# MONTE CARLO STUDY OF LIPID 

CHOLESTEROL INTERACTIONS

IN BIOMEMBRANES

BY

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## CHAPTER I

## INTRODUCTION

The purpose of this study is to explore the nature of lipid cholesterol interactions in biomembranes, using the Monte Carlo method.

Our understanding of the membrane and its functions has evolved considerably. It is widely accepted now that a membrane is a two dimensional bimolecular array of molecules of lipids, proteins and in some cases cholesterol. It is about $50 \mathrm{~A}^{\mathrm{O}}$ thick. Biomembranes are usually curved continuously and form closed sacs. The major components of biomembranes, lipids and proteins, are present in the varying amounts, depending on the type of the membrane (1). The lipids and proteins have certain physical properties that determine the structural organization of the membrane.

## The Membrane Components

Lipids : These are organic molecules that can be extracted from wet membranes by use of non polar solvents such as chloroform, benzene or ether. Membrane lipids are amphipathic i.e. a lipid molecule contains both hydrophobic (non-polar) and hydrophilic (polar) regions. These
regions are usually bridged by glycerol moiety or a sphinganine derivative. The most common lipids found in the eukaryotic membranes are phospholipids, glycolipids, sphingolipids and sterols. The last two classes are usually absent in the prokaryotic membranes. Figure 1 shows some typical lipid molecules.

The polar headgroups determine the affinity of the phospholipids for the water, whereas the acyl chains determine the solubility of these molecules in the solvents - polar or non polar. In an aqueous phase the amphipathic molecules reorient themselves so as to minimize unfavorable interactions between hydrocarbon chains and water. This leads to various arrangements that the lipid molecules assume in an aqueous phase (Figure 2). As seen in this figure the hydrophilic region always faces the aqueous environment and the hydrophobic region moves away from the aqueous zone.

The hydrophobic effect (2) has its origin in the strong attractive forces between water molecules. If the solute is to dissolve in the water, it must disrupt these strong attractive forces in favour of attractive forces between water and solute. This is why the ionic solutes readily dissolve in the water.

Apolar groups on the other hand, cause an extensive rearrangement of the neighboring water molecules. This ordering of molecules apparently leads to a decrease in entropy which is thermodynamically unfavorable. For this reason the solution of the apolar solvents in the


Figure 1. Some Typical Phospholipid Molecules.
(a) Phosphatidic Acid. (b) Phosphatidyl Choline. (c) Phophatidyl Ethanolamine. (d) Phosphatidyl Serine.


Figure 1. (continued) Sphingolipids and Glycolipids.
(a) Galactosyldiacylglycerol.
(b) Ceramide. (c) Sphingomylein.

(a)

WATER

(b)

WATER


WATER

(d)

Figure 2. (a) Monolayer. (b) Bilayer. (c) Micelles. (d) Vesicle.
water is resisted. The apolar groups - hydrocarbon chains of the lipid molecules cluster together, excluding water so as to minimize the free energy of the system. The hydrophobic nature of the lipid chains is thus an entropic consideration rather than any other specific interaction.

The geometry of hydrocarbon chains in their stretched form, called all trans configuration, forms a hydrophobic cylinder (Figure 3).

There is a rotation about $C-C$ bonds. In trans configuration the dihedral angle between $\mathrm{C}_{1}$ to $\mathrm{C}_{2}$ and $\mathrm{C}_{3}$ to $\mathrm{C}_{4}$ bonds is 180 degrees. For gauche rotation the most stable and thus lowest in energy, dihedral angles are 120 degrees and 240 degrees (i.e. -120 degrees).

Because of the steric strain the gauche confirmation is less stable by about 0.5 kcal/mole or more, than trans configuration. It is also possible to have two gauche rotations which produce a common chain configuration by rotating about one $C-C$ bond by 120 degrees then rotating either of the two next nearest neighbors by -120 degrees. This produces what is called a 'kink' in the chain. It is obvious that such kinks shorten the length of hydrocarbon chains and thereby increase the volume of the hydrophobic cylinder. The increase in temperature will allow more kinks in the acyl chains. Figure 4 shows some of the chain disorders that may take place in the membrane. At the lower temperatures however, when the phospholipids are in the solid


TRANS

GAUCHE


Figure 3: Trans and Gauche Configurations.

all TRANS TTT


GTTTG


KINK GTG


CIS-BOND

Figure 4. Possible Hydrocarbon Chain Configurations in a Membrane.


Figure 5. Lipid Phase Transition.
crystalline state the acyl chains are in fully stretched all trans state.

In the crystalline state the lipid molecules are packed together in an hexagonal array, with the acyl chains parallel to each other. If the temperature is increased the bilayers undergo distinct organizational changes, although the general structure of the membrane remains the same (Figure 5). At transition temperature the lipids change from crystalline solid state to the liquid gel state. The transition temperature depends on such factors as, type of phospholipid headgroup, acyl chain length (3), number of double bonds, their positions in the chains (4), and composition of the mixture of phospholipids. In general transition temperatures are higher for longer acyl chains and are lower for highly unsaturated acyl chains.

As seen in the Figure 5, below the transition temperature the acyl chains are predominantly in all trans state, parallel to each other but not perpendicular to the bilayer plane. The main transition is preceded by a pretransition which involves reorientation of chains from tilted to the perpendicular positions along with distortion of the bilayer by periodic ripple. Above the transition temperatures the kinks are introduced in the chains which decreases thickness of the bilayer and increases the area of the membrane. The hexagonal array is disrupted as well. The phase transition involves a small volume change (5). The change of pressure over temperature has been found (6) to be 00.44 atm per 1 degree Celsius, using Clausius-Claperon equation.

$$
\begin{equation*}
\Delta P / \Delta T=\Delta H /\left(T_{c}\left(V_{1}-V_{g}\right)\right) \tag{1}
\end{equation*}
$$

where $\Delta H=$ Enthalpy of Transition; $T_{c}=$ Transition Temperature and $\left(\mathrm{V}_{1}-\mathrm{V}_{\mathrm{g}}\right)$ ) Change in volume of two phases. The volume change of $00.037 \mathrm{ml} / \mathrm{mg}$ is observed (7) at the main transition temperature 41.4 degree Celsius for Diapalmitoyl phosphatidylcholine water system. The phase transition in the lipid bilayers are studied by several experimental techniques such as calorimetry (8), X-ray diffraction (9) and spin label resonance (10).

Sterols: are a third major class of lipids, first two being phospholipids and glycolipids. In animal membranes cholesterol is a predominant sterol but in plant membrane it is rare.

A cholesterol molecule consists of a rigid sterol ring about 1.1 nm in length with a hydroxyl group attached at one end (Figure 6). At the other end of the sterol ring structure there is a flexible hydrocarbon chain about 0.8 nm long. Most phospholipid molecules whose acyl chains are at least $9-\mathrm{CH}_{2}$ units long can accommodate cholesterol molecules in bilayers. The molecule is inserted into the bilayer with its hydroxyl OH , group towards polar headgroup of lipids and its apolar hydrocarbon tail towards hydrophobic acyl chains of the bilayer. The plane of the sterol ring is thus perpendicular to the plane of the bilayer. The hydrocarbon tail of cholesterol - with two methyl groups at the end - is rather mobile and interacts with neighboring acyl chains. The molecule is inserted deeply into the bilayer to allow hydrogen bonding between


Figure 6. Sterols: Cholesterol Molecule.
oxygen of -OH group and oxygen of $\mathrm{C}=0$ group of the lipid molecule (Figure 7). The rigid ring structure of cholesterol prevents kinks from forming in neighboring acyl chains. This decreases the molecular area of the phospholipids. Thus the area of cholesterol-phospholipid (1:2) mixture is $25 \%$ lower than the direct sum of their areas (11). This is so called 'Condensing effect'. On the other hand, the hydrogen bonding causes the separation between the polar headgroups of the lipids, thus minimizing electrostatic interaction among them allowing greater freedom of mobility. Incorporation of cholesterol has long been controversial to the extent that some of the early models do not propose hydrogen bonding at all, a claim later refuted (13). The structure of cholesterol is rather significant to the membrane properties but less so for its incorporation into the bilayer.

The amount of cholesterol that can be incorporated in the bilayer without disrupting the membrane function has a upper limit. At $>50$ mole \% some sterol molecules will have no phospholipid neighbors and there are too many sterol-sterol interactions destabilizing the membrane. At about 10 mole \% cholesterol there is an increased rate of lateral diffusion of phospholipids. At about 22 mole \% cholesterol the regions of pure phospholipids and cholesterol disappear and the bilayer consists of closely packed clusters of cholesterol and lipids. Between. 33 to 50 mole \% of cholesterol both species are distributed randomly with some sterols separated by only one lipid molecule. The increase in the amount of cholesterol slowly abolishes the phase transition. (14,15)


Figure 7. Orientation of Cholesterol in the Membrane, Hydrogen Bonding.

The effect of increase in cholesterol on lipid phase transition is shown in Figure 8.

Temperature plays a key role in the lipid-cholesterol interactions. At the temperatures higher than the transition temperature cholesterol increases bilayer rigidity by ordering the fluid state lipids whereas below this temperature it increases fluidity of the solid state lipid by disordering them.

Proteins: The proteins associated with the membranes can be classified in a number of ways - The ease of separation from membrane, geometric structure or simply by their chemical contents.

Weakly bound proteins (peripheral, extrinsic proteins)- The proteins that can be isolated easily using strong salt solutions or EDTA solution. Such an isolation does not significantly disrupt the membrane structure. Cytochrome $C$ found in the inner membrane of mitochondria is an example of peripheral protein.

Tightly bound proteins (Integral, Intrinsic proteins) - Proteins can be isolated by the use of detergents such as Sodium dodecyl sulfate, SDS. The isolation of integral proteins from the membrane causes a serious damage to the membrane structure. The integral proteins are firmly built into the membranes. Globular proteins are quite bulky. They consist of several loops of polypeptide chains. Fibrous proteins consist of a single strand of a polypeptide chain. Both, the globular


Figure 8. Effect of Cholesterol on lipid Phase Transition.
and the fibrous proteins may be transmembrane and therefore, integral proteins (Figure 9).

Proteins play key role in allowing passage of selective chemicals across the membrane. Specific proteins allow passage to a particular chemical species. Thus proteins too, like lipids, are found in the variety of kinds and amounts. The type and the amount of protein present depends on the function of the membrane in question. For example, inner mitochondrial membrane is highly active in its functions and therefore contains 25 different kinds of proteins which constitute 75\% of its weight. On the other hand, mylein which acts as an insulator contains only $20 \%$ protein by weight.

## Membrane Models

The membrane components described in the previous section namely lipids, cholesterol and proteins are organized in a special manner so as to form a functional membrane. Several models have been proposed by various researchers. Of these, the 'fluid mosaic model' is now widely accepted (15). This model stresses the dynamic aspects of the membrane structure such as membrane fluidity. The extrinsic proteins are external but close to the membrane and may interact electrostatically with the polar headgroups of the lipids. The globular proteins in this model float surrounded by lipids (Figure 10).

A. GLOEULAR PROTEIN
B. FIEROUS PROTEIN
C. EXTRINSIC PROTEIN

Figure 9. Proteins in the Membranes.


Figure 10. Model Membranes.

The lipids surrounding the proteins are further classified as the 'annular lipids' which are nearest neighbors of the protein and form a 'ring' around it. The lipids that are further away from the proteins are called 'bulk lipids'. Interaction of lipids and proteins has been under intense investigation both by experimentalists and theorists. Among experimental techniques x-ray diffraction (16), freeze etch fracture (17), thermal differential calorimetry (18, 19) and spin label spectroscopy ( 20,21 ) have been used. On theoretical front, Monte Carlo simulation technique has been used by Scott (22), to study lipid-protein interaction.

The 'annular lipids' due to closeness of the proteins are more ordered and less mobile than the lipids in the bulk. Results of the ESR studies (20,21) indicated the existence of a single layer of lipids surrounding protein, cytochrome C oxidase. This result was further confirmed by theoretical models $(23,24)$. The 'annular lipids' though relatively less mobile do frequently exchange themselves with the bulk lipids. This exchange is called 'hopping frequency'. In the bulk lipids this exchange takes place rather rapidly as compare to the exchange between bulk lipids and annular lipids. This reduction in exchange is attributed to the existence of interaction between protein and boundary lipids.

Although general structure of the membrane is preserved, the membrane components themselves are in continuous motion. (Figure 11)


Figure 11. Modes of Mobility of Membrane Components.
(a) Lateral Diffusion of Lipid. (b) Rotational Diffusion of Lipid. (c) Rotational Diffusion of Protein. (d) Lateral Diffusion of Protein. (e) Side to Side Chain Motion. (f) Lipid Exchange. (g) Rotation about C-C Bond.
A). Lateral Diffusion: Phospholipid and protein molecules diffuse laterally in the plane of the bilayer.
B). Rotational Diffusion: Phospholipid and protein molecules rotate about their long axis.
C). Lipid flip-flop motion: The phospholipid molecules mutually exchange themselves within the bilayers, going from one half of the bilayer to the other. But this motion is extremely slow on the order of days, compared to lateral diffusion which takes place in matter of seconds.
D). Chain motion: Above transition temperatures $T_{c}$, several disorders are introduced in the chain due to rotation about $\mathrm{C}-\mathrm{C}$ bond. The various modes of motions of the membrane constituents along with their mutual interactions indeed form quite an intricate organization. This study attempts to investigate one important aspect, that of lipid cholesterol interaction by using Scott's method (22) of Monte Carlo simulation technique.

The following chapter describes the essentials of this technique. Following this, results and discussion are presented.

## CHAPTER II

## THEORY

The lipid cholesterol interaction study presented here is based on Monte Carlo simulation technique similar to one used by Scott (22) in his investigation of lipid protein interactions.

The Monte Carlo method is an efficient technique used to compute average quantities. In the present case we wish to calculate the average of the quantities called order parameters. This quantity, denoted by 'S' presents a measure of the interactions between the lipids and cholesterol by allowing us to find the extent to which the acyl chains are 'distorted' due the presence of a cholesterol molecule. The average order parameter $\langle\mathrm{Sn}\rangle$, is defined as:

$$
\begin{equation*}
\left\langle s_{n}\right\rangle=\left\langle 3 / 2 \cos ^{2} \theta_{n}-1 / 2\right\rangle \tag{2}
\end{equation*}
$$

Where $\theta_{n}$ represents the angular deviation of nth $C-C$ bond in an acyl chain, from its position while the chain is in all trans state. Thus, for example if the average value of the order parameters were 1.000 it would mean this particular bond did not deviate at all from its original all trans position. A smaller average value of the order parameters
would indicate greater degree of orientational disorder. The average values of the order parameters are thus expected to be in the range of 1 to 0 . The values of the order parameters for each bond averaged over all the chains is then plotted against bond numbers as an pictorial indication of the lipid-cholesterol interaction.

In statistical mechanics the average of observable quantities Ai within canonical ensemble is given by $(25,26)$.

$r_{i}=$ position vector of $i$ th molecule, $E=$ total energy of the system, $T=$ Absolute temperature of the system and $k=$ Boltzmann constant, 1.987 cal/mole-Kelvin. But evaluation of such an integral is rather complex and thus calculation of $\langle A\rangle$ demands alternative, simpler method. The Metropolis Monte Carlo method (27) developed in 1953, provides an efficient procedure of calculating average quantities. This method can be briefly described as follows:

1) Construct a model of the system under consideration. The initial configuration of the particles in the system - positions of carbon atoms of lipids and cholesterol in this case - should be known and saved.
2) Calculate energy $E_{o}$ of this initial configuration and save it. Note that this energy consists of potential energy due to gauche rotations about $C-C$ bonds plus sum of potential energies due to pairwise interactions between all atoms in all molecules.
3) Pick any particle--lipid molecule in this case- and translate it within the plane of the bilayer by a small distance $d r$.

$$
r_{i} \longrightarrow r_{i}+e d r_{i}
$$

where $r_{i}=$ co-ordinates of particle in question, $d r_{i}=$ maximum allowed displacement, $e=$ random number.
4) Pick a bond at random on this translated lipid molecule and perform gauch rotation about $\mathrm{C}-\mathrm{C}$ bond according to rotational probabilities.
5) Apply periodic boundary condition to find if any of the carbon atoms on this chain have been displaced outside the unit cell. Also check for the chain overlaps.
6) Calculate the energy $E_{1}$ of this new configuration.
7) Calculate the energy change, $E=E_{1}-E_{0}$, due to translation and rotation of the chain. (In our model system the perturbent
cholesterol molecule is always held fixed in its position w.r.t. the origin, except its mobile hydrocarbon tail.)
8) If $E<0$ the transition is accepted and the lipid molecule is allowed to retain its new position. If $E>0$,then a quantity $\exp (-E / k T)$ is calculated.
9) The quantity $\exp (-E / k T)$ is compared to a random number RANF (28). $0<\operatorname{RANF}<1$. If $\exp (-E / k T)<$ RANF then the move is rejected and the chain is moved back to its previous position. If $\exp (-E / k T)>$ RANF then move is accepted.
10) Above procedure is carried out for a large number of steps.

In Metropolis Monte Carlo method the configurations are not chosen randomly but are selected such that the transition probability $\mathrm{P}_{\mathrm{ij}}$, between states $i$ and $j$ is proportional to a Boltzman factor, thus

$$
\begin{array}{ll}
P_{i j}=(1 / N) *\left(U_{i} / U_{j}\right) & i \neq j ; U_{i}>U_{j} \\
P_{i j}=(1 / N) & i=j ; U_{i}<U_{j} \\
P_{i i}=1-P_{i j} & \tag{7}
\end{array}
$$

where $\quad U_{i} \propto \exp \left(-E_{i} / k T\right)$

$$
\begin{equation*}
U_{j} \propto \exp \left(-E_{j} / k T\right) \tag{8}
\end{equation*}
$$

and $\quad N=$ number of states

Under these conditions

$$
\begin{equation*}
\langle A\rangle=\left(\sum_{i} A_{i} \exp \left(-E_{i} / k T\right)\right) /\left(\sum_{i} \exp \left(-E_{i} / k T\right)\right) \tag{9}
\end{equation*}
$$

simply reduces to arithmetic average. The average value of the quantity A at some step $s$ is given by

where, $n$ is the number of iterations carried out in the averaging process. In practice n is a large but finite number. Steps (8) and (9) above lead to selection of configurations that are lower in energy and thus eventually would take the system to its equilibrium state.

The average order parameter $\left\langle\mathrm{S}_{\mathrm{n}}\right\rangle$ for each bond number in all the chains is calculated by the procedure described above. For example, $S_{3}$ is an average order parameter for bond number 3 on all 35 chains. The flow chart (Figure 12) summarizes the procedure laid above for calculation of the average order parameters. It should be noted that the small displacement $d r$ mentioned in the flow chart is chosen withsome consideration. If dr is too small then it will take long time for the system to reach equilibrium (wasting valuable computer time) and if dr is too large then too many moves will be rejected.


Figure 12. Flow Chart Displaying Monte Carlo Averaging Procedure.
hydrocarbon chains of the lipid molecules in this unit cell but one of the molecules namely molecule at the 22 nd site is replaced bycholesterol molecule. The cell dimension are chosen so as to have approximately 29 Angstrom square area per acyl chain, (not including area of cholesterol). This area corresponds to lipid bilayer area per chain in its fluid state (29). The choice of site number 22 is arbitrary and was chosen to create an asymmetric unit cell. The cholesterol molecule with its surrounding lipids forms an hexagonal array (29). (figure 13). The first and the next nearest neighbors of cholesterol are clearly defined at the beginning of the program. Co-ordinates of the carbon atoms in the sterol ring structure were calculated assuming rings to be planar. The molecule itself is anchored to the membrane at the third carbon (at which B-hydroxy group is located, Figure 6).

Thirty six hydrocarbon chains were then simulated - including 'tail' on the cholesterol ring - by use of rotation matrix operator. C-C bond length was taken to be $1.53 \mathrm{~A} .$, and bond angle 109.5 degrees. The C-C bond position vector RVEC has its components as the projections along $x, y, z$ axes. Initially components of RVECs for all chains are set to be $(1.53,0,0)$. Next a rotation matrix operator ROT is defined,

$$
\operatorname{ROT}=\left[\begin{array}{ccc}
\operatorname{Cos} X & \operatorname{Sin} X \operatorname{Cox} Y_{i} & \operatorname{Sin} X \operatorname{Sin} Y_{i} \\
\operatorname{Sin} X & -\operatorname{Cos} X \operatorname{Cos} Y_{i} & -\operatorname{Cos} X \operatorname{Sin} Y_{i} \\
0 & -\operatorname{Sin} Y_{i} & \operatorname{Cos} Y_{i}
\end{array}\right]
$$



Figure 13. A Model of a Unit Cell.
where $X=70.5$ degrees ( complementary angle of 109.5 degrees) and $Y i=$ gauche rotation angle $=+120$ or -120 degrees for bond i. But initially all the chains are desired to be in all trans state and so $Y i$ is 0 degrees for all bonds. Operator ROT then becomes,

$$
\text { ROT }=\left[\begin{array}{ccc}
\operatorname{Cos} X & \operatorname{Sin} X & 0  \tag{11}\\
\operatorname{Sin} X & -\operatorname{Cos} X & 0 \\
0 & 0 & 1
\end{array}\right]
$$

The remaining chain i.e. $x, y, z$ components of RVECs (giving positions of carbons on the chain) are obtained by successive application of the matrix operator.
$\left[\begin{array}{ccc}\operatorname{Cos} x & \operatorname{Sin} x & 0 \\ \operatorname{Sin} x & -\operatorname{Cos} x & 0 \\ 0 & 0 & 1\end{array}\right]\left[\begin{array}{l}x \\ y \\ z\end{array}\right]=\left[\begin{array}{l}x^{\prime} \\ y^{\prime} \\ z^{\prime}\end{array}\right]$

The axes of these chains are not perpendicular to the $y-z$ plane. In order to achieve this, these chains should be tilted. Therefore, another rotation matrix operator RT is defined.


This operator operates on each component of RVECs to produce chains that are perpendicular to the $y z$ plane of the membrane.

$$
\left[\begin{array}{ccc}
\operatorname{Cos}(x / 2) & \operatorname{Sin}(x / 2) & 0  \tag{14}\\
\operatorname{Sin}(x / 2) & -\operatorname{Cos}(x / 2) & 0 \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{l}
x^{\prime} \\
y^{\prime} \\
z^{\prime}
\end{array}\right]=\left[\begin{array}{l}
x^{\prime \prime} \\
y^{\prime \prime} \\
z^{\prime \prime}
\end{array}\right]
$$

The chains simulated in this manner are in all trans state, their planes being parallel to $x-y$ plane. Each chain in our model is $16 \mathrm{CH}_{2}$ units long. The cholesterol tail is shorter, being only $6 \mathrm{CH}_{2}$ units long. This short chain is located on the 21st carbon atom of cholesterol. The chain is thus 'placed' on 21st atom simply by adding co-ordinates of 21st carbon to that of first carbon atom of the 'tail'.

Thus far a computer simulated model of the unit cell has been created, with 35 chains in all trans state and cholesterol molecule at the 22 nd site. This defines initial configuration of our system. The position co-ordinates of all carbon atoms are known and saved.

The total energy of each chain in this configuration can be computed by summing its internal energy due to any gauche rotations
about $\mathrm{C}-\mathrm{C}$ bonds and interaction energy between all carbon atoms of this chain and all other carbon atoms within interaction range, including those of cholesterol molecule.

$$
\begin{equation*}
E=E(i)+\sum_{C H_{2}^{\prime} s} \sum_{i \neq j} E\left(\left(\sigma / r_{i j}\right)^{12}-\left(\sigma / r_{i j}\right)^{6}\right) \tag{15}
\end{equation*}
$$

where $E(i)=$ internal energy due to gauche rotation (+120 or -120 deg.$)$ of bond number i. $E(i)=500$ cal/mole for single gauche rotation and $2500 \mathrm{cal} / \mathrm{mole}$ for successive gauche rotations.

The pairwise interaction is obtained by summing Van der Waal interaction energies over all pairs i.e. all $\mathrm{CH}_{2}$ 's of that chain and all other $\mathrm{CH}_{2}$ 's within interaction range. Here $\epsilon$ and $\sigma$ are Van der Waal parameters, with their values $(30) \in=118 \mathrm{cal} / \mathrm{mole}$ and $\sigma=3.905 \mathrm{~A}$. , $r_{i j}=$ distance between $\mathrm{CH}_{2}$ 's on $i$ th and $j$ th chain - including those on chain number 22 - within the interaction range. The condition $i \neq j$ is imposed so as to avoid 'self energy' being calculated. The total energy of initial configuration is thus known.

At this stage we are ready to put the system in a new configuration. A chain is picked and it is translated through a small distance dr. Its long axis still being perpendicular to $y-z$ plane. On the same chain a bond is picked randomly according to the transition probability $P_{i j}$ between states $i$ and $j$ and gauche rotation is attempted. The positions of the carbon atoms of a lipid chain, before and after a


Figure 14. Gauche Rotation.
gauche rotation can be described in terms of a dihedral angle. Consider for example the atoms labelled as A, B, C, D in Figure 14. For the all trans configuration of this chain all four atoms $A, B, C, D$ lie in one plane. More specifically the dihedral angle between the plane containing atoms $A, B, C$ and the plane containing atoms B, C, D is 180 degrees. If a gauche rotation is performed about the bond joining atoms $B-C$, then the positions of atoms $A, B, C$ remain unchanged. Atom D (and the subsequent atoms of this chain) will occupy new position as a result of gauche rotation. The dihedral angle between the plane containing atoms A, B, C and the plane containing atoms B, C, D is now $120^{\circ}$. Note that the first bond between $C_{1}-C_{2}$ remains fixed at all times i.e. it is never picked for attempting gauche rotation. The transition probability $P_{i j}$ can be calculated as follows.
(a) $\quad P_{i j}=P\left(t \rightarrow g^{+}\right)=P(t \rightarrow g-)=(1 / N) \exp (-E / k T)$
$=1 / 3 \exp ((-500 \mathrm{cal} / \mathrm{mole})) /((1.987 \mathrm{cal} / \mathrm{mole}-\mathrm{K})(300 \mathrm{~K})$
$=0.144$
(b) $\quad P_{g+\rightarrow t}=1 / 3$
(c) $\quad P_{t t}=1-2 / 3 \mathrm{epx}(-500 / 1.987 \mathrm{~T})$
(d) $\quad P_{g g^{-}}=1 / 3 \exp (-2200 / 1.98 \mathrm{~T})$
(e) $\quad P_{g^{+} \mathbf{g}^{+}}=1-1 / 3-1 / 3 \exp (-2200 / 1.987 \mathrm{~T})$

Energy of this new configuration is calculated as described previously (Equation 15). The energy difference between the previous (old) configuration and new configuration is calculated at this stage. Also, at this stage periodic boundary condition is applied. Following
which a subroutine CHECK, is devised in order to check overlap of two chains. If carbon atoms belonging to two chains come within a fixed hard-core diameter then they are said to overlap. If such an overlap occurs then the move is rejected and the chain is restored to its previous position. This makes saving the position co-ordinates very important in the program.

The energy difference ( $\operatorname{DEL}\left(E_{i j}\right)$ ), between the previous configuration and the newly accepted one is then examined as follows.

If $\operatorname{DEL}\left(E_{i j}\right)<0$, then the new state is accepted. If $\operatorname{DEL}\left(E_{i j}\right)>0$ then a quantity $\exp \left(-\operatorname{DEL}\left(E_{i j}\right) / k T\right)$, let it be denoted by $D$, is calculated and compared to a random number RANF between 0 and 1.

If $D>$ RANF then new state is accepted and If $D<$ RANF the new state is rejected. Such a test ensures that each new configuration is chosen so that system as a whole will reach the equilibrium in a large but finite number of steps.

Following this an average order parameter is calculated for all 15 bonds of all chains.

All computations were performed at the Oklahoma State University Computer Center facilities using IBM mainframe machine. The random number generated by the computer program RANF was developed by J. p.

Chandler of the Computer Science Department. The results of our study
is presented in the next chapter followed by discussion.

## CHAPTER III

RESULTS AND DISCUSSION

The results obtained by computer simulations are shown in Figures 15 and 16. The Tables in I and II show average values for the bond order parameter and the standard deviations of the bonds on cholesterol neighboring chains and all acyl chains respectively. Figure 15 shows graph of order parameter averaged over each bond in acyl chains neighboring cholesterol molecule versus bond number. Figure 16 shows values of order parameters for all chains plotted versus bond number. Each chain in our simulation had been $16 \mathrm{CH}_{2}$ units long.

Cholesterol ring structure was assumed to be planar although in reality the rings are 'puckered'. Yet our model is very close approximation of the actual molecule.

As mentioned eailier in Chapter II, the transition probabilities are propnitional to Boltzman factor $\exp \left(-E_{i j} / k T\right)$. The absolute temperature of the simulated model was chosen to be 300 K at all times. The rotational probabilities were thus proportional to $\exp \left(-E_{i j} / k T\right)$, with appropriate values of $E_{i j}$. Since the temperature enters in the calculation of the probabilities, one might suspect that it plays a


Figure 15. Plot of Sn vs. Bond Number for Boundary Lipids.

Average Order Parameters vs. Bond Numbers


Figure 16. Plot of Sn vs. Bond Number for Lipid Chains.

TABLE I
aVERAGE VALUES OF THE ORDER PARAMETERS AND THE STANDARD DEVIATIONS FOR THE BONDS ON THE CHOLESTEROL NEIGHBORING CHAINS.

| Bond Number | $\left\langle\mathrm{S}_{\mathrm{n}}\right\rangle$ | Standard Deviation |
| :---: | :---: | :---: |
| 1 | 1.00000 | $0.00000 \mathrm{E}+00$ |
| 2 | 0.88200 | $0.98259 \mathrm{E}-02$ |
| 3 | 0.88867 | $0.14815 \mathrm{E}-01$ |
| 4 | 0.76817 | $0.18964 \mathrm{E}-01$ |
| 5 | 0.87461 | $0.18454 \mathrm{E}-01$ |
| 6 | 0.71137 | $0.51546 \mathrm{E}-01$ |
| 7 | 0.82461 | $0.38985 \mathrm{E}-01$ |
| 9 | 0.73685 | $0.42919 \mathrm{E}-01$ |
| 10 | 0.73435 | $0.93022 \mathrm{E}-02$ |
| 11 | 0.77325 | $0.74824 \mathrm{E}-01$ |
| 12 | 0.72262 | $0.99968 \mathrm{E}-01$ |
| 13 | 0.71149 | $0.33530 \mathrm{E}-01$ |
| 14 | 0.66078 | $0.78854 \mathrm{E}-01$ |
| 15 | 0.52886 | $0.33124 \mathrm{E}-01$ |

TABLE II
average values of the order parameters and the STANDARD DEVIATIONS FOR THE BONDS ON THE ALL ACYL CHAINS.

| Bond Number | $\left\langle\mathrm{S}_{\mathrm{n}}\right\rangle$ | Standard Deviation |
| :---: | :---: | :---: |
| 1 | 1.00000 | $0.00000 \mathrm{E}+00$ |
| 2 | 0.84918 | $0.10306 \mathrm{E}-01$ |
| 3 | 0.87891 | $0.93375 \mathrm{E}-02$ |
| 4 | 0.76051 | $0.19716 \mathrm{E}-01$ |
| 5 | 0.89466 | $0.14034 \mathrm{E}-01$ |
| 6 | 0.72296 | $0.435117 \mathrm{E}-01$ |
| 7 | 0.84420 | $0.35723 \mathrm{E}-01$ |
| 9 | 0.73252 | 0.32989 E 001 |
| 10 | 0.75443 | $0.25289 \mathrm{E}-01$ |
| 11 | 0.79258 | $0.85399 \mathrm{E}-01$ |
| 12 | 0.72546 | $0.65777 \mathrm{E}-01$ |
| 13 | 0.71829 | $0.29268 \mathrm{E}-01$ |
| 14 | 0.63105 | $0.50648 \mathrm{E}-01$ |
| 15 | 0.53266 | $0.43373 \mathrm{E}-01$ |

significant role in the outcome of the results. In fact, as found by Scott (22), the values of order parameters are not affected appreciably for two identical systems at different temperatures.

The Monte Carlo averages of the order parameters were found after 20,000 steps, where each step involves more of a single molecule. Although a large number of steps is desirable for more reliable results, it is believed that these averages are adequate, i.e. these values of $S_{n}$ converge.

Superimposing plots shown in Figures 15 and 16 it is seen that there is very little difference in the order parameter profiles for the bulk and boundary lipids. This implies that the presence of a single cholesterol molecule in the unit cell simulated in our study did not affect the equilibrium of lipid chain states to a significant degree.

The length of a cholesterol molecule is about 19 angstroms. This includes the rigid ring structure (about 11 angstroms) and its tail (about 8 angstroms). The length of an acyl chain, in its all trans state, is also about the same. This was found by taking the product of the projection of the $\mathrm{C}-\mathrm{C}$ bond vector on the x axis (1.27 angstroms) and the number of bonds. The rigid ring structure should restrict the motion of first 8 to 9 bonds. This is implied by higher values of the order parameters. Remaining 6 to 7 bonds are less restricted and highly interact with the tail of the cholesterol. The values of the order parameters for these bonds declined rapidly (Figure 16).

As described in the flow chart (Figure 12) the acyl chains were translated in the plane of the bilayer before attempting gauche rotations. The principal axis of an acyl chain was still perpendicular to the plane of the bilayer. The side-to-side motion of the chains (Figure 11) was not included in our simulation, nor did we include rotational diffusion of acyl chains.

The effect of tilting of the chains on the order parameters has been studied (31). It is reasonable to expect that such motion will further enhance the interactions between $\mathrm{CH}_{2}$ groups on the neighboring chains. This will reduce the values of the order parameters. The values of the order parameters reflect the extent of disorder in the chains. Since an acyl chain is attached to the membrane surface at the carbon $C_{1}$, it is immobile. A first few top bonds show less disorder and tend to remain in their gauche states a longer time. The lower bonds being more free to rotate about $\mathrm{C}-\mathrm{C}$ bonds alter their rotational states frequently. Therefore, there is a consistent decline in the values of the order parameters. But because of the comparable lengths of the acyl chains and the cholesterol molecule, the chains are unable to fold themselves.

The principal conclusion derived from this study is that a single molecule of cholesterol situated among $6 \times 6$ array of lipid chains cannot affect the equilibrium of lipid states. This is why the order parameter profiles for the boundary lipids and the bulk lipids follow the same
pattern. This conclusion is consistent with the lipid-protein interaction study by Scott (22).

Increasing lipid-cholesterol ratio will increase computation time to some extent and complexity of the problem. It will be interesting to include at least one more cholesterol molecule in our simulation and observe some changes due to increased interactions.

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## APPENDIX A

COMPUTER PROGRAM FOR THE CALCULATION OF THE AVERAGE VALUES OF THE ORDER PARAMETERS

| I SN | 1 |  |
| :--- | ---: | :--- |
| I SN | 2 |  |
| I SN | 3 |  |
| I SN | 4 |  |
| I SN | 5 |  |
| I SN | 6 |  |
| I SN | 7 |  |
| I SN | 8 |  |
| I SN | 9 |  |
| I SN | 10 |  |
| I SN | 11 |  |
| I SN | 12 |  |
| ISN | 13 |  |
| I SN | 14 |  |
| ISN | 15 |  |
| ISN | 16 |  |
|  |  | $C$ |

```
    MCNTE-CARLO SIMULATION PROGRAM FOR LIF:C CHOLESTEROL INTERACTION
    CHAIN NL::EER 22 IS CHOLESTEROL
    THIS FROGRA:: COMPUTES AN ORDER PARA:AETER WHICH IS A MEASURE
    of INTERACTION EETWEEN LIPID CHAINS ANO CHOLESTEROL MOLECULE
    IN A MEMERANE
    **..........ARAMETERS USED IN THIS PROGRAM****+*********
    ANG=CHAIN LONG AXIS ROTATION
    EKT = RECIPROCAL OF (BOLTZMAN CONST*TEMP)
    CROT = RANDOM NU:MBER FOR AXIAL ROTATION
    CPS = SAVED CAREON CO-ORDINATES
    CHK = SUEROUTINE :CHECKS OVERLAPS.CALCULATES ENERGY
    CP = CAREON POSITION
    CEL = ENERGY DIFFERENCE IN GAUCH TRANS CONFIGURATIONS
    EPK = LIPID CHOLESTEROL INTERACTION ENERGY
    EOLD = OLD LIPID CHOLESTEROL INTERACTION ENERGY
    ENE:H = NEN TOTAL ENERGY
    EOLD = OLD TOTAL ENERGY
    EVWD = VANDER WAALS ENERGY
    ESV = SAVED ENERGY
    EPIL = 6 - }12\mathrm{ ENERGY PARAMETER
    GASIN = SIN 120 DEGREES
    GACOS = COS 12O DEGREES
    GR = +1(+120 DEGREES ROTATION OF BOND)
    GS = SAVED CO-ORDINATES
    IRAN = CALLS TO RAN BEFORE PROG STARTS
    IPRT = PRINT INTERVAL
    IC.ICL = USED TO PICK BONDS FOR GAUCH ROTATIONS
    COMMONS CP(3,27,36),RVEC(3,27,36),NCHAIN,NLINK,SIZEY.SIZEZ,RC
    COMMON/LST/RANG,ILST,ULST,IDST
    COMMON/VDW/SIG.EPIL
    DIMENSION ROT(3,3), \triangleVEC(3,27),D(3),ROTN(3.3),ROTP(3,3)
    DIMENSION RVECH(3,4),CHP(3,4).TVEC(3,16,36)
    COMMON/CHK/KTR,JR,SY,SZ.SAVG(27).SSVG(27).NPP(36).NNP(36)
    COMMON/CHK/KTR,JR,SY,SZ,SAVG(27),SSVG(27).NPP(36).NNP(36)
    DIMENSION GS(27.36),ESV(36),VRND(36,-1.80),DPP(36)
    DIMENSION GR(27,36)
    DIMENSION NN(36,36), EVDW(36,36),RSV(3, 27, 36),CPS(3,27,36)
    DIMENSION IC(36),ICL(36),E(36),LRU(27),GASIN(3),GACOS(3)
    DIMENSION DCH(2,27),CHOL(3,27).DST(16).DOV(3)
        DIMENSION ENEW(36),EOLD(36)
    DIMENSION DEL(36).EPK(36),EPOLD(36),CMP(36),RT(3.3),CROT (36)
    PARAMETER(RAD=4.,RREP=7.05,T=300..NMAX=50.NMIN=0)
    PARAMETER(IPRT=25.IRAN=17.RRR=9.,RPEP=40.)
    ******SOME MORE PARAMETERS IN THIS FROGRAM
```

| ISN | 17 |
| :--- | :--- |
| I SN | 18 |
| ISN | 19 |
| ISN | 20 |
| ISN | 21 |
| ISN | 22 |
| ISN | 23 |
| ISN | 24 |
| ISN | 25 |
| ISN | 26 |
| ISN | 27 |
| ISN | 28 |
| ISN | 29 |
| ISN | 30 |






| ISN | 172 | 21 | CONTINUE |
| :---: | :---: | :---: | :---: |
| ISN | 173 |  | DO $22 \mathrm{~J}=2.6 .2$ |
| I SN | 17.4 |  | DO $22 \mathrm{~L}=1.6$ |
| I SN | 175 |  | $U L=L+6^{*}(J-1)$ |
| $15 N$ | 176 |  | $X L=F L O A T(L-1)$ |
| I SN | 177 |  | $X J=F \operatorname{LOAT}(\mathrm{U}-1)$ |
| I SN | 178 |  | IF (JL.EQ. 22) GO TO 22 |
| ISN | 173 |  | $C P(2.1 . U L)=D L L * X L+1.425$ |
| ISN | 180 |  | $C P(3,1, U L)=R L Z+D L Z * X J$ |
| I SN | 18 : | 22 | CONT INUE |
| ISN | 182 |  | GO TO 48 |
| ISN | 183 | 15 $C$ | CONTINUE |
|  |  | C | USING ROTATION MATRICES SUCCESSIVELY INITIAL CHAIN POSITIONS |
|  |  | c | are calculated. |
|  |  | C |  |
| I SN | 184 |  | REWIND 9 |
| I SN | 185 |  | DO $15 \mathrm{~L}=1$. NCHAIN |
| I SN | 186 |  | READ (9,46)ANG(L) |
| I SN | 187 |  | IF (L .EQ. 22) THEN |
| ISN | 188 |  | IZ $1=21$ |
| ISN | 183 |  | $122=27$ |
| I SN | 190 |  | ELSE |
| ISN | 191 |  | I $21=1$ |
| ISN | 192 |  | I $22=16$ |
| I SN | 193 |  | ENDIF |
| ISN | 194 |  | DO $16 \mathrm{~J}=1, \mathrm{I} 22$ |
| I SN | 195 |  | READ (9,45)(CP(K, U.L), RVEC(K, J,L), K=1.3), GR(U.L) |
| I SN | 196 | 15 | CONTINUE |
| ISN | 197 | 45 | FORMAT (7F12.6) |
| ISN | 198 | 46 | FORMAT ( 12.6 ) |
| ISN | 199 | 48 | CONTINUE |
| I SN | 200 |  | XDN = NMAX-NMIN |
| I SN | 201 |  | EKT $=1 . /(1.987 * T)$ |
| ISN | 202 |  |  |
| ISN | 203 | 1233 |  |
| I SN | 204 |  | PRINT 1230 |
| I SN | 205 | 1230 |  |
| I SN | 206 |  | PRINT 1234.NMAX.NMIN, ILST, KSTART |
| I SN | 207 | 1234 | FORMAT ( ' . 4 (16.5X)//) |
| ISN | 208 |  | $P I=+3.14159265$ |
| I SN | 209 |  | Y $1=2 . * P I / 3$. |
| ISN | 210 |  | $\mathrm{Y} 2=0$. |
| ISN | 211 |  | Y $3=5 . * Y 1$ |
| ISN | 212 |  | $\operatorname{GASIN}(1)=\operatorname{SIN}(\mathrm{Y} 1)$ |
| ISN | 213 |  | $\operatorname{GACos}(1)=\cos \left(Y_{1}\right)$ |
| I SN | 214 |  | $\operatorname{GASIN}(2)=\operatorname{SIN}\left(Y_{2}\right)$ |
| ISN | 215 |  | $\operatorname{GACOS}(2)=\operatorname{Cos}\left(Y_{2}\right)$ |
| I SN | 216 |  | GASIN(3) $=\operatorname{SIN}\left(Y_{3}\right)$ |
| I SN | 217 |  | $\operatorname{GACOS}(3)=\operatorname{Cos}(Y 3)$ |
| ISN | 218 |  | $\mathrm{X}=70.5 * \mathrm{PI} / 180$. |
| I SN | 219 |  | $E S O=S I N(X)$ |
| I SN | 220 |  | $E C O=\cos (x)$ |
| ISN | 221 |  | ESOIV $=\operatorname{SIN}(-\mathrm{X})$ |
| ISN | 222 |  | $E C O N=\operatorname{COS}(-\mathrm{x})$ |
| ISN | 223 |  | $E S=\operatorname{SIN}(X / 2$. |



| I SN | 278 | 7048 | CONTINUE |
| :---: | :---: | :---: | :---: |
| $15 N$ | 279 |  | $007019 \mathrm{IZ}=1.27$ |
| ISN | 280 |  | 007029 IW $=1.3$ |
| ISN | 281 |  | CPS(IW,IZ.IY) $=$ CP(IW,IZ,IY) |
| I SN | 282 | 70.29 | CONTINUE |
| I SN | 283 | 7019 | CONT INUE |
|  |  | CL* | ******* |
| ISN | 284 |  | GO TO 150 |
| I SN | 285 | 6999 | CONTINUE |
| ISN | 286 |  | $\operatorname{RVEC}(1,1, K)=1.53$ |
| ISN | 287 |  | DO $6001 \mathrm{I}=2.3$ |
| I SN | 288 | 6001 | RVEC (I, 1.K) $=0$. |
| ISN | 289 |  | DO $145 \mathrm{~J}=2$. NLINK |
| ISN | 290 |  | $L=v-1$ |
| I SN | 291 |  | DO $147 \mathrm{I}=1.3$ |
| I SN | 292 |  | RVEC(I, J,K) $=0$. |
| ISN | 293 |  | DO 6002 I $Y=1.3$ |
| ISN | 294 | 6002 | RVEC(I, J.K) = RVEC(I,J.K)+RVEC(IY,L,K)*ROT(IY,I) |
| ISN | 295 | 147 | CONTINUE |
| ISN | 296 | 145 | CONTINUE |
| ISN | 297 |  | DO $6003 \mathrm{I}=1.3$ |
| I SN | 2.98 |  | DO $6004 \mathrm{~J}=1 . \mathrm{NLINK}$ |
| I SN | 299 | 6004 | $\operatorname{AVEC}(\mathrm{I} . \mathrm{U})=\operatorname{RVEC}(\mathrm{I}, \mathrm{J}, \mathrm{K})$ |
| I SN | 300 | 6003 | CONT INUE |
| ISN | 301 |  | DO $148 \mathrm{I}=1.3$ |
| I SN | 302 |  | DO $148 \quad J=1$. NLINK |
| I SN | 303 |  | RVEC(I.J.K) $=0$. |
| I SN | 30.4 |  | DO 6005 I $Y=1.3$ |
| I SN | 305 | 6005 |  |
| I SN | 305 | 148 | CONTINUE |
| ISN | 307 |  | DO $149 \mathrm{~J}=2 . \mathrm{NLINK}$ |
| : SN | 308 |  | $\checkmark \cup=J-1$ |
| I SN | 309 |  | DO $6006 \mathrm{I}=1.3$ |
| I SN | 310 | 6006 | CP(I, J.K) = CP (I, JJ,K)+RVEC (I.JU,K) |
| I SN | 311 | 149 | CONTINUE |
| I SN | 312 | 150 | CONTINUE |
| I SN | 313 | 140 | CONTINUE |
| I SN | 314 | 155 | PRINT 1109 |
| [SN | 315 | 1109 | FORMAT(18X.'INITIAL VALUES OF CP \& IG' ///) |
| I SN | 316 |  | DO 165 L=1.NCHAIN |
| ISN | 317 |  | $\mathrm{J} 1=1$ |
| I SN | 318 |  | $\mathrm{J} 2=$ NLINK |
| ISN | 319 |  | IF(L.EQ.22)THEN |
| ISN | 320 |  | $\mathrm{J}_{1}=21$ |
| ISN | 321 |  | $\mathrm{J} 2=27$ |
| ISN | 322 |  | END IF |
| ISN | 323 |  | CO $165 \mathrm{~J}=\mathrm{J} 1 . \mathrm{J} 2$ |
| I SN | 324 |  | PRINT 1110.(CP(K.U.L).K=1.3).GR(U.L) |
| ISN | 325 | $\begin{aligned} & 165 \\ & c \end{aligned}$ | CONTINUE |
|  |  | C | ***** INITIAL CONFIGURATION IS PRINTED AT THIS STEP ***** |
|  |  | C | MEANS CARBON POSITIONS CP ARE PRINTED.XYZ CO-ORDINATES. |
|  |  | C |  |
| I SN | 326 | 1110 | FORMAT (5X, 4F12.5) |
| I SN | 327 | 1114 | FORMAT (5X, '1114'.I4.I4) |
| ISN | 328 | 1115 | FORMAT(5X, '1115'.I4.I4) |




|  |  | C $C$ $C$ $C$ | **** PICK A BOND ON CHAIN NO. LABELLED LROT AND <br> "FLIP A COIN " TO MAKE A ROTATION OR NQT *+*** |
| :---: | :---: | :---: | :---: |
| ISN | 415 |  | DO 1030 LROT $=1$. NCHAIN |
| ISN | 416 |  | IF (LROT.EQ. 22 ) THEN |
| ISN | 417 |  | [ $21=21$ |
| ISN | 418 |  | IZ2=27 |
| ISN | 419 |  | ELSE |
| I SN | 420 |  | IZ $1=1$ |
| I SN | 421 |  | $I Z 2=16$ |
| ISN | 422 |  | NLINK=16 |
| I SN | 423 |  | ENDIF |
| I SN | 424 |  | DEL $($ LROT $)=0$. |
| ISN | 425 |  | ITR=LROT |
| I SN | 426 |  | $K T R=L R O T$ |
| ISN | 427 |  | FLIF = RANF ( 0 ) |
| I SN | 428 |  | IF(FLIP.LT.O.5)GO TO 6099 |
| I SN | 429 |  | $X V=(1 Z 2-2)+$ RANF (O) |
| ISN | 430 |  | XVL $=(\mathrm{IZ2-3)*RANF}(0)$ |
| ISN | 431 |  | IC (LROT) $=\operatorname{INT}(X V)+2$ |
| ISN | 432 |  | ICL(LROT $)=\mathrm{IC}(\mathrm{LROT})+1+\mathrm{INT}(X V L)$ |
| I SN | 433 |  | IF (ICL(LROT).GE.IZ2)GO TO 1025 |
| $15 N$ | 434 |  | LU=IC (LRDT) |
| ISN | 435 |  | $L L=I C L(L R O T)$ |
| I SN | 436 |  | GR (LU, LROT ) = GR (LU, LROT ) + 1 |
| ISN | 437 |  | IF (GR(LU, LROT ) . GT . 1.1) GR (LU, LROT $)=-1$. |
| I SN | 439 |  | GR (LL, LROT ) = GR (LL, LROT ) - 1 |
| I SN | 440 |  | $\mathrm{IF}(\mathrm{GR}(L L . L R O T) . L T .-1.1) \mathrm{GR}(\mathrm{LL} . \operatorname{LROT})=1$. |
| ISN | 4.42 |  | $A R=(G R(L L, L R O T)) * G R(L L, L R O T)$ |
| I SN | 4.3 |  | $A S=G S(L L . L R O T) * G S(L L . L R O T)$ |
| I SN | 444 |  | $B R=G R(L U, L R O T) * G R(L U, L R O T)$ |
| I SN | 445 |  | $B S=G S(L U, L R O T) * G S(L U, L R O T)$ |
| ISN | 446 |  | $D L=A R-A S$ |
| I SN | 447 |  | $D U=B R-B S$ |
| I SN | 448 |  | $R R L=G R(L L-1 . L R O T) * G R(L L-1 . L R O T)+G R(L L+1 . L R O T)+G R(L L+1 . L R O T)$ |
| ISN | 449 |  | $R R U=G R(L U-1 . L R O T) * G R(L U-1 . L R O T)+G R(L U+1 . L R O T) * G R(L U+1, L R O T)$ |
| ISN | 450 |  | $D E L(L R O T)=-500 . *(D L+D U)-2500 . *(D L * R R L+D U * R R U)$ |
| ISN | 451 |  | GO TO 6099 |
| ISN | 452 | 1025 | $L U=I C(L R O T)$ |
| ISN | 453 |  | GR (LU.LROT $)=\mathrm{GR}(\mathrm{LU}$, LROT $)-1$. |
| I SN | 454 |  | IF (GR(LU. LROT).LT. -1.01 ) GR (LU, LROT $)=1$. |
| I SN | 456 |  | $B R=G R(L U, L R O T)+G R(L U . L R O T) ~$ |
| I SN | 457 |  | ES=GS(LU,LROT)*GS(LU,LROT) |
| I SN | 458 |  | $R R U=G R(L U-1 . L R O T) * G R(L U-1 . L R O T)+G R(L U+1 . L R O T) * G R(L U+1 . L R O T)$ |
| I SN | 459 |  | $D E L(L R O T)=-500 . *(B R-B S)-2500 . * R R U *(B R-R S)$ |
| I SN | 460 | 6099 | CROT (LROT) = RANF (O) |
| I SN | 461 |  | IF (LROT.EQ. 22 ) GOTO 169 |
| ISN | 462 |  | $C P(2,1, K T R)=C P(2,1, K T R)+.03 *(1 .-2 . * R A N F(0))$ |
| ISN | 463 |  | $C P(3,1 . K T R)=C P(3,1 . K T R)+0.03 *(1 .-2 . * R A N F(0))$ |
|  |  | C |  |
|  |  | C | **** NEW CHAIN POSITIONS ARE CALCULATED AFTER ROTATION |
|  |  | C | and translation of chain no.labelled lrot. **** |
|  |  | C |  |
| I SN | 464 | 169 | CONTINUE |
| I SN | 465 | 170 | ANGSV = ANG (ITR) |


| ISN | 466 |  | RVEC(2,1, ITR) $=0$. |
| :---: | :---: | :---: | :---: |
| ISN | 467 |  | $\operatorname{RVEC}(3,1, I T R)=0$. |
| ISN | 468 |  | $\triangle N G(I T R)=A N G(I T R)+0.03 \cdot P I *(1 .-2 .+\operatorname{CROT}(\mathrm{ITR}))$ |
| ISN | $4 \mathrm{G9}$ |  | $E P S=S I N(\triangle N G(I T R))$ |
| ISN | 470 |  | $E P C=\operatorname{COS}(\triangle N G(I T R))$ |
| I SN | 471 |  | $R T(1,1)=E C$ |
| ISN | 472 |  | $\operatorname{RT}(2,1)=E S$ |
| ISN | 473 |  | $\mathrm{RT}(3,1)=0$. |
| ISN | 474 |  | $R T(1,2)=-E S+E P C$ |
| ISN | 475 |  | $R T(2.2)=E C \cdot E P C$ |
| I SN | 476 |  | $R T(3.2)=E P S$ |
| ISN | 477 |  | $R T(1.3)=E S * E P S$ |
| ISN | 478 |  | $R T(2,3)=-E C+E P S$ |
| I SN | 479 |  | $\operatorname{RT}(3,3)=E P C$ |
| I SN | 480 |  | $\operatorname{RVEC}(1.1 .1 T R)=1.53$ |
| ISN | 481 |  | DO $210 \mathrm{~J}=1 \mathrm{Z} 1+1.1 Z 2$ |
| ISN | 482 |  | DO $200 \mathrm{~K}=1.3$ |
| ISN | 483 |  | $L \mathrm{R}=\mathrm{J}-1$ |
| I SN | 484 |  | RVEC(K, J,ITR ) $=0$. |
| ISN | 485 |  | DO 6011 I $Y=1.3$ |
| I SN | 486 | 6011 | $\operatorname{RVEC}(K, U, I T R)=R V E C(I Y, L R, I T R) * R O T(I Y, K)+R V E C(K, J, I T R)$ |
| I SN | 487 | 200 | CONTINUE |
| ISN | 488 | 210 | CONT INUE |
| I SN | 489 |  | DO $206 \mathrm{~J}=\mathrm{IZ} 1+1$. IZ2-1 |
| I SN | 490 |  | $\mathrm{J}!=122-\mathrm{J}$ |
| ISN | 491 |  | $J_{2}=i Z 2+1-J$ |
| I SN | 492 |  | IF(GR(J2.ITR).EO.O.)GOTO 206 |
| I SN | 493 |  | XX1=.5*FLOAT(J1) |
| ISN | 494 |  | IXX1=2*INT ( $\times$ X 1 ) |
| ISN | 495 |  | $\operatorname{IF}(\mathrm{GR}(\mathrm{J} 2 . I T R) . E Q .+t .0) \quad \mathrm{N}=1$ |
| ISN | 497 |  | $\operatorname{IF}(\mathrm{GR}(\mathrm{U} 2.1 T R) . E Q,-1.0) \mathrm{N}=3$ |
| ISN | 49.9 |  | IF (IXX1.NE.J1)THEN |
| ISN | 500 |  | DO $806 \mathrm{~L}=\mathrm{J} 1+1 . \mathrm{IZ2-1}$ |
| I SN | 501 |  | TVEC( $2 . L . I T R)=\operatorname{RVEC}(2, L . I T R)$ |
| ISN | 502 |  | $\operatorname{TVEC}(3 . L . I T R)=R V E C(3, L, I T R)$ |
| I SN | 503 |  | $\operatorname{RVEC}(2, L . I T R)=\operatorname{TVEC}(2, L . I T R) * \operatorname{GACOS}(\mathrm{~N})+\operatorname{TVEC}(3 . L, I T R)+\operatorname{GASIN}(N)$ |
| ISN | 504 |  | $\operatorname{RVEC}(3 . L . I T R)=\operatorname{TVEC}(3.1 . I T R) * \operatorname{GACOS}(N)-\operatorname{TVEC}(2 . L . I T R) * \operatorname{GASIN}(N)$ |
| I SN | 505 | 806 | CONTINUE |
| ISN | 506 |  | ELSE |
| I SN | 507 |  | DO $807 \mathrm{~L}=\mathrm{V} 1, \mathrm{IZ2-1}$ |
| ISN | 508 |  | DO $808 \mathrm{~K}=1.3$ |
| ISN | 509 |  | $\operatorname{TVEC}(\mathrm{K}, \mathrm{L}, \mathrm{ITR})=\operatorname{RVEC}(\mathrm{K}, \mathrm{L}, \mathrm{ITR})$ |
| I SN | 510 | 808 | CONTINUE |
| 1 SN | 511 |  | OO 809 $K=1.3$ |
| $15 N$ | 512 |  | $\operatorname{RVEC}(\mathrm{K}, \mathrm{L} . \mathrm{ITR})=0.0$ |
| ISN | 513 |  | DO 810 I $Y=1.3$ |
| I SN | 514 | 810 | RVEC (K,L, ITR ) = RVEC (K,L,ITR) + TVEC(IY,L,ITR)*ROTP (IY,K) |
| ISN | 515 | 809 | CONTINUE |
| ISN | 516 | 807 | CONT INUE |
| ISN | 517 |  |  |
| I SN | 518 |  | $\operatorname{TVEC}(2 . L . I T R)=$ RVEC (2,L,ITR) |
| I SN | 519 |  | $\operatorname{TVEC}(3 . L . I T R)=R V E C(3, L, I T R)$ |
| I SN | 520 |  | $\operatorname{RVEC}(2, L, I T R)=\operatorname{TVEC}(2 . L . I T R)+\operatorname{GACOS}(N)+\operatorname{TVEC}(3, L, I T R)+\operatorname{GASIN}(N)$ |
| ISN | 521 |  | $\operatorname{RVEC}(3 . L . I T R)=\operatorname{TVEC}(3 . L . I T R) * \operatorname{GACOS}(\mathrm{~N})-\operatorname{TVEC}(2, L . I T R) * G A S I N(N)$ |
| I SN | 522 | 811 | CONTINUE |
| ISN | 523 |  | DO $812 \mathrm{~L}=\mathrm{J} 1 . \mathrm{IZ2-1}$ |



|  |  | C |  |
| :---: | :---: | :---: | :---: |
|  |  | C |  |
|  |  | C | IF(KMC.EO.KMOV)GO TO 2300 |
|  |  | C | GO TO 2500 |
| I SN | 579 |  | CALL CHECK(IFLAG.NN.ESV) |
| I SN | 580 |  | ENEW (ITR) $=0$. |
| I SN | 581 |  | $E D L D(I T R)=0$. |
| ISN | 582 |  | DO $350 \mathrm{~K}=1$. NCHAIN |
| ISN | 583 |  | EOLD (ITR ) = EOLD (ITR ) +EVDW (KTR, K) |
| ISN | 584 |  | ENEW (ITR) $=\operatorname{ENEW}(\mathrm{ITR})+\operatorname{ESV}(\mathrm{K})$ |
| ISN | 585 | 350 | CONTINUE |
|  |  | C |  |
|  |  | C | **** CHANGE IN ENERGY EXP(-DELTA E/KT) IS COMPARED |
|  |  | C | WITH RANDOM No. To accept or revect the Change**** |
|  |  | C |  |
| I SN | 586 |  | DEL $1=E N E W(I T R)-E O L D(I T R)+E P K(I T R)-E P O L D(I T R)$ |
| ISN | 587 |  | DELT = (DEL $1-D E L(L R O T))+B K T$ |
| I SN | 588 |  | IF(DELT.LE.O.) GO TO 400 |
| ISN | 589 |  | IF (DELT.GT. 10.) GO TO 500 |
| ISN | 590 |  | DDD $=E \times P(-D E L T)$ |
| ISN | 591 | , | TST $1=$ RANF (0) |
| I SN | 592 |  | IF(DDD.LE.TST1)GO TO 500 |
| I SN | 593 | 400 | DO 420 LE=1. NCHAIN |
| ISN | 594 |  | EVDW (KTR.LE) $=$ ESV(LE) |
| I SN | 595 | 420 | $E V D W(L E, K T R)=E V O W(K T R, L E)$ |
| ISN | 596 |  | EPOLD (ITR) = EPK (ITR) |
| ISN | 597 |  | GO TO 2000 |
|  |  | C |  |
|  |  | C | RESET After revected move. |
| I SN | 598 | 500 | CONTINUE |
| I SN | 599 |  | DO 6098 IY=1.3 |
| I SN | 600 |  | DO 6097 IZ $=121 . I Z 2$ |
| I SN | 601 |  | $C P(I Y, I Z, K T R)=C P S(I Y, I Z, K T R)$ |
| ISN | 602 | 6097 | RVEC(IY,IZ.KTR ) $=$ RSV(IY,IZ.KTR) |
| ISN | 603 | C | CONTINUE |
| I SN | 604 |  | $\triangle N G(K T R)=\Delta N G S V$ |
| ISN | 605 | 600 | IREU=IREJ+1 |
| ISN | 606 |  | DO 601 IR = IZ1,IZ2 |
| I SN | 607 | 601 | GR (IR.KTR) $=$ GS (IR,KTR ) |
| ISN | 608 | 2000 | CONTINUE |
| ISN | 609 | 1030 | CONTINUE |
| ISN | 610 |  | DO $3150 \mathrm{KC}=1$. NCHAIN |
| ISN | 611 |  | IF (NNP (KC) . EQ . 1) Y $M P=Y D P+1$ |
| I SN | 613 |  | $I F(N P D(K C) . E Q .1) X D P=X D P+1$. |
| ISN | 615 | 3150 | CONTINUE |
| ISN | 616 | 2500 | IF (LMC.LE.NMIN)GO TO 990 |
| ISN | 617 | 800 | CALL CH2 (XPR, YPR) |
| ISN | 613 |  | IF (LMC.EQ.JPRT)GO TO 900 |
| ISN | 619 |  | GO TO 990 |
| ISN | 620 | 900 | PRINT 2900.KMC.LMC.IREJ |
| ISN | 621 | 2900 | FORMAT ('AFTER'.I7.' X 10 $\mathrm{X}^{\prime} .14 .^{\prime}$ ( MC STEPS...IREJ='.I8/) |
| ISN | 622 |  | PRINT 3110 |
| ISN | 623 | 3110 | FORMAT( VALUES OF CP \& IG: WRITE ON DISK'/) |
| ISN | 624 |  | REWIND 9 |
| ISN | 625 |  | DO $950 \mathrm{~L}=1$. NCHAIN |


| ISN | 626 |  | IF (L.EQ. 22) THEN |
| :---: | :---: | :---: | :---: |
| I SN | 627 |  | $I Z 2=27$ |
| ISN | 628 |  | ELSE |
| I SN | 629 |  | IZ2 $=16$ |
| ISN | 630 |  | ENDIF |
| ISN | 631 |  | WRITE(9.46)ANG(L) |
| ISN | 632 |  | DO $950 \mathrm{~J}=1 . \mathrm{I} 22$ |
| ISN | 633 |  | WRITE(9,45)(CP(K, U.L.).RVEC(K, J., L) , K= 1, 3) , GR (U,L) |
| ISN | 634 | 950 | CONTINUE |
| ISN | 625 |  | PRINT 3100 |
| I SN | 636 | 3100 | FORMAT( ORDER PARAMETER PROFILE'/) |
| ISN | 637 |  | $F L M C=F L O A T(L M C)$ |
| ISN | 638 |  | FNMIN=FLOAT (NMIN) |
| I SN | 639 |  | XDN = 10.* (FLMC-FNMIN)-9 |
| I SN | 640 |  | YDN $=1 . /(($ NCHAIN -1$) *$ XDN $)$ |
| I SN | 641 |  | DO 6096 IY = 1. LLINK |
| ISN | 642 | 6095 | SSVG(IY) =SAVG(IY)*YDN |
| ISN | 643 |  | PRINT 3200. (K, SSVG(K).K=4.LLINK) |
| I SN | 644 | $\begin{aligned} & 3200 \\ & c \end{aligned}$ | FORMAT (5X.IA.5X,F12.6) |
|  |  | C | WRITE (18.3412).(K, SSVG(K), K=1, LLINK) |
|  |  | $C 3412$ | FORMAT(5X.14.5X.F12.6) |
| ISN | 645 |  | $003140 \mathrm{JP}=1.15$ |
| ISN | 646 |  | $Z N N(U P)=Y P R(U P) / Y D P$ |
| I SN | 647 |  | ZPR(UP) $=X P R(J P) / X D P$ |
| ISN | 648 | 3140 | CONTINUE |
| ISN | 649 |  | PRINT 3197 |
| I SN | 650 |  | PRINT 3198.( 2 PR(II).II $=1,15$ ) |
| ISN | 65 ; |  | PRINT 3198, (ZNN(II), II = 1, 15) |
| ISN | 652 | 3198 | FORMAT (5X.9F10.5 ) |
| ISN | 653 | 3197 | FORMAT(25X.'ORDER PARAMETERS FOR CHOLESTEROL NEIGHBORS'/!) |
| I SN | 654 |  | $J P R T=J P R T+I P R T$ |
|  |  | c |  |
|  |  | C | ***** LIPID-CHOL :VARIOUS INTERACTION ENERGIES |
|  |  | C | EOLD. ENEW. EPK.EPOL D AND DELIENERGY DIFF |
|  |  | C | getween gauch-trans config.)frinted here **** |
|  |  | C |  |
| ISN | 655 |  | PRINT 3199 |
| ISN | 656 | 3199 | FORMAT (12X.'ENEW', 12X.'EOLD', 12X, 'EPK'. 12 X , 'EPOLD', 12X.'DEL'/) |
| I SN | 657 |  | DO $5000 \mathrm{~L}=1$. NCHA IN |
| ISN | 658 | 5000 | PRINT 4199.ENEW(L), EOLO(L), EPK(L).EPOLD(L), DEL (L) |
| ISN | 659 | 4199 | FORMAT ( $5 \times .5 \mathrm{E} 16.6$ ) |
| ISN | 660 |  | IF (LMC.EO.NMAX)GO TO 1002 |
| ISN | 661 | 990 | IF(LMC.EO.ULI)GO TO 992 |
| $15 N$ | 662 |  | GO TO 1000 |
| ISN | 663 | 992 | DO 999 ILST $=1$. NCHAIN-1 |
| ISN | 664 |  | DO 999 JLST $=I L S T+1$, NCHAIN |
| ISN | 665 | 995 | CALL CLIST |
| I SN | 666 |  | IF(IDST.EQ.1)GO TO 996 |
| ISN | 667 |  | NN(ILST, JLST $)=0$ |
| I SN | 668 |  | NN (ULST, ILST) $=0$ |
| ISN | 659 |  | GO TO 999 |
| ISN | 670 | 996 | NN(ILST, JLST) $=1$ |
| ISN | 671 |  | NN(ULST, ILST) $=1$ |
| ISN | 672 | 999 | CONT INUE |



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OOOOO
SUBROUTINE CHECK(IFLAG;NN.ESV)
COMMON CP(3, 27, 36),RVEC(3,27,36),NCHAIN,NLINK,SIZEY,SIZEZ,RC
COMMON/VDW/SIG.EPIL
COMMON/CHK/KTR,JR,SY,SZ,SAVG(27),SSVG(27),NPP(36),NNP(36)
DIMENSION NN(36,36), ESV(36)
DIMENSION DIF(3.27).DIST(27).DEL(3,27),RECIP(27),EVV(27)
IF(KTR.EO.22)THEN
IZ3=27
ELSE
IZ3=NLINK
ENDIF
DO 51 I=1.NCHAIN
IF(I.EO.22)THEN
IZ4=27
ELSE
IZ4=NLINK
ENDIF
ESV(I)=0.
IF(NN(KTR.I).EQ.O)GO TO 51
ENEW=O.
DO 50 JC=1.123
JCC=IZ3-JC+1
DO 8000 IZ=1.3
DO 8100 IY=1.IZ4
DIF(IZ,IY)=CP(IZ,UCC,KTR)-CP(IZ,IY,I)
DIF(IZ,IY)=ABS(DIF(IZ,IY))
8100
8000
CONTINUE
IF(I.EQ.KTR)GO TO 45
DO 38 J=1.IZ4
IF(DIF(2.U).GT.SY)DIF(2.U)=DIF(2.U)-SIZEY
IF(DIF(3.U).GT.SZ)DIF(3.U)=DIF(3.U)-SIZEZ
DIST(U)=0
DO 8200 IY=1.3
8200 DIST(U)=DIF(IY,U)*DIF(IY.U)+DIST(U)
38 CONTINUE
DO 41 IJ=1,IZ4
41 IF(DIST(IJ).LE.2.33)GO TO 150
GO TO 49
45 DO 48 JJ=1.IZ4
J=IZ4-JJ+1
JP=JCC+1
        JPP=JCC+2
    JM=JCC-1
        JMM=JCC -2
    IF(U.EQ.JP)GO TO 48
        IF(U.EQ.JPP)GO TO 48
    IF(U.EQ.JM)GO TO 48
```



| ISN | 50 |  | IF (U.EO. JMM)GO TO 48 |
| :---: | :---: | :---: | :---: |
| ISN | 51 |  | IF (J.EQ.UCE)GO TO 48 |
| ISN | 52 |  | IF(DIF(2.J).GT.SY)OIF (2.J) $=$ DIF(2.J)-SIZEY |
| ISN | 5.4 |  |  |
| ISN | 56 |  | $\operatorname{OIST}(J)=0$ |
| ISN | 57 |  | DO 8900 Ir $=1.3$ |
| ISN | 58 | 8900 | DIST(U)=DIF(IY, U)*DIF(IY.U)+DIST(U) |
| ISN | 59 |  | IF(DIST(J).LE.2.33)GO TO 150 |
| ISN | 60 | 48 | continue |
| ISN | 61 |  | GO TO 50 |
| ISN | 62 | 49 | EATT $=0$ |
| ISN | 63 |  | DO 8300 IY=1.IZ4 |
| ISN | 64 |  | $\operatorname{RECIP}(\mathrm{IY})=1 . / \mathrm{DIST}$ (IY) |
| ISN | 65 |  | $\operatorname{EVV}(\mathrm{IY})=(\mathrm{RECIP}(I Y) * S I G) * * 6-($ RECIP $(I Y) * S I G) * * 3$ |
| ISN | 66 |  | $\operatorname{EVV}(\mathrm{IY})=E P I L+E V V(I Y)$ |
| ISN | 67 | 8300 | EATT EAATT EVV(IY) |
| İN | 68 |  | ENEW=ENEW+EATT |
| ISN | 69 | 50 | CONTINUE |
| ISN | 70 |  | $\operatorname{ESV}(\mathrm{I})=$ ENEW |
| ISN | 71 |  | GO TO 51 |
| ISN | 72 | 150 | $\operatorname{ESV}(\mathrm{I})=1 . \mathrm{E} 20$ |
| I SN | 73 |  | GO TO 300 |
| ISN | 74 | 51. | continue |
| ISN | 75 | 200 | IFLAG $=0$ |
| ISN | 76 | 300 | P.ETURN |
| ISN | 77 |  | END |

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| I SN | 1 |  | SUEROUTINE CLIST |
| :---: | :---: | :---: | :---: |
| I SN | 2 |  | COMMON CP $(3,27,36)$ ，RVEC $(3,27,36)$, NCHAIN，NLINK，SIZEY，SIZEZ，RC |
| I SN | 3 |  | COMMON／LST／RANG．ILST．JLST．IDST |
| I SN | 4 |  | COMMON／CHK／KTR．JR，SY，SZ，SAVG（ 27 ）．SSVG（ 27 ） |
| I SN | 5 |  | DIMENSION DDF（3．27）， |
| ISN | 6 |  | $I=I L S T$ |
| I SN | 7 |  | IDST $=0$ |
| I SN | 8 |  | J＝JLST |
| ISN | 9 |  | DO 7000 IY $=1.3$ |
| I SN | 10 |  | DO $7010 \mathrm{IZ}=1.16$ |
| I SN | 11 |  | $\operatorname{DDF}(I Y, I Z)=C P(I Y, I Z, J)-C P(I Y, I Z . I)$ |
| I SN | 12 | 7010 | $\operatorname{DDF}(I Y, I Z)=A B S(D D F(I Y, I Z))$ |
| I SN | 13 | 7000 | CONTINUE |
| ISN | 14 |  | DO $40 \mathrm{~L}=1$ ，NLINK |
| ISN | 15 |  | IF（DDF（2．L）．GT．SY） $\operatorname{CDF}(2 . L)=\operatorname{DDF}(2 . L)-S I Z E Y$ |
| ISN | 17 |  | $\operatorname{IF}(\operatorname{DDF}(3, L) . G T . S Z) D D F(3, L)=\operatorname{DDF}(3, L)-S I Z E Z$ |
| ISN | 19 |  | DST $=0$ ． |
| ISN | 20 |  | DO 7020 IY $=1.3$ |
| I SN | 21 | 7020 | $D S T=D S T+D D F(I Y, L) * D D F(I Y, L)$ |
| I SN | 22 |  | IF（DST．LE．RANG）GO TO 45 |
| ISN | 23 | 40 | CONTINUE |
| ISN | 24 |  | GO TO 50 |
| ISN | 25 | 45 | IDST $=1$ |
| ISN | 26 | 50 | CONTINUE |
| ISN | 27 |  | RETURN |
| ISN | 28 |  | END |

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SUEROUTINE CH2(XPR,YPR)
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SUEROUTINE CH2(XPR,YPR)
DIMENSION XPR(15),YPR(15)
DIMENSION XPR(15),YPR(15)
COMMON CP(3.27.36), RVEC(3,27.36),NCHAIN,NLINK.SIZEY.SIZEZ.RC
COMMON CP(3.27.36), RVEC(3,27.36),NCHAIN,NLINK.SIZEY.SIZEZ.RC
COMMMON/CHK/KTR.JR,SY,SZ,SAVG(27),SSVG(27).NPP(36),NNP(36)
COMMMON/CHK/KTR.JR,SY,SZ,SAVG(27),SSVG(27).NPP(36),NNP(36)
DIMENSION DLX(27:36),SO(27,36)
DIMENSION DLX(27:36),SO(27,36)
LLINK=NLINK-1
LLINK=NLINK-1
DO }70\quadU=1.NCHAI
DO }70\quadU=1.NCHAI
LLINK=15
LLINK=15
K1=1
K1=1
K2=LLINK
K2=LLINK
IF(U.EQ.22)THEN
IF(U.EQ.22)THEN
K1=21
K1=21
END IF
END IF
DO 70 K=K1.K2
DO 70 K=K1.K2
DLX(K,J)=RVEC (1,K,J)
DLX(K,J)=RVEC (1,K,J)
SO(K,U)=RVEC(2,K,U)*RVEC(2,K,J)+RVEC(`,K,U)+RVEC(3,K,J)     SO(K,U)=RVEC(2,K,U)*RVEC(2,K,J)+RVEC(`,K,U)+RVEC(3,K,J)
CONTINUE
CONTINUE
DO 9000 IZ=1.36
DO 9000 IZ=1.36
I f=1
I f=1
I2=15
I2=15
IF(IZ.EO.22)THEN
IF(IZ.EO.22)THEN
Iq=21
Iq=21
I2=25
I2=25
END IF
END IF
DO 9100
DO 9100
DO 9100 IY=I1.I2
DO 9100 IY=I1.I2
SO(IY,IZ)=ABS(SO(IY,IZ))
SO(IY,IZ)=ABS(SO(IY,IZ))
SO(IY,IZ)=SORT(SO(IY.IZ))
SO(IY,IZ)=SORT(SO(IY.IZ))
SO(IY,IZ)=DLX(IY,IZ)/SO(IY.IZ)
SO(IY,IZ)=DLX(IY,IZ)/SO(IY.IZ)
SO(IY,IZ)=DLX(IY,IZ)/SO(IY,IZ)
SO(IY,IZ)=DLX(IY,IZ)/SO(IY,IZ)
SO(IY,IZ)=ATAN(SO(IY,IZ))
SO(IY,IZ)=ATAN(SO(IY,IZ))
SO(IY,IZ)=SO(IY,IZ)-.g55566
SO(IY,IZ)=SO(IY,IZ)-.g55566
SO(IY,IZ)=COS(SO(IY,IZ))
SO(IY,IZ)=COS(SO(IY,IZ))
SO(IY,IZ)=SO(IY,IZ)=SO(IY,IZ)
SO(IY,IZ)=SO(IY,IZ)=SO(IY,IZ)
SO(IY,IZ)=1.5*SO(IY,IZ)
SO(IY,IZ)=1.5*SO(IY,IZ)
SO(IY.IZ)=SO(IY.IZ)-0.5
SO(IY.IZ)=SO(IY.IZ)-0.5
CONTINUE
CONTINUE
DO 100 J=1. NCHAIN
DO 100 J=1. NCHAIN
L 1=1
L 1=1
L2=15
L2=15
IF(U.EQ.22)THEN
IF(U.EQ.22)THEN
LY=21
LY=21
L2=25
L2=25
END IF
END IF
-DO 100 L=L1,L2
-DO 100 L=L1,L2
SAVG(L)=SAVG(L)+50(L.J)
SAVG(L)=SAVG(L)+50(L.J)
IF(NPP(U).EQ.1.)XPR(L)=XPR(L)+SO(L.J)
IF(NPP(U).EQ.1.)XPR(L)=XPR(L)+SO(L.J)
IF(NNP(U).EO.1)YFR(L)=YPR(L)+SO(L.U)
IF(NNP(U).EO.1)YFR(L)=YPR(L)+SO(L.U)
CONTINUE
CONTINUE
RETURN
RETURN
END
END
K2=25
K2=25
NO70
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SO(IY,IZ)=SORT (SO(IY

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SO(IY,IZ)=SORT (SO(IY
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**+**+***+*** SUSPROG CHOL, ********+*****************+*****+*+*
    SUBROUTINE CHOL 1(ROT,RT, AVEC)
    COMMON CP(3,27,36). FVEC(3,27,36),NSHAIN,NLINK,SIZEY,SIZEZ,RC
    DIMENSION ROT(3,3),RT(3,3),AVEC(3.27)
    K=22
    RVEC(1.21,K)=1.53
    DO 194 I =2,3
194 RVEC(I.21.K)=0.
    NLINCH=26
    DO 196 J=22,NLINCH
    L=J-1
    DO 198 I=1.3
    RVEC(I,U,K)=0.
    DO 200 IY=1.3
    RVEC(I.J.K)=RVEC(I.J,K)+RVEC(IY,L,K)*ROT(IY,I)
    200 CONTINUE
198 CONTINUE
198 CONTINUE
    CONTINUE 
    DO 2O4 J=21.NLINCH
2O4 AVEC(I,J)=RVEC(I,U,K)
2O2 CONTINUE
    DO 206 I=1.3
    DO 206 J=21.NLINCH
    RVEC(I, J.K)=0.
    DO 208 IY=1.3
    RVEC(I,J.K)=RVEC(I,J,K)+AVEC(IY,U)+RT(IY,I)
208 CONTINUE
206 CONTINUE
    CP(1.21.K)=9.59300
    CP(2.21,K)=20.054979
    DO 210 J=22,NLINCH
    JJ=v-1
    UJ=U-1
    DO 212 I=1.3
212 CP(I.U.K)=CP(I.JU.K)+RVEC(I.UJ.K)
210 CONTINUE
    RETURN
    END
```

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The original Computer program 'Monte Carlo Simulation program for lipid-protein interaction' written by Dr. H. L. Scott was modified in the present study of lipid-cholesterol interaction

The following changes were made:

1) Comments were inserted to define all parameters.
2) DIMENSION statements were modified to suit the cholesterol molecule structure. ( ISN 1-16)
3) DIMENSION statements were modified so as to accommodate longer acyl chains containing $15 \mathrm{C}-\mathrm{C}$ bonds each.
( ISN - 16 )
4) Comments were introduced at appropriate places to clarify the main steps of the program.
5) Neighboring matrix of the cholesterol molecule was defined differently than in the earlier program. ( ISN 49-67)
6) Coordinates of cholesterol molecules were included.
( ISN 68-148)
7) ISN 187 - 194 were added.
8) ISN 225-242 define two new rotation operations ROTN and ROTP.
9) ISN 316 - 325 were re-written to suit the cholesterol molecule.
10) ISN 352-373 were modified for cholesterol.
11) ISN 402-413 were re-written.
12) Necessary changes were made in the main loop so as to make it suitable for the present study concerning cholesterol rather than the protein model used earlier. ( ISN 415 550 )
13) ISN 699-702.
14) Sub-programs, CHECK and SUBROUTINE, were adjusted to accommodate longer acyl chains and the peculiar structure of the cholesterol molecule.
15) Sub-program, CHOL1, generates cholesterol 'tail'.

The structure of the main program is essentially the same, except the changes made so as to make it suitable for the present study of lipid-cholesterol interaction.

APPENDIX B

COMPUTER PROGRAM FOR THE CALCULATION

OF THE WEIGHTED AVERAGES AND THE STANDARD DEVIATIONS

|  |  | C *****A | program to calculate weighted averages. sto deviation. |
| :---: | :---: | :---: | :---: |
| I SN | 1 |  | IMPLICIT REAL (A-H, O-Z) |
| ISN | 2 |  | DIMENSION SUM1( 15 ), SUM2(15).SUM3(15) |
| I SN | 3 |  | DIMENSION TOTAL(15),AVE(15).STDEV(20) |
| I SN | 4 |  | DIMENSION $X(15.6), Y(15.6) .2(15.6) . S O S U M(20) ~$ |
| ISN | 5 |  | DIMENSION SOSUM1(20), SOSUM2(20), SOSUM3(20) |
| I SN | 6 | - | $N=17$ |
| ISN | 7 |  | DO 10 IBOND $=1.15$ |
| I SN | 8 |  | TSUM $1=0.00$ |
| ISN | 9 |  | REAO ( 2,15 ) ( $\times($ IBOND, L$), \mathrm{L}=1.6)$ |
| I SN | 10 |  | WRITE (6, 16) (X (IBOND,L), L= 1,6) |
| I SN | 11 | 15 | FORMAT( $6(F 7.5 .5 X)$ ) |
| ISN | 12 | 16 | FORMAT ( 1 H .6 (F7.5.5X)) |
| I SN | 13 |  | DO $401 \mathrm{~L}=1.6$ |
| ISN | 14 |  | TSUM $1=$ TSUM $1+$ X (IBOND, L) $=50$. |
| ISN | 15 | 404 | CONTINUE |
| ISN | 16 |  | SUM 1 ( IBOND $)=$ TSUM 1 |
| ISN | 17 | 10 | CONTINUE |
| I SN | 18 | 18 | FORMAT (5 (F7.5.5X)) |
| ISN | 19 |  | DO 20 IBOND $=1.15$ |
| I SN | 20 |  | TSUM2 $=0.00$ |
| I SN | 21 |  | READ ( 2,18 ) (Y(IBOND, M) , M $=1.5$ ) |
| ISN | 22 |  | WRITE (6, 16)(Y(I8OND, M) , M=1,5) |
| I SN | 23 |  | DO $402 \mathrm{M}=1.5$ |
| ISN | 24 |  | TSUM2 $=$ TSUM $2+Y($ IBOND,$M) * 100$. |
| ISN | 25 | 402 | CONTINUE |
| ISN | 26 |  | SUM2 ( IBOND) = TSUM2 |
| ISN | 27 | 20 | CONTINUE |
| ISN | 28 |  | DO 30 IBOND $=1.15$ |
| I SN | 29 |  | TSUM3 $=0.00$ |
| I SN | 30 |  | READ ( 2,15$)(\mathrm{Z}($ IBOND, N$), \mathrm{N}=1.6)$ |
| ISN | 31 |  | WRITE (6, 16) ( $\mathrm{Z}($ IBOND,N), $\mathrm{N}=1,6)$ |
| ISN | 32 |  | DO $403 \mathrm{~N}=1.6$ |
| ISN | 33 |  | TSUM3=TSUM3+Z(IBOND,N)*200. |
| I SN | 34 | 403 | CONTINUE |
| I SN | 35 |  | SUM3 ( IBOND) = TSUM3 |
| ISN | 36 | 30 | CONT INUE |
| I SN | 37 |  | DO 40 IBOND $=1.15$ |
| I SN | 38 |  | TOTAL (IBOND ) = SUM 1 ( IBOND) +SUM2 ( IBCND ) + SUM3 (IBOND ) |
| I SN | 39 |  | $A V E(I B O N D)=$ TOTAL (IBOND)/2000. |
| ISN | 40 | 40 | CONTINUE |
| I SN | 41 |  | DO 50 IBOND $=1.15$ |
| ISN | 42 |  | DO $60 \mathrm{~J}=1.6$ |
| I SN | 43 |  | PRINT 11.(X(IBOND, J)-AVE(IBOND) )**2 |
| ISN | 44 | 11 | FORMAT ( ', F14.6) |
| I SN | 45 | 60 | CONTINUE |
| ISN | 46 | 50 | CONTINUE |
| I SN | 47 |  | DO 70 IBOND $=1.15$ |
| ISN | 48 |  | DO $80 \mathrm{~K}=1.5$ |
| ISN | 49 |  | PRINT 22.(Y(IBOND.K)-AVE(IBOND) $)$ **2 |
| ISN | 50 | 22 | FORMAT(. , F 14.6) |
| ISN | 51 | 80 | CONTINUE |
| I SN | 52 | 70 | CONTINUE |
| ISN | 53 |  | DO 71 IBOND $=1.15$ |
| I SN | 54 |  | DO $81 \mathrm{I}=1.6$ |
| I SN | 55 |  | PRINT 33, ( 2 (IBOND, I)-AVE (IBOND) ) **2 |
| I SN | 56 | 33 | FORMAT ( $\cdot$, F14.6) |
| ISN | 57 | 81 | CONTINUE |
| ISN | 58 | 71 | CONTINUE |
| ISN | 59 |  | DO 12 IBOND $=1.15$ |
| I SN | 60 |  | DO $13 \mathrm{~J}=1.6$ |
| I SN | 61 |  |  |
| ISN | 62 | 13 | CONTINUE |
| I SN | 63 | 12 | CONTINUE |


| ISN | 64 |  | DO 34 IBOND=1.15 |
| :---: | :---: | :---: | :---: |
| ISN | 65 |  |  |
| ISN | 66 |  |  |
| ISN | 67 | 35 | CONTINUE |
| ISN | 68 | 34 | CONTINUE |
| ISN | 59 |  | DO 36 IBOND $=1.15$ |
| ISN | 70 |  |  |
| ISN | 71 |  | SOSUM3(IBOND) $=(2$ (IBOND. 1 ) $-\operatorname{AVE}$ (IBOND $)$ ) |
| ISN | 72 | 37 | CONTINUE |
| ISN | 73 | 36 | CONTINUE |
| ISN | 7.4 |  |  |
| ISN | 75 |  | SOSUM (IBOND) = SOSUM $1(180 N O)+$ SOSUM2 (IEOND $)$ SOSUMO (IBONO) |
| ISN | 76 |  | PRINT 44, SQSUM(IBONO) |
| ISN | 77 | 4. | FORMAT ( $30 \mathrm{X}, \mathrm{F} 12.6$ ) |
| ISN | 78 | 99 | CONTINUE (SOSUM(IBOND) IBOND $=1$ |
| ISN | 79 |  | PRINT 55.(SOSUM(IBOND).I8ONO $=1.15$ ) |
| I SN | 80 | 55 | FORMAT(20X.F8.5) |
| ISN | 81 |  | D 95 ISOND=1.15 |
| I SN | 82 |  | STCEV(IBOND) $=($ SQSUM (IBUND $) /(N-1)) * * 0.5$ |
| ISN | 83 |  | PRINT 98.STDEV(IBOND) |
| ISN | 84 | 98 | FORMAT(5X.F8.5/) |
| ISN | 85 | 95 | continue |
| ISN | 86 |  | PRINT 75 |
| ISN | 87 | 75 | FORMAT(5X.'TOTAL'.7X.'AVERG'.7X.'SOSUM'.7X.'STDEV'/) |
| ISN | 88 |  | DO $400 \mathrm{IB}=1,15$ |
| ISN | 89 |  | PRINT 85,TOTAL(IB).AVE(IB), SOSLiM(IB), STDEV(IB) |
| ISN | 90 | 85 | FORMAT(1H.4(E12.5)) |
| ISN | 91 | 400 | cuntinue |
| ISN | 92 |  | STOP |
| I SN | 93 |  | END |

VITA

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