike dominates the function and kernel weight is second in this position. Compared to discriminant function associated with 1978 Stillwater, the discriminant weight (a values) corresponding to kernel weight is considerably lower.

The top 30 two-way crosses are shown in Table IX. The best

[^2]combination is F23-71 (P17)** and Tam W-101 (P2), which are high in number of seeds per spike and number of tillers, respectively (Table IV). F23-71 (P17) also combined with Lovrin 6/T-W-101F6 (P32), high in tiller number and kernel weight, to give the second highest score. Tam W-101 (P2), which is high in tiller number and kernel weight (Table IV), combined with NR31-74 (P28) and NR 391-76 (P38), high in number of seeds per spike, and resulted in the third and fourth highest scores (Table IX). Vona (P13), which is relatively high in tiller number and number of seeds per spike (Table IV), was also classified as a good parent. Tam W-103 (P27), high in tiller number, was combined with cultivars high in kernel weight and/or number of seeds per spike, such as F23-71 (P17), Lovrin 6 (P16) and Priboy (P6) to give relatively high scores (Table IX).

The three-way crosses for 1979 Lahoma is shown in Table IX, and they may be evaluated with the same reasoning. Lovrin 6 (P16), F23-71 (P17), and Tam $\mathrm{W}-103$ (P27) have the highest kernel weight, number of seeds per spike, and tiller number, respectively (Table V). A threeway cross between these three cultivars gives the highest score. Tam W-103 (P27) and F23-71 (P17) may also combine with Lovrin 5/T-W-101F6 (P32), high in kernel weight, to give the same score. The combination of Tam W -101(P2) (high in tiller number), Lovrin 6 (P16) (high in kernel weight), and F23-71 (P17) (high in number of seeds per spike) was classified as good, three-way cross (Tab1es IV and IX).

A comparison between Tables VIII and IX shows that results of 1978 Stillwater are in general agreement with the 1979 Lahoma experiment. Lovrin 6 (P16), F23-71 (P17), and Tam $\mathrm{W}-103$ ( P 27 ) contributed in the

[^3]top score crosses in both experiments. Tam W-101 (P2) and Vona (P13)** were also classified as good parents.

Parental stocks giving a high hybrid score do not all need to be from the high yielding group. The combination of Tam W-103 (P27) Lovrin 6 (P16), and F23-71 (P17), which give the highest three-way cross score for both experiments, were from high, medium, and low yield groups, respectively. In a multiple comparison computed separately, these cultivars were significantly different in respect to yield.

$$
\mathrm{D}^{2} \text { Generalized Distance }
$$

The name and origin of cultivars used in 1979 for two locations are shown in Tables IV and V. Four cultivars with late maturity were not used in the Stillwater location. The $\mathrm{D}^{2}$ statistic was used to measure the genetic divergence for the pooled effect of the three yield components. There are other characters contributing to genetic diversity in wheat, such as height, date of maturity, etc.; however, the yield components would give a good estimate of genetic diversity.

The $\Sigma$ used for estimating genetic diversity was a $3 \times 3$ genotypic variance, covariance matrix as follows:

$$
\Sigma=\left(\begin{array}{ccc}
\sigma^{2}{ }_{\mathrm{Gs}} & \sigma_{\mathrm{GsGk}} & { }^{\sigma_{G s G t}} \\
& \sigma_{\mathrm{Gk}}^{2} & \sigma_{\text {GkGt }} \\
& & \sigma_{G t}
\end{array}\right)
$$

where $\sigma_{G s}^{2}, \sigma_{G K}^{2}$, and $\sigma_{G t}^{2}$ are the genotypic variances for number of seeds per spike, kernel weight, and tiller number, respectively. $\sigma_{G s G k}$,
${ }^{* *} \mathrm{P}$ in parentheses refers to parent number in Table IX.
$\sigma_{G s G k}, \sigma_{G s G t}$, and $\sigma_{G k G t}$ are the tenotypic covariances between each pair of components. The value for the genotypic variances and covariances are as follows:

|  | $\sigma_{\text {Gs }}^{2}$ | $\sigma_{\mathrm{Gk}}^{2}$ | $\sigma_{\mathrm{Gt}}^{2}$ | ${ }^{\sigma_{\text {GsGk }}}$ | ${ }^{\sigma_{\text {GsGt }}}$ | ${ }^{\sigma} \mathrm{GkGt}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Stillwater | 21.19 | 34.42 | 51.81 | -6.38 | -13.24 | -27.24 |
| Lahoma | 27.15 | 28.26 | 58.44 | -9.98 | -18.70 | -17.57 |

All of the genotypic covariances are negative, indicating that variations of any two components are in the opposite direction.

The estimate of genetic diversity for each pair of cultivars was computed for 1979 Lahoma; the results are shown in Appendix B (Table XII). The 435 possible distances between the 30 cultivars are arranged in increased order of magnitude with respect to each cultivar. Cultivars in each experiment were grouped into a number of clusters, $D^{2}$ being treated as the squared generalized distance according to the method described by Tocher as cited by Rao (16). Rao (16) stated that there is no formal rule for finding the clusters because a cluster is not a welldefined term. The only criterion appears to be that any two groups belonging to the same cluster should, at least on the average, show a smaller $\mathrm{D}^{2}$ than do those belonging to two different clusters. Based on these estimates of genetic divergence, the 30 cultivars in 1979 experiment could be grouped into nine clusters as follows:

1. Turkey, Triumph 64, Scout 66, Osage, Sturdy, Newton, TX71A562-6, TXR-Line 344-6, Dekalb 589, Pioneer HR940, Hart, and OK77827.
2. Bezostaia 1, Odesskaya 51, Burgas 2, Sodova I, NR173-75, and Russian.
3. Priboy and Lovrin 6/T-W-101F6.
4. Tam W-101.
5. NR72-837.
6. Lovrin 6.
7. F23-71 and NR391-76.
8. Vona, Payne, Tam W-103, and MS Tam 103/TXR 344-6F1.
9. NR31-74.

Tam W-101, NR72-837, Lovrin 6, and NR31-74 made sing1e-cultivar clusters. C1uster I consisted of 12 cultivars, all originating from the U.S.A. except Turkey. Turkey may have been involved as parental stock for developing other members of the group. Cluster 2 consisted of six cultivars originating from the U.S.S.R., Bulgaria, and Austria. Cluster 3 consisted of two cultivars, one originating from the U.S.S.R., and one developed by the cross between two cultivars from the U.S.S.R. and U.S.A. The two cultivars in cluster 7 originated from Romania and Austria. Cluster 8 had four cultivars, all originated from the U.S.A.

The pattern of cultivars in different clusters shows that cultivars originated from the U.S.A. were all grouped into two clusters (1 and 8). This is not in agreement with some of the reports (2, 3, 4) that genetic diversity is not related to geographical distribution. On the other hand, the four cultivars that originated from Austria (NR72-837, NR31-74, NR173-75, and NR391-76) were in four different clusters (2, 5, 7, and 9), and the four cultivars that originated from the U.S.S.R. (Bezostaia I, Odesskaya 51, Russian, and Priboy) were in two different clusters. It may be interpreted that cultivars in one cluster are related to each other by a combination of factors. Somayajulu et al. (20) claimed that pedigree relationship, geographical distribution, and similarity in characters contributing to genetic diversity are three
important factors in this respect.
The intra- and inter-cluster average $\mathrm{D}^{2}$ values for 1979 Lahoma are shown in Table X . The largest distance is between clusters 4 (Tam W101) and 5 (NR72-837). The second and third large $D^{2}$ values are between clusters 3 (Priboy and Lovrin 6/T-W-101F6 and 5 (NR72-837) and 4 (Tam W101) and 7 (F23-71 and NR391-76). Hybrids developed by crossing members of corresponding groups should give promising results. Bhatt (4) stated that in choosing among the genotypes of a cluster, other practical considerations, such as disease reaction, quality and lodging, should be taken into account. Other clusters with high distances are 5 (NR72-837) and 9 (NR31-74), 5 (NR72-837) and 6 (Lovrin 6), and 6 (Lovrin 6) and 8 (Vona, Payne, Tam W-103, and MS Tam 103/TXR 344-6F1). These results are generally in agreement with the discriminant function analysis.

The generalized distance for each pair of cultivars grown at Stillwater in 1979 are shown in Appendix B (Table XIII). Based on these distances, all 26 cultivars were grouped into nine clusters as follows:

1. Sturdy, Burgas 2, TXR-1ine 344-6, and OK77827.
2. Bezostaia 1, Priboy, Sadova 1, Lovrin 6/T-W-101F6, NR173-75, and Russian.
3. Triumph 64.
4. Scout 66, Tam W-101, and Hart.
5. TX71A562-6.
6. Lovrin 6.
7. NR391-76.
8. Vona, Payne, Tam W-103, Osage, Newton, MS Tam 103/TXR344-6F1, and Dekalb 589.
9. Odesskaya 51, and NR31-74.

Four cultivars (Triumph 64, TX71A562-6, Lovrin 6, and NR391-76) made single-genotype clusters. Cluster 1 had four cultivars originating from the U.S.A. and Bulgaria. The six cultivars in cluster 2 originated from the U.S.S.R., Austria, Bulgaria, and the U.S.A. The three cultivars in cluster 4 and seven cultivars in cluster 8 were all originated from the U.S.A. This may indicate the pedigree relationship between the members of each cluster. Cluster 9 had two cultivars originated from the U.S.S.R. and Austria. The distribution of cultivars in different clusters shows that geographical diversity may be one of the factors grouping cultivars in the same cluster.

Comparison of cluster composition between Lahoma and Stillwater shows that some of the cultivars grouped together in both locations. Clusters 1 and 2 in Lahoma and Stillwater have three and four cultivars in common, respectively. The only cultivar which made singlegenotype cluster in both locations was Lovrin 6. Cultivars in cluster 8 Lahoma were all in cluster 8 from Stillwater.

The intra- and inter-cluster average $D^{2}$ for 1979 Stillwater is shown in Table XI. Clusters 3 (Triumph 64) and 7 (NR319-76) had the largest distance followed by clusters 1 (Sturdy, Burgas 2, TXR-1ine 344-6, and 0K77827) and 5 (TX71A562-6). Crosses between members of corresponding clusters should be promising. Other clusters with high distances are 1 (Sturdy, Burgas 2, TXR-1ine 344-6, and OK77827) and 7 (NR391-76), and 3 (Triumph 64) and 5 (TX71A562-6.

## CHAPTER V

## SUMMARY AND CONCLUSIONS

The material for the present study was taken from a cultivar performance trial with 26-30 cultivars. The experiment was conducted at Stillwater, Oklahoma, during 1976-77 and at two locations--Stillwater and Lahoma, Oklahoma--during 1977-1978 and 1978-79. A11 of the experiments were laid out in a randomized complete block design with three replications during 1976-77 and 1977-78, and four replications during 1978-79. Cultivars used for each experiment were different in different years. Four cultivars were eliminated from the Stillwater location during 1978-79 because of later maturity.

The characters chosen for study were yield and yield components, viz., number of tillers per unit area, number of seeds per spike, and kernel weight. Before using any of the techniques, it was necessary to determine if the cultivars differed significantly among themselves with respect to yield components. This was tested by analysis of variance for each component. The results of this test showed that cultivars differ significantly with respect to each component. Two methods of choosing parents for hybridization aiming at yield improvement were discussed. In the first approach, a discriminant function analysis, as developed by Fisher, was applied. To employ discriminant analysis, the group of cultivars in each experiment was partitioned into high, medium, and low-yleld groups based on observed mean yields over
replication. A discriminant function was computed for each experiment and its significance was tested by Wilks' likelihood ratio criterion.

Two discriminant functions corresponding to 1978 Stillwater and 1979 Lahoma were significant. The discriminant weights (a-values) were determined and the resultant discriminant functions for 1978 Stillwater and 1979 Lahoma were

$$
\begin{aligned}
& \text { Score }=Z=0.0292(\text { TLR })+0.0640(\text { seeds } / \text { spike })+0.0546(\text { Kwt }) \\
& \text { Score }=Z=0.0165(\text { TLR })+0.06104 \text { (seeds/spike) }+0.0239(\text { Kwt })
\end{aligned}
$$

respectively. The order of contribution of yield components in both experiments were seeds per spike, kernel weight, and tiller number. For predicting the scores of all of the two-way and three-way crosses among the cultivars, the discriminant function was app1ied to the highest component values of either parents. Since it was assumed that the gene action is additive, i.e., there is no dominance and no epistasis, the discriminant function should, in fact, be applied to the average of component values in the parental cultivars. Thus, it is also assumed that by selecting in the further generations the high values of yield components would be recovered. Cultivars Involved in top two-way crosses were also involved in top three-way crosses in both locations. These genotypes were more often high in number of seeds per spike and/or kerne1 weight.

Besides the distinct differences between the two locations, the results of 1978 Stillwater were in general agreement with the 1979 Lahoma results. Cultivars classified as good parents in two-way and three-way crosses were from different yielding groups (high, medium,
low), indicating that parental materials chosen on only one single complex character such as yield may not necessarily provide transgressive segregates for yield potential. The reliability of this procedure may be determined by making crosses predicted to be promising.

The second method applied was Mahhalanobis' generalized distance known to be effective in measuring the degree of divergence for individual character or pooled effect of several characters. Genetic diversity measured by this approach was based on three characters (yield components). There are other characters contributing to genetic diversity in wheat, such as height, date of heading, date of maturity, etc.; however, the yield components would give a good estimate of genetic diversity. $\mathrm{D}^{2}$ distance, which is closely related to discriminant function, was used only for 1979 Stillwater and 1979 Lahoma.

The amount of divergence based on the yield components was computed for each genotype, and the closely related cultivars as expressed by their distance were grouped together according to the method described by Tocher. The analysis of inter-cluster and intra-cluster average $D^{2}$ values showed that the cultivars in each location could be grouped into nine clusters. Four cultivars classified as mone divergent in each location made single-cultivar clusters. Lovrin 6 was the only single-cultivar cluster in both locations. A comparison of cluster composition between Lahoma and Stillwater showed that some genotypes grouped together in both locations.

Cultivars grouped together more often originated from the same ecological area, indicating that geographical distribution could be one of the factors influencing genetic diversity. A close study of other cultivars grouped together indicated that pedigree relationship and
similarity in characters contributing to genetic diversity may be other factors influencing diversity.

The results of 1979 Lahoma were in general agreement with the discriminant function analysis. A study of genotypic covariances for yield components showed that all of the covariances were negative. This indicates that yield components are not mutually independent, and that an increase in one could be accompanied by a decrease in another.

TABLE I

AVERAGE YIELD AND YIELD COMPONENTS FOR ENTRIES GROWN IN 1977, STILLWATER

| Parent No. | Entry | $\begin{gathered} \text { Tiller }{ }^{2} \text { ) } \end{gathered}$ | Seeds/ <br> Spike | $\begin{gathered} \text { Kerne1 } \\ \text { Weight } \\ (\mathrm{gm} / 1000 \text { seeds }) \end{gathered}$ | $\begin{aligned} & \text { Yield* } \\ & (\mathrm{gm} / \mathrm{plot}) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Osage | 52 | 35 | 37 | 493.33 |
| 2 | Tam W-101 | 60 | 29 | 41 | 558.33 |
| 3 | Centurk | 68 | 38 | 31 | 476.67 |
| 4 | Bezostaia 1 | 49 | 39 | 43 | 566.67 |
| 5 | F26-70 | 37 | 46 | 43 | 525.00 |
| 6 | Odesskaya 51 | 54 | 38 | 41 | 520.00 |
| 7 | Turkey | 63 | 34 | 34 | 403.33 |
| 8 | Scout 66 | 62 | 31 | 38 | 426.67 |
| 9 | Triumph 64 | 62 | 32 | 39 | 471.67 |
| 10 | Lovrin 6 | 41 | 35 | 54 | 491.67 |
| 11 | Burgas 2 | 37 | 46 | 42 | 536.67 |
| 12 | Dwarf Bezostaia | 45 | 44 | 36 | 545.00 |
| 13 | Newton | 66 | 43 | 31 | 543.33 |
| 14 | Trison | 54 | 31 | 40 | 521.67 |
| 15 | Vona | 68 | 43 | 32 | 628.33 |
| 16 | David | 51 | 43 | 31 | 435.00 |
| 17 | NR31-74 | 53 | 43 | 36 | 601.67 |
| 18 | Predgornia | 34 | 44 | 47 | 570.00 |
| 19 | Payne | 53 | 41 | 31 | 473.33 |
| 20 | TX69A 330-1 | 73 | 38 | 32 | 535.00 |
| 21 | Tam W-103 | 84 | 38 | 31 | 586.67 |
| 22 | David 10 | 55 | 40 | 34 | 521.67 |
| 23 | NR 173-75 | 43 | 35 | 44 | 620.00 |
| 24 | F23-71 | 40 | 53 | 41 | 433.33 |
| 25 | Sturdy | 54 | 39 | 33 | 495.00 |
| 26 | OK711248-1 | 52 | 39 | 37 | 485.00 |
| 27 | Tam W-102 | 48 | 58 | 29 | 491.67 |
| 28 | Oasis | 52 | 36 | 39 | 545.00 |
| 29 | TRS 237 | 43 | 29 | 42 | 456.67 |
| 30 | Blueboy | 47 | 42 | 35 | 553.33 |

* High group included parents with yields greater than 540 grams/plot, medium group between 495 and 540 grams/plot, and low group less than 490 grams/plot.

TABLE II

AVERAGE YIELD AND YIELD COMPONENTS FOR ENTRIES GROWN IN 1978, LAHOMA

| Parent No. | Ent ry | $\underset{\left(\mathrm{no} . / 900 \mathrm{~cm}^{2}\right)}{\substack{\text { Tiller } \\ \hline}}$ | Seeds/ Spike | $\begin{gathered} \text { Kernel } \\ \text { Weight } \\ (\mathrm{gm} / 1000 \text { seeds }) \end{gathered}$ | $\begin{aligned} & \text { Yield* } \\ & (\mathrm{gm} / \mathrm{plot}) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Osage | 39 | 29 | 32 | 465.00 |
| 2 | Tam W-101 | 48 | 21 | 39 | 500.00 |
| 3 | Sturdy | 32 | 32 | 35 | 433.33 |
| 4 | Bezostaia 1 | 26 | 32 | 37 | 450.00 |
| 5 | Odesskaya | 43 | 29 | 36 | 515.00 |
| 6 | Priboy | 34 | 29 | 38 | 490.00 |
| 7 | Turkey | 44 | 27 | 30 | 325.00 |
| 8 | Scout 66 | 48 | 25 | 35 | 405.00 |
| 9 | Triumph 64 | 45 | 22 | 38 | 448.33 |
| 10 | Predgornia | 25 | 35 | 36 | 398.33 |
| 11 | Burgas 2 | 28 | 35 | 34 | 495.00 |
| 12 | Sadova I | 36 | 26 | 39 | 523.33 |
| 13 | Vona | 44 | 33 | 28 | 478.33 |
| 14 | Newton | 35 | 34 | 30 | 450.00 |
| 15 | Payne | 38 | 32 | 29 | 466.67 |
| 16 | Lovrin 6 | 30 | 22 | 48 | 386.67 |
| 17 | F23-71 | 29 | 42 | 33 | 341.67 |
| 18 | Blueboy | 38 | 35 | 32 | 450.00 |
| 19 | Plainsman V | 49 | 25 | 32 | 470.00 |
| 20 | OK711248-176 | 45 | 26 | 30 | 435.00 |
| 21 | Tam W-102 | 29 | 41 | 22 | 341.67 |
| 22 | BPS | 41 | 27 | 30 | 371.67 |
| 23 | TRS 237 | 30 | 27 | 35 | 345.00 |
| 24 | WA5829 | 40 | 26 | 17 | 110.00 |
| 25 | OK72271 | 46 | 28 | 33 | 463.33 |
| 26 | TX71A562-6 | 37 | 32 | 28 | 433.33 |
| 27 | Tam W-103 | 42 | 28 | 26 | 425.00 |
| 28 | NR31-74 | 33 | 35 | 29 | 430.00 |
| 29 | NR173-75 | 31 | 32 | 37 | 468.33 |
| 30 | David | 39 | 30 | 28 | 323.33 |

[^4]TABLE III
AVERAGE YIELD AND YIELD COMPONENTS FOR ENTRIES GROWN IN 1978, STILLWATER

| Parent No. | Entry | $\begin{gathered} \text { Tiller } \\ \text { (No. } / 900 \mathrm{~cm}^{2} \text { ) } \end{gathered}$ | Seeds/ Spike | $\begin{gathered} \text { Kerne1 } \\ \text { Weight } \\ (\mathrm{gm} / 1000 \text { seeds }) \end{gathered}$ | $\begin{aligned} & \text { Yield* } \\ & \text { (gm/plot) } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Osage | 49 | 28 | 30 | 278.33 |
| 2 | Tam W-101 | 47 | 24 | 37 | 311.67 |
| 3 | Sturdy | 37 | 31 | 30 | 273.33 |
| 4 | Bezostaia 1 | 29 | 31 | 35 | 230.00 |
| 5 | Odesskaya | 37 | 32 | 37 | 283.33 |
| 6 | Priboy | 40 | 33 | 38 | 293.33 |
| 7 | Turkey | 40 | 38 | 29 | 220.00 |
| 8 | Scout 66 | 44 | 27 | 33 | 255.00 |
| 9 | Triumph 64 | 44 | 27 | 35 | 283.33 |
| 10 | Predgornia | 29 | 31 | 36 | 231.67 |
| 11 | Burgas 2 | 32 | 39 | 32 | 306.67 |
| 12 | Sadova I | 30 | 32 | 38 | 256.67 |
| 13 | Vona | 40 | 38 | 29 | 308.33 |
| 14 | Newton | 42 | 34 | 32 | 305.00 |
| 15 | Payne | 37 | 33 | 27 | 291.67 |
| 16 | Lovrin 6 | 33 | 27 | 46 | 291.67 |
| 17 | F23-71 | 29 | 43 | 31 | 301.67 |
| 18 | Blueboy | 33 | 35 | 32 | 273.33 |
| 19 | Plainsman V | 48 | 27 | 29 | 273.33 |
| 20 | OK711248-176 | 44 | 30 | 31 | 313.33 |
| 21 | Tam W-102 | 36 | 39 | 25 | 286.67 |
| 22 | BPS | 45 | 24 | 31 | 221.67 |
| 23 | TRS237 | 26 | 31 | 30 | 205.00 |
| 24 | WA5829 | 38 | 38 | 22 | 233.33 |
| 25 | OK72271 | 44 | 30 | 33 | 268.33 |
| 26 | TX71A562-6 | 40 | 39 | 30 | 355.00 |
| 27 | Tam W-103 | 56 | 29 | 29 | 246.67 |
| 28 | NR31-74 | 34 | 34 | 20 | 245.00 |
| 29 | NR173-75 | 34 | 32 | 32 | 218.33 |
| 30 | David | 38 | 31 | 28 | 283.33 |

[^5]TABLE IV
ORIGIN AVERAGE YIELD AND YIELD CONPONENTS
FOR ENTRIES GROWN IN 1979, LAHOMA

| Parent No. | Entry | Origin | $\begin{aligned} & \text { Tiller } \\ & \text { (No. } \\ & \left.900 \mathrm{~cm}^{2}\right) \end{aligned}$ | $\begin{aligned} & \text { Seeds } \\ & \text { per } \\ & \text { Spike } \end{aligned}$ | ```Kernel Weight (gm/ 1000 seeds)``` | Yield* (gm/ plot) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | Turkey | Turkey | 70 | 30 | 30 | 418.75 |
| 9 | Triumph 64 | USA (OK) | 61 | 24 | 37 | 452.50 |
| 8 | Scout 66 | USA (NB) | 66 | 25 | 36 | 475.75 |
| 4 | Bezostaia 1 | USSR | 47 | 34 | 40 | 473.75 |
| 5 | Odesskaya 51 | USSR | 55 | 31 | 41 | 462.60 |
| 6 | Priboy | USSR | 57 | 30 | 45 | 457.50 |
| 1 | Osage | USA (OK) | 63 | 31 | 33 | 488.75 |
| 3 | Sturdy | USA (TX) | 59 | 34 | 32 | 505.00 |
| 2 | Tam W-101 | USA (TX) | 73 | 23 | 43 | 665.00 |
| 11 | Burgas 2 | Bulgaria | 54 | 32 | 38 | 571.25 |
| 12 | Sadovo 1 | Bulgaria | 48 | 29 | 44 | 498.75 |
| 31 | NR 72-837 | Austria | 51 | 38 | 29 | 480.00 |
| 13 | Vona | USA | 67 | 36 | 28 | 636.25 |
| 14 | Newton | USA (KS) | 58 | 33 | 35 | 545.00 |
| 15 | Payne | USA (OK | 72 | 30 | 32 | 600.25 |
| 16 | Lovrin 6 | Romania | 50 | 27 | 47 | 492.50 |
| 17 | F23-71 | Romania | 44 | 46 | 36 | 437.50 |
| 32 | Lovrin 6/T-W-101F6 | Rom. /USA | 62 | 25 | 47 | 473.75 |
| 26 | TX71A562-6 | USA (TX) | 60 | 34 | 33 | 608.75 |
| 27 | TAM W-103 | USA (TX) | 75 | 30 | 30 | 543.75 |
| 33 | $\begin{aligned} & \text { MS TAM 103/ } \\ & \text { TXR344-6 F1 } \end{aligned}$ | USA | 67 | 34 | 34 | 576.25 |
| 34 | TXR-Line 344-6 | USA (TX) | 63 | 30 | 32 | 501.25 |
| 35 | Dekalb 589 | USA | 58 | 24 | 39 | 437.50 |
| 36 | Pioneer HR940 | USA | 70 | 25 | 36 | 438.75 |
| 37 | Hart | USA (MO) | 65 | 25 | 37 | 453.75 |
| 28 | NR 31/74 | Austria | 62 | 39 | 34 | 472.50 |
| 29 | NR173/75 | Austria | 51 | 34 | 39 | 497.50 |
| 38 | NR $391 / 76$ | Austria | 49 | 40 | 38 | 501.25 |
| 39 | Russian | USSR | 57 | 32 | 39 | 441.25 |
| 40 | OK77827 | USA (OK) | 62 | 32 | 28 | 415.00 |

[^6]TABLE V
ORIGIN, AVERAGE YIELD, AND YIELD COMPONENTS
FOR ENTRIES GROWN IN 1979, STILLWATER

|  |  |  |  | Tiller |
| :---: | :--- | :--- | :---: | :---: | :---: | ---: |
| Parent |  |  |  |  |
| No. |  |  |  |  |

* High group includes parents with yields greater than 715 grams/plot, medium group between 625 and 715 grams/plot, and low group less than 625 grams/plot.

TABLE VI

MEAN SQUARES FOR TILLER NUMBER, SEEDS PER SPIKE, KERNEL WEIGHT AND YIELD FOR 1977, STILLWATER AND 1978 AND 1979, LAHOMA AND STILLWATER

| Year | Location | TLR | Seeds/Spike | Kwt | Yield |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 1977 | Stillwater | $395.60 * *$ | $129.49 * *$ | $101.12 * *$ | $19714.80 * *$ |
| 1978 | Lahoma | $151.14 * *$ | $76.19 * *$ | $98.02 * *$ | $19376.25 * *$ |
|  | Stillwater | $149.29 * *$ | $65.28 * *$ | $61.80 * *$ | $3716.87 * *$ |
|  | Lahoma | $537.90 * *$ | $684.37 * *$ | $698.34 * *$ | $16879.16 * *$ |
| 1979 | Stillwater | $497.33 * *$ | $558.73 * *$ | $842.50 * *$ | $32453.24 * *$ |

** Significant at the 0.01 level of probability.

TABLE VII

THE CHARACTERISTIC ROOTS, CHARACTERISTIC VECTORS AND V VALUES FOR ALL YEARS AND LOCATIONS

| Year and Location | ```Characteristic root (\lambda)``` | Characteristic Vectors (a-values) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{gathered} \text { Tiller No. } \\ \left(a_{1}\right) \end{gathered}$ | Seeds/ <br> Spike <br> ( $\mathrm{a}_{2}$ ) | Kerne1 <br> Weight ( $\mathrm{a}_{3}$ ) | V |
| 1977 |  |  |  |  |  |
| Stillwater | . 0310 | 0.0175 | 0.0342 | 0.0486 | 7.67 |
| 1978 |  |  |  |  |  |
| Stillwater | . 8159 | 0.0292 | 0.0640 | 0.0546 | 16.406* |
| 1978 |  |  |  |  |  |
| Lahoma | . 2631 | 0.0371 | 0.0366 | 0.0378 | 6.318 |
| 1979 |  |  |  |  |  |
| Stil1water | 0.148 | 0.0056 | 0.0086 | -0.0054 | 4.483 |
| 1979 |  |  |  |  |  |
| Lahoma | . 6739 | 0.0165 | 0.06104 | 0.0238 | 14.326** |
| * Significant at the .025 level of probability. **Significant at the .05 level of probability. |  |  |  |  |  |

TABLE VIII
THE 30 TOP TWO-WAY AND THREE-WAY CROSS SCORES FOR 1978 STILLWATER

| Two-Way Crosses |  |  |  |  | Three-Way Crosses |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rank | Par | ts* | Index Score | Rank |  | arent |  | Index Score |
| 1 | 16 | 17 | 6.239 | 1 | 16 | 17 | 27 | 6.906 |
| 2 | 16 | 26 | 6.186 | 2 | 1 | 16 | 17 | 6.703 |
| 3 | 13 | 16 | 6.150 | 3 | 16 | 19 | 17 | 6.674 |
| 4 | 2 | 17 | 6.122 | 4 | 11 | 16 | 27 | 6.650 |
| 5 | 16 | 21 | 6.081 | 5 | 16 | 21 | 27 | 6.650 |
| 6 | 16 | 24 | 6.070 | 6 | 16 | 26 | 27 | 6.650 |
| 7 | 16 | 27 | 6.064 | 7 | 2 | 16 | 17 | 6.645 |
| 8 | 17 | 27 | 6.010 | 8 | 16 | 22 | 17 | 6.587 |
| 9 | 11 | 16 | 6.002 | 9 | 13 | 16 | 27 | 6.586 |
| 10 | 6 | 17 | 5.983 | 10 | 16 | 24 | 27 | 6.586 |
| 11 | 14 | 16 | 5.953 | 11 | 8 | 16 | 18 | 6.558 |
| 12 | 9 | 17 | 5.924 | 12 | 9 | 16 | 17 | 6.558 |
| 13 | 2 | 11 | 5.894 | 13 | 16 | 20 | 17 | 6.558 |
| 14 | 2 | 21 | 5.894 | 14 | 16 | 25 | 17 | 6.558 |
| 15 | 2 | 26 | 5.894 | 15 | 14 | 116 | 17 | 6.500 |
| 16 | 6 | 16 | 5.880 | 16 | 6 | 17 | 27 | 6.466 |
| 17 | 6 | 27 | 5.878 | 17 | 12 | 17 | 27 | 6.466 |
| 18 | 11 | 27 | 5.860 | 18 | 1 | 11 | 16 | 6.447 |
| 19 | 1 | 16 | 5.849 | 19 | 1 | 26 | 16 | 6.447 |
| 20 | 1 | 17 | 5.843 | 20 | 6 | 16 | 17 | 6.442 |
| 21 | 2 | 13 | 5.843 | 21 | 7 | 16 | 17 | 6.442 |
| 22 | 2 | 24 | 5.830 | 22 | 13 | 17 | 16 | 6.442 |
| 23 | 5 | 17 | 5.830 | 23 | 17 | 26 | 16 | 6.442 |
| 24 | 8 | 17 | 5.826 | 24 | 11 | 19 | 16 | 6.418 |
| 25 | 12 | 27 | 5.802 | 25 | 19 | 21 | 16 | 6.418 |
| 26 | 16 | 20 | 5.770 | 26 | 19 | 26 | 16 | 6.418 |
| 27 | 16 | 25 | 5.762 | 27 | 2 | 27 | 17 | 6.411 |
| 28 | 17 | 19 | 5.762 | 28 | 5 | 17 | 27 | 6.411 |
| 29 | 17 | 25 | 5.746 | 29 | 16 | 18 | 27 | 6.394 |
| 30 | 15 | 16 | 5.746 | 30 | 2 | 11 | 16 | 6.389 |

* Numbers used as parents represent the entry number.

TABLE IX

THE 30 TOP TWO-WAY AND THREE-WAY CROSS
SCORES FOR 1979 LAHOMA

|  | Two-Way Crosses |  |  |  | Three-Way Crosses |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rank | Parents* |  | $\frac{\text { Index Score }}{5.012}$ | Rank 1 | Parents* |  |  | Index Score <br> 5.241 |
| 1 | 2 | 17 |  |  | 16 | 17 | 27 |  |
| 2 | 17 | 32 | 4.975 | 2 | 17 | 32 | 27 | 5.241 |
| 3 | 2 | 38 | 4.817 | 3 | 2 | 16 | 17 | 5.200 |
| 4 | 2 | 28 | 4.785 | 4 | 2 | 32 | 17 | 5.200 |
| 5 | 32 | 38 | 4.780 | 5 | 15 | 16 | 17 | 5.180 |
| 6 | 6 | 17 | 4.778 | 6 | 15 | 32 | 17 | 5.180 |
| 7 | 13 | 16 | 4.752 | 7 | 6 | 17 | 27 | 5.147 |
| 8 | 13 | 32 | 4.752 | 8 | 7 | 16 | 17 | 5.139 |
| 9 | 2 | 31 | 4.752 | 9 | 7 | 32 | 17 | 5.139 |
| 10 | 16 | 28 | 4.747 | 10 | 16 | 36 | 17 | 5.139 |
| 11 | 32 | 28 | 4.747 | 11 | 32 | 36 | 17 | 5.139 |
| 12 | 16 | 17 | 4.729 | 12 | 6 | 2 | 17 | 5.106 |
| 13 | 17 | 27 | 4.724 | 13 | 12 | 17 | 27 | 5.100 |
| 14 | 16 | 27 | 4.721 | 14 | 6 | 15 | 17 | 5.086 |
| 15 | 32 | 27 | 4.721 | 15 | 13 | 16 | 17 | 5.077 |
| 16 | 31 | 32 | 4.715 | 16 | 13 | 32 | 17 | 5.077 |
| 17 | 2 | 13 | 4.687 | 17 | 16 | 33 | 17 | 5.077 |
| 18 | 16 | 33 | 4.687 | 18 | 32 | 33 | 17 | 5.077 |
| 19 | 32 | 33 | 4.687 | 19 | 2 | 12 | 17 | 5.059 |
| 20 | 15 | 17 | 4.663 | 20 | 8 | 16 | 17 | 5.057 |
| 21 | 15 | 16 | 4.660 | 21 | 8 | 32 | 17 | 5.057 |
| 22 | 15 | 32 | 4.660 | 22 | 2 | 27 | 17 | 5.053 |
| 23 | 6 | 13 | 4.658 | 23 | 16 | 38 | 27 | 5.046 |
| 24 | 6 | 28 | 4.653 | 24 | 32 | 38 | 27 | 5.046 |
| 25 | 6 | 27 | 4.627 | 25 | 7 | 6 | 17 | 5.045 |
| 26 | 27 | 38 | 4.623 | 26 | 6 | 36 | 17 | 5.045 |
| 27 | 4 | 2 | 4.622 | 27 | 12 | 15 | 17 | 5.039 |
| 28 | 3 | 2 | 4.622 | 28 | 16 | 37 | 17 | 5.036 |
| 29 | 2 | 26 | 4.622 | 29 | 32 | 37 | 17 | 5.036 |
| 30 | 2 | 33 | 4.622 | 30 | 16 | 28 | 27 | 5.140 |

* Numbers used as parents represent the entry number.

TABLE X
INTRA- AND INTER-CLUSTER AVERAGE ${ }^{2}$ IN LAHOMA 1979

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 2.451 | 4.304 | 9.634 | 11.484 | 7.474 | 7.700 | 12.138 | 5.491 | 9.563 |  |
| 2 |  | 1.355 | 6.152 | 13.054 | 7.310 | 2.516 | 6.182 | 8.765 | 8.650 |  |
| 3 |  |  |  |  |  |  |  |  |  |  |

TABLE XI
INTRA- AND INTER-CLUSTER AVERAGE D ${ }^{2}$ IN STILLWATER 1979

|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 6.863 | 4.587 | 8.445 | 4.053 | 28.626 | 13.688 | 24.150 | 12.904 |  |
| 2 |  | 1.913 | 5.992 | 6.223 | 7.340 | 12.971 | 3.942 | 8.312 | 11.342 |  |
| 3 |  |  | 2.165 | 9.231 | 7.574 | 14.602 | 6.616 | 18.241 | 6.210 |  |
| 4 |  |  |  | 1.417 | 16.544 | 23.322 | 7.192 | 8.375 | 6.661 |  |
| 5 |  |  |  |  | 2.600 | 24.978 | 15.281 | 26.845 | 21.856 |  |
| 6 |  |  |  |  |  | 0.000 | 2.298 | 12.160 | 15.545 |  |
| 7 |  |  |  |  |  |  | 1.007 | 4.316 | 6.313 |  |
| 8 |  |  |  |  |  |  |  | 0.000 | 13.910 |  |
| 9 |  |  |  |  |  |  |  |  |  | 0.000 |

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APPENDIX A

CALCULATIONS RELATED TO DISCRIMINANT FUNCTION

## 1. Discriminant Criterion

The score on a linear combination of PX's for an individual of group $\mathrm{g}(\mathrm{g}=1,2$, . . . G) may be written as

$$
z_{g}=a_{1} x_{1 g}+a_{2} x_{2 g}+\cdots+a_{p} X_{p g}
$$

The values of the $a^{\prime} s$ are chosen such that $\lambda=\frac{S S_{a}}{S S_{w}}$ is maximized, where $\mathrm{SS}_{\mathrm{a}}$ and $\mathrm{SS}_{\mathrm{w}}$ are the sum of squares among and within groups, respectively. The maximum values of $\lambda$ are given by the largest root of $\mathrm{W}^{-1} \mathrm{~A}$ where W and A are the sum of squares and cross products matrices within and among groups, respectively.

## 2. Test of Discriminant Criterion

The characteristic criterion $\lambda$ may be tested by Wilks' likelihood ratio criterion. Wilks' $A$ is expressed as

$$
\frac{1}{\Lambda}=\frac{|W+A|}{|W|}
$$

This can be expressed as

$$
\frac{1}{\Lambda}=\left|\mathrm{W}^{-1}(\mathrm{~W}+\mathrm{A})\right|=\left|\mathrm{I}+\mathrm{W}^{-1} \mathrm{~A}\right|
$$

Since the determinant of a square matrix is equal to the product of its characteristic roots, and $\left(W^{-1} A+I\right)$ has $\left(1+\lambda_{1}\right)$ as its characteristic roots, then

$$
\frac{1}{\Lambda}=\left(1+\lambda_{1}\right)\left(1+\lambda_{2}\right) \cdot \ldots\left(1+\lambda_{r}\right)
$$

in which $r$ is the number of nonzero characteristic roots of $W^{-1} A$.

Bartlett showed that

$$
V=\left[n-1-\left(\frac{P+G}{2}\right)\right] 1_{n} \frac{1}{\Lambda}
$$

where $n=$ number of observations
$P=$ number of variables
$G=$ number of groups
is distributed approximately as chi-square with $P(G-1)$ degrees of freedom for large $n$.
3. Characteristic Vectors (a-values)

The significant $\lambda$ 's may be used to compute the characteristic vectors (discriminant weights) by solving the following system of equations:

$$
\left(W^{-1} A-\lambda I\right) \underset{\sim}{a}=0
$$

where $\underset{\sim}{a}$ is a column vector with three elements $\left(a_{1}, a_{2}, a_{3}\right)$. The score is calculated by the following formula:

$$
Z=\text { score }=a_{1} X_{1}+a_{2} X_{2}+a_{3} X_{3}
$$

APPENDIX B
$D^{2}$ VALUES BETWEEN EACH PAIR OF CULTIVARS

TABLE XII

## VALUES OF $\mathrm{D}^{2 *}$ based on the CHARACTERS ARRANGED IN INCREASING ORDER OF MAGNITUDE WITH RESPECT <br> TO EACH VARIETY - 1979 LAHOMA

| Parent Number | 1 |  | 2 |  | 3 |  | 4 |  | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | 0.861 | 23 | 0.299 | 25 | 0.077 | 27 | 0.721 | 29 | 0.196 |
| 22 | 0.949 | 3 | 1.284 | 24 | 0.609 | 11 | 0.835 | 27 | 0.926 |
| 20 | 1.135 | 25 | 1.643 | 22 | 0.966 | 10 | 1.019 | 10 | 1.207 |
| 15 | 1.430 | 22 | 1.978 | 2 | 1.284 | 5 | 2.576 | 6 | 1.214 |
| 24 | 1.533 | 7 | 2.971 | 7 | 1.238 | 29 | 2.626 | 14 | 1.436 |
| 3 | 1.858 | 10 | 3.091 | 1 | 1.858 | 14 | 2.829 | 16 | 1.731 |
| 19 | 1.913 | 24 | 3.606 | 23 | 1.990 | 16 | 3.064 | 11 | 2.234 |
| 13 | 1.985 | 30 | 3.927 | 14 | 2.270 | 8 | 3.607 | 19 | 2.304 |
| 25 | 2.130 | 14 | 3.945 | 19 | 2.774 | 19 | 3.762 | 4 | 2.576 |
| 8 | 2.243 | 8 | 4.024 | 10 | 2.796 | 23 | 4.357 | 25 | 2.746 |
| 14 | 2.394 | 11 | 4.151 | 29 | 2.936 | 28 | 4.531 | 7 | 2.925 |
| 30 | 2.737 | 19 | 4.765 | 8 | 3.158 | 7 | 4.882 | 28 | 3.213 |
| 21 | 3.633 | 1 | 4.769 | 5 | 3.585 | 12 | 5.123 | 3 | 3.585 |
| 29 | 4.317 | 29 | 5.118 | 15 | 3.795 | 22 | 5.270 | 8 | 3.775 |
| 10 | 4.603 | 27 | 5.482 | 30 | 4.264 | 2 | 5.551 | 22 | 3.939 |
| 2 | 4.768 | 4 | 5.552 | 20 | 4.318 | 25 | 6.164 | 18 | 4.123 |
| 5 | 6.011 | 5 | 5.636 | 27 | 4.762 | 3 | 6.682 | 24 | 4.282 |
| 27 | 6.462 | 16 | 6.368 | 11 | 5.433 | 6 | 6.750 | 21 | 4.814 |
| 23 | 6.635 | 12 | 8.444 | 16 | 6.140 | 30 | 7.344 | 23 | 4.885 |
| 26 | 6.901 | 15 | 9.117 | 13 | 6.310 | 17 | 7.697 | 2 | 5.635 |
| 12 | 9.116 | 20 | 9.609 | 21 | 6.418 | 24 | 9.773 | 15 | 5.662 |
| 6 | 9.416 | 6 | 10.423 | 6 | 6.505 | 1 | 9.842 | 26 | 5.942 |
| 9 | 9.589 | 13 | 10.983 | 4 | 6.682 | 13 | 11.035 | 1 | 6.011 |
| 4 | 9.842 | 21 | 12.484 | 9 | 7.647 | 21 | 11.736 | 13 | 6.782 |
| 28 | 10.336 | 18 | 13.099 | 18 | 8.171 | 26 | 11.862 | 9 | 7.980 |
| 11 | 10.538 | 9 | 14.219 | 12 | 10.428 | 18 | 12.464 | 17 | 8.25 |
| 16 | 12.118 | 28 | 14.258 | 26 | 10.651 | 15 | 12.616 | 20 | 8.260 |
| 18 | 12.269 | 26 | 17.017 | 28 | 11.078 | 20 | 15.299 | 30 | 8.756 |
| 17 | 16.208 | 17 | 21.594 | 17 | 18.531 | 9 | 19.170 | 12 | 10.544 |

* $D^{2}$ is a measure of genetic diversity, as $D^{2}$ increases, the genetic diversity between parents increases.

TABLE XII (Continued)

| Parent <br> Number | 6 |  | 7 |  | 8 |  | 9 |  | 10 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | 18 | 1.212 | 22 | 0.185 | 19 | 0.371 | 18 | 2.264 | 27 |
| 5 | 1.214 | 19 | 0.404 | 7 | 0.602 | 24 | 4.568 | 14 | 0.364 |
| 29 | 1.951 | 14 | 0.466 | 14 | 0.604 | 6 | 4.901 | 29 | 0.809 |
| 16 | 2.750 | 8 | 0.602 | 22 | 0.783 | 15 | 5.197 | 4 | 1.019 |
| 27 | 3.986 | 1 | 0.861 | 10 | 1.261 | 21 | 6.061 | 19 | 1.110 |
| 28 | 4.758 | 3 | 1.238 | 30 | 1.312 | 25 | 6.633 | 5 | 1.207 |
| 14 | 4.622 | 25 | 1.272 | 27 | 2.130 | 20 | 6.942 | 8 | 1.261 |
| 10 | 4.833 | 10 | 1.492 | 1 | 2.243 | 3 | 7.647 | 7 | 1.492 |
| 9 | 4.901 | 29 | 1.750 | 29 | 2.390 | 5 | 7.980 | 11 | 1.575 |
| 21 | 4.926 | 24 | 1.913 | 12 | 2.861 | 29 | 8.320 | 22 | 1.826 |
|  |  |  |  |  |  |  |  |  |  |
| 25 | 5.179 | 30 | 2.074 | 13 | 3.035 | 1 | 9.590 | 25 | 2.476 |
| 11 | 5.491 | 13 | 2.595 | 3 | 3.158 | 7 | 10.329 | 23 | 2.793 |
| 19 | 5.764 | 15 | 2.666 | 25 | 3.253 | 26 | 10.501 | 3 | 2.796 |
| 24 | 5.913 | 27 | 2.705 | 4 | 3.607 | 14 | 10.766 | 2 | 3.091 |
| 26 | 6.065 | 5 | 2.925 | 5 | 3.775 | 16 | 11.203 | 16 | 3.290 |
| 3 | 6.505 | 2 | 2.971 | 2 | 4.024 | 19 | 11.634 | 30 | 4.173 |
| 7 | 6.538 | 20 | 3.258 | 24 | 4.649 | 22 | 11.715 | 28 | 4.204 |
| 15 | 6.592 | 23 | 3.430 | 23 | 4.881 | 13 | 11.957 | 1 | 4.603 |
| 4 | 6.750 | 21 | 3.944 | 15 | 4.962 | 10 | 13.062 | 24 | 4.683 |
| 22 | 8.214 | 4 | 4.882 | 28 | 5.456 | 29 | 13.842 | 6 | 4.833 |
| 8 | 8.559 | 11 | 5.468 | 11 | 5.468 | 2 | 14.219 | 12 | 4.929 |
| 23 | 9.316 | 12 | 5.912 | 21 | 5.644 | 23 | 14.549 | 13 | 6.153 |
| 1 | 9.416 | 26 | 6.275 | 20 | 5.672 | 8 | 15.335 | 15 | 6.703 |
| 13 | 9.465 | 28 | 6.537 | 26 | 6.871 | 11 | 15.950 | 21 | 6.787 |
| 20 | 9.864 | 6 | 6.538 | 16 | 8.463 | 28 | 16.041 | 26 | 8.023 |
| 2 | 10.423 | 16 | 7.375 | 6 | 8.559 | 4 | 19.170 | 17 | 8.470 |
| 17 | 10.672 | 18 | 10.231 | 17 | 8.985 | 30 | 20.821 | 20 | 8.528 |
| 30 | 15.492 | 9 | 10.329 | 18 | 13.940 | 17 | 25.649 | 18 | 9.337 |
| 12 | 18.544 | 17 | 11.607 | 9 | 15.335 | 12 | 31.179 | 9 | 13.062 |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

TABLE XII (Continued)

| Parent Number | 11 |  | 12 |  | 13 |  | 14 |  | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | 0.835 | 30 | 2.723 | 21 | 1.510 | 19 | 0.136 | 20 | 0.362 |
| 16 | 1.068 | 8 | 2.861 | 15 | 1.616 | 7 | 0.466 | 21 | 0.907 |
| 10 | 1.575 | 10 | 4.929 | 20 | 1.900 | 10 | 0.548 | 1 | 1.430 |
| 27 | 1.690 | 19 | 4.955 | 1 | 1.985 | 8 | 0.604 | 13 | 1.616 |
| 5 | 2.234 | 4 | 5.123 | 19 | 2.065 | 29 | 0.611 | 24 | 1.921 |
| 23 | 2.604 | 14 | 5.431 | 26 | 2.307 | 27 | 1.00 | 7 | 2.666 |
| 29 | 2.833 | 22 | 5.565 | 7 | 2.595 | 22 | 1.025 | 19 | 3.205 |
| 14 | 3.816 | 27 | 5.706 | 8 | 3.035 | 5 | 1.434 | 25 | 5.538 |
| 2 | 4.151 | 7 | 5.912 | 14 | 3.071 | 25 | 1.998 | 26 | 3.596 |
| 25 | 4.841 | 2 | 8.444 | 22 | 3.714 | 3 | 2.270 | 22 | 3.652 |
| 19 | 5.271 | 29 | 8.685 | 29 | 4.799 | 1 | 2.394 | 14 | 3.656 |
| 3 | 5.433 | 11 | 8.872 | 24 | 5.258 | 4 | 2.829 | 3 | 3.795 |
| 8 | 5.468 | 1 | 9.116 | 30 | 5.345 | 13 | 3.071 | 29 | 4.302 |
| 6 | 5.491 | 23 | 9.175 | 10 | 6.153 | 24 | 3.194 | 8 | 4.962 |
| 7 | 5.618 | 13 | 9.504 | 25 | 6.189 | 30 | 3.362 | 9 | 5.197 |
| 22 | 5.778 | 28 | 9.799 | 3 | 6.310 | 15 | 3.656 | 5 | 5.662 |
| 28 | 7.141 | 25 | 10.910 | 28 | 6.326 | 28 | 3.725 | 6 | 6.592 |
| 24 | 8.360 | 3 | 10.428 | 27 | 6.642 | 21 | 3.775 | 10 | 6.703 |
| 12 | 8.872 | 5 | 10.544 | 5 | 6.782 | 11 | 3.816 | 30 | 7.639 |
| 30 | 9.355 | 17 | 10.790 | 6 | 9.465 | 2 | 3.945 | 27 | 7.734 |
| 18 | 9.459 | 24 | 14.168 | 12 | 9.504 | 23 | 4.297 | 18 | 8.206 |
| 1 | 10.538 | 15 | 14.953 | 17 | 9.696 | 6 | 4.622 | 28 | 8.984 |
| 17 | 12.193 | 16 | 15.030 | 2 | 10.983 | 20 | 5.019 | 2 | 9.117 |
| 21 | 12.950 | 26 | 15.203 | 4 | 11.035 | 26 | 5.049 | 23 | 10.805 |
| 15 | 13.035 | 21 | 15.406 | 9 | 11.957 | 16 | 5.274 | 16 | 12.494 |
| 13 | 13.663 | 20 | 15.530 | 23 | 12.893 | 12 | 5.431 | 4 | 12.616 |
| 26 | 14.435 | 6 | 18.599 | 11 | 13.663 | 17 | 7.960 | 1.1 | 13.035 |
| 20 | 15.872 | 18 | 27.367 | 18 | 13.821 | 18 | 8.837 | 12 | 14.953 |
| 9 | 15.950 | 9 | 31.179 | 16 | 15.104 | 9 | 10.766 | 17 | 14.041 |

TABLE XII (Continued)

| Parent <br> Number | 16 |  | 17 | 18 |  |  |  | 19 |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 11 | 1.068 | 28 | 1.248 | 6 | 1.212 | 14 | 0.136 | 15 | 0.362 |
| 5 | 1.731 | 27 | 5.750 | 9 | 2.264 | 8 | 0.371 | 1 | 1.135 |
| 6 | 2.750 | 26 | 5.769 | 5 | 4.123 | 7 | 0.404 | 13 | 1.900 |
| 29 | 2.912 | 29 | 7.541 | 16 | 4.894 | 22 | 0.949 | 21 | 2.153 |
| 27 | 3.030 | 19 | 7.693 | 29 | 5.289 | 10 | 1.110 | 24 | 2.337 |
| 4 | 3.064 | 4 | 7.697 | 24 | 6.574 | 29 | 1.173 | 7 | 3.258 |
| 10 | 3.290 | 14 | 7.960 | 25 | 6.717 | 27 | 1.605 | 22 | 3.931 |
| 23 | 4.443 | 5 | 8.251 | 21 | 7.330 | 1 | 1.913 | 19 | 4.286 |
| 18 | 4.894 | 10 | 8.470 | 3 | 8.171 | 13 | 2.065 | 3 | 4.318 |
| 25 | 5.125 | 8 | 8.985 | 15 | 8.206 | 5 | 2.306 | 25 | 4.363 |
|  |  |  |  |  |  |  |  |  |  |
| 14 | 5.274 | 13 | 9.696 | 14 | 8.837 | 25 | 2.593 | 14 | 5.019 |
| 3 | 6.140 | 21 | 10.016 | 27 | 8.924 | 3 | 2.774 | 26 | 5.486 |
| 2 | 6.368 | 6 | 10.672 | 10 | 9.337 | 30 | 2.806 | 8 | 5.672 |
| 19 | 7.080 | 12 | 10.790 | 11 | 9.459 | 15 | 3.205 | 29 | 6.466 |
| 7 | 7.375 | 7 | 11.607 | 26 | 10.029 | 21 | 3.324 | 9 | 6.942 |
| 28 | 7.614 | 11 | 12.193 | 7 | 10.23 | 24 | 3.518 | 30 | 7.114 |
| 24 | 7.961 | 16 | 13.842 | 19 | 10.337 | 4 | 3.762 | 5 | 8.260 |
| 22 | 8.031 | 22 | 14.027 | 28 | 10.592 | 28 | 3.855 | 10 | 8.528 |
| 8 | 8.463 | 15 | 15.041 | 20 | 11.458 | 20 | 4.286 | 2 | 9.609 |
| 9 | 11.203 | 30 | 15.991 | 22 | 11.898 | 26 | 4.411 | 6 | 9.864 |
|  |  |  |  |  |  |  |  |  |  |
| 21 | 11.916 | 1 | 16.208 | 23 | 11.962 | 2 | 4.765 | 27 | 10.162 |
| 1 | 12.118 | 25 | 17.312 | 1 | 12.269 | 12 | 4.955 | 18 | 11.458 |
| 15 | 12.494 | 20 | 18.497 | 4 | 12.467 | 11 | 5.271 | 23 | 11.899 |
| 26 | 13.731 | 3 | 18.531 | 2 | 13.099 | 23 | 5.460 | 28 | 12.133 |
| 17 | 13.842 | 18 | 18.750 | 13 | 13.821 | 6 | 5.764 | 4 | 15.299 |
| 30 | 14.012 | 24 | 19.592 | 8 | 13.940 | 16 | 7.080 | 12 | 15.530 |
| 20 | 15.931 | 23 | 20.885 | 17 | 18.750 | 17 | 7.693 | 11 | 15.872 |
| 12 | 15.030 | 2 | 21.594 | 30 | 21.249 | 18 | 10.337 | 16 | 15.931 |
| 13 | 15.104 | 9 | 25.694 | 12 | 27.367 | 9 | 11.634 | 17 | 18.497 |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

TABLE XTT (cont Inued)

| Parent <br> Number | 21 |  | 22 |  | 23 |  | 24 |  | 25 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 15 | 0.907 | 7 | 0.185 | 2 | 0.299 | 25 | 0.546 | 3 | 0.077 |
| 26 | 0.973 | 8 | 0.783 | 3 | 1.990 | 3 | 0.609 | 24 | 0.546 |
| 13 | 1.510 | 1 | 0.949 | 25 | 2.140 | 1 | 1.533 | 22 | 1.200 |
| 20 | 2.153 | 3 | 0.966 | 11 | 2.609 | 7 | 1.913 | 7 | 1.272 |
| 19 | 3.324 | 19 | 0.999 | 10 | 2.793 | 15 | 1.921 | 2 | 1.643 |
| 1 | 3.633 | 14 | 1.025 | 22 | 3.048 | 22 | 2.022 | 14 | 1.998 |
| 29 | 3.683 | 25 | 1.200 | 7 | 3.930 | 20 | 2.337 | 1 | 2.130 |
| 14 | 3.775 | 30 | 1.397 | 14 | 4.297 | 14 | 3.194 | 23 | 2.140 |
| 7 | 3.944 | 10 | 1.826 | 4 | 4.357 | 19 | 3.518 | 29 | 2.271 |
| 24 | 4.371 | 2 | 1.978 | 16 | 4.443 | 29 | 3.550 | 10 | 2.475 |
|  |  |  |  |  |  |  |  |  |  |
| 5 | 4.814 | 24 | 2.022 | 24 | 4.656 | 2 | 3.606 | 19 | 2.593 |
| 6 | 4.926 | 29 | 2.687 | 29 | 4.807 | 5 | 4.282 | 5 | 2.746 |
| 28 | 5.427 | 23 | 3.048 | 27 | 4.811 | 21 | 4.371 | 8 | 3.253 |
| 8 | 5.644 | 27 | 3.490 | 8 | 4.881 | 9 | 4.568 | 15 | 3.538 |
| 22 | 5.653 | 15 | 3.652 | 5 | 4.885 | 8 | 4.649 | 27 | 4.155 |
|  |  |  |  |  |  |  |  |  |  |
| 25 | 5.733 | 13 | 3.714 | 30 | 5.611 | 23 | 4.656 | 20 | 4.363 |
| 9 | 6.061 | 20 | 3.931 | 19 | 5.460 | 10 | 4.683 | 11 | 4.841 |
| 3 | 6.418 | 5 | 3.939 | 1 | 6.635 | 13 | 5.258 | 30 | 4.994 |
| 27 | 6.675 | 4 | 5.270 | 12 | 9.175 | 6 | 5.913 | 16 | 5.124 |
| 10 | 6.787 | 12 | 5.565 | 6 | 9.316 | 30 | 6.334 | 6 | 5.179 |
| 18 | 7.330 | 21 | 5.653 | 15 | 10.805 | 27 | 6.563 | 21 | 5.733 |
| 17 | 10.016 | 11 | 5.778 | 20 | 11.899 | 18 | 6.574 | 4 | 6.164 |
| 30 | 10.169 | 16 | 8.031 | 18 | 11.962 | 16 | 7.961 | 13 | 6.189 |
| 4 | 11.736 | 6 | 8.214 | 13 | 12.893 | 11 | 8.360 | 9 | 6.633 |
| 16 | 11.916 | 28 | 8.557 | 28 | 13.592 | 26 | 8.783 | 18 | 6.717 |
|  |  |  |  |  |  |  |  |  |  |
| 2 | 12.484 | 26 | 8.567 | 21 | 13.668 | 4 | 9.773 | 26 | 9.692 |
| 11 | 12.950 | 9 | 11.715 | 9 | 14.549 | 28 | 11.656 | 28 | 9.942 |
| 23 | 13.668 | 18 | 11.848 | 26 | 17.887 | 12 | 14.168 | 12 | 10.910 |
| 12 | 15.406 | 17 | 14.027 | 17 | 20.885 | 17 | 19.592 | 17 | 17.312 |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

TABLE XII. (Continued)

| Parent Number | 26 |  | 27 |  | 28 |  | 29 |  | 30 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 21 | 0.973 | 10 | 0.364 | 17 | 1.248 | 5 | 0.196 | 8 | 1.312 |
| 13 | 2.307 | 4 | 0.721 | 27 | 2.340 | 14 | 0.611 | 22 | 1.397 |
| 28 | 3.219 | 29 | 0.724 | 29 | 2.851 | 27 | 0.724 | 7 | 2.074 |
| 15 | 3.596 | 5 | 0.926 | 5 | 3.213 | 10 | 0.809 | 12 | 2.723 |
| 19 | 4.411 | 14 | 1.00 | 26 | 3.219 | 19 | 1.173 | 1 | 2.737 |
| 29 | 4.775 | 19 | 1.605 | 14 | 3.725 | 7 | 1.750 | 19 | 2.806 |
| 14 | 5.049 | 11 | 1.690 | 19 | 3.855 | 6 | 1.951 | 14 | 3.362 |
| 20 | 5.486 | 8 | 2.130 | 10 | 4.204 | 25 | 2.271 | 2 | 3.927 |
| 17 | 5.769 | 28 | 2.340 | 4 | 4.531 | 8 | 2.390 | 10 | 4.173 |
| 5 | 5.942 | 7 | 2.705 | 6 | 4.758 | 4 | 2.626 | 3 | 4.264 |
| 6 | 6.065 | 16 | 3.030 | 21 | 5.427 | 22 | 2.687 | 25 | 4.994 |
| 7 | 6.275 | 22 | 3.490 | 8 | 5.456 | 11 | 2.833 | 13 | 5.345 |
| 27 | 6.863 | 6 | 3.986 | 13 | 6.326 | 28 | 2.851 | 23 | 5.614 |
| 8 | 6.871 | 25 | 4.155 | 7 | 6.537 | 16 | 2.912 | 27 | 6.263 |
| 1 | 6.901 | 3 | 4.462 | 11 | 7.141 | 3 | 2.936 | 24 | 6.334 |
| 10 | 8.023 | 23 | 4.811 | 16 | 7.614 | 24 | 3.550 | 29 | 6.709 |
| 22 | 8.567 | 2 | 5.482 | 22 | 8.557 | 21 | 3.683 | 20 | 7.114 |
| 24 | 8.783 | 12 | 5.706 | 15 | 8.984 | 15 | 4.302 | 4 | 7.344 |
| 25 | 9.692 | 17 | 5.750 | 12 | 9.799 | 1 | 4.317 | 15 | 7.639 |
| 18 | 10.029 | 30 | 6.263 | 25 | 9.942 | 26 | 4.775 | 5 | 8.756 |
| 9 | 10.501 | 1 | 6.462 | 1 | 10.336 | 13 | 4.799 | 11 | 9.355 |
| 3 | 10.651 | 24 | 6.563 | 18 | 10.592 | 23 | 4.807 | 21 | 10.169 |
| 4 | 11.862 | 13 | 6.642 | 3 | 11.078 | 20 | 5.113 | 28 | 11.949 |
| 30 | 12.654 | 21 | 6.675 | 24 | 11.656 | 18 | 5.289 | 26 | 12.654 |
| 16 | 13.731 | 26 | 6.863 | 30 | 11.949 | 20 | 6.466 | 16 | 14.012 |
| 11 | 14.435 | 15 | 7.734 | 20 | 12.133 | 30 | 6.706 | 6 |  |
| 12 | 15.203 | 18 | 8.924 | 23 | 13.592 | 17 | 7.541 | 17 | 15.991 |
| 2 | 17.017 | 20 | 10.162 | 2 | 14.258 | 9 | 8.320 | 9 | 20.821 |
| 23 | 17.887 | 9 | 13.842 | 9 | 16.041 | 12 | 8.685 | 18 | 21.249 |

TABLE XIII
VALUES OF $\mathrm{D}^{2 *}$ BASED ON THE CHARACTERS ARRANGED IN INCREASING ORDER OF MAGNITUDE WITH RESPECT TO EACH PARENT - 1979 STILLWATER

| Parent <br> Number | 2 |  | 3 |  | 4 |  | 5 |  | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 23 | 2.226 | 25 | 0.777 | 27 | 0.263 | 26 | 1.007 | 11 | 0.502 |
| 8 | 2.569 | 9 | 1.308 | 29 | 0.477 | 14 | 2.149 | 29 | 0.515 |
| 22 | 2.781 | 18 | 2.709 | 23 | 1.494 | 7 | 2.163 | 18 | 1.015 |
| 6 | 3.051 | 20 | 3.928 | 6 | 1.840 | 13 | 3.396 | 23 | 1.231 |
| 29 | 3.591 | 7 | 4.952 | 21 | 1.933 | 25 | 3.493 | 4 | 1.840 |
| 18 | 3.883 | 23 | 5.086 | 11 | 2.233 | 29 | 3.699 | 27 | 3.024 |
| 21 | 3.919 | 6 | 6.004 | 10 | 2.853 | 16 | 3.938 | 2 | 3.053 |
| 15 | 4.113 | 2 | 6.298 | 8 | 3.981 | 21 | 4.098 | 21 | 4.092 |
| 4 | 4.980 | 13 | 6.420 | 7 | 4.058 | 23 | 4.118 | 16 | 4.246 |
| 11 | 5.068 | 21 | 6.471 | 15 | 4.807 | 20 | 4.255 | 5 | 4.398 |
| 30 | 5.172 | 15 | 6.656 | 2 | 4.980 | 6 | 4.398 | 7 | 4.435 |
| 10 | 5.692 | 5 | 7.009 | 22 | 5.055 | 18 | 4.565 | 25 | 4.771 |
| 3 | 6.298 | 14 | 7.571 | 5 | 5.069 | 4 | 5.069 | 3 | 6.004 |
| 25 | 6.690 | 16 | 7.606 | 18 | 5.218 | 19 | 5.499 | 15 | 6.051 |
| 7 | 6.832 | 29 | 7.637 | 14 | 6.367 | 11 | 5.708 | 8 | 6.101 |
| 27 | 6.953 | 11 | 9.412 | 20 | 7.024 | 28 | 6.123 | 20 | 6.746 |
| 20 | 7.317 | 26 | 9.711 | 26 | 7.538 | 27 | 6.490 | 10 | 6.783 |
| 14 | 11.605 | 19 | 10.110 | 30 | 7.715 | 3 | 7.009 | 22 | 7.427 |
| 5 | 11.646 | 8 | 10.934 | 25 | 8.234 | 9 | 7.442 | 14 | 7.670 |
| 13 | 12.032 | 4 | 11.468 | 13 | 8.666 | 15 | 7.476 | 26 | 8.530 |
| 9 | 12.348 | 30 | 11.823 | 16 | 9.190 | 2 | 11.646 | 9 | 9.074 |
| 16 | 12.904 | 22 | 14.881 | 28 | 11.461 | 8 | 11.920 | 13 | 9.252 |
| 26 | 15.730 | 27 | 15.097 | 3 | 11.468 | 30 | 14.384 | 30 | 10.355 |
| 19 | 24.150 | 10 | 19.915 | 9 | 16.341 | 10 | 15.180 | 28 | 16.246 |

## TABLE XITI (Cont inued)

| Parent Number | 7 |  | 8 |  | 9 |  | 10 |  | 11 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 0.574 | 22 | 0.675 | 3 | 1.308 | 22 | 1.809 | 6 | 0.502 |
| 14 | 0.635 | 30 | 0.945 | 25 | 2.167 | 27 | 2.582 | 29 | 1.179 |
| 21 | 0.824 | 15 | 1.459 | 18 | 4.338 | 4 | 2.853 | 18 | 2.186 |
| 13 | 0.969 | 21 | 2.149 | 16 | 5.970 | 8 | 2.971 | 4 | 2.233 |
| 23 | 1.653 | 23 | 2.520 | 20 | 7.342 | 29 | 4.668 | 27 | 2.846 |
| 15 | 1.745 | 2 | 2.569 | 5 | 7.442 | 23 | 5.343 | 23 | 3.023 |
| 25 | 2.037 | 10 | 2.971 | 7 | 8.133 | 21 | 5.651 | 16 | 4.045 |
| 5 | 2.163 | 4 | 3.981 | 19 | 8.739 | 2 | 5.692 | 2 | 5.068 |
| 26 | 2.215 | 29 | 4.359 | 13 | 8.846 | 30 | 6.681 | 21 | 5.417 |
| 29 | 3.086 | 7 | 5.203 | 6 | 9.074 | 6 | 6.783 | 5 | 5.078 |
| 4 | 4.058 | 27 | 5.368 | 23 | 9.465 | 11 | 7.197 | 10 | 7.197 |
| 6 | 4.435 | 20 | 5.678 | 14 | 10.060 | 15 | 7.289 | 7 | 7.210 |
| 18 | 4.907 | 6 | 6.101 | 26 | 10.455 | 7 | 10.607 | 25 | 7.920 |
| 3 | 4.952 | 14 | 8.454 | 21 | 11.324 | 18 | 12.292 | 8 | 8.768 |
| 8 | 5.203 | 11 | 8.768 | 29 | 11.508 | 20 | 13.542 | 3 | 9.412 |
| 30 | 5.763 | 18 | 8.948 | 11 | 12.173 | 14 | 14.455 | 22 | 9.522 |
| 27 | 5.994 | 25 | 9.082 | 2 | 12.348 | 5 | 15.180 | 15 | 9.541 |
| 19 | 6.413 | 13 | 9.111 | 15 | 12.623 | 25 | 16.948 | 20 | 10.546 |
| 2 | 6.832 | 3 | 10.934 | 4 | 16.341 | 13 | 17.061 | 14 | 10.686 |
| 11 | 7.210 | 5 | 11.920 | 8 | 18.865 | 26 | 18.027 | 26 | 10.702 |
| 9 | 8.133 | 26 | 13.273 | 27 | 20.258 | 3 | 19.915 | 9 | 12.173 |
| 16 | 9.110 | 9 | 18.865 | 30 | 20.265 | 16 | 20.826 | 13 | 13.020 |
| 22 | 9.147 | 16 | 19.288 | 22 | 24.006 | 28 | 22.283 | 30 | 14.343 |
| 10 | 10.607 | 19 | 22.579 | 28 | 26.273 | 9 | 28.530 | 28 | 16.348 |
| 28 | 10.640 | 28 | 23.178 | 10 | 28.530 | 19 | 32.995 | 19 | 21.247 |

TABLE XIII (Continued)

| Parent <br> Number | 13 |  | 14 |  | 15 |  | 16 |  | 18 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 14 | 0.336 | 13 | 0.336 | 21 | 0.814 | 18 | 2.839 | 6 | 1.015 |
| 20 | 0.722 | 7 | 0.635 | 30 | 1.209 | 5 | 3.938 | 11 | 2.186 |
| 7 | 0.969 | 26 | 0.892 | 8 | 1.459 | 11 | 4.045 | 23 | 2.476 |
| 26 | 1.809 | 20 | 1.252 | 20 | 1.480 | 6 | 4.246 | 29 | 2.544 |
| 25 | 2.962 | 5 | 2.149 | 7 | 1.745 | 9 | 5.970 | 25 | 2.621 |
| 19 | 3.165 | 21 | 2.497 | 23 | 1.840 | 29 | 6.159 | 3 | 2.709 |
| 21 | 3.274 | 25 | 3.565 | 13 | 3.519 | 25 | 6.407 | 16 | 2.839 |
| 5 | 3.396 | 15 | 3.588 | 14 | 3.588 | 3 | 7.606 | 2 | 3.883 |
| 15 | 3.519 | 19 | 3.985 | 22 | 4.095 | 23 | 7.962 | 9 | 4.338 |
| 23 | 5.086 | 23 | 4.172 | 2 | 4.113 | 26 | 8.689 | 5 | 4.565 |
| 3 |  |  |  |  |  |  |  |  |  |
| 29 | 7.428 | 29 | 5.636 | 29 | 4.347 | 7 | 9.110 | 21 | 4.772 |
| 30 | 8.133 | 3 | 6.367 | 25 | 4.498 | 4 | 9.190 | 7 | 4.907 |
| 4 | 8.666 | 6 | 7.670 | 4 | 4.807 | 21 | 10.700 | 4 | 5.218 |
| 9 | 8.846 | 28 | 7.814 | 3 | 6.051 | 27 | 10.780 | 20 | 6.257 |
| 18 | 8.880 | 18 | 8.188 | 27 | 6.885 | 14 | 11.090 | 15 | 7.290 |
| 8 | 9.111 | 27 | 8.243 | 10 | 7.289 | 13 | 12.011 | 27 | 7.328 |
| 6 | 9.252 | 30 | 8.346 | 18 | 7.290 | 2 | 12.990 | 14 | 8.188 |
| 28 | 10.918 | 8 | 8.454 | 5 | 7.476 | 19 | 13.910 | 13 | 8.880 |
| 27 | 11.117 | 9 | 10.060 | 26 | 7.552 | 28 | 15.545 | 26 | 8.948 |
| 2 | 12.032 | 11 | 10.686 | 11 | 9.541 | 15 | 15.833 | 22 | 11.171 |
| 16 | 12.690 | 16 | 11.090 | 9 | 12.623 | 8 | 19.288 | 10 | 12.292 |
| 11 | 13.020 | 2 | 11.605 | 19 | 13.072 | 10 | 20.826 | 30 | 12.666 |
| 22 | 14.576 | 22 | 13.475 | 16 | 15.833 | 22 | 22.684 | 19 | 14.568 |
| 10 | 17.061 | 10 | 14.455 | 28 | 18.343 | 30 | 24.628 | 28 | 19.846 |
|  |  |  |  |  |  |  |  |  |  |

TABLE XIII (Continued)

| Parent Number | 19 |  | 20 |  | 21 |  | 22 |  | 23 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 26 | 3.133 | 7 | 0.574 | 15 | 0.814 | 8 | 0.675 | 21 | 0.498 |
| 13 | 3.165 | 13 | 0.722 | 23 | 0.498 | 10 | 1.809 | 29 | 0.657 |
| 14 | 3.985 | 14 | 1.252 | 7 | 0.824 | 30 | 2.520 | 6 | 1.231 |
| 5 | 5.499 | 15 | 1.480 | 29 | 1.615 | 2 | 2.781 | 4 | 1.494 |
| 20 | 5.966 | 25 | 1.667 | 20 | 1.794 | 15 | 4.095 | 7 | 1.653 |
| 25 | 6.276 | 21 | 1.794 | 4 | 1.933 | 23 | 4.450 | 15 | 1.840 |
| 7 | 6.413 | 23 | 2.897 | 8 | 2.149 | 21 | 4.604 | 2 | 2.226 |
| 9 | 8.739 | 26 | 3.787 | 14 | 2.497 | 4 | 5.055 | 18 | 2.476 |
| 3 | 10.110 | 3 | 3.928 | 6 | 3.092 | 29 | 5.836 | 8 | 2.520 |
| 21 | 11.826 | 5 | 4.255 | 13 | 3.274 | 27 | 6.046 | 20 | 2.897 |
| 28 | 12.160 | 30 | 5.015 | 30 | 3.327 | 6 | 7.427 | 27 | 3.007 |
| 15 | 13.072 | 29 | 5.536 | 27 | 3.411 | 7 | 9.147 | 11 | 3.023 |
| 23 | 13.758 | 8 | 5.678 | 25 | 3.792 | 11 | 9.522 | 25 | 3.288 |
| 16 | 13.910 | 19 | 5.966 | 2 | 3.919 | 20 | 10.082 | 5 | 4.118 |
| 18 | 14.568 | 18 | 6.257 | 5 | 4.098 | 18 | 11.171 | 14 | 4.172 |
| 29 | 16.023 | 6 | 6.746 | 22 | 4.604 | 25 | 13.438 | 22 | 4.450 |
| 6 | 17.231 | 4 | 7.024 | 18 | 4.772 | 14 | 13.475 | 30 | 4.774 |
| 4 | 18.632 | 2 | 7.317 | 26 | 4.937 | 13 | 14.576 | 13 | 5.086 |
| 30 | 21.218 | 9 | 7.342 | 11 | 5.417 | 3 | 14.881 | 3 | 5.086 |
| 11 | 21.247 | 27 | 9.665 | 10 | 5.651 | 5 | 16.440 | 10 | 5.343 |
| 27 | 21.744 | 22 | 10.082 | 3 | 6.471 | 26 | 18.856 | 26 | 6.347 |
| 8 | 22.579 | 11 | 10.546 | 16 | 10.700 | 16 | 22.684 | 16 | 7.962 |
| 2 | 24.150 | 16 | 12.011 | 9 | 11.324 | 9 | 24.006 | 9 | 9.465 |
| 22 | 30.588 | 10 | 13.542 | 19 | 11.826 | 28 | 28.500 | 19 | 13.758 |
| 10 | 32.995 | 38 | 15.016 | 28 | 12.970 | 19 | 30.588 | 28 | 15.094 |

TABLE XIII (Continued)

| Parent <br> Number | 25 | 26 |  |  | 27 |  | 28 |  | 29 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  |  |  |  |  |  |  |
| 3 | 0.777 | 14 | 0.892 | 4 | 0.263 | 26 | 4.464 | 4 | 0.477 |
| 20 | 1.667 | 5 | 1.007 | 29 | 1.313 | 5 | 6.123 | 6 | 0.515 |
| 7 | 2.037 | 13 | 1.809 | 10 | 2.582 | 14 | 7.814 | 23 | 0.657 |
| 9 | 2.167 | 7 | 2.215 | 11 | 2.846 | 7 | 10.640 | 11 | 1.179 |
| 18 | 2.621 | 19 | 3.133 | 23 | 3.007 | 13 | 10.918 | 27 | 1.313 |
|  |  |  |  |  |  |  |  |  |  |
| 13 | 2.962 | 20 | 3.787 | 6 | 3.240 | 27 | 10.997 | 21 | 1.615 |
| 23 | 3.288 | 28 | 4.464 | 21 | 3.411 | 4 | 11.461 | 18 | 2.544 |
| 5 | 3.493 | 21 | 4.937 | 8 | 5.368 | 19 | 12.160 | 7 | 3.086 |
| 14 | 3.565 | 25 | 5.041 | 7 | 5.974 | 29 | 12.716 | 2 | 3.591 |
| 21 | 3.792 | 4 | 5.538 | 22 | 6.046 | 21 | 12.970 | 5 | 3.699 |
|  |  |  |  |  |  |  |  |  |  |
| 15 | 4.498 | 23 | 6.347 | 5 | 6.490 | 20 | 15.016 | 15 | 4.357 |
| 6 | 4.771 | 29 | 6.682 | 15 | 6.885 | 23 | 15.094 | 8 | 4.359 |
| 26 | 5.041 | 15 | 7.552 | 2 | 6.853 | 16 | 15.545 | 10 | 4.668 |
| 29 | 5.324 | 6 | 8.530 | 18 | 7.328 | 6 | 16.246 | 25 | 5.324 |
| 19 | 6.276 | 16 | 8.689 | 14 | 8.243 | 11 | 16.348 | 20 | 5.536 |
| 16 | 6.407 | 18 | 8.959 | 26 | 9.055 | 25 | 17.929 | 14 | 5.636 |
| 2 | 6.690 | 27 | 9.055 | 20 | 9.665 | 15 | 18.343 | 22 | 5.836 |
| 11 | 7.920 | 3 | 9.711 | 30 | 9.702 | 18 | 19.846 | 16 | 6.159 |
| 4 | 8.234 | 11 | 10.702 | 16 | 10.780 | 10 | 22.283 | 26 | 6.682 |
| 8 | 9.082 | 9 | 10.455 | 28 | 10.997 | 8 | 23.178 | 13 | 7.428 |
|  |  |  |  |  |  |  |  |  |  |
| 30 | 9.836 | 8 | 13.273 | 13 | 11.117 | 30 | 25.951 | 3 | 7.637 |
| 27 | 11.272 | 30 | 14.167 | 25 | 11.272 | 3 | 25.764 | 30 | 8.028 |
| 22 | 13.438 | 2 | 15.097 | 3 | 15.097 | 9 | 26.273 | 9 | 11.508 |
| 10 | 16.948 | 10 | 18.027 | 9 | 20.258 | 22 | 28.500 | 28 | 12.716 |
| 28 | 17.929 | 22 | 18.856 | 19 | 21.744 | 2 | 28.626 | 19 | 16.023 |
|  |  |  |  |  |  |  |  |  |  |

TABLE XIII (Continued)

| Parent <br> Number | 30 |
| ---: | :--- |
| 8 | 0.945 |
| 15 | 1.204 |
| 22 | 2.520 |
| 21 | 3.327 |
| 23 | 4.774 |
|  |  |
| 20 | 5.015 |
| 2 | 5.172 |
| 7 | 5.763 |
| 10 | 6.681 |
| 4 | 7.715 |
|  |  |
| 29 | 8.028 |
| 13 | 8.133 |
| 14 | 8.346 |
| 27 | 9.702 |
| 25 | 9.836 |
| 6 | 10.355 |
| 3 | 11.823 |
| 18 | 12.666 |
| 26 | 14.167 |
| 11 | 14.343 |
| 5 | 14.384 |
| 9 | 20.265 |
| 19 | 21.218 |
| 16 | 24.628 |
| 28 | 25.951 |

## VITA

Mohammad Taghi Assad<br>Candidate for the Degree of<br>Doctor of Philosophy

Thesis: MULTIVARIATE ANALYSIS APPROACH TO SELECTION OF PARENTAL MATERIAL FOR HYBRIDIZATION IN WINTER WHEAT

Major Field: Crop Science
Biographical:
Personal Data: Born in Sivand, Shiraz, Iran, October 7, 1949, the son of Mr. and Mrs. Assad.

Education: Graduated from Shahpour High School, Shiraz, Iran, in 1968; received Bachelor of Science degree from Pahlavy University, Shiraz, Iran, in 1972; received the Master of Science degree from Oklahoma State University, Stillwater, Oklahoma, in December, 1976; completed the requirements for the Doctor of Philosophy degree at Oklahoma State University, Stillwater, Oklahoma, in July, 1980.

Professional Experience: Served in the armed forces of Iran for two years--1973-1974; employed by the Department of Agronomy, Oklahoma State University, June, 1975, through September, 1976; Research Assistant in the Department of Agronomy, Oklahoma State University, October, 1976, to May, 1980.


[^0]:    * P in parentheses refers to parent number in Table VIII.

[^1]:    ${ }^{*} \mathrm{P}$ in parentheses refers to parent number in Table VIII.

[^2]:    ${ }^{*} \mathrm{P}$ in parentheses refers to parent number in Table VIII.

[^3]:    ${ }^{* *} \mathrm{P}$ in parentheses refers to parent number in Table IX.

[^4]:    * High group includes parents with yields greater than $460 \mathrm{gm} / \mathrm{plot}$, medium group between 420 and $460 \mathrm{gm} / \mathrm{plot}$, and low group less than $420 \mathrm{gm} /$ plot.

[^5]:    * High group includes parents with yield greater than $290 \mathrm{gm} / \mathrm{plot}$, medium group between 250 and $290 \mathrm{gm} / \mathrm{plot}$, and low group less than $250 \mathrm{gm} / \mathrm{plot}$.

[^6]:    * High group includes parents with yield greater than 530 grams/plot, medium group between 460 and 530 grams/plot, and low group less than 460 grams/plot.

