

PARTICLE COUNTING: AN ANALYSIS OF THE PROBLEM  
OF CALIBRATION AND UNCERTAINTY

By

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## CHAPTER I

### INTRODUCTION

The capability to accurately estimate the parameters of the distribution of sizes of small particles (i.e., 1 to 100 micrometres) is very important in a number of diverse fields. In medicine, blood cell counts are based on the size difference of red and white cells. The ultimate characteristics of sintered products in powder metallurgy is critically dependent on particle size. Of special concern to the author, the technology of contamination control in fluid power systems is totally dependent on accurate, easily obtained, counts of various size particles entrained in fluid samples.

There are a number of techniques employed in particle counting. Manual counts using microscopes have been used for many years. By the late 1960's, it had been recognized that microscopic counting techniques were neither accurate enough nor sufficiently economical to support the research and development effort required to evaluate the filters and components used in fluid power systems. The opto-electronic automatic particle counter was the most promising technique for a general methodology if a suitable standard method could be developed for calibration and use of the instrument.

The Fluid Power Research Center (FPRC) of Oklahoma State University undertook the task of developing and promulgating such a standard, and, in 1973, the American National Standard B93.28-1973 was adopted. This

standard is presently being circulated for ballot as an international (ISO) standard. As is the case with all such standards, the method proposed is a compromise of the technology in order to meet political constraints. The standard incorporates the use of Shewhart  $\bar{X}$  and R charting which was virtually unknown to the participating committee members both in the U.S.A. and abroad. At the time the standard was promulgated, the requirements were considered far too severe. The standard is now under attack as unacceptably lenient.

This is a healthy sign, reflecting the growing sophistication of the industry. The scope and nature of the problems of particle counting are much more generally understood, and the environment is conducive to the acceptance of statistical control techniques.

There are two considerations in applying statistical control aspects to automatic particle counting: (1) the physical nature of counting process including optical and electronic effects, and (2) the nature of the size vs. frequency of occurrence of various contaminants encountered. This thesis presents the results of an extensive investigation of the counting phenomena, an analysis of a large body of data from actual particle counts, and proposes a set of statistical quality control techniques to be incorporated into a revised proposed standard method.



## CHAPTER II

### SURVEY OF RELATED TOPICS

Over one hundred papers, books, and monographs relating to particle counting were reviewed in preparation of this thesis. Only fifteen made any mention of calibration or uncertainty. Nine of the papers were concerned with particle distributions, another nine addressed particle behavior, and the balance either advanced new particle counting methods or reviewed existing techniques. The lack of concern with the metrological aspects is surprising in view of the widespread interest in particle counting. Prior to the introduction of the first automatic particle counter in 1956 by W. H. Coulter, all particle counting was performed manually by microscope examination which may explain the absence of calibration studies.

As early as 1929 it was recognized that the most useful information about particulate contamination would be in the form of a mathematical relationship between particle size and frequency of occurrence [1]. Subsequently a number of investigations have postulated appropriate models including the Hyperbolic [2] and the log-normal [3]. These probabilistic models are intellectually appealing since most naturally occurring contaminants are of essentially infinite supply. However, the automatic particle counter yields only the number of particles greater than a selected size. There is no way to determine the total number of particles in a sample for estimating

relative frequency. A model proposed by Cole [4] provides a useful transformation of the log-normal. This equation is very tractable and particularly well suited for graphical analysis. The model is of the form

$$n = A \int_{-\infty}^{\ln X} \exp(-B \ln^2 X) \quad (2-1)$$

where A and B are empirical constants for the contaminant in question. This model has been generally accepted in the Fluid Power Industry and is an integral part of several American National Standards dealing with contamination control. Particle counting is concerned principally with the estimation of the parameters of this model and any method of calibration must be relevant to this application.

The major impetus for standardization came with the space program when strict cleanliness standards were imposed on various components being manufactured at different locations. A research group at Oklahoma State University was working on contamination sensitivity and filtration for N.A.S.A. and an evaluation of automatic particle counters was a part of the study. The study by Zaloudek [5] is one of the earliest attempts to quantify the uncertainty of an automatic particle counter. Zaloudek presented data which strongly supported the proposal by Michaelson [6] that the appearance of particles in the counter was a Poisson process.

In the late 1960's both the National Fluid Power Association and the Society of Automotive Engineers began the development of calibration standards for automatic particle counters. The SAE standard which was published in 1970 as Aerospace Recommended Practice (ARP) 1192 was

an outgrowth of earlier work with microscopic counting and in fact relied on correlation with microscopic results. The limitations of the latter technique were widely known and as a result ARP 1192 received little acceptance.

The N.F.P.A. Standard was directly the result of a broadly based study by the Fluid Power Research Center at Oklahoma State University which included a series of International Round Robin Tests using known and unknown (i.e., undisclosed) samples. The procedure uses an arbitrary calibration standard, A.C. Fine Test Dust, the distribution of which is accepted knowledge and conforms to the log-log<sup>2</sup> model. This standard was adopted as an American National Standard in 1973.

At the time the ANSI standard procedure was developed it was not uncommon to observe a 200% variation in counts of the same fluid by different laboratories. The round robin test of 1971-72 showed a coefficient of variation of 74% for laboratories not using the proposed procedure. Within two years of publication a large number of users had become sufficiently expert in the science of particle counting to detect serious deficiencies in the procedure. Primarily these problems are the result of the use of statistical procedures which do not discriminate against a process which does not have an origin in a stable region. If the particle counting process has an extremely large variance, or is operating in an invalid concentration region when the calibration procedure is started, the results are unrealistic.

The objective of this thesis is to develop analytical descriptions of the counting process and to apply these models to the structuring of a fundamental and general calibration and control procedure for automatic particle counters.

## CHAPTER III

### THE COUNTING PROCESS AND SOURCES OF ERROR

All of the automatic particle counting devices in use today exhibit a degree of non-repeatability and error. Although the actual counting technique varies widely between the different types of instruments, the concepts employed are similar and the basic sources of error are common to all. The total light reduction principle is by far the most widely used technique and will be used to illustrate the problems associated with reducing the uncertainty of particle counts.

The basic particle counting device is illustrated in Figure 1. A stream of fluid is passed through a transparent chamber (usually quartz) across which a collimated beam of light is focused. A photoelectric device (typically a photo diode) measures the intensity of the light passing through the fluid. If a particle whose index of refraction is sufficiently different from the fluid [7] passes between the light source and the detector, the light is scattered and/or blocked resulting in a reduction of intensity which is directly proportional to the projected area of the particle. The output of the photo detector is amplified and conditioned electronically to provide a train of pulses such as that shown in Figure 2. A level detector(s) determines whether or not the pulse exceeds a preset value. If it does, a counter is incremented. The levels correspond to the intensity reduction caused by a circular cross section particle of the specified

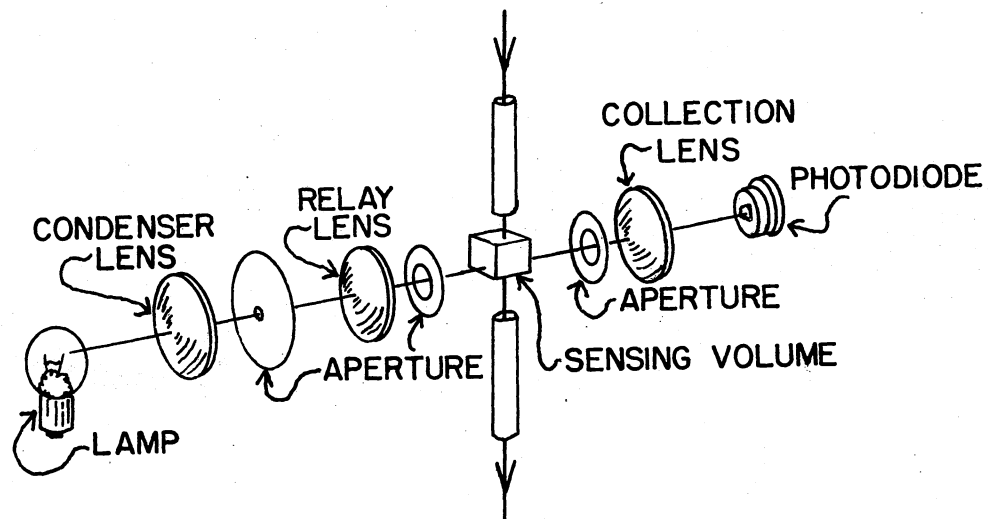


Figure 1. Particle Counting Device

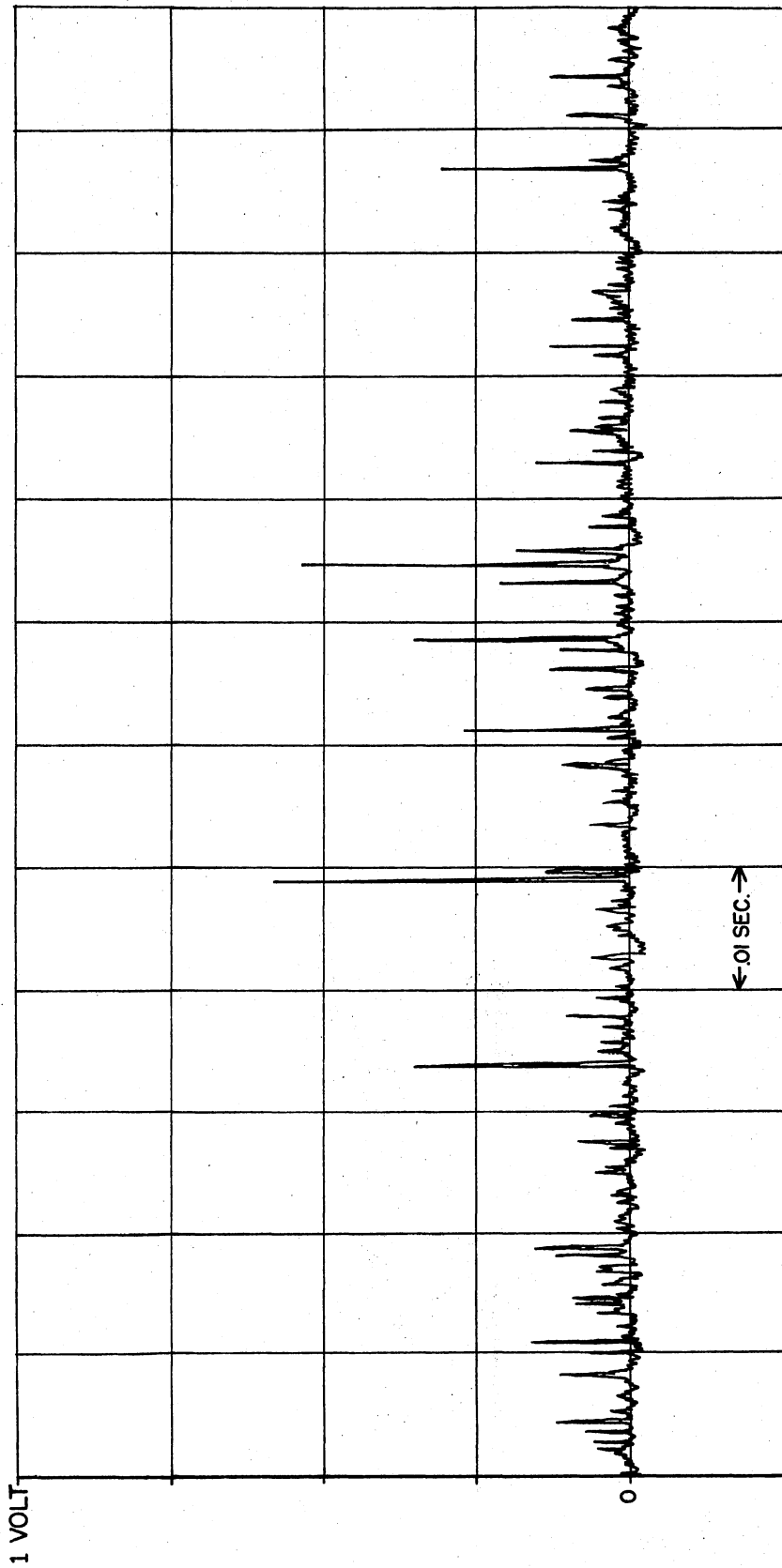


Figure 2. Electrical Output From Sensor

diameter. The result is the number of particles greater than a specified diameter which passed the sensing zone.

To the user, the variation in counts obtained from repeated samples is in the form of scatter of the counts about a mean value, the deviation of the mean from a known or expected correct count, and the failure of the observed count to increase proportionately with increasing particle concentration. This latter condition is generally called saturation and is depicted in Figure 3.

From an analytical viewpoint the sources of error can be grouped into three categories: (1) procedural, often erroneously called operator induced, which are effects not related to the actual counting phenomenon; (2) functional, which are limitations of the counting device; and (3) inherent variation in the counting process.

Generally the particle counting procedure consists of obtaining a sample of contaminated fluid from the system in a suitable container, passing a known portion of the sample through the sensing zone and reporting the result in terms of a standard volume, usually one millilitre. If the count exceeds the saturation level discussed above, the fluid is diluted with clean fluid and the process repeated. If the sample container is not extremely clean, the background contamination in the container will add to the actual count. Any variation in measurement of the fluid volume passing the sensor results in a directly proportional error in the perceived count. If dilution is required the inaccuracies of the volume measurements will reflect directly on the magnitude of the count and if the sample is not properly mixed, very erratic results are obtained. In addition, the particles tend to either settle or float in the fluid and care must be

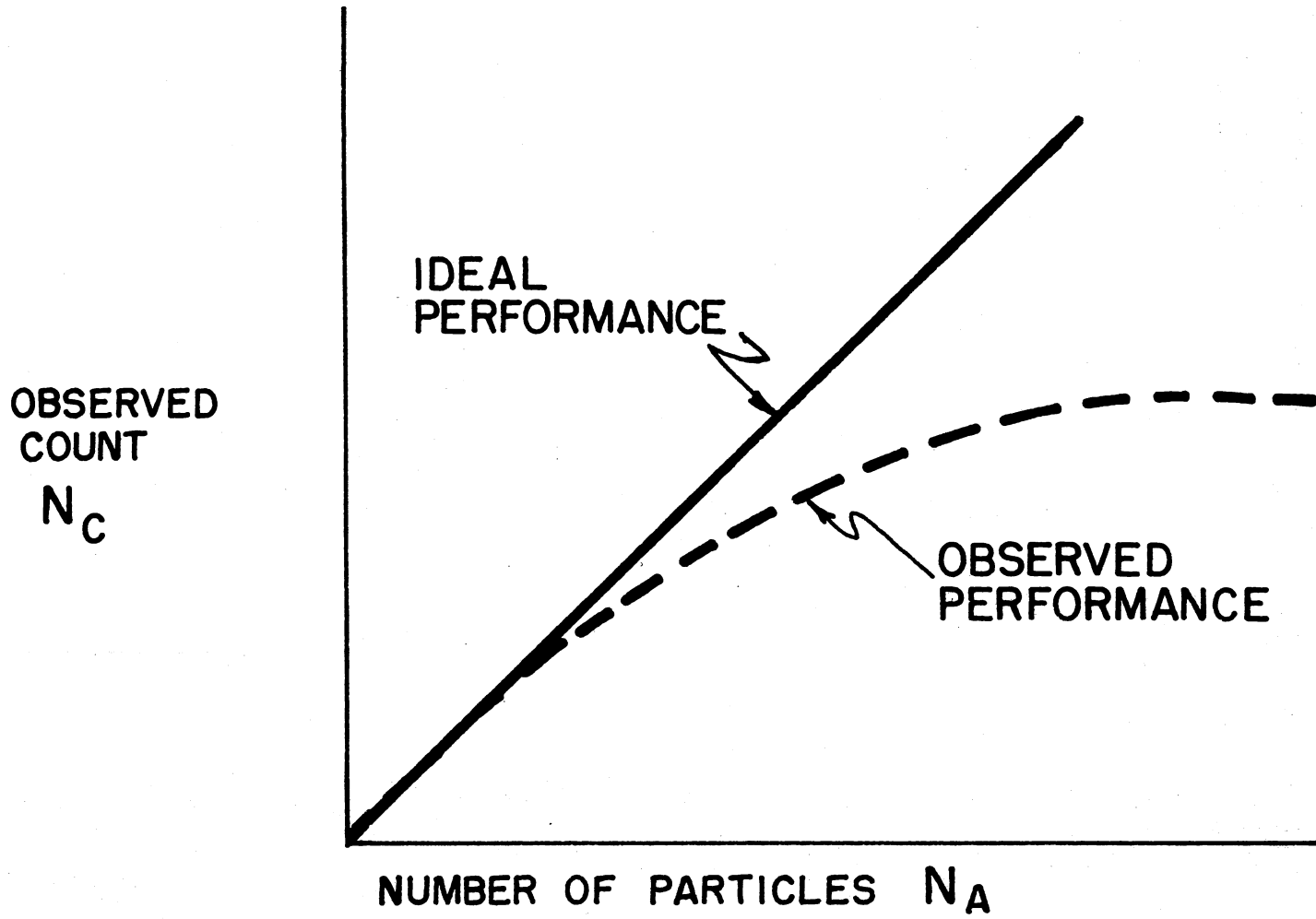


Figure 3. The Saturation Phenomenon



taken to assure proper dispersion of the particles. Until very recently these procedural effects were the major source of uncertainty in particle counts and in fact may still be significant. However, in 1970 a sample container cleanliness verification procedure was developed at the Fluid Power Research Center which has since been adopted as an international standard. Improved particle counters which incorporate photo-electric volume measuring have sharply reduced the variance from this source.

The requirement for dilution imposes a severe burden on the particle counting technician. Dilutions of 40 to 1 and higher are not uncommon and this requires very precise measurement of small volumes of fluid.

The functional errors of the particle counter are related both to design variables and the condition of the counter. The counter may simply fail to count correctly due to erratic behavior of the counting or display electronics. Variations in the reference level voltages will result in counts which represent a particle diameter other than that intended. Due to the extreme nonlinearity of the particle distribution a reduction in level would result in a positive increase in count much larger than the decrease associated with an equivalent upward shift in level. It should be noted that the signal from the photo detector is a function of the area and not the diameter and therefore if linear amplification is used the change in perceived particle size is proportional to the square root of the change in threshold setting.

The signal from the photo detector is a function of the rate at which the light source in the sensor is blocked. This is in

turn a function of the size of the particle and the flow rate.

If the amplifiers and associated circuitry do not exhibit acceptable frequency response, the output for a given particle size is lower for increasing flow rate. This effect is the same as increasing the threshold level so that increasing flow causes reduced counts. If the apparatus is calibrated in too high a flow region it will be operating within only a portion of the normal electronic regions.

The lowest particle size which can be counted accurately is for any particular instrument configuration ultimately determined by the signal to noise ratio. Any counter exhibits a random signal which results from vibration of sensor elements, electromagnetic interference and thermal emission. Instrument design and environment influence this phenomenon to a considerable degree but it cannot be eliminated; there is a threshold below which the counter will register the passage of a particle even when the sensor is empty. Electromagnetic fields may induce electrical impulses of a magnitude well above the normal noise level. While these might properly be called procedural problems related to the environment, the sensitivity to such phenomena are so strongly related to circuit design that they must be considered functional.

All of the light blocking counters currently in use employ asynchronous counting. Therefore it is essential that the signal from the photo detector fall below the threshold level for a sufficient length of time for the comparator and counter circuits to reset. This implies that no particle or group of particles with a total area greater than the size of interest may be in the sensor during the reset interval.

If all the sources of error described thus far were eliminated one would still expect some variation in repeated counts (unless by some means all the fluid in the population were counted) due to the natural difference in samples. In addition there exists a possibility that two or more particles will be passing through the sensor simultaneously. This phenomenon is called coincidence and is widely discussed in the literature and among users of particle counters. Coincidence is offered as an explanation for nearly every major defect including saturation.

It is apparent that not all of the potential sources of error can be of equal significance. In order to determine the appropriate statistical control techniques for evaluating particle count uncertainty, it is necessary to determine the degree to which each potential error can occur and the influence of the error on the resulting count. This is developed in the next chapter.

## CHAPTER IV

### ANALYSIS OF THE ERROR PROBABILITIES

In order to evaluate the error probabilities it is necessary to postulate a model for the appearance of the particles in the sensing zone. Most investigators have proposed the Poisson model. This is attractive both for the tractability of the mathematics and from experience with similar mechanisms encountered in industrial and natural processes. Analysis of a large amount of particle count data from various sources shows excellent agreement with this hypothesis.

The Poisson is a distribution on the number of occurrences in some interval or area [7]. The probability mass function is

$$P(X = x; \lambda) = \frac{e^{-\lambda} \lambda^x}{x!} ; X = 1, 2, \dots, n. \quad (4-1)$$

Lambda has units of occurrences per unit opportunity. In the case of estimating the coincidence probability this is particles per sensor volume which can be estimated as particles per millilitre of fluid multiplied by the volume of the sensing zone in millilitres. Thus for a particular particle size lambda can be estimated if the distribution is known. For example using Cole's model for A.C. Fine Test Dust the number of particles greater than 10 micrometers is

$$N > 10 = Ke^{-\beta \lambda t^2 D} = 144 \text{ particles per microgram , } \quad (4-2)$$

where

$$K = 1751.9, \text{ and}$$

$$\beta = 0.4714.$$

In a 28 mg/l solution of test fluid this would yield a Lambda of .11 with a sensor volume of  $2.58 \times 10^{-5}$  ml. The probability of 2 or more particles residing in the sensor simultaneously is given by

$$P(2 \text{ or more}) = 1 - P(1 \text{ or less}) = 1 - \sum_{K=0}^1 \frac{e^{-\lambda} \lambda^K}{K!} . \quad (4-3)$$

Unfortunately, repeated tests by a number of investigators including the particle counter manufacturer have shown that the ratio of observed count to expected count under these conditions is about .90 which implies a .10 coincidence probability. A careful analysis of the requirement for coincidence error reveals that this is almost certainly not occurring in any realistic particle counting situation.

If any two or more particles of a size greater than the threshold size (D) appear in the window at the same time, a count will be missed. If a particle of size  $\geq D$  and any quantity of particles  $< D$  appear simultaneously, no error occurs. However, if two or more particles of size  $< D$ , whose combined area is greater than the area associated with D, appear during an interval when no particle greater than D is in the sensor, a false count will be recorded (see Figure 4).

Analyzing multiple occurrences of particles in various size intervals requires that Lambda be a function of particle size and that the probabilities be evaluated for an infinite number of intervals. This

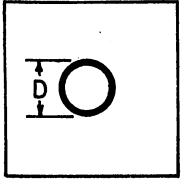

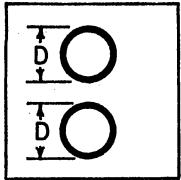
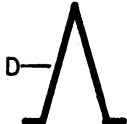
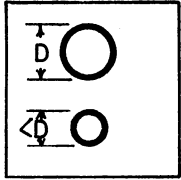
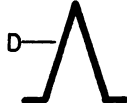
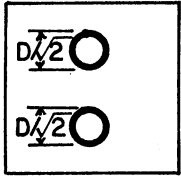

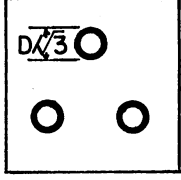

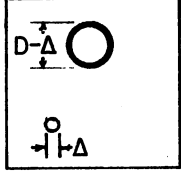

| PHOTO-DETECTOR VIEW   | PULSE   | OBSERVED COUNT | CORRECT COUNT | ERROR |
|---|---|----------------|---------------|-------|
|    |    | 1              | 1             | 0     |
|    |    | 1              | 2             | -1    |
|   |   | 1              | 1             | 0     |
|  |  | 1              | 0             | +1    |
|  |  | 1              | 0             | +1    |
|  |  | 1              | 0             | +1    |

Figure 4. Coincidence Error

of zero occurrences in an interval of time  $t$  is

$$P(0) = e^{-\lambda t} \quad (4-5)$$

where  $\lambda$  has the same meaning as described earlier. To translate  $\lambda$  from the volume domain to the time domain requires the consideration of flow through the sensor which is 30 ml per minute in current practice. Thus

$$\lambda = \frac{.11 \text{ particles}}{2.58 \times 10^{-5} \text{ ml}} \times \frac{30 \text{ ml}}{\text{min}} \times \frac{60 \text{ min}}{\text{sec}} = 2131.78 \quad (4-6)$$

considering the particle to be a point (a reasonable assumption for particles which are substantially smaller than the sensing volume) the time for a particle to transit the sensor is

$$\frac{2.58 \times 10^{-5} \text{ ml}}{.5 \text{ ml/sec}} = 5.16 \times 10^{-5} \text{ sec} \quad (4-7)$$

The particle counter requires a reset time of 12  $\mu$ s so that the total time between particles must be  $63.6 \times 10^{-6}$  sec. Therefore the probability that reset will occur is

$$e^{-2131.78(63.6 \times 10^{-6})} = .87 \quad (4-8)$$

which shows excellent correlation with published data [8, 9]. The equation can be generalized as follows

$$P(\text{count}) = e^{-N_D(V_S + QT_R)} \quad (4-9)$$

where

$N_D$  = actual number of particle  $\geq$  size  $D$ ,

$V_S$  = sensor volume,

$Q$  = flow rate, and

$T_R$  = minimum time to reset.

The error rate is sensitive to flow rate, especially for large reset times, which has also been documented by Moore [10].

The reduction in particle count due to increases in flow rate may also be caused by roll-off of the amplifier circuits as a function of the frequency response. However, the rate of change of the area shaded by a particle is a function only of the sensor configuration, particle size and particle velocity, thus the count loss due to frequency response characteristics is independent of particle concentration in the fluid. The effects of roll-off and reset error can therefore be separated.

If the coincidence and reset constraints are met, a lower bound can be placed on the counting uncertainty by virtue of the Poisson assumption. As has been implied in the earlier discussion, the parameter  $\lambda$  can be estimated from the particle counts. The unbiased point estimate of  $\lambda$  [11] can be determined as the ratio of total occurrences to the total opportunity. In the volume domain this is

$$\lambda = \frac{\text{particle count} \times \text{volume of sensor}}{\text{volume counted}} . \quad (4-10)$$

Probabilities of various particle counts can be computed readily using Equation (4-1). As a practical matter we are seldom concerned with a single count; the use of averages of five counts is the common practice. For this case we utilize the central limit theorem and the characteristics of the Poisson which dictate that the mean and the variance are both equal to  $\lambda$  [11], so that the confidence limits



on the mean are

$$n + \frac{1}{2} c_{\alpha/2}^2 \pm \sqrt{(n c_{\alpha/2}^2 + \frac{1}{4} c_{\alpha/2}^4)} \quad (4-11)$$

where  $c_{\alpha}$  is the upper  $\alpha$  point of the unit normal distribution and  $n$  is the estimate of  $\lambda$ . For large values of  $n$  this can be approximated by

$$n + c_{\alpha/2} \pm \sqrt{n} \quad (4-12)$$

The effects of volume measurement and dilution error are linear with particle count while sampling, mixing and cleanliness problems will most likely be more pronounced in the smaller particle sizes. There is no way to predict such errors individually from an unknown sample but various experimental designs incorporated into the calibration procedure can assign expected upper limits to these effects.

For example if solutions of A. C. Fine Test Dust of 2, 5, 10, 20, and 50 are diluted by 2 to 1, 5 to 1, etc., the resulting counts should be within the same limits as repeated samples from 1 mg/l solution. The variation in excess of this amount must be attributed to procedure. The uncertainty associated with procedural defects must be incorporated in any estimate of the accuracy of the particle counting process.

Industrial specifications that require contamination assessment for measuring performance criteria must be based on the assumption that reproducible and accurate particle counting is performed. Each of the potential sources of error must be evaluated and controlled by a methodology which is essentially free from subjective judgement.

The next chapter presents a general procedure which meets this objective.

## CHAPTER V

### PROPOSED CONTROL PROCEDURE FOR PARTICLE COUNTING

The extent of the uncertainty which can be tolerated in any measurement is related to the intended use of resulting information. The tape measure which is wholly satisfactory to the carpenter, finds little use in a precision machine shop. In the same manner, a laboratory attempting to identify small differences in filters would require much greater precision and repeatability in particle counting than would be needed for field contamination assessment of operating systems.

The flow rate and concentration effects inherent in the particle counter impose a direct trade off between minimal uncertainty and operating flexibility. The design of many particle counters is such that narrow confidence intervals would dictate such low concentration that virtually every sample would require dilution. The limitation of the procedural capabilities would effectively eliminate such instruments. In the recommendations which follow, this problem is avoided by addressing only the question of establishing .90 confidence limits. These limits may be too restrictive, but the techniques presented are not limited to the particular value chosen.

The calibration of the instrument must be accomplished independently of procedural errors if this is at all possible. The ANSI B93.28-1973 Standard avoids this question by pre-supposing that the

laboratory is fully competent in such areas. This approach is necessary to some extent as the standard contaminate (A.C. Fine Test Dust) is a particulate solid and must be suspended in a fluid for use. There are now a number of organizations marketing certified suspensions. Regardless of the source, the procedure must begin from an established base which is a solution containing a known concentration of A.C. Fine Test Dust.

The concentration to be used for calibration of the threshold levels of the counter must be such that the error due to the minimum reset time requirement is small. This is recognized in the ANSI Standard by placing the saturation procedure first. If the reset error is to be maintained at less than 1% then the value of  $N_D (V_S + QT_R)$  must be less than .01. If  $V_S$  or  $T_R$  is not known, an empirical approach such as a least squares fit to EG (4-9). If the equation is formulated as

$$\frac{N_C}{N_D} = ae^{-bN_D} \quad (5-1)$$

and repeated observations are made at various fluid concentrations, then

$$b = \frac{\sum X_i \ln Y_i - \frac{1}{n} (\sum X_i) (\sum \ln Y_i)}{\sum X_i^2 - \frac{1}{n} (\sum X_i)^2} \quad (5-2)$$

where  $X_i$  is the actual count and  $Y_i$  the ratio of observed count to actual count for the  $i^{\text{th}}$  concentration.  $b$  is a good approximation to  $(V_S + QT_R)$ . The coefficient  $a$  is given by

$$a = \exp \left[ \frac{\sum \ln Y_i}{n} - \frac{b \sum X_i}{n} \right] \quad (5-3)$$

and is a measure of the calibration error and should be equal to one for a correctly calibrated particle counter. The use of this method is shown in Figure 5, based on data from a HIAC particle counter.

The flow rate used for calibration must be such that frequency response is not a significant factor. Many of the counters in use do not exhibit such a region. It may be necessary for the purpose of developing a practical standard to require only that the flow rate be held within the range .99 to 1.01. Counters with poor frequency response characteristics would then be limited to a very narrow flow rate tolerance.

It is advantageous to determine the ultimate limitations of the counting process, at least approximately, before proceeding to the final calibration. This can be accomplished by testing the null hypothesis that a series of counts of a constant concentration are distributed as the Poisson with  $\lambda$  equal to the mean. Such a test is given by [12]

$$\chi^2 = \sum_{i=1}^m \frac{(f_i - e_i)^2}{e_i} \quad (5-4)$$

where

$f_i$  = observed frequency, and

$e_i$  = the expected frequency.

The null hypothesis is rejected if

$$\chi^2 \geq \chi_{\alpha, m-2}^2$$

where

$m$  = number of terms added, and  $\alpha$  = confidence level.

This test is not very practical for use with very small samples

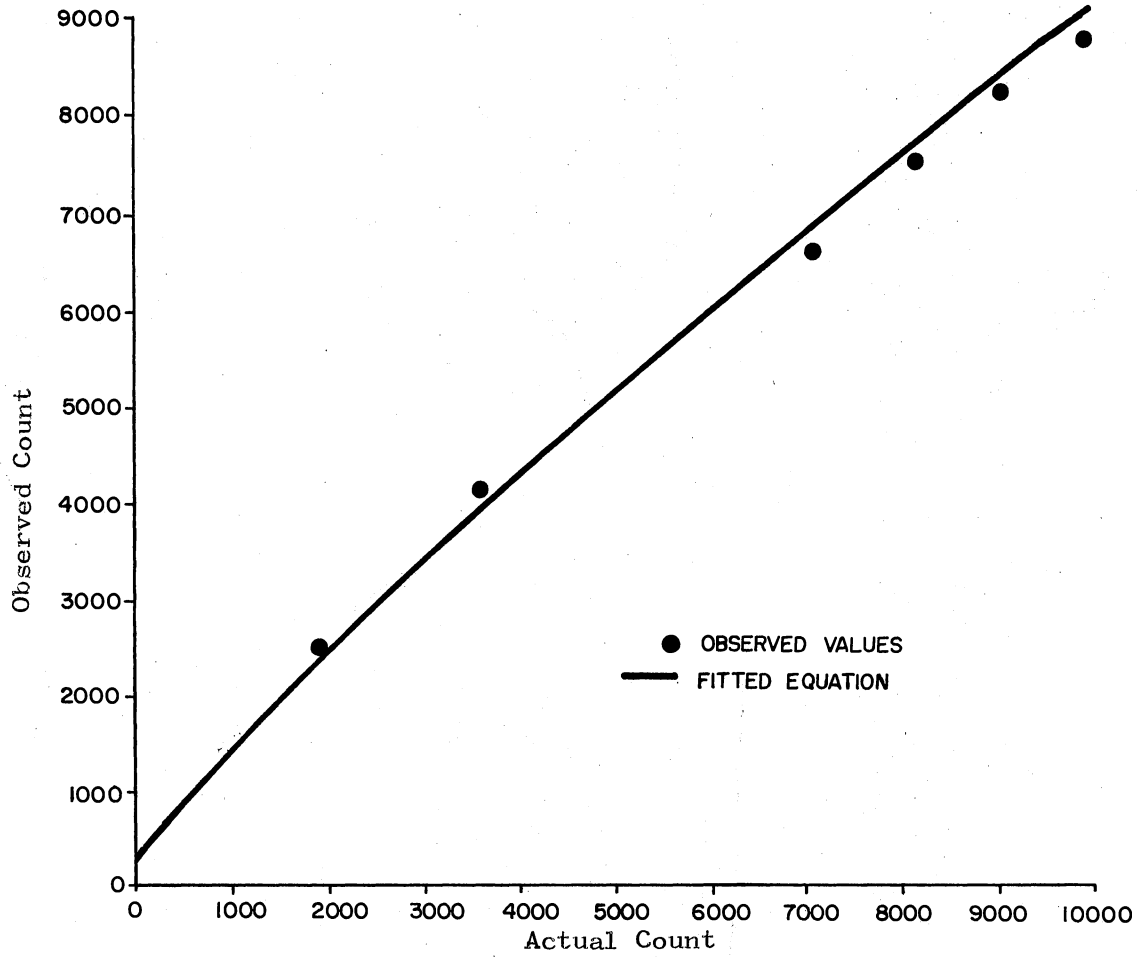


Figure 5. Analysis of Saturation Data

since the observed frequency for a particular value is almost certain to be 1. An alternative is proposed by Cox and Lewis [11] of the form

$$d = \sum_{i=1}^k \frac{(n_i - \bar{n})^2}{n} \quad (5-5)$$

where

$n$  = the observed value and

$\bar{n}$  = the mean value of  $k$  observations.

This is essentially a test of the hypothesis that  $\lambda = \bar{n}$  which is precisely the question posed.  $d$  is approximately distributed as Chi Square with  $k - 1$  degrees of freedom.

A large sample of particle count data collected by the Fluid Power Research Center was evaluated with this test. The results are summarized in Table I, and the original data are contained in the appendix. The tests are ranked in increasing order of the mean count, and it can be seen that the number of samples which do not fit the Poisson model increases rapidly at the higher levels, where saturation is probably a factor. In the cases where rejection occurs at the lower levels, such as ID No. 328C5, it is obvious that spurious counts were included at the 20 and 30 micrometer level.

If the null hypothesis is rejected the test may be altered as follows. If the principle deviation from Poisson behavior is caused by variation in volume counted, the variance of the volume, which is in fact a variation in  $\lambda$ , may be independent of the volume measured. Thus  $\bar{n} = f(N_D, V, X)$  where  $X$  is a R.V. with a mean of zero and  $V$  is the volume counted. If volume measurement is the dominant error, it should

TABLE I

## TEST FOR POISSON FIT OF PARTICLE COUNT DATA

| TEST FOR POISSON FIT... * INDICATES REJECTION AT .10 SIGNIFICANCE |       |         |         |    |         |     |         |     |         |     |         |     |
|---|-------|---------|---------|----|---------|-----|---------|-----|---------|-----|---------|-----|
| CBS   | ID    | MMCS    | TEST5   | R5 | TEST10  | R10 | TEST20  | R20 | TEST30  | R30 | TEST40  | R40 |
| 1   | 329B7 | 2587.4  | 1.757   |    | 3.8195  |     | 2.3514  |     | 5.7273  |     | 9.0000  | *   |
| 2   | 329B8 | 2751.4  | 9.721   | *  | 4.0153  |     | 2.7761  |     | 5.2857  |     | 2.6667  |     |
| 3   | 328C8 | 3351.6  | 5.343   |    | 1.2203  |     | 0.5872  |     | 1.0000  |     | 9.7647  | *   |
| 4   | 328C7 | 3536.8  | 1.555   |    | 0.9795  |     | 3.6667  |     | 1.2308  |     | 0.6667  |     |
| 5   | 328C6 | 3761.0  | 12.516  | *  | 3.0349  |     | 5.8033  |     | 4.2222  |     | 5.3333  |     |
| 6   | 328C5 | 3806.2  | 6.328   |    | 4.0000  |     | 8.5000  | *   | 10.3636 | *   | 3.7143  |     |
| 7   | 329B6 | 3841.4  | 0.292   |    | 2.8218  |     | 2.2963  |     | 5.8182  |     | 4.0000  |     |
| 8   | 328J4 | 4061.4  | 7.804   | *  | 6.6184  |     | 3.5000  |     | 4.6250  |     | 3.0000  |     |
| 9   | 328J3 | 4087.0  | 123.555 | *  | 7.0153  |     | 6.8571  |     | 3.2500  |     | 1.0000  |     |
| 10  | 328J2 | 4518.4  | 13.138  | *  | 1.0433  |     | 1.9420  |     | 6.3333  |     | 5.6667  |     |
| 11  | 329B5 | 4523.8  | 13.950  | *  | 7.4171  |     | 12.9620 | *   | 6.5185  |     | 13.8571 | *   |
| 12  | 328I1 | 4611.6  | 4.910   |    | 5.4422  |     | 2.0000  |     | 5.0000  |     | 3.5000  |     |
| 13  | 328J1 | 4884.2  | 9.443   | *  | 3.5967  |     | 3.5303  |     | 3.0526  |     | 2.0000  |     |
| 14  | 328G1 | 4928.6  | 12.002  | *  | 6.4031  |     | 5.8136  |     | 5.1875  |     | 11.2727 | *   |
| 15  | 328G3 | 5113.8  | 17.465  | *  | 3.6471  |     | 5.1264  |     | 3.3750  |     | 12.2857 | *   |
| 16  | 328G2 | 5116.0  | 28.239  | *  | 0.3870  |     | 5.2187  |     | 2.7500  |     | 3.5000  |     |
| 17  | 328I3 | 5588.4  | 3.865   |    | 4.4248  |     | 5.8681  |     | 3.1111  |     | 1.2727  |     |
| 18  | 328I2 | 5626.8  | 2.926   |    | 0.1620  |     | 3.4468  |     | 1.2000  |     | 0.4615  |     |
| 19  | 328G4 | 6366.0  | 48.503  | *  | 2.2613  |     | 17.3902 | *   | 8.5882  | *   | 16.0000 | *   |
| 20  | 328I4 | 7157.2  | 18.676  | *  | 2.2528  |     | 15.1613 | *   | 9.3333  | *   | 5.3333  |     |
| 21  | 334C5 | 25268.4 | 72.001  | *  | 3.7023  |     | 2.8950  |     | 8.0000  | *   | 8.2500  | *   |
| 22  | 329B3 | 26731.8 | 50.685  | *  | 16.3964 | *   | 6.4927  |     | 9.8394  | *   | 14.4444 | *   |
| 23  | 329B4 | 29094.2 | 271.623 | *  | 38.2751 | *   | 4.9944  |     | 9.7828  | *   | 13.3176 | *   |
| 24  | 329B2 | 29149.0 | 206.696 | *  | 85.3937 | *   | 53.6018 | *   | 36.0676 | *   | 36.1250 | *   |
| 25  | 329B1 | 30415.0 | 208.802 | *  | 50.8339 | *   | 21.8071 | *   | 28.9496 | *   | 38.3701 | *   |
| 26  | 328C4 | 30952.8 | 193.357 | *  | 46.5396 | *   | 42.9070 | *   | 46.9036 | *   | 50.0036 | *   |
| 27  | 328G5 | 31485.0 | 3.150   |    | 10.5952 | *   | 10.0219 | *   | 18.8423 | *   | 19.6364 | *   |
| 28  | 328I5 | 31521.8 | 8.336   | *  | 15.6651 | *   | 21.4829 | *   | 24.3861 | *   | 17.6792 | *   |
| 29  | 328I6 | 31724.2 | 253.155 | *  | 25.1213 | *   | 22.3812 | *   | 52.3867 | *   | 46.7124 | *   |
| 30  | 328G7 | 31993.0 | 2.315   |    | 4.0323  |     | 10.9198 | *   | 7.3881  |     | 12.6836 | *   |
| 31  | 328G6 | 32097.0 | 7.941   | *  | 5.2009  |     | 6.3798  |     | 4.2670  |     | 6.2110  |     |
| 32  | 334C8 | 32332.2 | 106.773 | *  | 6.1275  |     | 5.4041  |     | 3.5556  |     | 2.3333  |     |
| 33  | 328I7 | 32545.6 | 113.942 | *  | 25.6854 | *   | 11.4016 | *   | 18.0359 | *   | 26.0885 | *   |
| 34  | 328C3 | 32799.8 | 10.900  | *  | 8.8920  | *   | 26.2195 | *   | 38.4678 | *   | 50.6753 | *   |
| 35  | 328J7 | 33320.8 | 4.373   |    | 7.8756  | *   | 14.5221 | *   | 36.9158 | *   | 30.1148 | *   |
| 36  | 328I8 | 33483.2 | 192.770 | *  | 40.2330 | *   | 19.8845 | *   | 18.6050 | *   | 19.8304 | *   |
| 37  | 328J5 | 34671.4 | 239.525 | *  | 55.6834 | *   | 28.9261 | *   | 17.7631 | *   | 10.6499 | *   |
| 38  | 328J6 | 34821.6 | 82.803  | *  | 6.3777  |     | 4.7050  |     | 6.5303  |     | 2.1862  |     |
| 39  | 328G8 | 34908.4 | 67.713  | *  | 18.3826 | *   | 8.1226  | *   | 5.5868  |     | 8.1719  | *   |
| 40  | 328C2 | 35322.2 | 15.650  | *  | 22.7216 | *   | 16.5303 | *   | 34.5419 | *   | 23.3919 | *   |
| 41  | 328J8 | 35556.8 | 29.693  | *  | 14.0220 | *   | 9.6149  | *   | 6.7526  |     | 10.3500 | *   |
| 42  | 328C1 | 36229.2 | 74.126  | *  | 7.7686  |     | 25.6976 | *   | 33.0524 | *   | 53.5914 | *   |
| 43  | 334C6 | 41969.4 | 97.213  | *  | 3.2513  |     | 1.7706  |     | 5.4211  |     | 5.6667  |     |
| 44  | 334C7 | 50803.6 | 9.983   | *  | 3.6414  |     | 4.9988  |     | 2.7879  |     | 6.0000  |     |
| 45  | 334C1 | 59995.4 | 48.805  | *  | 13.3831 | *   | 4.6624  |     | 16.4757 | *   | 16.8702 | *   |
| 46  | 334C4 | 68745.0 | 41.838  | *  | 9.4989  | *   | 5.2160  |     | 7.9460  | *   | 12.2215 | *   |
| 47  | 334C2 | 72436.8 | 44.470  | *  | 9.4267  | *   | 1.0205  |     | 2.2633  |     | 12.6742 | *   |
| 48  | 334C3 | 84453.8 | 48.823  | *  | 4.7178  |     | 3.6542  |     | 9.0407  | *   | 15.4639 | *   |

be possible to find a counting volume for which  $d$  is not sufficient to reject  $H_0$ .

It should be noted that the methods used in most volume measuring mechanisms is such that the error is increasing for increasing flow rate. For this reason it is desirable to repeat the flow and reset error analysis after the optimum volume is selected.

The final calibration procedure specified in the A.N.S.I. Specification requires very little alteration. The grand average of a series of particle counts of a correctly calibrated counter converges stochastically on the correct value. The problem for the user is to determine when to stop adjusting the machine. The Shewhart control chart provides this information. However it may be desirable to modify the chart by using the Poisson model, for which the control limits for .90 confidence are given in Chapter IV, specifically

$$N + 0.98 \pm \sqrt{3.84N + 3.69} \quad .$$

These limits replace those calculated as the setting tolerance. The range chart is replaced by the test for a Poisson distribution. The value of  $d$  must not exceed 7.779.

If the counter is properly calibrated and conforms to a Poisson process, the same procedure can be used to provide a confidence interval on counts from an unknown sample. The use of the  $d$  statistic provides a continuing measure of procedural control.

When unknown samples are evaluated, another source of error is raised particularly if the sample represents a system which incorporates a filter. The particle count distribution may not follow the  $\log\text{-}\log^2$  model or even if it does, the slope parameter may be so large that the



particles in the size range below the counting level are so many as to create a significant coincidence factor. An analysis of this phenomenon requires the evaluation of a Gamma function with a parameter  $\lambda$  which is in turn a function of particle size. There is no analytical method available for solving this equation but a simulation technique could be applied. Even this approach requires that the particle distribution be known. As a practical alternative it may be advisable to use the lowest size for which the counter is calibrated as a check on the next higher level so that the former is not reported nor used as a reliable count. The optimum size interval for such a practice is probably  $D$  to  $D/\sqrt{2}$  although this does not preclude errors induced by a drastic change in slope below the lower count level. Although not specifically a part of the calibration and control procedure, such consideration must be given in the practical application of particle counting.

## CHAPTER VI

### CONCLUSIONS AND RECOMMENDATIONS

An analytical description of the particle counting process has been developed. The models postulated are fundamental and are applicable to any counter using the light reduction technique. Each of the basic sources of error in the particle counting process is evaluated and a mathematical technique is formulated to measure the degree to which that error is contributing to the total uncertainty.

There are four key elements in the calibration and control process:

- (1) The determination or estimation of the concentration saturation curve to locate a suitable operating region.
- (2) The evaluation of the extent of procedural errors affecting the count, especially the effect of volume measurement error.
- (3) The determination of sufficient convergence of the mean count with the true value to justify termination of the calibration procedure.
- (4) The continued surveillance of observed counts to detect the onset of procedural defects, saturation or coincidence error.

#### Recommendations for Further Development

The present American National Standard has two major weaknesses, both related to the use of the normal distribution model to develop

control limits for a Shewhart Chart. The saturation level is determined by counting at increasing concentrations until the average count falls outside the control limits. If the procedure is begun at too high a concentration, the control limits change as rapidly as the mean, and no out-of-control level is reached.

This procedure should be replaced using the same data to fit Equation (5-1). Saturation could then be defined as the point at which the ratio  $N_C/N_D$  falls below an arbitrary value.

A Shewhart Chart is also used to terminate calibration and provide continued control of the counting process. The control limits (called a setting tolerance in the ANSI standard) should be determined with Equation (4-11) with Equation (5-5) used to establish that the counting procedure is properly conducted.

The exact levels of confidence and numerical values are not purely technical questions. There are economic implications which must be considered. The selection of such values is properly a task of standards-formulating committees. A modified standard should be prepared and circulated to users for evaluation and comment. If the technique is generally acceptable and suitable parameters for the tests can be found, the document should be promulgated as a revised standard.

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**APPENDIX**

## F.P.R.C. PARTICLE COUNT DATA

----- ID=328C1 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 35597 | 6609  | 2312  | 982   | 462   |
| 2   | 36943 | 6661  | 2279  | 881   | 432   |
| 3   | 36231 | 6420  | 2119  | 874   | 393   |
| 4   | 37129 | 6466  | 2074  | 750   | 281   |
| 5   | 35246 | 6660  | 2061  | 829   | 346   |

----- ID=328C2 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 35051 | 6696  | 2270  | 987   | 486   |
| 2   | 35921 | 6729  | 2263  | 933   | 475   |
| 3   | 35432 | 6604  | 2189  | 918   | 446   |
| 4   | 35023 | 6349  | 2096  | 845   | 367   |
| 5   | 35184 | 6321  | 2062  | 761   | 400   |

----- ID=328C3 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 32295 | 6114  | 2062  | 869   | 389   |
| 2   | 33059 | 6086  | 1995  | 797   | 380   |
| 3   | 32942 | 5888  | 1920  | 733   | 299   |
| 4   | 32781 | 5977  | 1890  | 752   | 323   |
| 5   | 32922 | 5855  | 1765  | 637   | 232   |

----- ID=328C4 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 28910 | 5368  | 1809  | 737   | 333   |
| 2   | 31775 | 5900  | 1979  | 762   | 362   |
| 3   | 31740 | 5812  | 1977  | 812   | 390   |
| 4   | 31629 | 5856  | 1849  | 740   | 345   |
| 5   | 30710 | 5415  | 1638  | 568   | 222   |

----- ID=328C5 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 3808 | 106   | 9     | 1     | 1     |
| 2   | 3779 | 94    | 5     | 1     | 1     |
| 3   | 3854 | 118   | 16    | 6     | 3     |
| 4   | 3897 | 108   | 8     | 3     | 2     |
| 5   | 3693 | 94    | 6     | 0     | 0     |

## F.P.R.C. PARTICLE COUNT DATA

----- ID=328C6 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 3610 | 147   | 10    | 3     | 1     |
| 2   | 3790 | 143   | 8     | 1     | 0     |
| 3   | 3850 | 168   | 11    | 3     | 0     |
| 4   | 3864 | 145   | 19    | 5     | 0     |
| 5   | 3691 | 143   | 13    | 6     | 2     |

----- ID=328C7 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 3483 | 154   | 8     | 2     | 1     |
| 2   | 3564 | 155   | 13    | 3     | 1     |
| 3   | 3524 | 162   | 17    | 4     | 2     |
| 4   | 3535 | 163   | 11    | 2     | 1     |
| 5   | 3578 | 148   | 11    | 2     | 1     |

----- ID=328C8 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 3322 | 160   | 23    | 12    | 5     |
| 2   | 3323 | 171   | 20    | 10    | 7     |
| 3   | 3453 | 166   | 24    | 8     | 0     |
| 4   | 3380 | 158   | 20    | 11    | 4     |
| 5   | 3280 | 153   | 22    | 9     | 1     |

----- ID=328G1 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 4778 | 162   | 16    | 4     | 2     |
| 2   | 5011 | 191   | 30    | 7     | 0     |
| 3   | 4822 | 207   | 26    | 10    | 3     |
| 4   | 4977 | 178   | 27    | 8     | 6     |
| 5   | 5055 | 175   | 19    | 3     | 0     |

----- ID=328G2 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 4859 | 182   | 17    | 3     | 1     |
| 2   | 4988 | 178   | 13    | 5     | 1     |
| 3   | 5336 | 178   | 14    | 3     | 2     |
| 4   | 5202 | 171   | 14    | 4     | 0     |
| 5   | 5195 | 180   | 6     | 1     | 0     |

## F.P.R.C. PARTICLE COUNT DATA

----- ID=328G3 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 4849 | 227   | 21    | 6     | 5     |
| 2   | 5170 | 212   | 19    | 2     | 0     |
| 3   | 5187 | 219   | 11    | 3     | 1     |
| 4   | 5209 | 231   | 22    | 3     | 1     |
| 5   | 5154 | 250   | 14    | 2     | 0     |

----- ID=328G4 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 5976 | 274   | 30    | 8     | 4     |
| 2   | 6228 | 257   | 9     | 3     | 0     |
| 3   | 6386 | 250   | 15    | 3     | 0     |
| 4   | 6556 | 263   | 18    | 1     | 0     |
| 5   | 6684 | 280   | 10    | 2     | 0     |

----- ID=328G5 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 31630 | 5467  | 1808  | 756   | 343   |
| 2   | 31626 | 5447  | 1791  | 746   | 355   |
| 3   | 31364 | 5292  | 1711  | 708   | 343   |
| 4   | 31525 | 5204  | 1726  | 664   | 289   |
| 5   | 31280 | 5248  | 1644  | 619   | 265   |

----- ID=328G6 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 31988 | 5503  | 1859  | 755   | 362   |
| 2   | 32234 | 5524  | 1842  | 782   | 364   |
| 3   | 32474 | 5638  | 1909  | 822   | 420   |
| 4   | 31901 | 5529  | 1878  | 786   | 371   |
| 5   | 31888 | 5400  | 1764  | 750   | 369   |

----- ID=328G7 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 31924 | 5563  | 1896  | 762   | 371   |
| 2   | 31878 | 5638  | 1903  | 786   | 393   |
| 3   | 31909 | 5515  | 1850  | 753   | 360   |
| 4   | 32208 | 5448  | 1812  | 752   | 342   |
| 5   | 32046 | 5479  | 1730  | 686   | 304   |



## F.P.R.C. PARTICLE COUNT DATA

----- ID=328G8 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 33605 | 5752  | 1897  | 761   | 339   |
| 2   | 34888 | 6045  | 1928  | 803   | 409   |
| 3   | 35372 | 6119  | 2063  | 824   | 394   |
| 4   | 35538 | 6187  | 1970  | 839   | 402   |
| 5   | 35139 | 6059  | 1945  | 771   | 376   |

----- ID=328I1 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 4508 | 108   | 7     | 1     | 1     |
| 2   | 4584 | 145   | 11    | 4     | 0     |
| 3   | 4713 | 125   | 10    | 2     | 1     |
| 4   | 4612 | 127   | 6     | 3     | 2     |
| 5   | 4641 | 126   | 9     | 0     | 0     |

----- ID=328I2 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 5715 | 225   | 21    | 5     | 3     |
| 2   | 5614 | 228   | 21    | 4     | 3     |
| 3   | 5555 | 231   | 15    | 7     | 2     |
| 4   | 5666 | 232   | 23    | 4     | 2     |
| 5   | 5584 | 232   | 14    | 5     | 3     |

----- ID=328I3 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 5553 | 226   | 23    | 4     | 3     |
| 2   | 5488 | 223   | 10    | 2     | 2     |
| 3   | 5582 | 217   | 19    | 2     | 1     |
| 4   | 5667 | 240   | 22    | 4     | 3     |
| 5   | 5652 | 257   | 17    | 6     | 2     |

----- ID=328I4 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 6888 | 370   | 43    | 10    | 6     |
| 2   | 7146 | 354   | 29    | 6     | 2     |
| 3   | 7224 | 333   | 16    | 3     | 1     |
| 4   | 7134 | 364   | 27    | 6     | 2     |
| 5   | 7394 | 359   | 40    | 14    | 4     |

## F.P.R.C. PARTICLE COUNT DATA

----- ID=328I5 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 31207 | 5384  | 1788  | 718   | 322   |
| 2   | 31566 | 5464  | 1833  | 776   | 353   |
| 3   | 31747 | 5521  | 1873  | 810   | 370   |
| 4   | 31779 | 5395  | 1793  | 750   | 337   |
| 5   | 31310 | 5141  | 1617  | 634   | 270   |

----- ID=328I6 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 29226 | 5207  | 1749  | 700   | 313   |
| 2   | 32020 | 5616  | 1940  | 863   | 401   |
| 3   | 32652 | 5653  | 1882  | 816   | 391   |
| 4   | 32483 | 5531  | 1823  | 700   | 303   |
| 5   | 32240 | 5370  | 1688  | 619   | 254   |

----- ID=328I7 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 30847 | 5248  | 1711  | 652   | 279   |
| 2   | 33121 | 5681  | 1858  | 756   | 370   |
| 3   | 33108 | 5671  | 1884  | 793   | 389   |
| 4   | 32922 | 5681  | 1802  | 736   | 338   |
| 5   | 32730 | 5498  | 1753  | 680   | 297   |

----- ID=328I8 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 31222 | 5185  | 1701  | 724   | 342   |
| 2   | 34128 | 5769  | 1886  | 758   | 336   |
| 3   | 34209 | 5755  | 1930  | 823   | 403   |
| 4   | 33894 | 5620  | 1788  | 690   | 342   |
| 5   | 33963 | 5616  | 1751  | 678   | 287   |

----- ID=328J1 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 4722 | 259   | 27    | 7     | 3     |
| 2   | 4841 | 224   | 18    | 5     | 2     |
| 3   | 5003 | 251   | 28    | 11    | 5     |
| 4   | 4921 | 250   | 30    | 9     | 2     |
| 5   | 4934 | 231   | 29    | 6     | 3     |

## F.P.R.C. PARTICLE COUNT DATA

----- ID=328J2 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 4487 | 191   | 16    | 5     | 3     |
| 2   | 4507 | 173   | 11    | 1     | 0     |
| 3   | 4726 | 188   | 11    | 0     | 0     |
| 4   | 4464 | 187   | 16    | 3     | 2     |
| 5   | 4408 | 185   | 15    | 3     | 1     |

----- ID=328J3 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 3779 | 170   | 19    | 3     | 1     |
| 2   | 4691 | 218   | 17    | 0     | 0     |
| 3   | 3893 | 210   | 11    | 2     | 1     |
| 4   | 4071 | 193   | 7     | 1     | 1     |
| 5   | 4001 | 192   | 16    | 2     | 1     |

----- ID=328J4 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 3924 | 236   | 16    | 3     | 2     |
| 2   | 4059 | 245   | 18    | 1     | 1     |
| 3   | 4104 | 282   | 27    | 6     | 4     |
| 4   | 4054 | 233   | 20    | 4     | 2     |
| 5   | 4166 | 262   | 19    | 2     | 1     |

----- ID=328J5 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 32349 | 6056  | 2045  | 874   | 424   |
| 2   | 34189 | 6383  | 2180  | 944   | 504   |
| 3   | 35798 | 6658  | 2265  | 973   | 479   |
| 4   | 35488 | 6759  | 2365  | 1051  | 514   |
| 5   | 35533 | 6750  | 2323  | 928   | 464   |

----- ID=328J6 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 33345 | 6483  | 2279  | 997   | 470   |
| 2   | 34882 | 6736  | 2317  | 1003  | 493   |
| 3   | 35410 | 6627  | 2197  | 931   | 484   |
| 4   | 35163 | 6510  | 2213  | 928   | 471   |
| 5   | 35308 | 6633  | 2289  | 1006  | 509   |

## F.P.R.C. PARTICLE COUNT DATA

----- ID=328J7 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 33090 | 6251  | 2157  | 983   | 514   |
| 2   | 33443 | 6339  | 2189  | 1000  | 506   |
| 3   | 33401 | 6444  | 2185  | 961   | 491   |
| 4   | 33147 | 6195  | 1977  | 818   | 371   |
| 5   | 33523 | 6175  | 2110  | 813   | 504   |

----- ID=328J8 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 34654 | 6701  | 2263  | 958   | 470   |
| 2   | 35681 | 6943  | 2398  | 1038  | 538   |
| 3   | 35909 | 7138  | 2455  | 1068  | 550   |
| 4   | 35842 | 6892  | 2310  | 1025  | 486   |
| 5   | 35698 | 6937  | 2378  | 1000  | 482   |

----- ID=329B1 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 28238 | 4895  | 1704  | 666   | 300   |
| 2   | 30783 | 5428  | 1782  | 707   | 318   |
| 3   | 31516 | 5549  | 1773  | 679   | 331   |
| 4   | 30850 | 5152  | 1637  | 631   | 285   |
| 5   | 30688 | 5147  | 1554  | 531   | 198   |

----- ID=329B2 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 27723 | 4749  | 1443  | 576   | 248   |
| 2   | 29980 | 5316  | 1699  | 670   | 302   |
| 3   | 30804 | 5350  | 1710  | 612   | 239   |
| 4   | 28611 | 4793  | 1401  | 476   | 171   |
| 5   | 28627 | 4685  | 1632  | 626   | 240   |

----- ID=329B3 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 25839 | 4720  | 1485  | 552   | 225   |
| 2   | 26743 | 4825  | 1533  | 554   | 247   |
| 3   | 26595 | 4878  | 1506  | 552   | 238   |
| 4   | 27342 | 5089  | 1543  | 576   | 239   |
| 5   | 27140 | 4782  | 1419  | 480   | 176   |

## F.P.R.C. PARTICLE COUNT DATA

----- ID=32984 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 26832 | 5023  | 1609  | 617   | 278   |
| 2   | 29204 | 5389  | 1693  | 670   | 305   |
| 3   | 29742 | 5500  | 1709  | 595   | 255   |
| 4   | 29065 | 5270  | 1613  | 564   | 229   |
| 5   | 30628 | 5611  | 1650  | 611   | 246   |

----- ID=32985 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 4329 | 171   | 17    | 10    | 8     |
| 2   | 4471 | 171   | 18    | 4     | 3     |
| 3   | 4603 | 168   | 10    | 5     | 2     |
| 4   | 4577 | 159   | 8     | 2     | 0     |
| 5   | 4639 | 206   | 26    | 6     | 1     |

----- ID=32986 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 3815 | 149   | 10    | 2     | 1     |
| 2   | 3843 | 135   | 13    | 4     | 2     |
| 3   | 3858 | 124   | 7     | 0     | 0     |
| 4   | 3853 | 143   | 11    | 1     | 0     |
| 5   | 3838 | 145   | 13    | 4     | 2     |

----- ID=32987 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 2635 | 122   | 18    | 5     | 2     |
| 2   | 2605 | 132   | 18    | 8     | 5     |
| 3   | 2547 | 150   | 13    | 4     | 3     |
| 4   | 2579 | 137   | 13    | 4     | 0     |
| 5   | 2571 | 124   | 12    | 1     | 0     |

----- ID=32988 -----

| OBS | MIC5 | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|------|-------|-------|-------|-------|
| 1   | 2612 | 123   | 11    | 2     | 2     |
| 2   | 2748 | 118   | 11    | 0     | 0     |
| 3   | 2793 | 139   | 15    | 4     | 2     |
| 4   | 2817 | 146   | 12    | 3     | 2     |
| 5   | 2787 | 129   | 18    | 5     | 3     |

## F.P.R.C. PARTICLE COUNT DATA

----- ID=334C1 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 58497 | 6844  | 2041  | 892   | 446   |
| 2   | 60397 | 7160  | 2124  | 877   | 398   |
| 3   | 60366 | 7222  | 2064  | 804   | 369   |
| 4   | 60604 | 6976  | 2029  | 782   | 365   |
| 5   | 60113 | 6975  | 1992  | 761   | 341   |

----- ID=334C2 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 70918 | 7776  | 2184  | 870   | 437   |
| 2   | 73155 | 8091  | 2197  | 825   | 406   |
| 3   | 73035 | 8114  | 2134  | 817   | 352   |
| 4   | 72639 | 7922  | 2174  | 819   | 358   |

----- ID=334C3 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 83421 | 9206  | 2334  | 873   | 422   |
| 2   | 83629 | 9137  | 2317  | 908   | 442   |
| 3   | 84324 | 9361  | 2380  | 928   | 422   |
| 4   | 85886 | 9387  | 2265  | 842   | 374   |
| 5   | 85009 | 9268  | 2278  | 821   | 347   |

----- ID=334C4 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 67290 | 8725  | 2277  | 895   | 462   |
| 2   | 69417 | 9113  | 2394  | 884   | 418   |
| 3   | 68745 | 8912  | 2334  | 856   | 382   |
| 4   | 69159 | 9030  | 2300  | 832   | 407   |
| 5   | 69114 | 8940  | 2253  | 793   | 372   |

----- ID=334C5 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 24996 | 826   | 45    | 9     | 4     |
| 2   | 24462 | 776   | 48    | 7     | 3     |
| 3   | 25030 | 783   | 37    | 1     | 0     |
| 4   | 25635 | 840   | 50    | 5     | 1     |
| 5   | 26219 | 806   | 39    | 3     | 0     |

## F.P.R.C. PARTICLE COUNT DATA

----- ID=334C6 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 40632 | 1624  | 100   | 2     | 0     |
| 2   | 41210 | 1644  | 95    | 9     | 3     |
| 3   | 42389 | 1707  | 108   | 10    | 0     |
| 4   | 42551 | 1705  | 109   | 9     | 1     |
| 5   | 43065 | 1663  | 111   | 8     | 2     |

----- ID=334C7 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 50221 | 2474  | 191   | 14    | 1     |
| 2   | 51080 | 2507  | 156   | 16    | 1     |
| 3   | 50770 | 2413  | 166   | 8     | 0     |
| 4   | 50846 | 2428  | 161   | 14    | 3     |
| 5   | 51101 | 2521  | 157   | 14    | 0     |

----- ID=334C8 -----

| OBS | MIC5  | MIC10 | MIC20 | MIC30 | MIC40 |
|-----|-------|-------|-------|-------|-------|
| 1   | 31706 | 2111  | 153   | 12    | 1     |
| 2   | 31020 | 2055  | 186   | 12    | 1     |
| 3   | 32740 | 2180  | 159   | 6     | 2     |
| 4   | 33114 | 2154  | 182   | 8     | 0     |
| 5   | 33081 | 2197  | 159   | 7     | 2     |

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