# DETERMINATION OF VARIATIONS IN CERTAIN <br> MECHANICAL PROPERTIES ACROSS THE <br> WIDTH OF A FINISHED PRODUCT <br> OF POLYPROPYLENE WEB 

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Thesis Approved:


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## CHAPTER I

## INTRODUCTION

A web is a long continuous film of material with its length much greater than its width or thickness. Used in most high production rate plants, webs can be any material, from paper to steel, that can be processed on a continuous basis. This rapid handling of material benefits the user by reducing time of production, but the web form can sometimes cause serious problems.

Out of plane deformation of the web, e.g. waves, can ruin the finished product, costing the producer untold dollars in not only time but material. If some way can be determined to predict when waves occur, then methods of prevention could be investigated. Some base information has to be established before one can begin to predict such a complicated instability.

The aspects of the web that should be investigated include: yield strength, Young's modulus and anistropy. Usually, averages of these values are reported, but local values are also needed to determine how processing is affecting the web's properties. A profile of these properties across the width of the final product could provide useful information on the local attributes that may
lead to waves and other instabilities.
It is proposed that the processing may cause variations across the web and that under certain conditions in handling or winding, these may be extremely harmful to the final product. This probe determines what variations in mechanical properties across the width of a finished product of web exist and develops techniques to measure as many of these variations in a static testing mode as possible to help prevent disastrous results. Once the techniques have been established and data is obtained, methods of presenting the information in a useful manner will be explored. Anistropy, local mechanical properties, and other parameters will be investigated to ascertain their effects, if any, on the onset of wave formation in association with the biaxial orientation process.

## CHAPTER II

## BACK GROUND

Material properties of polypropylene and polyester vary with respect to the history of their processing. Young's moduli of polypropylene range from loo to 575 ksi [19]. The Young's moduli for polyester range from 280 to $3,500 \mathrm{ksi}$ depending on the type of reinforcement. The maximum yield strengths are 4.5 to 5.4 ksi and 23 ksi for polypropylene and polyester, respectively [19].
"The glass transition is associated with the amorphous phase of a polymer and occurs at a temperature Tg at which segments of the main chain become mobile" [2]. Polypropylene is brittle below this temperature before the biaxial orientation is performed. The range of glass transition temperature for polypropylene is -30 C to 20 C , depending on tacticity and thermal history [2]. Polyester's glass transition ranges from 73 C to 81 C [19].

Biaxial orientation is the process that produces equal or balanced material properties in two perpendicular directions [2l]. In polymers, this is achieved by heating the material above the glass transition temperature (to allow greater ease of chain disentanglement and slippage) while stretching in the MD until the desired MD modulus and
yield strength are obtained. Then stretching the material in the $C D$ is utilized until the desired $M D$ and $C D$ properties are equal. This stretching process is akin to work hardening, also known as strain hardening in metals. As the polymer is stretched, higher values for the. properties are achieved (see figure 2.1). "Strain hardening continues by molecular alignment (sometimes called cold drawing) up to the fracture stress" [22]. From a random orientation, the polymeric chains are aligned approximately parallel to the applied stress [8]. This alignment brings the chains closer together where mutual attraction increases, especially when the chains are polar or symmetrical. As the stretching takes place, bond stretching or valence angle deformation also results. This is the elastic component of the biaxial stretching and is recovered when the applied stress is removed. Bond stretching, the viscous flow of molecular chains past one another, causes friction losses that cannot be recovered. All three molecular activities must be considered when determining the amount of overall elongation needed for the desired product. The main goals of the biaxial orientation process is to achieve molecular alignment of polymeric chains which increases strength, decreases brittleness and eliminates anistropy.

When dealing with polymers, viscoelastic effects must be examined. Viscoelasticity characteristics are between those of metals and viscous fluids. The models shown in


Figure 2.l Stress-strain behavior usually found in crystalline polymers. [22]
figure 2.2 represent viscoelasticity. Keep in mind that this model is a highly simplified representation of the very complex polymer response. The springs, each with a different spring constant, in the models symbolize the elastic portions of the response which include bond stretching, crystallinity and chain rigidity [19]. Representing the fluid time dependent response, the dashpots each have a different viscosity. Figure 2.3 shows the standard time versus strain viscoelastic response. Stress and strain in this type of a model are time, rate of loading and temperature dependent. "Plastics have no true proportion limits" [19]. Most polymers have a curvilinear stress-strain curve. Depending on the polymer, test temperature and thermal history, length of the linear segment of the curve can vary greatly. Using moduli obtained from these linear regions, the prediction of deformation is very difficult. A polymer's yield point does not indicate the onset of "significant flow" as it does for most metals. The yield point is defined, in the case of polymers, in the general area of the "knee" in the engineering stress-strain curve. This "knee" is due to thinning of the cross-sectional area of the polymer in the tensile test. If true stress, based on instantaneous cross-sectional area rather than initial area, were plotted versus true strain, the "knee" would be much less defined. It is interesting to note that in general polymers' Poisson's ratios are much greater than those found in

(a)

(b)

(c)

(d)

(e)

Figure 2.2 Mechanical analogs reflecting processes in polymeric solids:
(a) elastic; (b) pure viscous;
(c) Maxwell model for
viscoelastic flow; (d) Voigt model for viscoelastic flow; (d) four-element viscoelastic model. [22]


Figure 2.3 Creep response of four element model. [22]
metals resulting in much greater necking in polymers.
Figure 2.4 represents the Voigt model. At $t=0$, there is a step jump in stress due to the dashpot in figure 2.2 which appears to have infinite stiffness. As time progress from 0 to 100 seconds in figure 2.3 , stress is held constant while strain continues to increase. This is called creep. "Creep curves generally show three continuous stages: a first stage marked by large and rapid initial deformation; a second stage where deformation continues at a relatively slow, constant rate; a third stage in which rupture occurs" [19]. At $t=100$ seconds, the strain is held contant while the stress drops in a stepwise fashion. Stress relaxation then ensues as strain is held constant. Stress relaxation can be approximated by:

$$
\begin{equation*}
\sigma(t)=\sigma_{0} e^{-t / T} \tag{I}
\end{equation*}
$$

where $\sigma_{0}$ is the initial stress before stretching is stopped, $t$ is time and $T$ is relaxation time defined by
$\boldsymbol{\pi} / \mathrm{E} . \boldsymbol{\pi}$ is the viscosity and E is Young's modulus.
Detection of local thinning can be done with the use of circles printed on the surface of a deforming specimen. Figure 2.5 demostrates how changes in the circle as it becomes an ellipse can give information about thinning [21]. The major axis indicates the major direction and magnitude of stretching. The engineering strain, in the direction of the major axis, can be measured by noting the length of the major axis of the ellipse and comparing it to


Figure 2.4 Voigt model's stressstrain diagram. [22]


Figure 2.5 Ellipse deformation [21]
the major axis of the original circle. The same can be done for the minor axis and its direction, but where the major strain is always positive for the case of a tensile test, the "minor" strain may be positive or negative. In the tensile test, the minor strain is induced by the Poisson effect and the constancy of volume in plastic flow of a noncompressible material. If there is an area change from the circle to the ellipse then the thickness has changed. For example, if the area of the ellipse increases, the thickness must decrease to maintain the constant volume of the continuum. "This can be easily observed by experimenting with a wide rubber band" [12]. Notice when stretching the rubber band, an ellipse forms and the thickness decreases. If the continuum is to exist then constancy of volume must prevail.

Several methods of testing are available to obtain the needed mechanical property values. One method is optical. Using laser speckle interferometry, the in-plane elastic constants can be obtained [15]. The out-of-plane elastic constants are determined by conventional or holographic interferometry results and the Maxwell Relationships. Optical methods can only measure displacements and Poisson ratios. "Nevertheless, when combined with the necessary stress information (provided by other means), in-plane Young moduli and shear modulus can also be measured" [15]. Another method of measuring elastic constants is by acoustical means. Using ultrasonic waves, the constants
can be determined by measuring the effects of the sound waves as they pass through the medimum in certain directions [12], [16] and [18]. This method can be used in dynamic testing, but the elastic constants are always higher than those produced by mechanical means. This is possibly due to the time involved in the two methods. In ultrasonic testing, there is very little time for viscoelastic relaxation to take place. Mechanical testing gives the material much more time for viscoelastic relaxation to occur. Mechanical testing, the last method examined for possible use, is accomplished by measuring extension, load applied and physical dimensions, from which a stress-strain curve is generated. The elastic contants and yield point can then be derived.

Waves are out-of-plane deformations. Several theories on their formation vary greatly. One theory is that the waves form similar to those in elastic columns in compression. Euler's formula [25] :

$$
\begin{equation*}
F_{c r}=\pi^{2} E I / L^{2} \tag{2}
\end{equation*}
$$

E is Young's modulus, $L$ is the length of the column (the width in the case of films) and $I$ is the moment of inertia of the cross section about the bending axis. Notice the critical force depends on $E$ and geometry. In the case of thin films, a "critical" strain is caused by Poisson's effect. The tensile load applied to films causes a compression strain in the transverse direction that induces waves. It is possible that the strain that causes the
waves is somehow related to the $E, L$, and $I$ of equation (2).

The Von Mises stress defines the start of yielding.
Von Mises stress is represented by

$$
\begin{equation*}
\sigma^{\prime}=\left(\left[\left(\sigma_{1}-\sigma_{2}\right)^{2}+\left(\sigma_{2}-\sigma_{3}\right)^{2}+\left(\sigma_{3}-\sigma_{1}\right)^{2}\right] / 2\right)^{1 / 2} \tag{3}
\end{equation*}
$$

when a triaxial stress state exists where $\sigma_{1}, \sigma_{2}$ and $\sigma_{3}$ are the principal stresses [26]. Two specific cases can exist: plane strain and plane stress. Plane strain is where strain exists in two principle directions but not in the third principle direction. In the case of plane stress, the stress exists in two directions and does not exist in the third. Thin films under tension in a web handling process can be under plane stress. The above equation reduces to

$$
\begin{equation*}
\sigma^{\prime}=\left(\sigma_{1}^{2}-\sigma_{1} \sigma_{2}+\sigma_{2}^{2}\right)^{1 / 2} \tag{4}
\end{equation*}
$$

for plane stress. Plastic deformation occurs when the von Mises stress exceeds $Y$ (uniaxial yield stress of the material). The following is the relationship equation:

$$
\begin{equation*}
\sigma^{\prime 2}=Y^{2} \tag{5}
\end{equation*}
$$

Figure 2.6 shows a 3-D stress element with stresses in the $\mathrm{x}, \mathrm{y}$ and z directions with corresponding shear stresses. This is a triaxial stress state. The plane stress case is illustrated in figure 2.6. Notice there is no stress in the $z$ direction. Figure 2.7 shows how one of the principal stresses relates to stress and shear. Figure 2.8 shows how a Mohr's circle, where stress is plotted versus shear for


Figure 2.6 (a) 3-D Stress cube,
(b) plane stress. [26]


Figure 2.7 Relationships
of stresses
in $3-D$
stress
element to
principal
stress. [26]


Figure 2.8 Mohr's circle
diagram. 26


Figure 2.9 Two examples of stress
(a) Plane stress,
(b) Plane strain. [26]
the stress element, is constructed to yield the principal stresses. The principal stresses are those points of Mohr's circle where the stress is at its maximum and minimum. Plane strain is compared with plane stress in figure 2.9. Figure 2.10 shows Mohr's circles in various stress states.

Crazing can be an important part in the deformation of polymers. Yefimov, Bulayev, Ozerin, Rebrov, Godovskii and Bakeyev have done tests that show "crazing in polypropylene is accompanied by a considerable rise of polymer internal energy due to new surface created inside the crazes" [14]. They studied films of isotactic polypropylene 100 to 200 micrometers thick and 20 to 40 millimeters long at a relative elongation of up to 100 percent. The rate of deformation was 5 millimeters per minute. The samples were prepared by annealing oriented polypropylene at near its melting point. Using a microcalorimeter, they noticed heat was absorbed before crazes started forming. Small-angle X-ray scattering was used to detect crazing. A great number of crazes, $2.5 \times 10^{5}$ per centimeter, formed when the stress reached the "limit of forced elasticity", $\sigma_{f}$. After craze formation began, a "substantial" amount of energy was generated. "The energy stored in PP elongated to $100 \%$ amounts to $20-25 \mathrm{~J} / \mathrm{g}$ " [14]. They concluded the heat dissipated was much less than the deformation energy so that the net internal energy increased during crazing. They also state that the change

(e)


Figure 2.10 Mohr's circles for various states of stress.
(a) Uniaxial tension.
(b) Uniaxial compression.
(c) Biaxial tension
(plane stress).
(d) Triaxial tension.
(e) Biaxial compression
with tension. [26]
in internal energy increases linearly with deformation. Jenkins and Jenkins studied the induction of a prefered orientation in a liquid crystal co-polyester by extrusion and drawing [10]. They found that the "rod-like" molecules of co-polyester tend to align themselves along the fiber axis during hot stretching following extrusion. But what they discovered later has a great importance, the stiffness peaked when the heat treatment was 170 C . At temperatures greater than 170 C , the preferred orientation would decrease. In other words, the stiffness in the preferred orientation would drop. They concluded that the mechanical properties are critically dependent on thermal and strain history.

In this study, the tentering process takes place at elevated temperate as well. The tentering region may be effected by this phenomenon.

## CHAPTER III

## EXPERIMENTAL

All experimentation was performed using an Instron tensile testing machine in correlation with specially designed grips and a load cell-tranducer-plotter arrangement (figure 3.1). Set for a constant displacement rate of 0.5 inches/minute, the Instron extended the sample positioned between the two roller grips. Each grip consisted of a steel bar bounded by "channel iron" supports. Down the length of the steel bar, a thin straight groove was cut at a depth of one half of the diameter of the bar. This groove is used to prevent the sample from slipping from the grip. Through the "channel iron" support and the steel bar, holes were drilled and removable bolts fitted stopping the bar's rotation during testing and allowing easy sample mounting and removal. The load cell-transducer-plotter set-up recorded voltage, proportional to load, versus time once testing began. System calibration was three-fold: first, measuring actual displacement of the Instron versus time; second, affixing a known load to the system and noting plotter displacement; third, comparing real time against plotter pin movement (see appendix for calibration results).


Figure 3.1 Instron and associated equipment.

The heating of samples to a specific temperature and maintaining that temperature (figure 3.2) during testing was achieved by the use of strip heaters, a Plexiglas heat reflector and a PID (Proportional Integral Derivative) controller (see figure 3.3).

Specimens of both polypropylene and polyester were tested. Polypropylene was taken from a "frozen" production line (figure 3.4) and samples were secured from sections of the finished product. Sampling along the length of the transverse direction orientation (TDO) (figure 3.5), provided information on the degree orientation or anistropy occurring as the polypropylene is being elongated in the cross-machine direction (CD). At ten foot intervals from the exit of the TDO, samples were cut in both the machine direction (MD) and $C D$ to give data concerning change in anistropy as the material process attempts to approach desired biaxial material orientation. Specimens were also taken in the finished product across the width of the web to form a profile of data concerning uniformity (figure 3.6 \& 3.7). Some samples were taken at a 45-degree angle to the MD to test biaxiality. Not knowing the past processing history of polyester and its size limitations, tests were run only in the MD. Experiments were also done at elevated temperatures to observe changes in material properties at different temperatures (figure 3.8).

Preparation of samples followed this format. First, the specimens were cut with a new razor blade after the


Figure 3.2 Schematic of PID controller and


Figure 3.3 PID Controller.


Cont'd.


Figure 3.5 TDO Sampling

Figure 3.6 Across the web sampling between winder and $\begin{gathered}\text { treater. }\end{gathered}$


Figure 3.7 $\begin{gathered}\text { Sampling between winder and } \\ \text { treater. }\end{gathered}$


Figure 3.8 Polyester specimen being tested at an elevated temperature.
appropriate section and direction of the material was marked with a permanent marker. Care was taken not to damage the integrity of the material's edge. Specimen size was typically 6 x 24 inches, although final size may be altered slightly to remove sharp edge stress concentrations. Second, the 6 inch ends are covered with l/4 inch of masking tape promoting sample mounting into grip groove. Third, using a permanent marker and a circle template, 1 inch diameter circles are drawn onto the surface of the specimen, again being careful not to damage the material's surface.

The samples are mounted by inserting the taped ends into the bar's slot and then rolling the bar until the specimen has been wound around approximately three times. (Note: on thicker materials, greater than 2 mils, adhesive can be applied onto the bar and specimen before wrapping to ensure traction as long as the adhesive is much stiffer than the sample.) This is repeated for both top and bottom grips. When winding the bar, care is taken to leave the sample in an unloaded condition. The bolts are then inserted through the "channel iron" and bar to prevent bar rotation.

Following mounting and before Instron start up, some pre-test data is recorded (see appendix for test blank) information such as width, gage length, test temperature, etc.

Testing begins with the starting of the Instron and
the plotter at the same time. As the test progresses, ellipse dimensions, both major and minor axes, are measured and recorded on the plotter curve marking the location where the sampling was taken. Figure 3.9 show a typical MD oriented test with deformed ellipses. Width changes are also recorded in a similar manner to that of the eclipse data. Figure 3.10 shows typical test data. The onset of wave formation is noted by marking on the plotter curve as well. (Note: onset of wave formation was very loosely defined as that point in the test when out of plane deformation occured when all waves were no longer touching the grips. If the waves were still in contact with the bar then waves could be caused by a slack edge due to some minor misalignment.) Tests were taken either to failure or to two-thirds of the plotter's overall time range, then the Instron was stopped. If the sample had not failed, the plotter was allowed to run to its full time range, which recorded stress relaxation information on the sample. Post-test data included final ellipse and minimum width dimensions in an attempt to measure elastic recovery after the sample is completely unloaded.

The following table shows number of tests run and their general location in the production line:

TABLE I
NUMBER OF TEST RUN

| Material | Orientation | Number of tests |
| :--- | :---: | :---: |
| Polyester |  |  |
| Polyester (300-D) | $[F P]$ MD | 4 |
| Polyester (400-D) | $[F P]$ MD | 8 |
| Polypropylene | $[F P]$ MD | 2 |
| Polypropylene | $[F P]$ CD | 22 |
| Polypropylene | $[F P] 45$ | 22 |
| Polypropylene | $[T D O]$ MD | 8 |
| Polypropylene | $[T D O]$ CD | 30 |
|  |  | 29 |

FP : Final Product
TDO: Transverse Direction Orientation taken every ten feet down the length.


Figure 3.9 Polypropylene sample cut
in the MD being tested at room temperature.


Figure 3.10 Typical time vs load plot for polypropylene in MD.

## CHAPTER IV

## EXPERIMENTAL RESULTS

Figures 4.1 - 4.3 show the MD specimen as it undergoes testing. Increasing length at a constant rate, the specimen deforms until failure. As it deforms, the test set up generates a load versus time plot, figure 4.4. The shape of the curve is typical for all of the tests that were run in the $M D$, regardless of the location of the sampling. The testing of the $C D$ is shown in stages of deformation in figures 4.5 - 4.7. CD curves all have similar load/time curves as recorded in figure 4.8. Points were entered from the load/time curves into a computer program (see Appendix C) that converted the raw data into a more useful form. The beginning and ending points of the linear elastic regions were entered to establish Young's modulus for the test. Using the load and time points at which the test became plastic, the yield point was established. Points from the load/time plot were entered to determine the stress at specific strains. Neck dimension data was entered to yield stress information, as well. If the test specimen provided stress relaxation information, the appropriate load and time points were entered to yield relaxation time. After unloading or


Figure 4.1 Polypropylene sample with MD orientation awaiting loading.


Figure 4.2 Polypropylene sample with MD orientation under tension.


Figure 4.3 Polypropylene sample with MD orientation before failure.

Figure 4.4 Typical MD test plot of time vs load.


Figure 4.5 Polypropylene sample with CD orientation before
loading.


Figure 4.6 Polypropylene sample with $C D$ orientation under tension.


Figure 4.7 Polypropylene sample with CD orientation before failure.


Figure 4.8 $\begin{gathered}\text { Typical } C D \\ \text { vs load. }\end{gathered}$
failure, final neck and ellipse dimensions were recorded. Using this data and the last neck or ellipse information, the program would yield elastic recovery. See Appendix C for the program's output from the above points.

Normalized moduli versus distance in feet from the center (figure 4.9) were plotted in bar chart form to show a profile of changes across the final product of polypropylene. The moduli were normalized with respect to thickness to aid comparison. Figure 4.10 is a plot of Emd/Ecd versus distance in feet from center. This plot of anistropy aids in the relationships between the MD and CD moduli. Plotting yield point, also normalized with respect to thickness, versus distance from the center in feet demostrates another anistropic aspect of the final product, figure 4.11. To understand how the final product came to be as it is, normalized moduli, $M D$ and $C D$, were plotted down the length of the TDO. Emd/Ecd down the length of the TDO was also charted to help show how the biaxial process progressed (figures 4.12 and 4.13).

Dr. Good entered some of the information from one of the 45 degree tests into a finite element code and plotted stress distribution [27]. Figure 4.14 illustrates sigma $x$ stresses in the 45 degree test while figure 4.15 shows the sigma $y$ stresses. At the bottom grip, grid deformation was plotted in close up figure 4.l6. An overall grid deformation was plotted in figure 4.17. All of the previous figures from the finite element model were


Figure 4.9 (E $x$ t) vs distance from centerline
of web. (Constant thickness of
$0.79 \mathrm{mils})$



Figure 4.11 Yield point vs distance from centerline of web. (Constant thickness of 0.79 mils$)$


Figure 4.12 Normalized modulus ( $\mathrm{E} \times \mathrm{t}$ ) vs
position from exit of TDO (varying
thickness).




Figure 4.14 Finite element model of 45 degree orientation of polypropylene featuring sigma $x$.


Figure 4.15 Finite element model of polypropylene oriented 45 degrees to MD. Featuring sigma $y$.


Figure 4.16 Grid deformation near grip for 45 degree orientation polypropylene sample modeled by finite element method.


Figure 4.17 Overall grid
deformation for 45
degree orientation polypropylene sample modeled by finite element method.
generated in the elastic range.

## CHAPTER V

## DISCUSSION

Static stress-strain tests on the final product of polypropylene were carried out on samples taken from different locations across the width of the web, starting from what was originally the center. From these tests, Young's moduli, normalized with respect to thickness, and plotted versus position from the center edge. In figure 4.9, the variations between normalized MD and CD moduli across the web, can be seen. The important point to note not only is that the $M D$ and $C D$ are not equal, but also that ratio of the modulus in the $C D$ to that in the $M D$ varies from l. 25 to l.4. As can be seen in figure 4.10 , the 1.25 ratio occurs near the center of the material while the l.4 ratio of $C D$ to $M D$ appears at four feet from the center. The range of ratios may be caused by the distribution of stress as the polypropylene is oriented. Stress is applied in the desired direction of orientation in an attempt to align the molecular chains, but the stress distribution varies across the width of the web. This can be seen in the results of the finite element model, figure 4.l4 [27]. If the stress varies across the web then the molecular alignment would also vary. Variations in molecular
alignment will result in variations in yield point and stiffness. Forty-five degree to MD tests corroborate the inequality of the MD and CD moduli, figure 5.1. Figure 5.1 shows a deviation of the major axis from the direction of applied tension. Because the stiffnesses in the MD and CD are unequal, tests run in the 45 degree orientation have principal stresses that are rotated away from the MD and CD directions of loading. This is indicated by the change in the ellipse's major and minor axis directions. This rotation of principal stress directions induce shear stresses in both the MD and CD directions that warp the printed grid and ellipse's major axis directions. This can be seen in figure 5.1 and the finite element model simulation, figure 4.15 [27]. The simulation uses the same defined conditions as the 45 degree test while still in the elastic region. Figure 4.15 [27] provides an indication of the local stresses involved. Figure 4.3, a test run in the MD orientation, shows the principal stresses remain in the same directions as $M D$ and $C D$ of loading according to the axes' directions. Equal stiffnesses in both MD and CD do not yield a deviation of principal stress directions like that in figure 5.l. The purpose of biaxial stretching includes achieving equal stiffness in MD and CD. Figure 4.10 illustrates the amount of anisotropy of stiffness versus distance from center. Notice the inclination of higher anisotropy as distance increases away from the center. Kimura and Shimizu [17] point out that within

rectangular specimens "the maxima of stress and strain could be found at the center of the sample." This is due to boundary conditions and geometry. The boundary conditions are: negligible $C D$ displacement at the grips and applied displacement in the MD. This and the results shown in figure 4.9 suggest the biaxial process works to a varying degree with respect to the width of the web in the tenter. The non-uniformity of the stress distribution is partially hampering the process.

Figures 4.14-4.17 [27] were plotted while still in the elastic region of deformation. As the web enters the plastic region, the maxima stress would approach the center. The chart in figure 4.11 shows the trend for yield point versus distance from the center edge is similar to the trend for stiffness. CD Yield points are also 1.25 to 1.4 times higher than their MD counterparts. Because yield point and stiffness are similarly affected by the biaxial stretching, it is also affected by the uneven stress distribution instilled by the process in a likewise manner. Tests were also run on samples taken from the treater down to almost half the length of the TDO. As across the final product, $M D$ and $C D$ normalized moduli varied. The CD moduli were almost always consistently higher than the MD. The TDO is theoretically where the CD stiffness is increased to match that of the MD in figure 4.12. It is possible that as the web was stretched and annealed in the MDO that the material's molecular alignment did not occur
to the degree desired. The MDO is supposed to achieve an MD preferred orientation, but the degree of orientation may not have been reached. It is possible the MDO stretching that occurs before the annealing takes place causes crazing that raises the internal energy of the material "due to new surface created inside the crazes" similar to results reported by Yefimov, Bulayev, Ozerin, Rebrov, Godovskii and Bakeyev [14]. This increase in internal energy could promote molecular chain randomness instead of alignment. As stated by Jenkins and Jenkins [l0], there is an optimum temperature for achieve maximum preferred orientation. If that temperature is exceeded then the preferred orientation is decreased. Crazing could supply the additional energy needed to decrease the preferred orientation while in the MDO. Thicker samples, near the middle of the TDO, were visually observed to craze easily when loaded. The sample turned opaque in spots at a relative elongation of about 50 percent. As the test progressed, the opacity diminished. Another possiblity that involves molecular alignment is a complex mixture of changing stress distribution, geometry and thermal energy. Because there was a relatively short time between the MDO operation and the start of the TDO stretching, little thermal energy has had time to be released. The geometry was changed between 70 and 40 feet and then held constant after 30 from the exit. If the molecular alignment was not given time to "set" after the stress from the TDO stretching was released, the
web could have "snapped back" into its higher anisotropy configuration. Remember, the web is still at an elevated temperature and the TDO stress has been removed, but the inline tension that keeps the web on the rollers remains. This inline tension combined with stress relaxtion could cause the molecular chains to re-align in an unwanted manner. This might be prevented by allowing more "setting time" after the tenter.

Wave formation was also studied in both the polyester and the polypropylene. Wave formation is that point when the sample visibly displayed out of plane deformation. The onset of wave formation began within the elastic-plastic region described by Nilkanth [8] of the stress-strain curve usually before the yield point is reached. Typically, waves occurred at 80 percent of the yield point for the MD samples, but their formation in the $C D$ direction behaved in a different manner. The onset of waves (CD direction tests) occurred at 125 percent of the yield values. Both $M D$ and $C D$ onsets were within the elastic-plastic region. This can be partially explained by looking at the elastic column buckling shown by Stevens [25] which is derived from Euler's formula for critical load. Only $E$ and geometry play a part in that calculation for critical load. Therefore changes in $E$ where the geometry is the same would proportionally affect the critical strain. The reverse is also true. Changing geometry, e.g. thickness, and keeping E constant would also change the point at which waves form.

Because CD is stiffer, it is presumed the critical strain would increase and therefore cause a higher strain for the onset of waves. However, the relationship between onset to wave formation and yield point is interesting. Euler's equation predicts "elastic" column buckling yet waves were observed to form in the elastic-plastic region. There seems to be some possible dependence on yield point. Euler's equation might be modified to include yield point for polymers to obtain a critical strain value for wave formation.

Mechanical tensile testing was chosen over optical and acoustical methods of determining E. They compare with the mechanical tensile testing in the following ways: Optical can measure displacements and Poisson's ratios but requires additional stress infomation to be useful (refer [15]); ultrasonics will return $E$ values quickly from various points on the web, but those values are consistently higher than the mechanical E's observed. Mann, Baum, and Habeger [12] believe this is because ultrasonic testing gives much less time for viscoelastic relaxation than does mechanical tensile testing. Because there is not an established correlation between mechanically measured Young's moduli and acoustically measured values and the cost of the acoustical equipment is expensive, the mechanical tensile testing method was chosen.

Recommendations for future work include the following. It is necessary to find more accurate ways to
detect the onset of waves, such as through laser interferometry. More material based testing on paper and other polymers to derive a unitless number based on material properties and geometry for the onset of waves needs to be done. Very useful information can be collected by either scanning with a digitizing camera for use on a computer or taking numerous photographs with a scale in the picture. Thinning information will prove useful in wave formation considerations. Image analysis techniques, either with video frame grabbing or high resolution still photography could prove to be useful. Joint work between finite element modeling and material testing is required. Dymanmic testing that could be used on-line to measure characteristics of wave formation, such as the start of out of plane deformation, amplitude of deformation, stress state at formation, vibrational effects on viscoelasticity and their effect on permanent setting of waves. Temperature effects on wave formation and setting should also be studied. Direction and values of principle moduli need to be determined. Poisson's ratios and shear moduli are also needed.

CONC LUS IONS

The biaxial orientation process used in production of this web works with a varying degree of success relative to the location of sampling. This can be seen in variations in yield point and stiffness throughout the web. These variations may be caused by unequal stress distribution that affects molecular alignment. It is also possible while the web was stretched and annealed in the MDO that alignment did not occur to the desired degree. Crazing may have played an important part here, raising the web's internal energy to a point where it adversely affected the molecular alignment. Along with this, insufficient "setting time" could have prevented the desired alignment. Further study of how the stress is distributed and how this distribution affects molecular alignment could prove invaluable in improving the properties of the web through production technique changes.

1. Kresser, T. O. J. (1960). Polypropylene. New York: Reinhold Pub. Corp.
2. Frank, H. P. (1968). Polypropylene. New York: Gordon \& Breach Science Publishers.
3. Opschoor, A. (1968). Conformations of Polyethylene and Polypropylene. Rotterdam: Rotterdam University Press.
4. Goodman, I. and Rhys, A. J. (1965). Polyesters, Vol. I Saturated Polymers. New York: American Elsevier Pub. Co.
5. Bjorksten Research Laboratories, Inc. (1965). Polyesters and their Applications. New York: Reinhold Pub. Corp.
6. Bruins, P. F. (1976). Unsaturated Polyester Technology. New York: Gordon and Breach Science Publishers.
7. Galanti, A. V., and Mantell, C. L. (1965). Polypropylene Fibers and Films. New York: Plenum Press.
8. Nilkanth, V. K. (1987). Web Material Effects on Wrinkling Instability Experimental and Computer Analysis.
9. Miller, D. L. (1985). An Experimental Technigue for Dymanic Analysis of Flexible Disk Drive Read/Write Head Designs.
10. Jenkins, J. C. and Jenkins, G. M. (1987). The Induction of Preferred Orientation in a Liquid Crystal Co-ployester by Extrusion and Drawing. Material Science, 22(10), 3784-3972.

1l. Lukovkin, G. M., Volynskii, A. L. and Bakeyev, N. F. (1986). Analytical Form of the Dynamometric Curves for Polymers in Isothermal Conditions of Deformation. Polymer Science, 28(6), 13961402 .
12. Mann, R. W., Baum, G. A. and Habeger, C. C. (1980). Determination of All Nine Orthotropic Elastic Constants for Machine-made Paper. Tappi, 63(2), 163-166.
13. Filyanov, Ye. M. (1986). Role of Structual Factors in Resistance to Inelastic Deformation of Network Polymers. Polymer Science, 28(6), l833-1840.
14. Yefimov, A. V., Bulayev, V. M., Ozerin, A. N., Rebrov, A. V., Godovskii, Yu. K. and Bakeyev, N. F. (1986). Formation of Crazes in Isotactic Polypropylene and Accompanying Changes of Energy. Polymer Science, 28(8), 1951-1958.
15. Castagnede, B., Mark, R. E. and Seo, Y. B. (1987). New Concepts and Experimental Implications in the Description of the 3-D Elasticity of Paper. International Paper Conference, 15l-156.
16. Baum, G. A. (1987). Polar Diagrams of Elastic Stiffness: Effects of Machine Variables. International Paper Conference, 161-166.
17. Kimura, M. and Shimizu, H. (1984). Stress and Strain Analysis of a Rectangular Specimen in Elongation Testing. Tappi, 67(4), 128-131.
18. Mann, R. W., Baum, G. A. and Habeger, C. C. (1979) Elastic Wave Propagation in Paper. Tappi, 62(8), l15-118.
19. Modern Plastics Encyclopedia. (1985). 61.
20. Van Vlack, L. H. (1980). Elements of Material Science and Engineering. Reading: Addison-Wesley Pub. Co.
21. Kalpakjian, S. (1985). Manufacturing Processes for Engineering Materials. Reading: Addison-Wesley Pub. Co.
22. Hertzberg, R. W. (1983). Deformation and Fracture Mechanics of Engineering Materials. New York: John Wiley \& Sons.
23. Johnson, W. and Mellor, P. B. (1985). Engineering Plasticity. Chichester: Ellis Horwood Ltd.
24. Budinski, K. (1983). Engineering Materials Properties and Selection. Reston: Reston Pub. Co., Inc.
25. Stevens, K. K. (l979). Statics and Strength of Materials. Englewood Cliffs: Prentice-Hall, Inc.
26. Shigley, J. E. and Mitchell, L. D. (1983). Mechanical Engineering Design. New York: McGraw-Hill Book Co.
27. Good, J. K. (l988). Private Communication.

AP PENDIXES

## APPENDIX A

## ANALYSIS OF UNCERTIANITY FOR NORMALIZED YOUNG'S MODULUS <br> $$
E * t=(F 2-F l) * L o /[(L 2-L l) * W]
$$

Where: Fl and F2 are the loads selected on the linear portion of the stress-strain curve; Ll and L2 are the lenghts of the elastically deformed specimen correponding with Fl and F2; Lo is the original length of the undeformed specimen; $W$ is the width of the undeformed specimen.

```
Estimation of uncertainity intervals:
    \(\mathrm{F}=10 \pm 0.1 \mathrm{lb}\)
    \(\mathrm{L}=12 \pm 0.032 \mathrm{in}\)
    \(\mathrm{W}=6 \pm 0.032 \mathrm{in}\)
```

Relative Uncertainities:

```
    \(\mathrm{Uf}= \pm(.1) /(10)= \pm 0.0100\)
    \(\mathrm{Ul}= \pm(0.032 / 12)= \pm 0.0027\)
    \(U \mathrm{Uw}= \pm(0.032 / 6)= \pm 0.0053\)
    \(\mathrm{U}_{\Delta} \mathrm{f}= \pm!(0.0100)^{2}+\left.(0.0100)^{2}\right|^{\frac{1}{2}}= \pm 0.0141\)
    \(U_{\Delta l}= \pm 1(0.0027)^{2}+(0.0027)^{2} 1^{\frac{1}{2}}= \pm 0.0038\)
    \(\mathrm{Ue}= \pm 1\left(U_{\Delta} \mathrm{f}\right)^{2}+\left(U_{\Delta} I\right)^{2}+\left(U_{W}\right)^{2} 1^{\frac{1}{2}}\)
    \(\mathrm{Ue}= \pm 1(0.0141)^{2}+(0.0038)^{2}+(0.0053)^{2} 1 \frac{1}{2}= \pm 0.0155\)
        or
    \(\mathrm{Ue}= \pm 1.6\) percent.
```


## APPENDIX B

## ANALYSIS OF UNCERTAINITY FOR YIELD POINT

$$
Y p(p l i)=F / W
$$

Where: $F$ is load at the yielding point and $W$ is width of undeformed specimen.
from APPENDIX A:
$\mathrm{Uf}= \pm 0.0100$
$U w= \pm 0.0027$
The relative uncertainity for $Y$ is:
$U y= \pm\left|(U f)^{2}+(U W)^{2}\right|$
$U y= \pm\left((0.0100)^{2}+\left.(0.0027)^{2}\right|^{\frac{1}{2}}= \pm 0.0100\right.$
or $U y= \pm 1.00$ percent.

# APPENDIX C <br> <br> COMPUTER PROGRAM FOR FINDING 

 <br> <br> COMPUTER PROGRAM FOR FINDING}

ALL VALUES AND OUTPUT

```
'
I
Mr. Thesis
Dim Neck$(50,3),Elc$(50,4),D$(100,25),E$(100, 20,3),
    F$(l00, 20,4),Parml$(2),Parm2$(8)
Parml$(l)="Thickness (mm)"
Parml$(2)="Thickness (mils)"
Parm2$(1)=" Neck Reduction"
Parm2$(2)=" Ellipse A- circle A"
Parm2$(3)=" E (PSI)"
Parm2$(4)="Relaxation time (Sec)"
Parm2$(5)="Wave formation (PSI)"
Parm2$(6)="Wave formation (PLI)"
Parm2$(7)="Elastic Recovery"
Parm2$(8)=" Ell. Strains (True)"
5:
Cls
Print "Mr. Thesis"
Print "by Scott Robertson"
Print
Print "(D)ata entry"
Print "(C)alculation"
Print "(A)lter entry (correct)"
Print "(E)nd"
10:
A$=Upper$(Inkey$)
If A$="" Then
    Goto l0
Endif
A=Instr("DCAE",A$)
If A<>O Then
    On A Gosub Zdata_entry,Calc,Edit,Endit
Endif
Goto 5
End
,
```

```
Procedure Endit
    Cls
    Print "Are you sure you want to END (Y/N)?"
    15:
    A$=Upper$(Inkey$)
    If A$="" Then
        Goto 15
    Endif
    If A$="Y" Then
            End
    Endif
Return
!
Procedure Zdata entry
    If Exist("TEST.DAT") Then
        Open "A",#8,"TEST.DAT"
    Else
        Open "O",#8,"TEST.DAT"
    Endif
    20:
    Cls
    Print "(R)eturn to MAIN MENU"
    Print "(E)nter another test"
    25:
    A$=Upper$(Inkey$)
    If A$="" Then
        Goto 25
    Endif
    A=Instr("RE",A$)
    If A<>0 Then
        If A=1 Then
            Goto 30
            Endif
            If A=2 Then
                @Edata
                Goto 20
            Endif
    Endif
    Goto 25
    30:
    Close #8
Return
I
Procedure Edata
    40:
    @Input("Date",*Dated$)
    @Input("Test #",*Test$)
    @Input("Material note",*Material$)
    @Input("Thickness (mm)",*Thickness$)
    @Input("Specimen length (in.)",*Length$)
    @Input("Specimen width (in.)",*Width$)
    @Input("Material Orientation",*Material_orientation$)
    @Input("Test temp. (F)",*Test_temp$)
```

```
@Input("X scale (sec/cm)",*X_scale$)
@Input("Y scale (v/cm)",*Y_scale$)
@Input("E-Xl Coord. (in.)",*Exl$)
@Input("E-Yl. Coord. (in.)",*Eyl$)
@Input("E-X2 Coord. (in.)",*Ex2$)
@Input("E-Y2 Coord. (in.)",*Ey2$)
@Input("Wave formation x (in.)",*Wave_x$)
@Input("Wave formation y (in.)",*Wave_y$)
@Input("# of NECK data points",*Neck$)
W=Val (Neck $)
If W<>0 Then
    For X=l To W
        @Input("Enter "+Str$(X)+" of "+Str$(W)+" NECK dim.
        (in.)",*B$)
        Neck $(X,I)=B$
        @Input("Enter "+Str$(X)+" of "+Str$(W)+" NECK X-
        coord. (in.)".,*C$)
        Neck $(X, 2)=C$
        @Input("Enter "+Str$(X)+" of "+Str$(W)+" NECK Y-
        coord. (in.)",*D$)
        Neck $(X,3)=D$
    Next X
Endif
@Input("# of ELC data points",*Elc$)
U=Val(Elc$)
If U<>0 Then
    For X=1 To U
        @Input("Enter "+Str$(X)+" of "+Str$(U)+" ELC Major
        dim. (in.)",*E$)
        Elc$(X,l)=E$
        @Input("Enter "+Str$(X)+" of "+Str$(U)+" ELC Minor
        dim. (in.)",*F$)
        Elc$(X,2)=F$
        @Input("Enter "+Str$(X)+" of "+Str$(U)+" ELC X-coord.
        (in.)",*G$)
        Elc$(X,3)=G$
        @Input("Enter "+Str$(X)+" of "+Str$(U)+" ELC Y-coord.
        (in.)",*H$)
        Elc$(X,4)=H$
    Next X
Endif
@Input("Start Stress Relax x-coord. (in.)",*Stressrx$)
@Input("Start Stress Relax y-coord. (in.)",*Stressry$)
@Input("2nd Stress Relax x-coord. (in.)",*Stressr2x$)
@Input("2nd Stress Relax y-coord. (in.)",*Stressr2y$)
@Input("Elastic Recovery Neck dim. (in.)",*Ernd$)
@Input("Elastic Recovery ELC Major dim. (in.)",
*Eremajord$)
@Input("Elastic Recovery ELC Minor dim. (in.)",
*Ereminord$)
Print
Print "Everything correct (Y/N)?"
50:
```

A\$=Upper \$ (Inkey\$)
If $A \$=" "$ Then
Goto ..... 50
Endif
If AS="N" Then
Goto ..... 40
Endif
If A\$="Y" Then
@Savedata
Else
Goto ..... 50
Endif
Return
1
Procedure Savedata
@Output(Dated\$) ..... $!1$
@Output(Test\$) ..... 12
@Output(Material\$) ..... $!3$
@Output(Thickness\$) ..... $!4$
@Output(Length\$) ..... ! 5
@Output(Width\$) ..... $!6$
@Output(Material orientations) ..... 17
@Output(Test temp\$) ..... $!8$
@Output(X scale\$) ..... $!9$
@Output( $\mathrm{Y}^{-}$scale\$) ..... $!10$
@Output(Ex $1 \$$ ) ..... $!11$
@Output(Eyl\$) ..... ! 12
@Output(Ex2\$) ..... !13
@Output(Ey2\$) ..... ! 14
@Output(Wave x\$) ..... $!15$
@Output(Wave y\$) ..... !16
@Output(Neck \$) ..... ! 17
W=Val (Neck \$)
If $W<>0$ Then
For $X=1$ To $W$
@Output(Neck \$(X,1))
@Output(Neck \$(X,2))
@Output(Neck \$(X,3))
Next X
Endif
@Output(E1c\$) ..... !18
U=Val(Elc\$)
If $\mathrm{U}<>0$ Then
For X=1 TO U
@Output(Elc\$(X,l))
@Output(Elc\$(X,2))
@Output(Elc\$(X,3))
@Output(Elc\$(X,4))
Next X
Endif
@Output(Stressrx\$) ..... ! 19
@Output(Stressry\$) ..... ! 20
@Output(Stressr2x\$) ..... ! 21

```
    @Output(Stressr2y$)! 22
```

@Output(Ernd\$) ..... ! 23
@Output(Eremajord\$) ..... ! 24
@Output(Ereminord\$) ..... ! 25
Return

```
|
Procedure Input(W$,X%)
    Print W$;
    Input Temp$
    If Temp$<>"" Then
        *X% =Temp$
    Endif
Return
!
Procedure Output(S$)
    If S$<>"" Then
        Print #8,S$
    Else
        Print #8,"None"
    Endif
Return
I
Procedure Calc
    Cls
    Print "Loading...."
    Open "I",#8,"test.dat"
    Test=0
    Repeat
        Test=Test+1
        @Load(Test)
    Until Eof(#8)
    Close #8
    Print "Done."
    @Select
Return
I
Procedure Load(T)
    For Zz=1 TO 17
        Input #8,D$(T,Zz)
    Next Zz
    If Val(D$(T,17))<>0 Then
        For Zz=1 To Val(D$(T,17))
            For W=1 To 3
                    Input #8,E$(T,Zz,W)
                Next W
        Next Zz
    Endif
    Input #8,D$(T,18)
    If Val(D$(T,18))<>0 Then
        For Zz=1 To Val(D$(T,l8))
            For W=1 To 4
                    Input #8,F$(T,Zz,W)
            Next W
```

```
        Next Zz
    Endif
    For Zz=19 To 25
        Input #8,D$(T,Zz)
    Next Zz
Return
!
Procedure Decimal(A$,X%)
    Let Decimal=0
    If Instr(A$,".")=0 And Instr(A$,"/")<>0 Then
        A=Instr (A$," ")
        If A<>0 Then
            Let Decimal=Val(Left$(A$,A))
            A$=Mid$(A$,A+l)
        Endif
        C=Instr (A$,"/")
        If C<>0 Then
            Let Decimal=Decimal+Val(Left$(A$,C))/Val(Mid$(A$,C+l)
            )
            Endif
    Else
        Let Decimal=Val(A$)
    Endif
    *X%=Decimal
Return
I
Procedure E
    @Cdo (D$ (T,4) +D$ (T,5)+D$(T,6)+D$(T,ll) +D$(T,12) +D$(T,l3)
    +D$(T,14))
    If Cdo! Then
        @Decimal (D$ (T,5),*Lo)
        @Decimal(D$(T,6),*W)
        Ll=@Xcon(Val (D$(T,ll)),T)
        L2=@Xcon(Val (D$(T,13)),T)
        @Force(D$(T,l2),*Forcel)
        @Force(D$(T,l4),*Force2)
        Thickness=Val(D$(T,4))/25.4
        Deltal=L2-Ll
        E=(Force2-Forcel)*Lo/(Deltal*W*Thickness)
        Round=Int(Logl0(E+l))+l
        Mid$(Work$,67,Round)=Str$(E)
    Else
        Mid$(Work$,67,4)= "NCDO"
    Endif
Return
I
Deffn Tcon(T)=T/25.4
Deffn Xcon(X,T)=\operatorname{Val (DS (T,9))*0.0212*X}
I
Procedure E area
    On Which Gosub Screen,Prnter
    Work$=K$
    Mid$(Work$,40,19)="Strain Stress(psi)"
```

```
    On Which Gosub Screen,Prnter
    Kr=Val (D$(T,18))
    If Kr<>0 Then
        For D=l To Kr
            Work$=K$
            @Cdo(D$(T,ll)+F$(T,D,l)+F$(T,D,2)+F$(T,D,3)+F$(T,D,4
            ))
If Cdo! Then
                            @Decimal(D$(T,5),*LO)
            @Decimal(F$(T,D,l),*Major)
            @Decimal(F$(T,D,2),*Minor)
            @Decimal(D$(T,6),*W)
            E_area=Pi*Major*Minor/4-Pi/4
            Xj=@Xcon(Val (F$(T,D,3)),T)-@xcon(Val (D$(T,ll)),T)
            Xj=xj/Lo
            @Stress(W,F$(T,D,4),*Yj)
            Mid$(Work$,40,5)=Left$(Str$(Xj),5)
            Mid$(Work$,50,Int(Logl0(Yj+l)+l))=Str$(Yj)
            Mid$(Work$,67,5)=Left$(Str$(E_area),5)
            Else
            Mid$(Work$,40,4)="NCDO"
            Endif
            On Which Gosub Screen,Prnter
        Next D
    Endif
    Work$=K$
Return
!
Procedure Cdo(Check$)
    Cdo!=True
    If Instr(Upper$(Check$),"NONE")<>0 Then
        Cdo!=False
    Endif
Return
'
Procedure Select
    Select2:
    Cls
    Print "(l): Select print parms"
    Print "(2): Test order"
    Print "(3): Print"
    Print "(4): Quit"
    Print
    @One_key(4)
    If Key=4 Then
        Goto Selectl
    Endif
    On Key Gosub Parms,Order,Prnt
    Goto Select2
    Selectl:
Return
I
```

```
Procedure One key (O)
    Key:
    \(A \$="\) "
    A \(\$=\) Inkey \(\$\)
    If \(A \$="\) " Then
        Goto Key
    Endif
    If Val(A\$)>=1 And Val(A\$)<=0 Then
        Key=Val (A\$)
    Else
        Goto Key
    Endif
Return
1
Procedure Order
    Order\$=" "
    Order:
    Cls
    Print "Current Order: ";Order\$
    Input "Enter test\# (Return/returns, All/All)";J\$
    If J\$="" Then
        Goto Order2
    Endif
    If Upper\$(J\$)="ALL" Then
        For Dd=1 To Test
            @Order_sum (D\$(Dd,2))
        Next Dd
        Goto Order2
    Endif
    @Order sum(J\$)
    Goto Or\(d e r\)
    Order2:
Return
I
Procedure Order sum(H\$)
    If Order\$="" Then
        Order\$=H\$
    Else
        Order\$=Order\$+","+H\$
    Endif
Return
1
Procedure Parms
    Cls
    Print "Select Parm 1 "
    Print "(l): Thickness (mm)"
    Print "(2): Thickness (mils)"
    @One_key(2)
    Pl=Key
    Print
    Print "Select Parm 2"
    Print "(1): Neck Reduction"
    Print "(2): Ellipse area- 1 inch. circle area"
```

```
    Print "(3): E (PSI)"
    Print "(4): Relaxation time (Sec)"
    Print "(5): Wave formation (PSI)"
    Print "(6): Wave formation (PLI)"
    Print "(7): Elastic Recovery"
    Print "(8): Ell. Strains (Engr)"
    @One_key(8)
    P2=K\overline{e}Y
    Print
    Print "Select Parm 3"
    Print "(l): Pre 4/l4/88 correction factor"
    Print "(2): Exit"
    @One key(2)
    P3=-(Key=1)*0.35-(Key=2)
Return
I
Procedure Prnt
    Cls
    K$=String$(79," ")
    Print "(l): Screen"
    Print "(2): Printer"
    @One key(2)
    Which=Key
    Print "Want a header? (Y/N)"
    Prnt:
    A$=""
    A$=Inkey$
    If A$="" Then
    Goto Prnt
Endif
A$=Upper$(A$)
If A$<>"Y" And A$<>"N" Then
    Goto Prnt
Endif
If Which=2 Then
    Open "",#7,"PRN:"
Endif
If A$="Y" Then
    Header$=K$
    First=Len(Parml$(Pl))
    Last=Len(Parm2$(P2))
    Mid$(Header$,42,First)=Parml$(Pl)
    Mid$(Header$,59,Last)=Parm2$(P2)
    Mid$(Header$,l,6)="Test #"
    Mid$(Header$,6,14)="Mat. Orient."
    Mid$(Header$,22,9)="Mat. Note"
    Work$=Header$
    On Which Gosub Screen,Prnter
    Work$=String$(79,"-")
    On Which Gosub Screen,Prnter
Endif
Repeat
    Work $=K$
```

```
    Xcv=Val(Order$)
    T=0
    Repeat
        T=T+l
    Until (Xcv=Val(D$(T,2)) Or* T=>Test)
    Ww=Instr(Order$,",")
    Mid$(Work$,1,Len(D$(T,2)))=D$(T,2)
    Mid$(Work$,6,Len(D$(T,7)))=D$(T,7)
    Mid$(Work$,ll,Len(D$(T,3)))=D$(T,3)
    On Pl Gosub Thickmm,Thickmils
    On P2 Gosub Necking,E_area,E,Relax,Wavepsi,Wavepli,
    Elastic,Ed
    On Key Gosub Screen,Prnter
    If Ww<>0 Then
        Order$=Mid$(Order$,Ww+l)
    Endif
    Until Ww=0
    If Which=2 Then
    Close #7
    Endif
    Input "Hit return";Ab$
Return
'
Procedure Screen
    Print Work$
Return
'
Procedure Prnter
    Print #7,Work$
Return
'
Procedure Thickmm
    Mid$(Work$,48,Len(D$(T,4)))=D$(T,4)
Return
I
Procedure Thickmils
    Mils=l000*Val(D$(T,4))/25.4
    Mid$(Work$,48,5)=Left$(Str$(Mils),5)
Return
'
Procedure Relax
    @Cdo(D$(T,19)+D$(T, 20)+D$(T, 21)+D$(T, 22))
    If Cdo! Then
        Zzz=2.54*Val(D$(T,9))
        Timl=Zzz*Val(D$(T,19))
        Tim2=Zzz*Val(D$(T,2l))
        @Decimal(D$(T,6),*W)
        Relax=-(Tim2-Timl)/(Log(Val (D$(T, 22))/Val (D$ (T, 20))))
        Mid$(Work$,67,5)=Left$(Str$(Relax),5)
    Else
        Mid$(Work$,67,4)="NCDO"
    Endif
Return
```

```
|
Procedure Wavepsi
    @Cdo(D$(T,1l)+D$(T,l5)+D$(T,16))
    If Cdo! Then
        @Decimal (D$ (T, 6),*W)
        @Stress(W,D$(T,16),*Stress)
        Mid$(Work$,67,Int(Logl0(Stress+l)+1))=Str$(Stress)
    Else
        Mid$(Work$,67,4)="NCDO"
    Endif
Return
'
Procedure Wavepli
    @Cdo(D$(T,ll)+D$(T,l5)+D$(T,16))
    If Cdo! Then
        @Decimal (D$(T,6),*W)
        @Force(D$(T,l6),*Pli)
        Pli=Pli/W
        Mid$(Work$,67,5)=Left$(Str$(Pli),5)
    Else
        Mid$(Work$,67,4)="NCDO"
    Endif
Return
'
Procedure Necking
    On Which Gosub Screen,Prnter
    Work $=K$
    Mid$(Work$,10,21)="TStrain TStress(psi)"
    Mid$(Work$,40,21)="EStrain EStress(psi)"
    On Which Gosub Screen,Prnter
    Kr=Val(D$(T,17))
    If Kr<>O Then
        For D=l To Kr
        Work$=K$
        @Cdo(D$(T,ll)+E$(T,D,l)+E$(T,D,2)+E$(T,D,3))
        If Cdo! Then
            @Decimal (D$ (T,5),*LO)
            @Decimal(D$(T,6),*W)
            @Decimal(E$(T,D,1),*Necko)
            Neck=(W-Necko)/W
            Xj=@xcon(Val (E$(T,D,2)),T)-@Xcon(Val (D$ (T,ll)),T)
            Xtrue=Log((Xj+Lo)/Lo)
            Xj=Xj/Lo
            @Force(E$(T,D,3),*Ytrue)
            Ytrue=25.4*Ytrue/(Necko*Val(D$(T,4)))
            @Stress(W,E$(T,D,3),*Yj)
            Mid$(Work$,10,5)=Left$(Str$(Xtrue),5)
            Mid$(Work$, 20,Int(Logl0(Ytrue+l)+l))=Str$(Ytrue)
            Mid$(Work$,40,5)=Left$(Str$(Xj),5)
            Mid$(Work$,50,Int(Logl0(Yj+l)+l))=Str$(Yj)
            Mid$(Work$,67,5)=Left$(Str$(Neck),5)
        Else
            Mid $(Work$, 40,4)="NCDO"
```

```
        Endif
            On Which Gosub Screen,Prnter
        Next D
    Endif
    Work$=K$
Return
'
Procedure Stress(W,H$,X%)
    @Force (H$,*F)
    *X% =25.4*F/(W*Val(D$(T,4)))
Return
|
    Procedure Force(G$,F%)
    Volts=Val (G$) *Val (D$(T,l0))
    If Val(D$(T,2))>44 Then
        *F%
    Else
        *F% =P3*Volts*45.9
    Endif
Return
I
Procedure Edit
    Cls
    Print "Loading...."
    Open "I",#8,"test.dat"
    Test=0
    Repeat
        Test=Test+l
        @Load(Test)
    Until Eof(#8)
    Close #8
    Print "Done."
    Ditl:
    Input "Test# to edit (return to quit)";T$
    If T$<>"" Then
        Gt=0
        Repeat
            Gt=Gt+1
        Until (Val(T$)=Val(D$(Gt, 2)) Or Gt>=Test)
        @Display(Gt)
            Goto Ditl
    Endif
    Open "O",#8,"Edited.dat"
    For T=l To Test
        For Zz=l To l7
            Print #8,D$(T,Zz)
        Next Zz
        If Val(D$(T,l7))<>0 Then
            For Zz=l To Val(D$(T,l7))
                For W=l To 3
                    Print #8,E$(T,Zz,W)
                    Next W
            Next Zz
```

```
Endif
Print #8,D$(T,18)
If Val(D$(T,l8))<>0 Then
    For Zz=1 To Val(D$(T,18))
        For W=1 To 4
            Print #8,F$(T,Zz,W)
        Next W
    Next Zz
Endif
For Zz=19 To 25
    Print #8,D$(T,Zz)
Next Zz
    Next T
    Close #8
    Kill "test.dat"
    Name "edited.dat" As "test.dat"
Return
'
Procedure Display(T)
    Dis:
    Cls
    For Zz=1 To l7
    Print Zz;":";D$(T,Zz),
    Next Zz
    If Val(D$(T,l7))<>0 Then
        For Zz=l To Val(D$(T,17))
            For W=1 To 3
                Print "N ";Zz;",";W;":";E$(T,Zz,W),
            Next W
        Next Zz
    Endif
    Print 18;":";D$(T,18),
    If Val(D$(T,18))<>0 Then
    For Zz=1 To Val(D$(T,18))
                For W=1 To 4
                    Print "E ";Zz;",";W;":";F$(T,Zz,W),
        Next W
    Next Zz
    Endif
    For Zz=19 To 25
    Print Zz;":";D$(T,Zz),
    Next Zz
    Print
    Input "Enter character";A$
    A$=Upper$(A$)
    Input "# l";Dx$
    Dx=Val (Dx$)
    Input "# 2 ";Dy$
    Dy=Val (Dy$)
    If Val(AS)}>=1\mathrm{ And Val(A$) <=25 Then
            Input "Enter new value";D$(T,Val(A$))
            Goto Dis
    Endif
```

```
    If A$="N" Then
    Input "Enter new neck";E$(T,Dx,Dy)
    Goto Dis
    Endif
    If A$="" Then
    Goto Dis3
    Endif
    If A$="E" Then
    Input "Enter new neck";F$(T,Dx;Dy)
    Goto Dis
    Endif
    Dis3:
Return
I
Procedure Elastic
    On Which Gosub Screen,Prnter
    Work$=K$
    Mid$(Work$,10,33)="Elastic Neck Recover% (Nu-Nl/Nl)="
    @Cdo(D$(T,23))
    If Cdo! Then
    Rt=Val(D$(T,l7))
    If Rt<>0 Then
        @Decimal(E$(T,Rt,l),*Nl)
        @Decimal(D$(T, 23),*Nu)
        Hk=(Nu-Nl)/Nl
        Mid$(Work$,5l,5)=Left$(Str$(Hk),5)
    Else
        Mid$ (Work$,5l,4)="NCDO"
    Endif
    Else
    Mid$(Work$,5l,4)="NCDO"
    Endif
    On Which Gosub Screen,Prnter
    Work$=K$
    Mid$(Work$,l0,39)="Elastic Major Axis Recover% (Mu-
    Ml/M1)="
    @Cdo(D$(T, 24))
    If Cdo! Then
        Rt=Val(D$(T,18))
    If Rt<>O Then
        @Decimal(F$(T,Rt,l),*Nl)
        @Decimal(D$(T, 24),*Nu)
        Hk=(Nu-Nl)/Nl
        Mid$(Work$,5l,5)=Left$(Str$(Hk),5)
    Else
        Mid$(Work$,51,4)="NCDO"
    Endif
    Else
    Mid$(Work$,51,4)="NCDO"
    Endif
        On Which Gosub Screen,Prnter
    Work$=k$
    Mid$(Work$,l0,39)="Elastic Minor Axis Recover% (Mu-
```

```
    Ml/Ml)="
        @Cdo(D$(T,25))
        If Cdo! Then
            Rt=Val (D$(T,l8))
        If Rt<>0 Then
    @Decimal(F$(T,Rt,2),*Nl)
    @Decimal(D$(T, 25),*Nu)
    Hk=(Nu-Nl)/Nl
    Mid$(Work$,5l,5)=Left$(Str$(Hk),5)
    Else
    Mid$(Work$,5l,4)="NCDO"
    Endif
    Else
    Mid$(Work$,51,4)= "NCDO"
    Endif
    On Which Gosub Screen,Prnter
    Work$=K$
Return
,
Procedure Ed
    On Which Gosub Screen,Prnter
    Work$=K$
    Mid$(Work$,40,37)="Strain Stress(psi) Major Minor"
    On Which Gosub Screen,Prnter
    Kr=Val(D$(T,18))
    If Kr<>0 Then
        For D=1 To Kr
            Work$=K$
            @Cdo(D$(T,ll)+F$(T,D,l)+F$(T,D,2)+F$(T,D,3)+F$(T,D,4
            ))
            If Cdo! Then
                    @Decimal(FS(T,D;l),*Major)
                    @Decimal(F$(T,D,2),*Minor)
                    @Decimal (D$(T,5),*Lo)
                    @Decimal (D$ (T,6),*W)
                    Xj=@Xcon(Val(F$(T,D,3)),T)-@Xcon(Val(D$(T,ll)),T)
                    Xj=Xj/Lo
                    @Stress(W,F$(T,D,4),*Yj)
                    Mid$(Work$,40,5)=Left$(Str $(Xj),5)
                    Mid$(Work$,50,Int(Logl0(Yj+l)+l))=Str$(Yj)
                    Ma=Int(Log(Major)*l0000)/10000
                    Mi=Int(Log(Minor)*10000)/10000
                    Mid$(Work$,63,5)=Left$(Str$(Ma),5)
                    Mid$(Work$,72,5)=Left$(Str$(Mi),5)
                    If Abs(Abs(Ma)-Abs(Mi))>0.06 Then
                    Mid$(Work$,78,1)="*"
                    Endif
            Else
                    Mid$(Work$,40,4)= "NCDO"
            Endif
            On Which Gosub Screen,Prnter
            Next D
    Endif
    Work $=K$
Return
```

OUTPUT
Test Mat. Orient. Mat. Note Thick. (mils) Neck Reduc.
31 MD Pp South Piece
$\begin{array}{cc}\text { TStrain } & \text { TStress(psi) } \\ 0.264 & 2156\end{array}$
0.787

EStrain EStress(psi)
$0.302 \quad 17970.166$

35 MD PP South Piece
0.787

TStrain TStress(psi) 0.2271804

EStrain EStress(psi) 0.2551578
0.125

40 CD PP South Piece
0.787

TStrain TStress(psi) $0.087 \quad 8617$ 0.13513248 0.20019431

| 0.091 | 8433 | 0.021 |
| :--- | :--- | :--- |
| 0.144 | 12402 | 0.063 |
| 0.221 | 17363 | 0.106 |

42 CD PP South Piece TStrain TStress(psi) $0.127 \quad 11906$
0.787

EStrain EStress(psi) 0.13611420
0.040
$30 \quad C D \quad P P$ North Piece TStrain TStress(psi) 0.0913442
0.787
$\begin{array}{ccc}\text { EStrain } & \text { EStress(psi) } & \\ 0.095 & 3285 & 0.045\end{array}$
57 MD PP TDO O' from Exit 0.866
TStrain TStress(psi) EStrain EStress(psi)
$0.107 \quad 3752$
0.113
3596
0.041 0.2055161
0.2274623
0.104

62 MD PP TDO $0^{\prime}$ from Exit 0.866
TStrain TStress(psi) EStrain EStress(psi)

| 0.100 | 4288 | 0.106 | 4110 | 0.041 |
| :--- | :--- | :--- | :--- | :--- |
| 0.194 | 5978 | 0.214 | 5480 | 0.083 |
| 0.280 | 7618 | 0.323 | 6507 | 0.145 |

61 MD PP TDO $0^{\prime}$ from Exit 0.866
$\begin{array}{ccccc}\text { TStrain } & \text { TStress(psi) } & \text { EStrain } & \text { EStress(psi) } & \\ 0.091 & 4697 & 0.095 & 4513 & 0.039\end{array}$
$53 \mathrm{CD} \quad \mathrm{PP}$ TDO $0^{\prime}$ from Exit 0.866 TStrain TStress(psi) EStrain EStress(psi) $\begin{array}{lllll}0.071 & 9932 & 0.074 & 9535 & 0.04\end{array}$

60 CD PP TDO $0^{\prime}$ from Exit 0.866 TStrain TStress(psi) EStrain EStress(psi) $\begin{array}{lllll}0.105 & 11437 & 0.111 & 10960 & 0.041\end{array}$

55 MD PP TDO 20' from exit 1.259 TStrain TStress(psi) EStrain EStress(psi) $\begin{array}{lllll}0.093 & 3366 & 0.098 & 3229 & 0.040 \\ 0.190 & 4623 & 0.209 & 4152 & 0.102\end{array}$

59 MD PP TDO 20' from exit l. 259

| TStrain | TStress(psi) | EStrain | EStress(psi) |  |
| :---: | :---: | :---: | :---: | :---: |
| 0.112 | 3516 | 0.119 | 3296 | 0.062 |
| 0.176 | 4205 | 0.193 | 3767 | 0.104 |

91 CD PP TDO 20' from exit 1.259

| TStrain | TStress(psi) | EStrain | EStress(psi) |  |
| :---: | :---: | :---: | :---: | :---: |
| 0.077 | 4997 | 0.080 | 4945 | 0.010 |
| 0.118 | 7125 | 0.125 | 6828 | 0.041 |

$90 \mathrm{MD} \quad \mathrm{PP}$ TDO $30^{\prime}$ from exit 1.377

| TStrain | TStress(psi) | EStrain | EStress(psi) |  |
| :---: | :---: | :---: | :---: | :---: |
| 0.085 | 2319 | 0.089 | 2251 | 0.029 |
| 0.128 | 2583 | 0.136 | 2455 | 0.049 |
| 0.187 | 3032 | 0.206 | 2762 | 0.089 |
| 0.241 | 3523 | 0.273 | 3069 | 0.128 |
| 0.301 | 3936 | 0.351 | 3274 | 0.168 |
| 0.343 | 4410 | 0.410 | 3581 | 0.188 |
| 0.410 | 5861 | 0.507 | 3888 | 0.336 |

72 MD PP TDO 30' from exit 1.377
TStrain TStress(psi) EStrain EStress(psi)

| 0.105 | 2741 | 0.110 | 2583 | 0.057 |
| :--- | :--- | :--- | :--- | :--- |
| 0.170 | 3298 | 0.185 | 2981 | 0.096 |
| 0.235 | 3789 | 0.265 | 3279 | 0.134 |
| 0.336 | 4551 | 0.399 | 3676 | 0.192 |

$85 \mathrm{MD} \quad \mathrm{PP}$ TDO 40' from exit 1.456
TStrain TStress(psi) EStrain EStress(psi) $\begin{array}{lllll}0.100 & 2172 & 0.106 & 2125 & 0.021\end{array}$

87 MD PP TDO 40' from exit 1.456
TStrain TStress(psi) EStrain EStress(psi)

| 0.100 | 2160 | 0.106 | 2094 | 0.030 |
| :--- | :--- | :--- | :--- | :--- |
| 0.152 | 2606 | 0.164 | 2394 | 0.081 |
| 0.192 | 2888 | 0.212 | 2593 | 0.102 |
| 0.213 | 3069 | 0.238 | 2693 | 0.122 |
| 0.259 | 3258 | 0.296 | 2793 | 0.142 |
| 0.292 | 3620 | 0.339 | 2992 | 0.173 |
| 0.345 | 4010 | 0.413 | 3192 | 0.204 |

83 CD PP TDO 40' from exit 1.456
$\begin{array}{ccccc}\text { TStrain } & \text { TStress(psi) } & \text { EStrain } & \text { EStress(psi) } & \\ 0.113 & 5430 & 0.119 & 5199 & 0.042\end{array}$
77 CD PP TDO 40' from exit 1.456 TStrain TStress(psi) EStrain EStress(psi)

| 0.085 | 5332 | 0.089 | 5100 | 0.043 |
| :--- | :--- | :--- | :--- | :--- |
| 0.115 | 7047 | 0.122 | 6587 | 0.065 |
| 0.159 | 8970 | 0.172 | 8287 | 0.076 |

80 MD PP TDO 50' from exit l.574 TStrain TStress(psi) EStrain EStress(psi) 0.1152511
$0.122 \quad 2354$
0.062

| 0.168 | 2877 | 0.184 | 2637 | 0.083 |
| :--- | :--- | :--- | :--- | :--- |
| 0.246 | 3639 | 0.278 | 3108 | 0.145 |
| 0.301 | 4173 | 0.351 | 3390 | 0.187 |
| 0.327 | 4462 | 0.387 | 3579 | 0.197 |

79 MD PP TDO 50' from exit 1.574 TStrain TStress(psi) EStrain EStress(psi) $\begin{array}{lllll}0.115 & 2441 & 0.122 & 2347 & 0.038\end{array}$

33 MD PP TDO 60' from exit l.771
TStrain TStress(psi) EStrain EStress(psi)

| 0.157 | 1118 | 0.171 | 1025 | 0.083 |
| :--- | :--- | :--- | :--- | :--- |
| 0.231 | 1369 | 0.260 | 1198 | 0.125 |
| 0.338 | 1833 | 0.402 | 1489 | 0.187 |
| 0.306 | 2214 | 0.358 | 1684 | 0.239 |

43 MD. PP TDO 60' from exit 1.771 TStrain TStress(psi) EStrain EStress(psi)

| 0.141 | 3051 | 0.151 | 2860 | 0.062 |
| :--- | :--- | :--- | :--- | :--- |
| 0.244 | 4194 | 0.277 | 3670 | 0.125 |
| 0.331 | 5314 | 0.393 | 4318 | 0.187 |
| 0.377 | 6021 | 0.459 | 4641 | 0.229 |
| 0.435 | 6764 | 0.545 | 5073 | 0.25 |

50 MD PP TDO 60' from exit 1.771 TStrain TStress(psi) EStrain EStress(psi)

| 0.071 | 2992 | 0.074 | 2930 | 0.020 |
| :--- | :--- | :--- | :--- | :--- |
| 0.187 | 5297 | 0.206 | 4856 | 0.083 |

65 MD PP TDO 60' from exit l.771

| TStrain | TStress(psi) | EStrain | EStress(psi) |  |
| :---: | :---: | :---: | :---: | :---: |
| 0.211 | 54477 | 0.235 | 50030 | 0.081 |
| 0.246 | 54207 | 0.279 | 47569 | 0.122 |
| 0.324 | 65673 | 0.382 | 54951 | 0.163 |
| 0.373 | 74194 | 0.453 | 59052 | 0.204 |

52 CD PP TDO 60' from exit 1.771 $\begin{array}{lcccc}\text { TStrain } & \text { TStress(psi) } & \text { EStrain } & \text { EStress(psi) } & \\ 0.059 & 3444 & 0.060 & 3364 & 0.023\end{array}$

78 CD PP TDO 60' from exit 1.771 TStrain TStress(psi) EStrain EStress(psi) $\begin{array}{lllll}0.077 & 3253 & 0.080 & 3105 & 0.045\end{array}$

69 CD PP TDO 70' from exit 1.968 TStrain TStress(psi) EStrain EStress(psi)

| 0.113 | 4438 | 0.120 | 4245 | 0.043 |
| :--- | :--- | :--- | :--- | :--- |
| 0.192 | 6200 | 0.212 | 5661 | 0.086 |
| 0.260 | 7595 | 0.297 | 6604 | 0.130 |
| 0.300 | 8346 | 0.350 | 7076 | 0.152 |
| 0.351 | 9580 | 0.421 | 7705 | 0.195 |
| 0.393 | 10166 | 0.482 | 8177 | 0.195 |

105 MD \#l (6" from center edge) 0.787 TStrain TStress(psi) EStrain EStress(psi)
0.1663741 $0.181 \quad 3426 \quad 0.084$

| 103 MD \#2 (12" from center | edge) 0.787 |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| TStrain | TStress(psi) | EStrain | EStress(psi) |  |
| 0.070 | 3078 | 0.072 | 3014 | 0.020 |
| 0.159 | 4420 | 0.172 | 4144 | 0.062 |
| 0.219 | 5046 | 0.245 | 4521 | 0.104 |

109 MD \#5 (42" from center edge) 0.787 TStrain TStress(psi) EStrain EStress(psi)

| 0.077 | 3078 | 0.080 | 3014 | 0.020 |
| :--- | :--- | :--- | :--- | :--- |
| 0.130 | 3974 | 0.139 | 3767 | 0.052 |
| 0.178 | 4521 | 0.195 | 4144 | 0.083 |
| 0.219 | 5046 | 0.245 | 4521 | 0.104 |
| 0.276 | 5734 | 0.318 | 4897 | 0.145 |
| 0.317 | 6409 | 0.373 | 5274 | 0.177 |
| 0.359 | 7138 | 0.432 | 5651 | 0.208 |
| 0.410 | 7927 | 0.507 | 6028 | 0.239 |

108 MD \#6 (48" from center edge) 0.787 TStrain TStress(psi) EStrain EStress(psi) $\begin{array}{lllll}0.115 & 3889 & 0.122 & 3728 & 0.041\end{array}$
115 MD \#10 (48" from center edge) 0.787 TStrain TStress(psi) EStrain EStress(psi) $0.035 \quad 2260$
0.0362214
0.020
114 MD \#ll (96" from center edge) 0.787 TStrain TStress(psi) EStrain EStress(psi)

| 0.038 | 2474 | 0.039 | 2448 | 0.010 |
| :--- | :--- | :--- | :--- | :--- |
| 0.103 | 3538 | 0.108 | 3390 | 0.041 |
| 0.168 | 4521 | 0.184 | 4144 | 0.083 |
| 0.201 | 4893 | 0.223 | 4332 | 0.114 |
| 0.250 | 5513 | 0.284 | 4709 | 0.145 |

97 MD \#l2(102" fromm center edge) 0.787

| TStrain | TStress(psi) | EStrain | EStress(psi) |  |
| :---: | :---: | :---: | :---: | :---: |
| 0.056 | 2637 | 0.058 | 2583 | 0.020 |
| 0.123 | 3734 | 0.131 | 3506 | 0.061 |

100 CD \#13 (6" from center edge) 0.787 TStrain TStress(psi) EStrain EStress(psi)

| 0.054 | 5194 | 0.055 | 5086 | 0.020 |
| :--- | :--- | :--- | :--- | :--- |
| 0.100 | 9042 | 0.106 | 8665 | 0.041 |

104 CD \#l4 (6" from center edge) 0.787 TStrain TStress(psi) EStrain EStress(psi) $\begin{array}{llll}0.088 & 8850 & 0.092 & 8665\end{array}$
93 CD \#l6 (42" from center edge) 0.787 TStrain TStress(psi) EStrain EStress(psi)

| 0.100 | 9435 | 0.106 | 9042 | 0.041 |
| :--- | :--- | :--- | :--- | :--- |
| 0.164 | 13563 | 0.178 | 12433 | 0.083 |


| 113 CD \#17 | (78" from | edge) | 787 |  |
| :---: | :---: | :---: | :---: | :---: |
| TStrain | TStress(psi) | EStrain | EStress(psi) |  |
| 0.027 | 3078 | 0.027 | 3045 | 0.010 |
| 0.090 | 7551 | 0.094 | 7233 | 0.042 |
| 0.120 | 10363 | 0.128 | 9708 | 0.063 |
| 101 CD \#18 | (78" from c | edge) | 787 |  |
| TStrain | TStress(psi) | EStrain | EStress(psi) |  |
| 0.075 | 6059 | 0.078 | 5845 | 0.035 |
| 0.115 | 8465 | 0.122 | 8037 | 0.050 |
| 0.149 | 11008 | 0.161 | 10229 | 0.070 |

96 CD \#19 (84" from center edge) 0.787 TStrain TStress(psi) EStrain EStress(psi)

| 0.056 | 5274 | 0.058 | 5167 | 0.020 |
| :--- | :--- | :--- | :--- | :--- |
| 0.100 | 8272 | 0.106 | 7935 | 0.040 |

66 CD \#20 (84" from center edge) 0.787
TStrain TStress(psi) EStrain EStress(psi)

| 0.149 | 13664 | 0.161 | 12810 | 0.062 |
| :--- | :--- | :--- | :--- | :--- |
| 0.192 | 17664 | 0.212 | 15824 | 0.104 |

116 MD PP TDO 10' from exit l.181 TStrain TStress(psi) EStrain EStress(psi)

| 0.125 | 1048 | 0.133 | 994 | 0.051 |
| :--- | :--- | :--- | :--- | :--- |
| 0.159 | 1205 | 0.172 | 1118 | 0.072 |
| 0.232 | 1435 | 0.262 | 1242 | 0.134 |
| 0.288 | 1617 | 0.334 | 1367 | 0.154 |
| 0.301 | 1786 | 0.351 | 1491 | 0.164 |
| 0.301 | 1786 | 0.351 | 1491 | 0.164 |

11745 PP North Piece $\quad 0.787$
TStrain $\begin{gathered}\text { TStress(psi) }\end{gathered} \quad$ EStrain EStress(psi)

| TStrain | TStress(psi) | EStrain | EStress(psi) |  |
| :---: | :---: | :---: | :---: | :---: |
| 0.082 | 2358 | 0.085 | 2308 | 0.021 |
| 0.141 | 3269 | 0.151 | 3078 | 0.058 |
| 0.262 | 4973 | 0.300 | 4232 | 0.148 |

$118 \mathrm{CD} \quad \mathrm{PP}$ TDO $10^{\prime}$ from exit l.181

| TStrain | TStress(psi) | EStrain | EStress(psi) |  |
| :---: | :---: | :---: | :---: | :---: |
| 0.106 | 2157 | 0.111 | 2049 | 0.05 |
| 0.162 | 2883 | 0.176 | 2652 | 0.08 |

11945 PP North Piece
0.787

TStrain TStress(psi)
EStrain EStress(psi)

| 0.107 | 1808 | 0.113 | 1695 | 0.062 |
| :--- | :--- | :--- | :--- | :--- |
| 0.171 | 2944 | 0.186 | 2637 | 0.104 |
| 0.233 | 4410 | 0.262 | 3767 | 0.145 |

121 MD PP TDO 10' from exit l.181
TStrain TStress(psi) EStrain EStress(psi)

| 0.002 | 0 | 0.002 | 0 | 0.02 |
| :--- | :--- | :--- | :--- | :--- |
| 0.005 | 0 | 0.005 | 0 | 0.06 |

Mat.: Material, Orient.: Orientation, Thick.: Thickness, Reduc.: Reduction, PP: Polypropylene.
TStrain: True Strain with respect to neck. TStress: True Stress with respect to neck. EStrain: Engineering Strain with respect to neck. EStress: Engineering Stress with respect to neck. Neck Reduc.: (Original width of web-New width)/Original width.


Strain Stress(psi)
$0.151 \quad 3690-0.05$
59 MD PP TDO 20' from exit 1.259
Strain Stress(psi)
0.1513532
$-0.01$
91 CD PP TDO 20' from exit 1.259
$\begin{array}{lcl}\text { Strain } & \text { Stress(psi) } & \\ 0.064 & 4003 & -0.02 \\ 0.011 & 6357 & -0.05\end{array}$

94 CD PP TDO 20' from exit 1.259
Strain Stress(psi)
0.0844914
$-0.05$
90 MD PP TDO $30^{\prime}$ from exit 1.377
Strain Stress(psi)
0.1172353
$0.184 \quad 2660$
$0.239 \quad 2967$
0.3063171
$0.390 \quad 3478$
0.471 - 3785

72 MD PP TDO $30^{\prime}$ from exit 1.377 Strain Stress(psi)
$0.096 \quad 2484 \quad-0.09$
0.202 2981 -0.06
$0.334 \quad 3577$-0.04
85 MD PP TDO $40^{\prime}$ from exit 1.456

| Strain | Stress(psi) |  |
| :--- | :---: | :--- |
| 0.089 | 2018 | -0.05 |

$0.167 \quad 2337 \quad-0.03$
0.217 -0.06

87 MD PP TDO $40^{\prime}$ from exit 1.456
Strain Stress(psi)
$0.090 \quad 1995$-0.07
$0.196 \quad 2493-0.08$
$0.304 \quad 2793-0.08$
$0.402 \quad 3192 \quad-0.07$
83 CD PP TDO 40' from exit 1.456 Strain Stress(psi) $0.103 \quad 4679$-0.02

77 CD PP TDO 40' from exit 1.456

| Strain | Stress(psi) |  |
| :--- | :---: | :--- |
| 0.106 | 5950 | -0.07 |
| 0.156 | 7969 | -0.05 |

80 MD PP TDO 50' from exit 1.574 Strain Stress(psi)

| 0.100 | 2166 | -0.07 |
| :--- | :--- | :--- |
| 0.248 | 3014 | -0.04 |
| 0.384 | 3579 | -0.04 |

79 MD PP TDO 50' from exit 1.574 Strain Stress(psi) 0.1142260
$-0.07$
25 CD PP TDO 50' from exit 1.574 Strain Stress(psi)

| 0.193 | 10201 |
| :--- | :--- |
| 0.251 | 11901 |

-0.01
-0.02
33 MD PP TDO 60' from exit l.771 Strain Stress(psi) 0.154982
-0.01
$0.330 \quad 1360$
$0.450 \quad 1586$
-0.11
0.024

43 MD PP TDO 60' from exit l.771 Strain Stress(psi) 0.1112536
$-0.15$ $0.217 \quad 3346$-0.06 $0.353 \quad 4102 \quad-0.04$ $0.456 \quad 4318 \quad-0.01$ 0.5124911 -0.01 $0.585 \quad 5289-0.00$

50 MD PP TDO 60' from exit 1.771 Strain Stress(psi) 0.1323935 0.3075525 .
$-0.05$ 0.012

65 MD PP TDO 60' from exit l.771 Strain Stress(psi) $\begin{array}{lll}0.135 & 34447 & -0.05 \\ 0.235 & 44289 & -0.06 \\ 0.412 & 57412 & -0.04\end{array}$

52 CD PP TDO 60' from exit l.771 Strain Stress(psi) 0.1667009
$-0.05$
69 CD PP TDO 70' from exit 1.968 Strain Stress(psi) $\begin{array}{ll}0.103 & 3774 \\ 0.191 & 5346 \\ 0.279 & 6447 \\ 0.359 & 7233 \\ 0.432 & 7862\end{array}$
$-0.09$
-0.01
$-0.02$
0.024
0.171

105 MD \#l(6" from center edge) 0.787 Strain Stress(psi) 0.1113045
$-0.02$
103 MD \#2(12" from center edge) 0.787 Strain Stress(psi) $0.055 \quad 3014$
$\begin{array}{ll}0.114 & 3579 \\ 0.206 & 4144\end{array}$
-0.02
-0.05
$-0.06$
106 MD \#4 (30" from center edge) 0.787

| Strain | Stress(psi) |  |
| :--- | :---: | :--- |
| 0.055 | 3045 | $\mathbf{- 0 . 0 2}$ |
| 0.122 | 3807 | -0.05 |

109 MD \#5(42" from center edge) 0.787
Strain Stress(psi)
$0.066 \quad 3014$
0.1223579
$-0.05$
$0.228 \quad 4521 \quad-0.06$
$0.301 \quad 4897$-0.05
$0.357 \quad 5274-0.03$
0.4185651 -0.14
$0.490 \quad 6028 \quad-0.04$
108 MD \#6(48" from center edge) 0.787
Strain Stress(psi)
$0.066 \quad 2983$
0.1063355
0.1724101
$-0.02$
$-0.02$
$-0.03$
115 MD \#lO(48" from center edge) 0.787 Strain Stress(psi) 0.0612583
$-0.00$
114 MD \#ll(96" from center edge) 0.787
Strain Stress(psi)
$0.061 \quad 2825$
-0.02
$0.150 \quad 3767$
$0.251 \quad 4521$
0.2564521
-0.00 0.009 0.001

97 MD \#l2(102" form center edge) 0.787 Strain Stress(psi) $\begin{array}{ll}0.041 & 2399 \\ 0.108 & 3321\end{array}$ 0.108 3321 -0.02

100 CD \#13(6" from center edge) 0.787 Strain Stress(psi) $0.039 \quad 3767$
$-0.02$ $0.089 \quad 7535$-0.02

104 CD \#l4(6" from center edge) 0.787 Strain Stress(psi) 0.075 - 5651 -0.02

93 CD \#16(42" from center edge) 0.787
Strain Stress(psi)
$0.117 \quad 9419$
$-0.00$
$0.167 \quad 12056$
0.25115070
$-0.03$
-0.01
113 CD \#l7(78" from center edge) 0.787
Strain Stress(psi) 0.0786091
0.156 11421
$-0.02$
$-0.05$
101 CD \#l8(78" from center edge) 0.787
Strain Stress(psi)

| 0.066 | 5114 |
| :--- | :--- |
| 0.111 | 7672 |

$-0.02$
$-0.02$
$0.145 \quad 9499$
-0.05
$96 \mathrm{CD} \# 19(84 "$ from center edge) 0.787
Strain Stress(psi) $\begin{array}{ll}0.044 & 4059 \\ 0.089 & 7012\end{array}$
-0.04
$0.089 \quad 7012 \quad-0.05$
66 CD \#20(84" from center edge) 0.787
Strain Stress(psi) $0.100 \quad 8854$
$-0.09$
$0.186 \quad 14317 \quad-0.02$
67 CD \#22(48" from center edge) 0.787
Strain Stress(psi) 0.11710518
$-0.09$
64 CD \#24(12" from center edge) 0.787 Strain Stress(psi) 0.11610549
$-0.05$
116 MD PP TDO $10^{\prime}$ from exit 1.181 Strain Stress(psi)
0.106994

$$
\begin{aligned}
& -0.00 \\
& 0.059 \\
& -0.00 \\
& -0.01
\end{aligned}
$$

0.2231242
$0.295 \quad 1267$
0.3511491

11745 PP North
0.787
$\begin{array}{lc}\text { Strain Stress(psi) } \\ 0.116 & 2693\end{array}$

| 0.116 | 3270 |
| :--- | :--- |
| 0.171 | 3463 |
| 0.232 | 4232 |

$$
-0.02
$$

$$
-0.01
$$

$$
\begin{array}{lll}
0.302 & 4232 & -0.04 \\
0.302 &
\end{array}
$$



| 114 | MD | \#ll(96" from center edge) | 0.787 | 86828 |
| :---: | :---: | :---: | :---: | :---: |
| 97 | MD | \#12(102" from center edge) | ) 0.787 | 72455 |
| 100 | $C D$ | \#13(6" from center edge) | 0.787 | 135067 |
| 104 | $C D$ | \#14 (6" from center edge) | 0.787 | 81040 |
| 102 | $C D$ | \#15(42" from center edge) | 0.787 | 148527 |
| 93 | CD | \#16(42" from center edge) | 0.787 | 135067 |
| 113 | CD | \#17(78" from center edge) | 0.787 | 98575 |
| 101 | CD | \#18(78" from center edge) | 0.787 | 98230 |
| 96 | CD | \#19(84" from center edge) | 0.787 | 139274 |
| 66 | CD | \#20(84" from center edge) | 0.787 | 168834 |
| 68 | CD | \#21 | 0.787 | 114807 |
| 67 | CD | \#22(48" from center edge) | 0.787 | 122860 |
| 63 | CD | \#23(12" from center edge) | 0.787 | 120849 |
| 64 | CD | \#24(12" from center edge) | 0.787 | 106070 |
| 116 | MD | PP TDO 10' from exit | 1.181 | 22279 |
| 117 | 45 | PP North Piece | 0.787 | 41580 |
| 119 | 45 | PP North Piece | 0.787 | 31101 |
| 120. | $C D$ | PP TDO $10{ }^{\prime}$ from exit | 1.181 | 25591 |

Mat.: Material, Thick.: Thickness, E: Young's Modulus.

| Test |  | Orient. Mat. Note Thick. | (mils) | (Sec) |
| :---: | :---: | :---: | :---: | :---: |
| 31 | MD | PP South Piece | 0.787 | 780.3 |
| 29 | MD | PP North Piece | 0.787 | 739.8 |
| 34 | $C D$ | PP North Piece | 0.787 | 1085 |
| 90 | MD | PP TDO 30' from exit | 1.377 | 1181 |
| 72 | MD | PP TDO 30' from exit | 1.377 | 629.9 |
| 87 | MD | PP TDO 40' from exit | 1.456 | 1158 |
| 77 | CD | PP TDO 40' from exit | 1.456 | 784.0 |
| 80 | MD | PP TDO 50' from exit | 1.574 | 603.0 |
| 43 | MD | PP TDO 60' from exit | 1.771 | 834.5 |
| 65 | MD | PP TDO 60' from exit | 1.771 | 907.6 |
| 36 | MD | PP TDO 70' from exit | 1.968 | 719.2 |
| 69 | $C D$ | PP TDO 70' from exit | 1.968 | 991.3 |
| 109 | MD | \#5(42" from center edge) | 0.787 | 977.0 |
| 116 | MD | PP TDO lo' from exit | 1.181 | 595.1 |
| 117 | 45 | PP North Piece | 0.787 | 980.9 |
| 118 | $C D$ | PP TDO 10' from exit | 1.181 | 317.5 |
| 119 | 45 | PP North Piece | 0.787 | 739.8 |
| 121 | MD | PP TDO $10{ }^{\prime}$ from exit | 1.181 | 13.65 |

Relax. time: Relaxation time.

| Test Mat. Orient. Mat. Note Thick. (mils) | Wave form. | (PSI) |  |  |
| :--- | :--- | :--- | :--- | :--- |
| 31 | MD | PP South Piece | 0.787 | 859 |
| 35 | MD | PP South Piece | 0.787 | 1020 |
| 40 | CD | PP South Piece | 0.787 | 4464 |
| 42 | CD | PP South Piece | 0.787 | 5710 |
| 17 | 45 | PP South Piece | 0.787 | 2855 |
| 20 | 45 | PP South Piece | 0.787 | 971 |


| 22 | MD | PP North Piece | 0.787 | 2428 |
| :---: | :---: | :---: | :---: | :---: |
| 26 | MD | PP North Piece | 0.787 | 2671 |
| 30 | CD | PP North Piece | 0.787 | 1059 |
| 32 | $C D$ | PP North Piece | 0.787 | 1076 |
| 34 | CD | PP North Piece | 0.787 | 1700 |
| 23 | 45 | PP North Piece | 0.787 | 1774 |
| 57 | MD | PP TDO O' from Exit | 0.866 | 3082 |
| 62 | MD | PP TDO $0^{\prime}$ from Exit | 0.866 | 3596 |
| 58 | MD | PP TDO O' from Exit | 0.866 | 4646 |
| 61 | MD | PP TDO O' from Exit | 0.866 | 3868 |
| 56 | CD | PP TDO $0^{\prime}$ from Exit | 0.866 | 8220 |
| 53 | CD | PP TDO O' from Exit | 0.866 | 6576 |
| 60 | CD | PP TDO $0^{\prime}$ from Exit | 0.866 | 7535 |
| 45 | MD | PP TDO l0' from exit | 1.181 | 1539 |
| 47 | CD | PP TDO 10' from exit | 1.181 | 1107 |
| 55 | MD | PP TDO 20' from exit | 1.259 | 2537 |
| 59 | MD | PP TDO 20' from exit | 1.259 | 2590 |
| 94 | CD | PP TDO 20' from exit | 1.259 | 3194 |
| 24 | CD | PP TDO 50' from exit | 1.574 | 1700 |
| 25 | CD | PP TDO 50' from exit | 1.574 | 728 |
| 33 | MD | PP TDO 60' from exit | 1.771 | 431 |
| 43 | MD | PP TDO 60' from exit | 1.771 | 1889 |
| 50 | MD | PP TDO 60' from exit | 1.771 | 1674 |
| 65 | MD | PP TDO 60' from exit | 1.771 | 22144 |
| 52 | CD | PP TDO 60' from exit | 1.771 | 2616 |
| 54 | $C D$ | PP TDO 60' from exit | 1.771 | 2846 |
| 69 | CD | PP TDO 70' from exit | 1.968 | 2673 |
| 93 | CD | \#16(42" from center edge) | 0.787 | 4897 |
| 67 | CD | \#22(48" from center edge) | 0.787 | 4798 |
| 64 | CD | \#24(12" from center edge) | 0.787 | 6028 |
| 116 | MD | PP TDO ${ }^{\prime} 0^{\prime}$ from exit | 1.181 | 372 |
| 117 | 45 | PP North Piece | 0.787 | 1539 |
| 118 | CD | PP TDO $10{ }^{\prime}$ from exit | 1.181 | 1929 |
| 119 | 45 | PP North Piece | 0.787 | 1130 |
| 120. | CD | PP TDO $10{ }^{\prime}$ from exit | 1.181 | 1205 |

Wave form.: Wave formation or Onset of Waves.



# Elastic Major Axis Recovery (Mu-Ml/Ml)= 0.212 <br> Elastic Minor Axis Recovery (Mu-Ml/Ml)= -0.2 

29 MD PP North Piece 0.787
Elastic Neck Recovery (Nu-Nl/Nl)= 0
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.09
Elastic Minor Axis Recovery (Mu-M1/Ml)= 0
34 CD PP North Piece 0.787
Elastic Neck Recovery (Nu-Nl/Nl)=
Elastic Major Axis Recovery (Mu-MI/MI)= -0.05
Elastic Minor Axis Recovery (Mu-Ml/MI)= 0.037
57 MD PP TDO $0^{\prime}$ from Exit 0.866
Elastic Neck Recovery (Nu-N1/N1)= 0.069
Elastic Major Axis Recovery (Mu-Ml/MI)= -0.11
Elastic Minor Axis Recovery (Mu-M1/MI)=0.071
62 MD PP TDO $0^{\prime}$ from Exit 0.866
Elastic Neck Recovery (Nu-Nl/N1)= 0.073
Elastic Major Axis Recovery (Mu-M1/MI)= -0.13
Elastic Minor Axis Recovery (Mu-M1/M1)=0
61 MD PP TDO $0^{\prime}$ from Exit 0.866
Elastic Neck Recovery (Nu-N1/N1)= 0.020
Elastic Major Axis Recovery (Mu-Ml/Ml)= ----
Elastic Minor Axis Recovery (Mu-M1/MI)= ----
53 CD PP TDO O' from Exit 0.866
Elastic Neck Recovery (Nu-N1/Nl)= 0.020
Elastic Major Axis Recovery (Mu-Ml/Ml)= ----
Elastic Minor Axis Recovery (Mu-Ml/Ml)= ----
$50 \quad \mathrm{CD} \quad \mathrm{PP}$ TDO $0^{\prime}$ from Exit 0.866
Elastic Neck Recovery (Nu-Nl/Nl)= 0.021
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.05
Elastic Minor Axis Recovery (Mu-M1/Ml)=0.107
55 MD PP TDO 20' from exit l. 259
Elastic Neck Recovery (Nu-Nl/Nl)= 0.068
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.05
Elastic Minor Axis Recovery (Mu-Ml/Ml)=0.071
59 MD PP TDO 20' from exit I. 259
Elastic Neck Recovery (Nu-N1/N1)= 0.069
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.08
Elastic Minor Axis Recovery (Mu-M1/M1)=0.071
91 CD PP TDO 20' from exit l. 259
Elastic Neck Recovery ( $\mathrm{Nu}-\mathrm{Nl} / \mathrm{Nl}$ ) = 0.021
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.02
Elastic Minor Axis Recovery (Mu-M1/M1)=0.035

90 MD PP TDO 30' from exit 1.377
Elastic Neck Recovery (Nu-N1/N1)= 0.261
Elastic Major Axis Recovery (Mu-Ml/M1)= -0.13
Elastic Minor Axis Recovery (Mu-MI/M1)= 0.130
72 MD PP TDO $30^{\prime}$ from exit 1.377
Elastic Neck Recovery ( $\mathrm{Nu}-\mathrm{N} 1 / \mathrm{N} 1$ ) $=0.071$
Elastic Major Axis Recovery (Mu-M1/M1)= -..-
Elastic Minor Axis Recovery (Mu-M1/M1)= ----
87 MD PP TDO 40' from exit 1.456
Elastic Neck Recovery ( $\mathrm{Nu}-\mathrm{Nl} / \mathrm{Nl}$ )= -0.08
Elastic Major Axis Recovery (Mu-M1/M1)= -0.l4
Elastic Minor Axis Recovery (Mu-Ml/Ml)= 0.272
80 MD PP TDO 50' from exit l.574
Elastic Neck Recovery (Nu-N1/N1)= 0.064
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.1
Elastic Minor Axis Recovery (Mu-Ml/Ml)= -0.4l
25 CD PP TDO 50' from exit 1.574
Elastic Neck Recovery (Nu-N1/N1)=
Elastic Major Axis Recovery (Mu-M1/M1)= -0.13
Elastic Minor Axis Recovery (Mu-Ml/Ml)= 0.076
33 MD PP TDO 60' from exit 1.771
Elastic Neck Recovery (Nu-N1/Nl)= 0.095
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.13
Elastic Minor Axis Recovery (Mu-M1/M1)=0.083
43 MD PP TDO 60' from exit 1.771
Elastic Neck Recovery (Nu-N1/Nl)= 0.069
Elastic Major Axis Recovery (Mu-M1/M1)= -0.13
Elastic Minor Axis Recovery (Mu-M1/MI)=0.090
50 MD PP TDO 60' from exit 1.771
Elastic Neck Recovery (Nu-N1/N1)= 0.022
Elastic Major Axis Recovery (Mu-M1/M1)= -0.17
Elastic Minor Axis Recovery (Mu-M1/MI)= 0.076
52 CD PP TDO 60' from exit l.771
Elastic Neck Recovery (Nu-N1/Nl)= 0
Elastic Major Axis Recovery (Mu-M1/M1)= -0.05
Elastic Minor Axis Recovery (Mu-Ml/Ml)= 0.07l
36 MD PP TDO 70' from exit 1.968
Elastic Neck Recovery (Nu-Nl/Nl)= 0.025
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.09
Elastic Minor Axis Recovery (Mu-M1/M1)=0.083
51
CD PP TDO 70' from exit 1.968
Elastic Neck Recovery (Nu-Nl/Nl)= -0.04
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.08

Elastic Minor Axis Recovery (Mu-M1/M1)= 0.071
69 CD PP TDO 70' from exit l.968
Elastic Neck Recovery (Nu-Nl/Nl)= 0
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.23
Elastic Minor Axis Recovery (Mu-Ml/Ml)= 0
109 MD \#5(42" from center edge) 0.787
Elastic Neck Recovery (Nu-Nl/Nl)= 0.082
Elastic Major Axis Recovery (Mu-Ml/M1)= -0.13
Elastic Minor Axis Recovery (Mu-Ml/Ml)=0.090
93 CD \#l6(42" from center edge) 0.787
Elastic Neck Recovery (Nu-N1/N1)= 0.045
Elastic Major Axis Recovery (Mu-Ml/M1)= -0.08
Elastic Minor Axis Recovery (Mu-M1/M1)=0.071
116 MD PP TDO 10' from exit l.181
Elastic Neck Recovery (Nu-N1/Nl)= 0.061
Elastic Major Axis Recovery (Mu-M1/M1)= -0.14
Elastic Minor Axis Recovery (Mu-Ml/M1)=0.166
$11745 \quad$ PP North Piece 0.787
Elastic Neck Recovery (Nu-N1/N1)= 0.1
Elastic Major Axis Recovery (Mu-M1/M1)= -0.1
Elastic Minor Axis Recovery (Mu-M1/M1)=0.166
118 CD PP TDO 10' from exit l.181
Elastic Neck Recovery ( $\mathrm{Nu}-\mathrm{Nl} / \mathrm{Nl}$ ) $=\quad 0.043$
Elastic Major Axis Recovery (Mu-Ml/M1)= -0.08
Elastic Minor Axis Recovery (Mu-M1/Ml)= 0.034
$11945 \quad$ PP North Piece 0.787
Elastic Neck Recovery (Nu-Nl/Nl)= 0.073
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.05
Elastic Minor Axis Recovery (Mu-Ml/M1)= 0.076
121 MD PP TDO $10^{\prime}$ from exit l.181
Elastic Neck Recovery (Nu-Nl/Nl)= -0.03
Elastic Major Axis Recovery (Mu-Ml/Ml)= -0.07
Elastic Minor Axis Recovery (Mu-M1/MI)=0.076

Elastic Rec.: Elastic Recovery.
(Nu-Nl/Nl): (Unload Neck dimension-last measured Loaded Neck dimension)/last measured Loaded Neck dimension.
(Mu-Ml/Ml): (Unload Axis dimension-last measured Loaded Axis dimension)/last measured Loaded Axis dimension.

Test Mat. Orient. Mat. Note Thick. (mils) Ell. Strains
31 MD PP South Piece $\begin{array}{r}0.787 \\ \text { Strain }\end{array}$ Strain Stress(psi) $\begin{array}{ll}0.189 & 1530 \\ 0.277 & 1748\end{array}$

| Major | Minor |
| :--- | :--- |
| 0.117 | -0.13 |
| 0.171 | -0.28 |
| 0.318 | -0.37 |

35 MD PP South Piece
0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.130 | 1263 | 0.060 | -0.13 |
| 0.226 | 1505 | 0.171 | -0.20 |

$40 \quad C D \quad P P$ South Piece
0.787
$\begin{array}{lccc}\text { Strain } & \text { Stress(psi) } & \text { Major } & \text { Minor } \\ 0.110 & 9922 & 0.060 & -0.13\end{array}$
42 CD PP South Piece
0.787

Strain Stress(psi)
0.103

8565
26 MD PP North Piece
0.787

Strain Stress(psi)
0.111

5586
0.2097043

$$
\begin{array}{ll}
\text { Major } & \text { Minor } \\
0.060 & -0.13
\end{array}
$$

$\begin{array}{ll}\text { Major } & \text { Minor } \\ 0.060 & -0.06 \\ 0.030 & -0.06\end{array}$
34 CD PP North Piece
0.787

Strain Stress(psi)
$0.127 \quad 3400$
0.2174906
$\begin{array}{ll}\text { Major } & \text { Minor } \\ 0.060 & -0.13 \\ 0.117 & -0.16\end{array}$
$62 \mathrm{MD} \quad \mathrm{PP}$ TDO 0 ' from Exit
0.866

Strain Stress(psi) Major Minor
0.1434795

| 0.060 | -0.13 |
| :--- | :--- |
| 0.171 | -0.13 |

$60 \quad C D \quad P P$ TDO $0^{\prime}$ from Exit
0.866

Strain Stress(psi) Major Minor $0.143 \quad 13700 \quad 0.060 \quad-0.13$

MD PP TDO 20' from exit 1.259

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.151 | 3532 | 0.117 | -0.13 |

91 CD PP TDO 20' from exit l.259

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.064 | 4003 | 0.030 | -0.06 |
| 0.111 | 6357 | 0.060 | -0.13 |

$94 C D$ PP TDO 20' from exit 1.259 $\begin{array}{lccc}\text { Strain } & \text { Stress(psi) } & \text { Major } & \text { Minor } \\ 0.084 & 4914 & 0.060 & -0.13\end{array}$
$90 \mathrm{MD} \quad \mathrm{PP}$ TDO 30' from exit 1.377

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.117 | 2353 | 0.060 | -0.13 |
| 0.184 | 2660 | 0.117 | -0.16 |
| 0.239 | 2967 | 0.271 | -0.20 |
| 0.306 | 3171 | 0.318 | -0.24 |
| 0.390 | 3478 | 0.318 | -0.28 |
| 0.471 | 3785 | 0.318 | -0.33 |

72 MD PP TDO 30' from exit l.377

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :--- | :--- |
| 0.096 | 2484 | 0 | -0.13 |
| 0.202 | 2981 | 0.117 | -0.20 |
| 0.334 | 3577 | 0.223 | -0.28 |

85 MD PP TDO $40^{\prime}$ from exit 1.456

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.089 | 2018 | 0.030 | -0.09 |
| 0.167 | 2337 | 0.089 | -0.13 |
| 0.217 | 2762 | 0.117 | -0.20 |

87 MD PP TDO $40^{\prime}$ from exit 1.456

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.090 | 1995 | 0.030 | -0.13 |
| 0.196 | 2493 | 0.089 | -0.20 |
| 0.304 | 2793 | 0.171 | -0.28 |
| 0.402 | 3192 | 0.271 | -0.37 |

$83 \mathrm{CD} \quad \mathrm{PP}$ TDO $40^{\prime}$ from exit 1.456
Strain Stress(psi) Major Minor
$0.103 \quad 4679 \quad 0.030 \quad-0.06$

77 CD PP TDO 40' from exit l.456

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.106 | 5950 | 0.030 | -0.13 |
| 0.156 | 7969 | 0.060 | -0.13 |

80 MD PP TDO 50' from exit l.574

| Strain | Stress(psi) |
| :--- | :---: |
| 0.100 | 2166 |
| 0.248 | 3014 |
| 0.384 | 3579 |


| Major | Minor |
| :--- | :--- |
| 0.030 | -0.13 |
| 0.223 | -0.28 |
| 0.223 | -0.28 |

79 MD PP TDO 50' from exit 1.574

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.114 | 2260 | 0.030 | -0.13 |

25 CD PP TDO 50' from exit 1.574

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.193 | 10201 | 0.117 | -0.13 |
| 0.251 | 11901 | 0.171 | -0.20 |

33 MD PP TDO 60' from exit l.771

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.154 | 982 | 0.117 | -0.13 |
| 0.330 | 1360 | 0.223 | -0.37 |
| 0.450 | 1586 | 0.318 | -0.28 |

43 MD PP TDO 60' from exit 1.771

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.111 | 2536 | 0.060 | -0.28 |
| 0.217 | 3346 | 0.117 | -0.20 |
| 0.353 | 4102 | 0.223 | -0.28 |
| 0.456 | 4318 | 0.271 | -0.28 |
| 0.512 | 4911 | 0.271 | -0.28 |
| 0.585 | 5289 | 0.362 | -0.37 |

50 MD PP TDO 60' from exit 1.771

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.132 | 3935 | 0.060 | -0.13 |

0.1323935
0.060 -0.13
$0.307 \quad 5525 \quad 0.223 \quad-0.20$
65 MD PP TDO 60' from exit l.771

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.135 | 34447 | 0.060 | -0.13 |
| 0.235 | 44289 | 0.117 | -0.20 |
| 0.412 | 57412 | 0.223 | -0.28 |

52 CD PP TDO 60' from exit l.771

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.166 | 7009 | 0.060 | -0.13 |

69 CD PP TDO 70' from exit 1.968

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :--- | :--- |
| 0.103 | 3774 | 0 | -0.13 |
| 0.191 | 5346 | 0.117 | -0.13 |
| 0.279 | 6447 | 0.171 | -0.20 |
| 0.359 | 7233 | 0.318 | -0.28 |
| 0.432 | 7862 | 0.485 | -0.28 |

105 MD \#l(6" from center edge) 0.787
Strain Stress(psi) Major Minor $\begin{array}{llll}0.111 & 3045 & 0.060 & -0.09\end{array}$

103 MD \#2(12" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.055 | 3014 | 0.030 | -0.06 |
| 0.114 | 3579 | 0.060 | -0.13 |
| 0.206 | 4144 | 0.117 | -0.20 |

106 MD \#4 (30" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.055 | 3045 | 0.030 | -0.06 |
| 0.122 | 3807 | 0.060 | -0.13 |

109 MD \#5(42" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.066 | 3014 | 0.030 | -0.09 |
| 0.122 | 3579 | 0.060 | -0.13 |
| 0.178 | 4144 | 0.089 | -0.16 |
| 0.228 | 4521 | 0.117 | -0.20 |
| 0.301 | 4897 | 0.171 | -0.24 |
| 0.357 | 5274 | 0.247 | -0.28 |
| 0.418 | 5651 | 0.271 | -0.47 |
| 0.490 | 6028 | 0.318 | -0.37 |

108 MD \#6(48" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :--- | :--- |
| 0.066 | 2983 | 0 | -0.03 |
| 0.106 | 3355 | 0.030 | -0.06 |
| 0.172 | 4101 | 0.089 | -0.13 |

115. MD \#l0(48" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.061 | 2583 | 0.030 | -0.03 |

114 MD \#ll(96" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.061 | 2825 | 0.030 | -0.06 |
| 0.150 | 3767 | 0.089 | -0.09 |
| 0.251 | 4521 | 0.145 | -0.13 |
| 0.256 | 4521 | 0.171 | -0.16 |

97 MD \#l2(102" form center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :--- | :--- |
| 0.041 | 2399 | 0 | -0.03 |
| 0.108 | 3321 | 0.030 | -0.06 |

100 CD \#l3(6" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :--- | :--- |
| 0.039 | 3767 | 0 | -0.03 |
| 0.089 | 7535 | 0.030 | -0.06 |

104 CD \#14(6" from center edge) 0.787

$$
\begin{array}{lccc}
\text { Strain } & \text { Stress(psi) } & \text { Major } & \text { Minor } \\
0.075 & 5651 & 0.030 & -0.06
\end{array}
$$

93 CD \#l6(42" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.117 | 9419 | 0.060 | -0.06 |
| 0.167 | 12056 | 0.089 | -0.13 |
| 0.251 | 15070 | 0.117 | -0.13 |

113 CD \#l7(78" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.078 | 6091 | 0.030 | -0.06 |
| 0.156 | 11421 | 0.060 | -0.13 |

101 CD \#l8(78" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.066 | 5114 | 0.030 | -0.06 |
| 0.111 | 7672 | 0.060 | -0.09 |
| 0.145 | 9499 | 0.060 | -0.13 |

96 CD \#19(84" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :--- | :--- |
| 0.044 | 4059 | 0 | -0.06 |
| 0.089 | 7012 | 0.030 | -0.09 |

66 CD \#20(84" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :--- | :--- |
| 0.100 | 8854 | 0 | -0.13 |
| 0.186 | 14317 | 0.171 | -0.20 |

68 CD \#21
0.787

Strain Stress(psi) Major Minor $0.064 \quad 6405 \quad 0 \quad-0.06$

67 CD \#22(48" from center edge) 0.787 $\begin{array}{lccc}\text { Strain } & \text { Stress(psi) } & \text { Major } & \text { Minor } \\ 0.117 & 10518 & 0 & -0.13\end{array}$

64 CD \#24(12" from center edge) 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.116 | 10549 | 0.060 | -0.13 |

116 MD
PP TDO lo' from exit 1.181

| Strain | Stress(psi) |
| :--- | :---: |
| 0.106 | 994 |
| 0.223 | 1242 |
| 0.295 | 1267 |
| 0.351 | 1491 |


| Major | Minor |
| :--- | :--- |
| 0.060 | -0.06 |
| 0.171 | -0.09 |
| 0.197 | -0.20 |
| 0.271 | -0.28 |

11745 PP North Piece
0.787

Strain Stress(psi)
$0.116 \quad 2693$
0.1713270
0.2323463
0.3024232

| Major | Minor |
| :--- | :--- |
| 0.060 | -0.09 |
| 0.117 | -0.13 |
| 0.171 | -0.20 |
| 0.223 | -0.28 |

$118 \mathrm{CD} \quad \mathrm{PP}$ TDO 10' from exit l.181

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.141 | 2411 | 0.089 | -0.06 |
| 0.200 | 2893 | 0.117 | -0.09 |

$11945 \quad$ PP North Piece 0.787

| Strain | Stress(psi) | Major | Minor |
| :--- | :---: | :---: | :---: |
| 0.131 | 1883 | 0.060 | -0.13 |
| 0.206 | 2825 | 0.171 | -0.20 |

121 MD PP TDO 10' from exit 1.181
Strain Stress(psi) Major Minor

| 0.004 | 0 | 0.060 | -0.13 |
| :--- | :--- | :--- | :--- |
| 0.008 | 0 | 0.171 | -0.20 |

Ell. strains: True Strains of Major and Minor axes of the Ellipses.

## APPENDIX D

## CALIBRATION FOR INSTRON SYSTEM



## APPENDIX E

## TEST BLANK

WEB HANDLING MATERIAL TESTING.
DATE/TEST NUMBER $\qquad$
$\qquad$
Adhesive:
Material:
Thickness: ___ in. (__ mm)
Test Specimen Size:
Test Specimen Grip: Roll __ Clamp
Material Orientation: MD CD $\qquad$ Other $\qquad$ \# of times wrapped around bar: Test temperature: __ F ( $\quad$ C) Crosshead Speed: ___ (in/min)

| Superimposed Grid | Circles <br> $\quad$dia. <br> Squares <br> Other |
| :--- | :--- |
| side |  |
| description: |  |

## Observations:

Necking:
Center buckling:
Cross web waves:
End Failure:
Edge Failure:
Other:

VITA<br>Scott E. Robertson Candidate for the Degree of<br>Master of Science

Thesis: DETERMINATION OF VARIATIONS IN CERTAIN MECHANICAL PROPERTIES ACROSS THE WIDTH OF A FINISHED PRODUCT OF POLYPROPYLENE WEB

Major Field: Mechanical Engineering
Biographical:
Personal Data: Born in Tulsa, Oklahoma, November 22, 1963, the son of Dick Ross and Vida Marie Robertson.

Education: Graduated from Broken Ar row High School, Broken Arrow, Oklahoma, in May 1982; recieved Bachelor of Science Degree in Mechanical Engineering from Oklahoma State University at Stillwater in May, 1986; completed requirements for Masters of Science degree at Oklahoma State University in May, 1989.

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