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 GRADUATE COLLEGEBREAK UP OF A ROUND LIQUID JET IN A LOW WEBER NUMBER CROSS FLOW

A DISSERTATION SUBMITTED TO THE GRADUATE FACULTY in partial fulfillment of the requirements for the degree of Doctor of Philosophy

By
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## BREAK UP OF A ROUND LIQUID JET IN

 A LOW WEBER NUMBER CROSS FLOWA DISSERTATION APPROVED FOR THE SCHOOL OF AEROSPACE AND MECANICAL ENGINEERING

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## TABLE OF CONTENTS

LIST OF TABLES ..... VIII
LIST OF FIGURES ..... IX
LIST OF FIGURES ..... IX
ABSTRACT. ..... XII
CHAPTER 1 ..... 1
INTRODUCTION ..... 1
1.1 Scope ..... 1
1.2 Background ..... 2
1.2.1 Structure of JICF ..... 2
1.3 Literature Review ..... 5
1.3.1 Nozzle Geometry ..... 5
1.3.2 Single Phase JICF ..... 8
1.3.2 Two Phase JICF ..... 19
1.3.3 Flow Visualization ..... 29
1.3.4 Objectives ..... 33
CHAPTER 2 ..... 35
METHODS AND PROCEDURES ..... 35
2.1 Methods ..... 35
2.1.1 Experimental Setup ..... 35
2.1.2 Flow meter ..... 39
2.1.3 Submersible Pump ..... 40
2.1.4 Injector Design ..... 40
2.1.5 Flow System Hardware ..... 41
2.1.6 Particle Image Velocimetry System ..... 42
2.1.7 PIV Background ..... 44
2.1.8 Two Phase JICF Methodology. ..... 51
CHAPTER 3 ..... 56
COMPUTATIONAL RESULTS ..... 56
3.1 Computational Results ..... 56
CHAPTER 4 ..... 65
EXPERIMENTAL RESULTS ..... 65
4.1 Experimental Results ..... 65
4.1.1 Liquid Jet Analysis ..... 65
4.1.2 Stability Analysis ..... 66
4.1.3 Spray Characteristics ..... 77
4.1.4 PIV Cross Sectional Velocity Map ..... 83
4.1.5 Axial PIV Results for JICF ..... 85
4.1.6 Spanwise JICF Results. ..... 97
CHAPTER 5 ..... 108
CONCLUSIONS AND RECOMMENDATIONS ..... 108
5.1 Conclusions. ..... 108
5.2 Recommendations ..... 109
REFERENCES ..... 111
APPENDIX A ..... 117
APPENDIX B ..... 154

## LIST OF TABLES

Table 2.1 Flow system components ..... 42
Table 2. 2 Select Experimental parameters for two phase JICF ..... 52
Table 3. 1 Break up locations with varying momentum ratios. ..... 62
Table 4.2 Adjusted momentum ratio's for re-calibrated free stream velocities. ..... 98

## LIST OF FIGURES

Figure 1.1 Single phase JICF structures .....  3
(courtesty of Blanchard et al. 1999) ..... 3
Figure 2.1 Open circuit wind tunnel ..... 36
Figure 2.2 Water delivery setup ..... 36
Figure 2.3 Experimental Setup at North Campus ..... 37
Figure 2.4 Wind Tunnel Calibration of test section velocity (m/s) ..... 38
Figure 2.5 Water jet injector design ..... 41
Figure 2.6 TSI Particle Image Velocimetry setup ..... 43
Figure 2.7 Illustration of a typical PIV arrangement in a wind tunnel ..... 44
(Courtesy of Grant 1997) ..... 44
Figure 2.8 Illustration of the "interrogation" cell for source (a), and image density (b)45(Courtesy of Grant 1997). ..... 45
Figure 2.9 Double pulsed particle image (courtesy of Dantec Dynamics.com) ..... 46
Figure 2.10 Schematic of the image capture process. ..... 47
(Courtesy of Grant 1997) ..... 47
Figure 2.11 Vector and vorticity contours from PIV measurements ..... 48
(courtesy of Dantec Dynamics.com) ..... 48
Figure 2.12 Transmission spectra for optical filter ..... 55
(courtesy of TSI.com) ..... 55
Figure 3.1. Computational domain for free jet ..... 58
Figure 3.2. Computational domain for 2-d JICF ..... 58
Figure 3.3. Break up locations of a free jet for various grid sizes. ..... 59
Figure 3.4. Convergence of equivalent diameter with grid size for a 2-d JICF. ..... 60
Figure 3.5. Volume of fluid solution for $\mathrm{q}=20$. ..... 61

Figure 3.6. Volume of fluid solution for $\mathrm{q}=81.3$......................................................... 63
Figure 4.1 Images of 2mm water jet exit................................................................... 65
Figure 4.2 Instability frequency as a function of Weber number. .............................. 28
Figure 4.3 Illustration of the break up process of a two phase JICF .......................... 67
(courtesy of Fuller et al. 1997).................................................................................... 67
Figure 4.4 Visualization of the break up process of a water jet in cross flow: a) $q=$ 172 , $\mathrm{We}=1.72$, Column break up; b) $\mathrm{q}=69.25, \mathrm{We}=4.3$, Column break up; c) q $=40.7, \mathrm{We}=7.32$, Bag break up; d) $\mathrm{q}=18.8, \mathrm{We}=15.85$, Multimode break up. 68

Figure 4.5 Break up process for $\mathrm{q}=10, \mathrm{We}=29.29$, Multimode break up. ............. 69
Figure 4.6 View of disturbances in the body of the jet in the $x-y$ plane at: a) $q=$ 40.7, $\mathrm{We}=7.32$, multimode break up; b) $\mathrm{q}=18.8$, $\mathrm{We}=15.85$, shear break up; c) $\mathrm{q}=10$, $\mathrm{We}=29.29$, shear break up...................................................................... 75

Figure 4.7 Transient nature of the break off point for $q=40.7$.................................. 76



Figure 4.11 Non-dimensional spray width at various downstream locations............. 80
Figure 4.12 Display of change in the cross section of the jet at various downstream
$\qquad$
Figure 4.13 Wind tunnel velocity validation using PIV. ............................................ 83
Figure 4.14 Wind tunnel velocity in the cross section of the...................................... 84
wind tunnel using PIV. ............................................................................................... 84
Figure 4.15 PIV measurement plane for all axial locations........................................ 85
Figure 4.16 PIV vector field for $\mathrm{q}=172$ at $\mathrm{Y} / \mathrm{d}=0$. ...................................................... 87
Figure 4.17 PIV vector field for $\mathrm{q}=172$ at $\mathrm{Y} / \mathrm{d}=2$. ....................................................... 88

Figure 4.18 PIV vector field for $\mathrm{q}=172$ at $\mathrm{Y} / \mathrm{d}=4$. ....................................................... 89
Figure 4.19 PIV vector field for $\mathrm{q}=69$ at $\mathrm{Y} / \mathrm{d}=0$. ........................................................ 90
Figure 4.20 PIV vector field for $\mathrm{q}=69$ at $\mathrm{Y} / \mathrm{d}=2$. ........................................................ 91
Figure 4.21 PIV vector field for $\mathrm{q}=40$ at $\mathrm{Y} / \mathrm{d}=0$. ........................................................ 92
Figure 4.22 PIV vector field for $\mathrm{q}=40$ at $\mathrm{Y} / \mathrm{d}=2$. ........................................................ 92
Figure 4.23 PIV vector field for $\mathrm{q}=18.8$ at $\mathrm{Y} / \mathrm{d}=0$. ..................................................... 93
Figure 4.24 PIV vector field for $\mathrm{q}=18.8$ at $\mathrm{Y} / \mathrm{d}=2$. ..................................................... 94
Figure 4.25 PIV vector field for $\mathrm{q}=10$ at $\mathrm{Y} / \mathrm{d}=0$. ........................................................ 95
Figure 4.26 PIV vector field for $\mathrm{q}=10$ at $\mathrm{Y} / \mathrm{d}=2$. ........................................................ 96


Figure 4.29 Near field velocity profiles at $\mathrm{Z} / \mathrm{d}=10$. .................................................. 103


## ABSTRACT

The break up of a liquid jet in cross flow has applications in fuel atomization processes. The break up of a water jet in a high speed cross flow was studied with momentum ratios ranging between 10 and 172. High-speed camera images showed break up characteristics ranging from bag break up (break up due to large ligaments or "bags" of fluid sheared off the liquid jet) to multimode break up (break up in which large ligaments and small drops are present), with large disturbances developing on the jet boundary. The disturbance wavelengths and break up locations were measured and compared, and the agreement was very good. It was also observed that as the cross flow velocity increased, the jet boundary spread linearly outward in the spanwise direction. Particle Image Velocimetry (PIV) results showed that the cross flow did not follow the jet boundary, but passed around the jet, similar to the flow around a bluff body. This implies that the Rayleigh-Taylor instability cannot be a dominant mechanism for the jet break-up. Spanwise PIV results indicate the presence of a high shear region along the sides of the jet, which might serve as the primary cause of jet break-up.

## CHAPTER 1

 INTRODUCTION
### 1.1 Scope

The study of Jets in cross flows (JICF) has many different applications. Some of these applications are, but not limited to, liquid rocket engines, diesel engines, air breathing propulsion systems, and agricultural sprays. In some combustion applications, premixed fuel and air is injected upstream of the combustion chamber into a cross flow of air atomizing the mixture. In air breathing propulsion systems such as ramjets and scramjets, the study of a two phase JICF has many applications. For example, a scramjet turbine uses a fuel injected perpendicular to a high speed cross flow to atomize the column of fuel for proper ignition to create thrust. The importance in understanding this interaction lies in efficiently delivering the fuel in its properly "atomized" state for the combustion process.

The most challenging aspect of this research is in the validity of the experimental methods used. The complexity of the two interacting flows: 1) Boundary layer flow (due to no slip along a solid wall), and 2) Free jets makes this topic very difficult to study. When the jet and cross flows are of the same phase, the methodology is somewhat simplified and several options for flow tracking are applicable. However, when the jet and cross flow are in two different phases, the
flow is not easily amenable to conventional methods of measurement. Also, the computation of such flows is cumbersome. The computational time and effort required to model such a complex flow system is far reaching. As a result, few CFD studies of JICF have been undertaken. In addition to the complexities described above very little knowledge exists of the actual process that goes into the atomization of a liquid column by a high speed cross flow. Ideas abound, however little factual evidence has been documented, resulting in an overall "accepted" idea of the reasons behind this break up process.

### 1.2 Background

### 1.2.1 Structure of JICF

The study of a JICF is complex due to the interaction of a couple complex fluid phenomena, namely, boundary layer flow and free jets. The cross flow of fluid is usually bounded resulting in a complex boundary layer along the wall which interacts with the jet. Usually wind or water tunnels are used to provide this cross flow and a flush mounted, or elevated circular orifice is used to inject the jet perpendicular to the flowing stream of fluid. Several different arrangements for nozzle geometries have been studied and will be discussed later in this chapter. The inertial force of the cross flow results in a momentum transfer, which bends the jet in the direction of the flowing stream. The depth and penetration of the jet has been
linked to several design factors, such as exit momentum of either fluid, as well as injector designs, which will be described later as well.

A JICF can be single-phase or multiphase. In the single phase JICF, several large-scale structures result in the interaction between the cross flow and the jet. These structures include: Counter-rotating Vortex Pairs (CVP) which originate as an effect of the bending of the jet itself and the shear layer between the cross flow and jet boundary, Horse Shoe Vortices (HSV) which are formed upstream of the jet and close to the wall which act as a carrier of fluid from the upstream side of the jet into the wake of the jet, Wall Vortices (WV) which develop downstream of the jet and near the wall, Upright Vortices (UV) which are formed from the interaction between the wall boundary layer and the jet flow, and are typically unsteady for low jet Reynolds Numbers (figure 1.1).


Figure 1.1 Single phase JICF structures
(courtesty of Blanchard et al. 1999)

Also, Ring Like Vortices (RLV) are formed from the jet shear layer; their shape and spatial evolution are influenced by the cross flow. These structures act as the driving force for the mass and momentum transfer.

In the case of the two-phase JICF, the structures that are formed are somewhat different. Less is known of the wake structures for a two phase JICF but several general structures have been observed (Figure 1.2).


Figure 1.2 Illustration of the break up process of a two phase JICF (courtesy of Fuller et al. 1997)

Initially near the wall, the column of liquid exits much like a cylinder of diameter equal to that of the jet. On the windward side of the jet (upstream), the jet stays fairly steady along its boundary until the presence of waves along the trajectory of the jet is observed, resulting in column break up. There are three main break up types for a two phase JICF, bag break up, multimode break up, and shear break up. For the shear break up regime on the leeward side of the jet (downstream), close to
the wall, surface break up is seen resulting in small droplets spreading and bending in the cross flow direction. For the bag break up regime, at the peak of a single wave on the windward side of the jet, large "ligaments" of liquid break off and form ligaments. These ligaments undergo a secondary break up mechanism due to aerodynamic forces resulting in smaller and smaller droplets. Multimode break up is described by any combination of both shear break up and bag break up characteristics. Very little is known about the wake of the two-phase JICF and how it contributes to the break up of the liquid jet, which is the main focus of this research topic.

### 1.3 Literature Review

### 1.3.1 Nozzle Geometry

The main purpose of a two-phase JICF is to aid in the atomization. Various nozzle geometries have been proposed for this purpose. One of these nozzles is an airblast nozzle. Airblast nozzles are typically used for fuel injection processes because of better atomization properties. This type of injector uses a stream of air inside the injector to more efficiently break up the column of liquid surrounding it by cones of air. Carvalho et al. (1998) studied this very arrangement. The air-blast nozzle consisted of a conical shaped nozzle with an annular portion for liquid, surrounded by two air ports. Carvalho et al. (1998) used the influence of the surrounding air shear forces as a means for atomization of the liquid column. The images were processed using shadowgraphy, and a high speed CCD camera with spot lights. The liquid mass flow rate was varied at values of $5.8,10.8$, and $13.9 \mathrm{~g} / \mathrm{s}$, with
air Reynolds numbers ranging from 66,000-93,000. In addition, the inner airflow velocities, and swirl level of the outer air was also varied from $40-200 \mathrm{~m} / \mathrm{s}$, and swirl rates $\leq 2.5$, respectively.

The results showed that as the inner air velocity was increased, the level of atomization was increased, and the break-up length decreased. The authors proposed an inner air threshold of $40 \mathrm{~m} / \mathrm{s}$ for the proper atomization of the liquid jet. The primary result of interest was that as the swirl level of the jet was increased, the spreading rate of the atomized jet was increased. This paper showed conclusively that shear forces from the surrounding air blast positively affect the atomization of the liquid jet breaking it up into smaller droplets further upstream of the injector. These aerodynamic shear forces act in a very similar manner to secondary drop break up downstream, further accelerating the break up process.


Figure 1.3 Illustration of the break up process of an airblast atomizer (courtesy of Aalburg et al. 2004)

A circular jet exit geometry has been used in most studies. However, some authors have studied other shapes as well as different injection angles, Padhye and Schetz (1977). These influences will be discussed in section 1.3.3. The influence of injection angles is beyond the scope of this study and is discussed in other research papers. Pourdeyhimi and Tafreshi (2003) studied the effect of a conical jet in different positions on a JICF. Results were compared to Ohnesorge classification of high Reynolds number liquid jets, which atomize quickly after discharge. The experiment consisted of a high pressure pump, digital camera, and CCD high speed camera. The flow passed through a cone style nozzle with a capillary section 0.127 mm in diameter and conical section 0.34 mm in diameter. The nozzle configuration was changed by flipping the nozzle for a cone down configuration (water discharges from conical taper), and a cone up configuration (water discharges from straight capillary section). The results showed that the cone up nozzle followed Ohnesorge classification, while the cone down configuration did not. At a Reynolds number of 18,600, a first wind-induced break up mode was observed, while according to Ohnesorge theory this should not occur at Reynolds numbers above 8,600. Pourdeyhimi and Tafreshi (2003) stated that due to the cone down geometrical configuration the flow separated from the nozzle wall and resulted in a recirculation zone, which resulted in the elimination of wall friction vortices inside the injector that would normally influence the break up mechanism of the jet. It was concluded that a constricted (cone down) water jet did not follow the classifications of Ohnesorge. This paper showed that the geometry of the nozzle has an affect on the break up of
the liquid jet, and should be taken into consideration when studying the break up of a liquid jet in a cross flow.

### 1.3.2 Single Phase JICF

The study of single phase JICF has many environmental applications, such as pollution control of smoke stacks into atmospheric cross flows, or injection of pollutants into flowing streams. The early studies of single-phase JICF centered around the penetration and mixing properties of the interaction between an air jet, and an air cross flow. One such study was Baines and Keffer (1962). Using an air jet, and air cross flow, the penetration at velocity ratios $\left(\mathrm{R}=\mathrm{U}_{\mathrm{j}} / \mathrm{U}_{\infty}\right)$ of 2-10 was studied. The cross flow of air was generated by a low speed wind tunnel with a $4 \mathrm{ft} x 8 \mathrm{ft}$ cross section. The air jet issued perpendicular to the cross flow from a $3 / 8$ " diameter orifice. Hot wire anemometers were used at various locations to map out the velocity profiles in the jet. The results showed that the penetration of the jet into the cross flow decreased as the velocity ratio decreased. The entrainment into the jet was shown to increase as the velocity ratio decreased.

Hester et al. (1971) studied the presence of shed vortices in the wake of a single phase JICF. Hester et al. (1971) utilized a subsonic wind tunnel with a constant freestream velocity of $50 \mathrm{ft} / \mathrm{s}$. Velocity ratios of 8 and 12 were studied, by varying the exit velocity of an air jet through a 2 " diameter pipe. Flow visualization was achieved by placing a tuft screen in the wake of the jet. The tuft screen consisted of a wire mesh with bits of thread taped to the screen. The effect of the flow on the
tufts was recorded using a high-speed movie camera ( 240 frames/sec). The results indicated the presence of periodic eddies in the wake of the jet. The high-speed camera images allowed the determination of the vortex-shedding frequency, which was quantified using the Strouhal number (St):

$$
\begin{equation*}
S t=\frac{f d}{U_{\infty}} \tag{eq1}
\end{equation*}
$$

Where, f is the frequency, d is the diameter of the column of liquid, and $\mathrm{U}_{\infty}$ is the cross flow velocity. The measurements indicated that the Strouhal number was less than one-half of the Strouhal number associated with the shedding of vortices behind a solid cylinder of comparable dimension. The authors also stated that the vortices in the wake of the jet appeared to travel in the downstream direction along the plate, surrounding the jet, instead of along the axis of the jet. This study was important in showing the connection between the shedding vortices from a solid cylinder, and shed vortices in a single phase JICF, which is generally only present in a range of Reynolds numbers, $250<\operatorname{Re}<2 \times 10^{5}$.

Chassaing et al. (1974) continued the work of Baines and Keffer (1962) by focusing on the trajectory of the jet, and defining planes of symmetry within the body of the jet. Using experimental measurements with pitot probes and hot wire anemometers, Chassing et al. (1974) were able to develop a new method for evaluating the axis of the jet. Fearn and Weston (1974) shifted the focus of the study of a single phase JICF from trajectory to the influence of the Counter-rotating Vortex

Pair (CVP). The experimental investigation utilized a V/STOL wind tunnel with cross flow velocities ranging from $100-175 \mathrm{ft} / \mathrm{s}$, and a 4 " diameter air jet with velocity ratios ranging from 3-10. Velocity measurements were made using a rake of $1 / 4$ " pitot static probes attached to an airfoil at 2-45 jet diameters downstream. The results indicated that the CVP was generated very close to the exit of the jet with strength directly proportional to the speed of the jet at the orifice as well as the diameter of the jet. The vorticity strength of the CVP was also shown to weaken as the vortex pair traveled downstream, because of the diffusion of vorticity.

Eskinazi et al. (1976) set out to experimentally document the exit conditions of the flow at the jet exit and to prove the three-dimensional nature of the interaction between an air jet and an air cross flow. The motivation behind the study was to use the results to provide some insight into the validity of the computational studies of a single phase JICF, which were just beginning at the time. Eskinazi et al. (1976) utilized a 2.39 cm jet in a wind tunnel providing a $29.6 \mathrm{~m} / \mathrm{s}$ cross flow, with a jet Reynolds number of $4.4 \times 10^{4}$. The velocity was measured using a constanttemperature anemometer at 1,000 separate points, 1 diameter upstream and downstream of the jet center. Both skirted and unskirted pipes were used to study the differences between a "hole in a wall" JICF (skirted) and a "pipe exit" JICF (unskirted). The results indicated that the shedding frequency of vortices from a single pipe with no skirting at $\mathrm{R}<5.5$ was very close to that of a solid cylinder, where " R " is the ratio of the cross flow velocity to the jet velocity. The researchers were one of the first to show experimentally that a single pipe in cross flow was
influenced by the vortices shed off the pipe itself, which was shown to be quite different from the structure of a skirted JICF. The results further highlighted the strong connection between the vorticity generated within the pipe and the CVP vorticity in the jet body. Eskinazi et al. (1976) also mapped out a new way of defining the jet boundary as a function of not only the paths of the center of the jet, but also the locations of maximum vorticity in the CVP.

Andreopoulos (1985) conducted another early study of a single-phase JICF with the intention of studying the interaction of a boundary layer channel flow and the boundary-layer pipe flow. The experimental setup consisted of a 50 mm pipe, 12 diameters in length. The cross flow developed a boundary layer 4 diameters upstream of the jet at a free stream velocity of $13.9 \mathrm{~m} / \mathrm{s}$. Mean and fluctuating velocity measurements were made with a DISA X-wire probe. The flow was visualized using a fog of paraffin oil droplets, and the images were captured by a NIKON camera. A conditioning technique was used to track the jet and cross flow separately by heating one and using a thermal anemometer to discern between the two flows. For this experiment, the jet was heated using heating elements along the pipe length. For R values greater than 3 , and jet Reynolds numbers less than $5 \times 10^{3}$, ring vortices were formed at the top of the jet. These ring vortices were of opposite vorticity to that of the cross flow, but similar to that of the pipe flow. The ring vortices underwent bending and stretching, as they are convected downstream and were finally broken down to turbulence. As the value of R was decreased, the ring vortices were visually less organized and more randomly generated in their occurrence. At higher Reynolds
numbers, the generation of these large-scale structures from the jet decreased and the size began to fluctuate.

Up to this point, much of the research on a single phase JICF had been focused on the large-scale structures in the flow. It had always been assumed that as the free stream passed around the body of the jet, the flow behaved similar to the flow passing over a solid cylinder. Fric and Roshko (1994) were the first to question this assumption. Fric and Roshko (1994) studied the near-wake of the JICF and set out to prove that the wake that formed due to the interaction of a boundary layer flow and a jet was not similar to the wake which forms due to the flow around a cylinder. It had been assumed that the vortices seen in the wake of the JICF were due to vortexshedding from the jet, similar to the flow around a solid cylinder.

The air jet velocity was varied from 3 to $45 \mathrm{~m} / \mathrm{s}$ and the value of $R$ value was varied between 2 and 10. The flow visualization was achieved using a smoke-wire arrangement in different planes and at different locations. By placing the smoke wires at different distances from the wall, the boundary layer flow as well as the flow outside of the boundary layer was visualized. For velocity measurements, a single hot wire probe was used with a XYZ traversing mechanism for placement.

Cross-sectional slices of the flow around a JICF at different locations in the Z direction were documented. Most notable was the formation of the horseshoe-vortex at the upstream exit of the jet, which acted to carry fluid from the upstream side of the jet into the wake of the jet. At the rear of the jet, various wake structures were observed. The most noticeable and organized structures are seen at a momentum
ratio of 4 . Contrary to the flow around a solid cylinder which experiences a very "open" separation at the rear of the cylinder, the wake around the jet was closed. The separation region is defined as the location where the streamlines separate from the boundary along the sides and the immediate rear section of the boundary resulting in a "dead zone" of fluid which typically consists of a pair of bound vortices. The separation of flow around a solid cylinder was shown to result in a very large separation region, whereas the separation region for the JICF was much smaller in size adhering more closely to the boundary of the liquid jet. A comparison of the two flows showed noticeable differences in their geometry. Through the use of smoke injection within the jet, it was also observed that the wake vortices were not shed from the jet body. By injecting smoke into the boundary layer, it was seen that the wake vortices were entrained upward into the jet itself. Initially, the wake folded up under itself at a "separation event" due to the adverse pressure gradient imposed by the flow outside of the boundary layer (external flow). This folding resulted in vortices primarily in the Y direction. The wake vortices were then tilted and bent upward into the bottom side of the jet. For lower $R$ values $(R=4)$, the formation of these wake vortices was well defined and the side views showed the presence of large tornado-like vortices. For other values of R, the tornado vortices were less defined. This research showed that the wake vortices did contribute to the mixing and entrainment of the cross stream into the body of the jet. The wake entrainment drew surrounding fluid into the CVP, resulting in the mixing of the two streams.

The stability of the CVP was studied by Kelso et. al (1996). In this paper, a study of a round jet in cross-flow was analyzed at Reynolds numbers ranging from 440 to 6200 , and velocity ratios ranging from 2.0 to 6.0 . The study was conducted in a water channel with liquid-liquid cross-flow jet interaction. Flow visualization was achieved with the introduction of a dye upstream of the jet exit as well as from circumferential slits around the sides of the jet as well as on the downstream side. Further experimentation was done for a gas in gas cross-flow along with the measurement of pressure gradients and smoke streams to validate any assumptions made by the liquid in liquid case.

The main results indicated that the jet contained many complex vortical systems. Dye injection showed that on the upstream side of the jet, some of the crossflow was actually entrained into the jet due to adverse pressure gradients formed within the jet pipe. The CVP was observed at various Reynolds numbers and was attributed partially to the separation pattern within the upstream side of the pipe. Ring vortices were also observed due to Kelvin-Helmholtz instabilities. These rings in the jet shear layer were tilted and appeared to fold and contribute to the CVP. On the back side of the jet, wall vortices appeared due to the wake from the jet. At low Reynolds numbers (440), these wall vortices were less apparent, but still entrained fluid from the wall into the CVP. At higher Reynolds numbers (2700), a von-Karman vortex street was readily observed. At these high Reynolds number values, the wall vortices were advected upward into the jet causing upright vortices contributing to the

CVP; the non-dimensionalized phase-averaged vorticity contours showed a peak vorticity in the wake of the jet with a value of $11.26\left(\omega_{\mathrm{nd}}=\omega \mathrm{D} / \mathrm{U}_{\infty}\right)$.

Blanchard et al. (1999) also studied the influence of the CVP on the stability of a jet in cross flow. The generation of the CVP was said to be due to the interaction of the cross flow moving around the body of the jet folding the jet in upon itself. Other large-scale structures observed were the street of transverse vortices (ring vortices) as well as vertical wake vortices (wall vortices). All three of these structures were unsteady in nature. The experimental setup consisted of a square test section water channel with a water slot jet $(2 \mathrm{~cm} * 0.2 \mathrm{~cm})$ under hydrodynamic isothermal conditions. The values of R were varied from 1.5-6.5, also, the Reynolds numbers ranged from 100-600. The main objective of this study was to measure the spatial and temporal characteristics and the development of the unsteady vortex structures for a JICF at low velocities. This was achieved by the use of two methods of measurement, Laser Induced Fluorescence Tomography (LIFT), and Particle Streak Velocimetry (PSV). For the LIFT technique, a fluoresceine salt was dissolved in the water and excited by a laser light sheet from an argon ion laser. The reflected green light was used to resolve only the jet fluid flow.

PSV was used in this study to visualize the surrounding stream due to the cross flow of water. PSV uses small solid particles in the flow and records their paths in different cross sectional planes of light provided by an argon-ion laser centered on wavelengths of 488 and 514 nm . Using optics similar to that of the LIFT method, the motion of the fluid particles was tracked. This method was used to formulate
topological data (size of the CVP). The results using LIFT showed the entrainment of the cross-flow fluid into the body of the CVP. The authors indicated that this proved that the CVP served as the primary mixing structure in the JICF. Using PSV methods, the evolution of the CVP was tracked. The authors showed that the CVP grew in both the Y and Z directions, where Y is the distance from the injector, and Z is the spanwise distance or "width" from the injector. The CVP grew until the size was nearly equal to the breadth of the entire channel, whereby they finally became stable in size. Throughout the growth of the CVP, the authors indicated that there was no significant difference in size between the left and right vortices. At the region of stability $(\mathrm{X} / \mathrm{e}=20)$ the size of the CVP in the y direction and the z direction were dissimilar, where "e" is the thickness of the injection slit. Using this data, the authors indicated that the CVP was most nearly elliptical in shape.

Next the location of the instability was studied. A jet with a $\mathrm{Re}=300$ and $\mathrm{R}=$ 3 was steady and stable in its structure. At a value of $\operatorname{Re}=500$ and $\mathrm{R}=4.5$, the jet became unsteady and the ring vortices were formed due to the unsteadiness. The authors went on to show that the common belief that these vortices were a result of Kelvin-Helmholtz instabilities was incorrect. Through the use of a histogram and calculation of the min and max wavelengths, it was shown that the instability was not characteristic of "Kelvin-Helmholtz" instabilities, but characterized generally by the Landman and Saffman theory of instability. Kelvin-Helmholtz instability arises when a mixing layer is present between two fluids. Amplifications of small local disturbances in this shear flow lead to the unstable nature of the flow. Landman and

Saffman theory of instability focuses on the highly unstable nature of the elliptical shape of the CVP. Comparisons between the Landman and Saffman theoretical rate of thickening and experimental measurements showed good agreement, leading the authors to characterize the instability of the CVP as Landman and Saffman instability. These findings were later validated by Ferre et al. (2001), and Camussi et al. (2002).

Ferziger et al. (1999) used Large Eddy Simulation (LES) to study a single phase JICF. The program used the incompressible, unsteady Navier-Stokes equations to model the complex flow. Simulations were performed for values of R of 2 and 3.3, and Reynolds numbers of 1050 and 2100. A total of $1.34 \times 10^{6}$ control volumes were used in a domain that spanned $13.7 \mathrm{~d} \times 8.0 \mathrm{~d} \times 9.0 \mathrm{~d}$. The simulations were compared with experimental results and the two sets of results were found to be very similar. Any differences were attributed to the difference in jet inflow conditions, as well as Reynolds number discrepancies resulting in differing boundary layer configurations at the lower wall. Four main structures were observed in the near wake of the jet: hanging vortices, ring vortices, wall vortices, and CVP. The hanging vortices were observed to originate at the lateral side of the jet, and are seen as an extension of the horseshoe vortex. These hanging vortices transported flow to the rear of the jet originating from the near wall of the pipe and the upstream cross-flow boundary layer. Breakdown of these vortices occurred due to adverse pressure gradients experienced as the flow passes around the jet (similar to flow around a bluff body) and compressive stresses due to upsweeping motion of the cross flow fluid into the jet body.

Span-wise rollers were formed due to K-H instabilities on the upstream and downstream side of the jet. The span-wise rollers were found to carry high amounts of velocity fluctuation in the near field of the jet resulting in high turbulent kinetic energy (TKE). In the wake of the jet stream-wise vortices were observed as well as vertical or upright vortices. The formation of the upright vortices was shown to be due to the reorientation of the stream-wise vortices due to the strain field behind the jet. The phase-averaged vorticity contours in the wake showed a peak value of 0.4 $\left(\omega_{\mathrm{nd}}=\omega \mathrm{D} / \mathrm{U}_{\infty}\right)$. All three structures were shown to contribute to the evolution of the CVP.

A number of studies have involved reacting jets in cross flows. Chang and Huang (1994) studied the stability of an elevated combusting jet in cross flow. Using a high-speed wind tunnel and a propane jet, the structures in the wake of an elevated jet in cross flow were studied. Images were compiled using a Schlieren technique in the wake of the jet. The results showed the presence of organized vortices in the wake of the elevated jet. The vortices were shown to directly affect the stability of the flame in cross flow resulting in a "flickering" flame.

In a similar paper by Huang and Yang (1996), the temperature profiles and concentration in the wake of a combusting jet were measured. The results also showed the dependence of concentration profiles in the wake of the jet on the mixing structures in the wake of the jet. Gollahalli and Pardiwalla (2002) studied the characteristics of a turbulent reacting jet in cross flow. Using a wind tunnel with a thermocouple and gas sampler, the temperature and concentration of products in the
wake of the jet were studied. Results showed the dependence of the flame configuration on the presence of bound vortices in the wake of the jet. Similar to the findings of Chang and Huang (1994), the two-zone structure was shown to "flicker" due to the presence of vortices in the wake of the jet. Most importantly, results showed that larger wakes downstream of the jet resulted in increased soot production in the wake of the jet.

### 1.3.2 Two Phase JICF

Much of the study of two phase jets in cross flows focuses on the break up process of the jet itself. One of the first studies to analyze jet penetration and break up in a subsonic cross flow along with different nozzle geometries was by Padhye and Schetz (1977). A 9" by 9" blow down wind tunnel was used with a flat plate and flush mounted water injector. Injectors of different sizes were used along with different orientations to the free stream. Photographs were taken using a longexposure camera, and a short-exposure camera, both cases used a back light to view the image. Measurements were made downstream at an $x / d$ location of 6.25 from the center of the injector. A non-dimensional momentum ratio " $q$ " was used to relate the exit momentum of the jet ( j ) to the cross flow momentum ( $\infty$ )
$q=\frac{\rho_{j} U_{j}^{2}}{\rho_{\infty} U_{\infty}^{2}}$

The results showed that penetration (axial distance into the cross flow) decreased with an increase in the cross stream Mach number. This was said to be due to the increased drag coefficient due to the flow over the bluff body. Droplet size was shown to decrease with increased free stream Mach number. The orientation of the rectangular injector aligned with the free stream resulted in a reduced mean droplet diameter, while the transverse orientation resulted in an increase in the mean droplet diameter. The study also showed that an increase in the flux q resulted in an increase in the axial distance to the jet fracture, and a decrease in the amplitude and wavelength of the surface waves. The axial distance to gross fracture was greatest for the aligned rectangular slot jet.

Along with this study, Less and Schetz (1986) studied that transient behavior of the JICF. The objectives of the study were to "quantitatively characterize the time dependent behavior of a liquid jet in gas cross flow." The authors described the interaction of the liquid jet with the gaseous cross flow as an initial formation of a liquid column, followed by axial waves that developed along the surface of the jet, and propagated till the jet fractured at the trough of a high-amplitude wave. The experimental apparatus consisted of a high velocity wind tunnel with a flush mounted jet, 0.91 mm in diameter. A high-speed camera with a CCD detector was used to measure the diffraction patterns of the light column passing through the spray plume. The designed system allowed for droplet measurements ranging from 7 to 100 micrometers in diameter.

The results indicated that at every location, the droplet size varied greatly as a function of time. The measured frequency of the axial waves was 60 kHz , with a fracture point frequency of 15 kHz . The authors also indicated that initially the waves propagated at velocities equal to that of the jet, then were accelerated further downstream at velocities nearing that of the free stream. The frequency of instability was expressed in the form of the Strouhal number, which turned out to be constant at 0.4 .

The authors made a comparison between this Strouhal number and that for the flow around a solid cylinder, 0.2 , noting that there was a distinct similarity between the two flows. The authors also stated that there was a strong interaction between the mechanics of the gas flow, shed vortices, and the instability in the column of the liquid jet. This was the first study of its time to question the role of the wake and its influence on the break up of the liquid column.

Following this study, Fuller et al. (1997) studied the near-field of the twophase JICF, along with the influence of differing fluid types. Much of the experimental setup was similar to the previous study. The four fluids used were water, ethyl alcohol, $30 \%$ alcohol/water, and $40 \%$ glycerol/water. The results showed that the primary break up of a liquid jet was a result of aerodynamic factors. The liquid column was initially deformed, then flattened and broken up by the cross flow. The interaction between the two flows was shown to be a variable of the Weber number (We).
$W e=\frac{\rho_{\infty} d u_{\infty}^{2}}{\sigma}$
Where $\rho_{\infty}$ is the density of the cross flow $\left(1.21 \mathrm{~kg} / \mathrm{m}^{3}\right), \mathbf{u}_{\infty}$ is the cross flow velocity, and $\sigma$ is the surface tension of the jet fluid. The study found that at lower Weber numbers the liquid column exhibited "bag break up", whereas at higher Weber numbers the primary break up was due to waves in the column due to shearing forces. For higher viscosity fluids the waves were more prominent, along the upstream side of the jet. When the momentum flux ratio was large, the jet underwent a surface break up mechanism, in which the rear side of the jet broke into smaller droplets. Using an aerodynamic analysis on a single droplet, several equations were derived to predict column trajectories, and break up locations for a liquid jet in cross flow. The theoretical results were in good agreement with the experimental measurements, thus indicating that the primary break up mode of a liquid jet was due to the aerodynamic forces on the liquid column. The analysis also showed that the drag coefficient for a liquid jet in cross flow was similar to that of a cylinder of comparable size, and increased for higher viscosity fluids, contrary to the findings of Fric and Roshko (1994) for a single phase JICF. The y-location of break up indicated a high dependence on the momentum flux, while the x-location was constant for all momentum flux values.

Fuller et al. (1998) went on to study the primary structures in a two-phase JICF. The experiment consisted of a water jet injected through a 0.5 mm hole at velocities ranging from 12.8 to $42.5 \mathrm{~m} / \mathrm{s}$. The cross flow of air at Mach $0.3,0.4$, and
0.5 was delivered in a high-speed wind tunnel. Through a clear side panel, Phase Doppler Particle Analyzer (PDPA) measurements with a $10-\mathrm{mW}$ helium-neon laser were made at $\mathrm{X} / \mathrm{d}=300,400$, and 500 . The results showed that as the momentum flux increased, the maximum volume flux of water passing through the measurement plane decreased. Also, the Sauter Mean Diameter (SMD) decreased, as the cross flow velocity increased, due to increased secondary droplet break up downstream of the jet. The authors showed that large droplets were distributed towards the top of the spray plume when $q$ was large, but for small $q$ the large droplets were found in the central portion of the spray plume. The difference was said to be due to the intense momentum exchange between the two fluids resulting in obvious wake regions for most cases. The importance of the presence of a wake may shed light into the fact that wake structures could play a part in the atomization of the liquid column. The wake was most evident at an $\mathrm{X} / \mathrm{d}$ value of 200 for 0.3 Mach air flow. Also, at $\mathrm{X} / \mathrm{d}$ of $300, \mathrm{U}_{\mathrm{j}}=12.8 \mathrm{~m} / \mathrm{s}$, and $\mathrm{q}=9.5$ a relatively strong wake presence was noted. The structure of the wake was evident through the high velocity of the droplets at the sides of the spray plume. Fuller et al. (1998) stated that this was most likely due to the shearing action of the cross flow resulting in a high momentum exchange thereby accelerating the droplets in the cross flow direction.

A study by Azzopardi et al. (2003) later contradicted the bag break up findings of Fuller et al. (1998). The authors found that at higher cross flow Weber numbers the bag break-up mode was dominant while at lower Weber numbers column break-up prevailed. A comparison with lower viscosity fluids showed little to
no difference in the break-up modes for each flow regime. The authors stated that this implied that the fluid viscosity did not influence the break-up mode of a liquid jet in cross flow, contrary to the findings of Fuller et al. (1998). However, at liquid viscosities higher than water, the penetration in the transverse and stream direction was influenced by both the viscosity and the momentum flux ratio. At lower liquid viscosities, this trend was not observed.

Madabhushi (2003) used a computational algorithm to analyze a two-phase JICF and validate many of the findings of Fuller et al. (1998) for the presence of a wake. The results were validated by comparison of measurements made by a PDPA system. The cross flow was simulated by using the Reynolds averaged Navier-stokes equations, with pressure correction and a standard, $\mathrm{k}-\varepsilon$ turbulence model. The droplet motion was modeled using a Lagrangian approach. The test conditions consisted of a 0.5 mm injector with water injection velocities of 12.8 to $42.5 \mathrm{~m} / \mathrm{s}$. The cross flow velocities were varied at values of $68.7,103$, and $137 \mathrm{~m} / \mathrm{s}$. These values resulted in momentum flux ratios ranging from 9.5 to 48.8 . All measurements experimentally and computationally were made 300 diameters downstream. The results showed a generally good comparison between the CFD results and the PDPA measurements. Near-wall values of droplet velocity and size from the CFD results were higher than measured values. This was said to be due to the presence of a wake, which was not modeled in the CFD. The study of the SMD showed the presence of smaller sized droplets near the wall, said to be due to the "stripping" of droplets from the jet surface due to the wake. At $q=9.5$, this occurred at a height of $\mathrm{Y} / \mathrm{d}=20$. Stream-wise
velocity contours showed a high velocity region at the outer portion of the jet due to the flow wrapping around the jet body and accelerating the stream-wise flow. These measurements agreed with the findings of Fuller et al. (1997), showing the presence of a wake.

Aalburg et al. (2004) also studied experimentally and computationally a twophase JICF. This study computationally assumed that initially the jet column acted as an upright cylinder. The validity of the assumption remains to be seen; however, the results showed that eddy shedding in the wake of the cylinder was onset at a Reynolds number of 40. Plotting the eddy shedding frequency in a graph of Strouhal number versus the Reynolds number yielded very good agreement between the computational results and experimental results. The JICF experimental results showed that the liquid/gas density ratio had a small effect on the deformation and break up of the jet at density ratios less than 30 and small Oh numbers. The Reynolds number was also found to have a small effect on the deformation of the jet. For Reynolds numbers approaching Stokes flow, the jet deformation was relatively small due to increased drag coefficients. Conversely, the authors stated that this drag could also contribute to increased jet break up.

As an extension of the previous study Aalburg et al. (2004) went on to show, experimentally, that the transition points for the break up of a liquid jet under, bag, multimode, and shear break up were onset at critical Weber numbers of 4, 30, and 110 , respectively. The authors stated that the primary mechanism leading to the break up of a round nonturbulent liquid jet, were classical Raleigh Taylor instabilities
resulting from the acceleration of a fluid of greater density toward a fluid of lesser density. Deformations of the liquid column were also attributed to pressure imbalances due to the accelerated cross flow fluid moving around the body of the jet.

Aalburg et al. (2005) performed a study detailing the properties of surface waves seen in a two phase JICF using computational methods. The study used FLUENT's VOF model with jet diameters ranging from $0.5-2 \mathrm{~mm}$ and momentum ratios of 3-8,000. The primary findings showed that the computational results were in good agreement with experimental measurements of measured disturbance wavelengths and break up locations. Aalburg et al. (2005) also formulated a relationship between the Weber number (We), jet diameter, and disturbance of the wavelength along the upstream side of the jet $\left(\lambda_{\mathrm{s}}\right)$.

$$
\begin{equation*}
\frac{\lambda_{s}}{d}=3.4 \cdot W e^{-.045}, \quad \mathrm{We}>4 \tag{eq4}
\end{equation*}
$$

Where $d$ is the exit diameter of the liquid column, and the Weber number (We) is the ratio of inertial forces to surface tension forces (eq. 3). The research also showed that as the Weber number increased, the wavelength and amplitude decreased, similar to the observations of Less and Schetz (1986).

The wavelengths and frequencies of the disturbances on the upwind side of the jet have been well documented by researchers such as Less and Schetz (1986), and Aalburg et al. (2004 \& 2005). Both research groups showed that as the momentum ratio, q , increased, these wavelengths decreased in size. Aalburg et al.
(2004 \& 2005) formulated a correlation between the wavelengths and the Weber number (eq. 4), while Less and Schetz (1986) used the Strouhal number to relate the frequency of instability to the cross flow velocity and column diameter (eq 1). In order to specify the frequency of the disturbances measured by Aalburg et al. (2004 \&2005), the wavelength velocity must be known. For comparison purposes, the wavelengths of Aalburg et al. were used with the findings that the waves propagate at a velocity equal to that of the jet. Much like the fluid velocity, the wave velocity near the injector should travel very close to the exit velocity of the liquid, and as aerodynamic forces due to the cross flow build, the fluid is accelerated in the downstream direction.

Taking into account these two assumptions, two frequencies of instability were calculated. Comparing these results to the Von Karman frequency of shedding from a solid cylinder, a relationship was formulated between the frequency of instability and the Weber number.


Figure 1.4 Instability frequency as a function of Weber number.

Figure 1.4 shows that the relationship of Less and Schetz (1986) is closely correlated to the vortex-shedding frequency, while the relationship of Aalburg et al. (2004) is closer. The importance of these findings shows that there is some correlation between the instability measured in the jet, and the instability from a pair of shedding vortices off a circular cylinder in cross flow. Much is still not known about the break up mechanisms of a two phase JICF, but many theories were proposed. Less and Schetz (1986) showed that there was a distinct connection between the shedding of vortices from a solid cylinder and the frequency of the waves on the upstream side of the jet. Taking this into consideration they felt that the break
up mechanism was very closely related to any disturbances in the wake. Aalburg et al. (2004) proposed that, similar to secondary droplet break up, the break up mechanism of a two phase JICF was more than likely related to a Rayleigh-Taylor break up mechanism, where the shearing of two differing density fluids generates the surface waves on the upstream side of the jet. The break up mechanism for a two phase JICF is still a matter of much debate as it stands currently.

### 1.3.3 Flow Visualization

The current study will focus mainly on the influence of the wake, for a two phase JICF, on the break up of the liquid column. Previous studies by Fuller et al. (1997) and Madabhushi (2003) have shown the presence of a wake for this arrangement. Outside of the findings of Fric and Roshko (1994) for a single phase JICF, no visualization of any wake structures has been made for a two-phase JICF. The study of these wake structures is important because of their influence on the instability of the JICF as mentioned by Less and Schetz (1986). The complexity in visualizing the wake structures lies in the tracking of the two phases.

Bartelheimer et al. (2000) studied the velocity field of a two-phase flow without any particle seeding at all. For this experiment, the authors used a Bosch automobile spray nozzle to inject water into ambient air. Seeding particles were replaced by NO (Nitric Oxide) gas which was used as a tracer injected through a valve very close to atmospheric pressure preventing any influence in the flow field. Using the same lasers and CCD camera, two images were recorded with a $150 \mu \mathrm{~s}$
delay. The small delay was said to be necessary to prevent any molecular diffusion of the gaseous tracer. With a very small delay time, the tracer accurately followed the flow field. The ICV method was used to post process the signals. An optical filter was used to remove any Mie-scattered images from the water spray. It was noted by the authors that for more dense sprays, the filter should be improved. The authors used signal suppression for LIF signals less than 15\% of the average LIF signal. This suppression helped to reduce the shot noise in the measurements. To validate the results, the second image of each pair was simulated numerically and compared to the actual second image. The results showed a very good comparison with an average error in the velocity of $3.1 \%$. Other validation tests indicated that the accuracy was dependent upon the spatial resolution. Further tests showed that if the spatial resolution was improved then the error in the measurements increased. Smoothing techniques were also shown to have little effect on the accuracy of the measurements. The molecular diffusion error was also studied and showed little significance in the present study. Further errors were said to be due to out of plane motion by the NO tracer.

Bartelheimer et al. (2000) wrote a similar paper where they studied the velocity field measurements in a two phase water aerosol embedded vortex generator. The specific objective was to compare and contrast PIV and gas phase velocimetry (based on LIF). The PIV system for this experiment uses a double pulsed Nd:YAG laser with a CCD camera. The seeded particles were distributed using an aerosol generator and water. For the gas phase velocimetry technique, the flow was seeded
with NO to act as the tracer gas. Two KrF excimer lasers were used with a CCD camera to track the flow. Both measurements system were pulsed at different intervals to eliminate any interference between the two lasers. The delay of each pulsed laser was .1 ms , thereby making each measurement relatively instantaneous. For the PIV system, a common cross-correlation technique was used to resolve the data. For the gas phase velocimetry technique, the Instantaneous Correlation Velocimetry (ICV) method was used. By dividing the interrogation volume into "spots" and using a mapping function, based on the intensity of scattered light, the velocity and direction of each particle was determined. The flow field studied was very two-dimensional, so any movement out of the interrogation field was neglected.

The results showed that some differences did exist in the two methods for instantaneous measurements. Primarily, the use of water droplets for PIV yielded a "lag" in the data due to the inertia of each droplet. This "lag" was prevalent in areas where a steep change in velocity direction occurred. The deviation due to this 'lag" was at most $3.6 \%$. However, the authors determined that the total average error between the liquid and gas phase was $8 \%$ indicating the presence of another error. The authors attributed the other source of error to primarily "shot noise."

Boedec and Simoens (2001) also made velocity field measurements for twophase spray flows. The main focus was on the development of an experimental method for the measurement of both the gas and fluid phase velocities of a highpressure spray. One of the main issues with simultaneous measurement devices is the discrimination between the signals from water droplets in the jet and the signals from
particles in the seeded gas. Post-processing techniques, such as autocorrelation, have been known to cause problems for simultaneous measurement systems such as this. To remedy this, the velocity fields of both phases were processed using a crosscorrelation technique. The experimental setup consisted of a high pressure spray issuing into an open air vessel with four clear windows at $0,90,180$, and 270 degrees. Two Nd:YAG lasers were used to illuminate a fluorescent dye for the liquid phase, and smoke particles for the gas phase. Incense particles were used because they avoid any coalescence with the atomized liquid phase. The images were recorded using two CCD cameras. One camera was fitted with a band-pass filter to read only the water droplets of the liquid phase. The other camera was used to image both Miescattered diffusion, and LIF light (droplets and solid particles). After digital image processing, binary operations, the images were able to discern between both gas and liquid phases. The results showed that liquid-phase comparisons with LDV measurements showed a very good comparison with a global error of 5\% for mean values, and a global RMS error near $30 \%$. The importance of this paper is in the development of the methodology for simultaneous measurement of liquid and gas phase velocities. Cessou et al. (2005) used fluoresceine particles and the proper optical filters to simultaneously measure the velocity field of both the gas and liquid phase of an axial co-flow. Using a Nd-YAG laser at wavelengths of 532, and 355 nm, two CCD cameras fitted with optical filters, each phase was tracked independently of the other. Initially a spectral study was conducted to pair the proper fluoresceine powder with optical filter for each emitted wavelength of light. At 532
nm , the authors chose Rhodamine 610 for the gas phase and LD88 for the liquid phase with the appropriate band pass optical filters. At 355 nm , Stilbene 420 was chosen for the gas phase and Coumarin 450 for the liquid phase. The authors chose to use the 355 nm wavelength because of the larger spectral range, but both wavelengths showed to be accurate. The use of fluoresceine particles for flow tagging and optical filters allowed the authors to probe both phase velocities simultaneously and opens many doors in making measurements in multiphase flows.

### 1.3.4 Objectives

Previous research in two-phase JICF indicates the presence of disturbances on the upstream side of the liquid jet leading to jet break up. The origin of these disturbances remains a point of debate. Some researchers have argued that the instability was a classic case of Rayleigh-Taylor instabilities (Aalburg et al. 2004), while others allude to the influence of shedding vortices in the wake, which contribute to the unsteady nature of the jet (Less and Schetz 1986). It is the aim of this study to shed some light on the validity of these two theories. The specific objectives of this research topic for a two phase JICF are to: i) Develop a methodology to track the gas cross flow and observe how it interacts with the liquid jet ii) Document and measure the characteristics of the instabilities in the jet column iii) Provide new insight on the source of the instabilities and the break up mechanism of a two phase jet in cross flow.

In this chapter, a detailed background was provided along with a structural understanding of a JICF. In chapter 2, a detailed summary of the methods and procedures used to successfully achieve the objectives are stated. In chapter 3, the computational results of the experiment will be covered in full detail with explanation of all findings. In chapter 4 , the experimental results of the experiment will be discussed. In chapter 5, a summary of the entire study will be given with conclusions and recommendations.

## CHAPTER 2

## METHODS AND PROCEDURES

### 2.1 Methods

In this section, a full description of the methods used to fulfill the objectives stated will be given. Detailed schematics of the experimental setup and experimental components will also be included. Due to the complexity of visualizing the wake in a two phase JICF, a detailed explanation of physics behind the method, Particle Image Velocimetry (PIV), will also be included.

### 2.1.1 Experimental Setup

In order to visualize the wake created through the interaction of a water jet issuing perpendicularly to gaseous cross flow, a setup had to be constructed to deliver a high- speed cross flow along with a column of liquid. The primary provider for the cross flow of air was a high-speed open circuit wind tunnel (University of Oklahoma, North Campus). A variable speed controller was used along with the wind tunnel to vary the velocity of the air in the test section. A water flow system was also constructed to deliver the water as the jet issued perpendicular to the cross flow in the test section. A detailed schematic diagram of the open circuit wind tunnel, schematic
of the water delivery setup, along with a picture of the setup are found in figures 2.1, 2.2 , and 2.3 , respectively.


Figure 2.1 Open circuit wind tunnel


Figure 2.2 Water delivery setup


Figure 2.3 Experimental Setup at North Campus

The wind tunnel is a suction type open circuit wind tunnel that is open to the atmosphere at the discharge, with a 5 foot inlet, and 18 " diameter circular clear plexiglass test section that is 45 " long. The inlet of the wind tunnel has a turbulence screen and honeycomb to damp out any inlet turbulence that may be carried to the test section. The liquid injector is placed 4 diameters from the start of the test section, and injects the liquid downward into the cross flow of air. A submersible pump at the bottom of the fluid reservoir pushes the fluid through the flexible tubing, rotameter flow meter, and into the injector. The electric motor, which drives the wind tunnel fan, is attached to a Cuttler-Hammer frequency controller (SVX9000). Using the motor controller and a $1 / 4$ " pitot static probe with a pressure transducer a calibration was completed to relate the frequency output with the measured air velocity in the test
section from the pitot probe (figure 2.4). The pitot probe was placed in the test section at various heights. An average of all the measured velocities at various locations in the test section was taken with an uncertainty in the values of $5 \%$. The estimated thickness of the boundary layer along the wall was no more than 12 jet diameters from the wall. The mean velocity in the test section was used to formulate the calibration curve. Using this calibration, a desired cross flow velocity may be set as a function of the output frequency of the motor controller.


Figure 2.4 Wind Tunnel Calibration of test section velocity ( $\mathrm{m} / \mathrm{s}$ )

The calibration shows a linear trend with a very good correlation coefficient $\left(R^{2} \approx 1\right)$ between the equation and the actual data. This linear calibration equation was
used to set the wind tunnel cross section velocity to vary the momentum value, q , for the remainder of this study.

### 2.1.2 Flow meter

The flow meter used in the setup was an OMEGA 65 mm FLD series direct read rotameter flow meter. The flow meter came standard with a flow adjustable needle and a flow range of $0.2-1.2 \mathrm{lpm}$. The position of the float is linearly proportional to the flow passing around it. The float is read at the center of the ball, with a measured accuracy of $\pm 5 \%$ of full scale with a repeatability of $\pm .25 \%$.

To ensure that the flow readout is entirely accurate, a validation procedure was used to compare the indicated flow reading to the actual flow rate measured. Testing showed that the flow meter had an average of $3.5 \%$ error, when compared to the actual flow rate. The actual flow rate was determined by filling a bucket to a 1 gallon level. The time to fill the bucket was recorded and used to calculate the actual flow rate. This was compared to the indicated flow rate, and plotted against one another. The data showed a linear relationship between the two flow rates, whereby a linear fit was used to determine a calibration equation for future flow rate settings (figure B1, Appendix B). The validation procedure showed a very good agreement between the indicated flow rate and the measured flow rate with an average error of $3.5 \%$, which is well within acceptable range for this study.

### 2.1.3 Submersible Pump

The primary fluid mover of the experiment was a Little GIANT compact submersible centrifugal pump. The pump has a screened inlet to filter out large particles with a $1 / 2$ inch Male NPT outlet. The pump has a flow range of $13.5-.8 \mathrm{gpm}$ at 1 and 24 feet of head, respectively. Since pump is centrifugal, the flow rate is greatly sensitive to the downstream head loss. This meant that accurate flow control can be achieved using a needle style flow control valve, which can greatly increase or reduce downstream head. The submersible pump was fitted to the flow setup taking into account all major and minor losses in the system to assure that proper flow was deliverable.

### 2.1.4 Injector Design

The water jet was designed to provide a steady flow. Standard tap water was used as the injected fluid. The fluid properties were as follows: a density of 998 $\mathrm{kg} / \mathrm{m}^{3}$, a kinematic viscosity of $1.13 \mathrm{E}-6 \mathrm{~m}^{2} / \mathrm{s}$, and a surface tension of $0.07073 \mathrm{~N} / \mathrm{m}$. A Cannon-Fenske Capillary tube viscometer was used to measure the fluid viscosity, while a CAHN flat plate surface tensiometer (Courtesy of OU Chemical Engineering) was used to measure the surface tension. The flat plate tensiometer works by measuring the force on a plate, which is pulled through the surface of the test liquid. With knowledge of the perimeter of the plate, the surface tension is found. The tap water was found to have a $3.5 \%$ difference in surface tension than pure distilled water, which was also measured for comparison purposes.

A 2 mm inner diameter injector made of stainless steel was selected with a 2 " exit length, and made from aluminum. Designing the jet with an exit length of 25 jet diameters, ensures that the flow is fully developed when exiting the nozzle. To limit the presence of vortices in the flow, a gradual reduction with a $45^{\circ}$ taper was designed taking the cavity from a $1 / 4$ " diameter to 2 mm diameter smooth exit. A schematic diagram of the injector is presented in figure 2.5.


Figure 2.5 Water jet injector design.

### 2.1.5 Flow System Hardware

The piping used to deliver the fluid was $3 / 8$ " high pressure flexible rubber tubing. The flexible tubing allowed for minimal head loss, and provided ease of use
without complex tube bending. All the components of the flow system are summarized in Table 2.1

Table 2.1 Flow system components

| Description | Specification | Accuracy |
| :---: | :---: | :---: |
| Flowmeter | OMEGA 65mm <br> FLD Series | $\pm 5 \%$ F.S. |
| Fluid Pump | Little Giant |  |
| $13.5-.8$ gpm | NA |  |
| Fluid Piping | $3 / 8$ " High Pressure |  |
| Flexible Hose | NA |  |
| Handheld Pressure <br> Transducer | OMEGA <br> HHP-90 | $\pm 0.2 \%$ F.S. |

### 2.1.6 Particle Image Velocimetry System

A TSI Powerview ${ }^{\text {TM }}$ Particle Image Velocimetry (PIV) system (Figure 2.6) was used to measure flow velocity. A double-pulsed Nd:YAG laser ( $90 \mathrm{~mJ} / \mathrm{pulse}, 6$ ns pulse time) was used to provide the light source through the test section of the
wind tunnel. The time in between pulses (dT) was varied at values of $6-30 \mu \mathrm{~s}$, depending on the momentum ratio studied. Higher cross flow velocities required a shorter dT due to the movement of the particles within each interrogation volume. The light scattered from the seed particles was captured by a CCD (charge coupled device) camera with a 28 mm lens ( 30 Hz frame rate, $355 \mu \mathrm{~s}$ shutter time, and $2.8 \mathrm{f} \mathrm{\#}$ ). The camera has a pixel resolution of $1200 \times 1600$ pixels, with each pixel being $7.4 \times$ $7.4 \mu \mathrm{~m}$. The laser and CCD camera were controlled using a Laser Pulse ${ }^{\mathrm{TM}}$ Synchronizer. The synchronizer was programmed using an INSIGHT 3G-2TDR software which provided data acquisition, analysis, and display. Processing of the images was achieved by using a Nyquist Grid with a spot size of $32 \times 32$ pixels. The Fast Fourier Transform (FFT) correlator was chosen with a Gaussian Peak engine, and signal to noise ratio (SNR) filter set at SNR filter $>1.2$.


Figure 2.6 TSI Particle Image Velocimetry setup

### 2.1.7 PIV Background

Particle image velocimetry is a non-intrusive technique for flow measurement using a two-dimensional laser light sheet. A laser beam is formed into a 2 mm twodimensional sheet using a combination of cylindrical lenses. The light sheet can be arranged parallel or perpendicular to the direction of flow, with the receiving optics oriented perpendicular to the plane of light.


Figure 2.7 Illustration of a typical PIV arrangement in a wind tunnel (Courtesy of Grant 1997).

One possible arrangement of the PIV set-up in a wind tunnel is illustrated in Figure 2.7. The thickness of the light sheet is dependent on the cylindrical lens characteristics. The flow is "seeded" with small particles, and the particles are tracked as they pass through the light sheet. The tracking is achieved by pulsing the laser a number of times with very short pulses in duration. The scattered light from
the seeded flow is captured using either a digital camera or photo paper. Each photo paper includes both pulses capturing the movement of the particle within the photo paper. The average number of particles found in a cylindrical resolution cell (Figure 2.8 ) is defined as the source density. If the source density $\mathrm{N}_{\mathrm{s}} \gg 1$, then there is a high particle density in the flow and interference from the scattered light will occur. If $\mathrm{N}_{\mathrm{s}} \ll 1$, then the flow has a low particle density and is then referred to as low density PIV.


Figure 2.8 Illustration of the "interrogation" cell for source (a), and image density (b) (Courtesy of Grant 1997).

Figure 2.8 shows the test volume from within the thickness of the incident light sheet. The "interrogation" window is defined as the intersection of the light
sheet with the image window. The image density $\mathrm{N}_{\mathrm{I}}$ is very similar to the source density, but is a measurement of the density of the particles within the "interrogation" window on the photo sheet. In other words, it is a measure of the number of particles within an elemental volume focused on the receiving optics. For $\mathrm{N}_{\mathrm{I}} \ll 1$, the image is said to have low image density. For high image density cells, it becomes difficult to discern complimentary pairs of a particle requiring extensive statistical measures to determine which particles coincide. An example of a high seeding density image is found in Figure 2.9.


Figure 2.9 Double pulsed particle image (courtesy of Dantec Dynamics.com)

While older methods utilize PIV transparency sheets to create Young's fringe patterns, advances in PIV methodology allow for the image to be captured and digitized using a CCD camera (Grant 1997). Using the CCD, and post-processing software, autocorrelation of what is done through digital transformation. The CCD allows for real time data collection that can be monitored for the SNR. The real time
data stream allows for the user to adjust the autocorrelation techniques, spot size, pulse time, as well as the beam intensity to attain a more desirable SNR. Optimizing the signal to noise ratio helps to reduce the number of bad measurements that may arise due to light noise in the image. After the image pair is digitized an autocorrelation technique must be chosen to relate each seed particle captured from one time step image to the next. The user specifies an "interrogation area" which is made up of a group of pixels in the image (figure 2.10). Within each "interrogation area" correlation produces signal peaks relating each individual particle movement from one laser pulse to the next. The correlation process produces three peaks with the two end peaks being located at $\pm \Delta X$, where $\Delta X$ is the displacement of the individual particle from one image to the next. With knowledge of the change in position of the light intensity peak as a function of laser pulse time, the velocity magnitude and direction can be resolved.


Figure 2.10 Schematic of the image capture process (Dantec Dynamics.com).

Currently, the autocorrelation is computed automatically by the PIV software giving the user several autocorrelation options resulting in the same peaks seen in figure 2.10. The end result is a processed set of images with velocity vectors throughout the field of view (FOV). After all images have been processed, several post-processing techniques such as erroneous vector removal, and vector interpolation allow the user to optimize the final image accuracy, also included in the PIV software package. Other post processing techniques may be used to get more information from the vector field such as, velocity biasing, strain rate information, vorticity contours, and various other turbulence quantities (figure 2.11).


Figure 2.11 Vector and vorticity contours from PIV measurements (courtesy of Dantec Dynamics.com)
. The validity of PIV measurements is hinged on the ability of the seeded particles to accurately follow the flow. Some research in the past has been devoted to this subject. Using the particle dynamic equations, taking into account the steadystate drag force, gravitational force, mass effect, fluid acceleration, and the Basset force, Lecuona et al. (2002) modeled particle trajectories in strong vortices. A nondimensional time scale, called the Stokes number, was used to relate the particle response time to the flow response time.

$$
\begin{equation*}
S t=\frac{\omega d_{p}^{2}}{18 v \varepsilon} \tag{eq.5}
\end{equation*}
$$

Where, $\omega$ is the vortex frequency of revolution, $\mathrm{d}_{\mathrm{p}}$ is the particle diameter, $\nu_{\mathrm{c}}$ is the fluid kinematic viscosity, and $\varepsilon$ is the ratio of the density of the fluid to the density of the particle. It is generally accepted that particles with Stokes numbers less than 0.1 will follow the fluid streamlines accurately. For this particular study, the particle diameters were distributed around a mean diameter of $1 \mu \mathrm{~m}$, with fluid and particle density ratios of the order of $10^{-3}$ (corresponding to water seeding). For the Rankine vortex, the tangential velocity at the edge of the vortex was $25 \mathrm{~m} / \mathrm{s}$ with a vortex radius of 0.05 m . Rankine vortices have a solid rotation at the center, where the tangential speed in the vortex is inversely proportional to the distance from the center. Lecuona et al. (2002) showed that with single injection, particles tended to migrate away from vortex centers creating particle-free zones. The lack of high
seeding density in the vortex center was shown to result in velocities, which were in error when comparing PIV results of azimuthal velocities with theory, at various radial coordinates. This is one of the drawbacks of PIV measurements in low particle-density zones. The lack of particles results in low signal to noise ratio, and requires larger spot sizes, which increase the chance for erroneous image pairing throughout the entire flow field.

Khalitov and Longmire (2003) studied the response of glass beads in a fullydeveloped turbulent channel flow of air. Five different particle sizes were used with Stokes numbers ranging from $0.2-10$, based on the integral time scales. To calculate these Stokes numbers, the authors used the channel half width (h) and the gas streamwise fluctuation ( $u^{\prime}$ ) in the calculation of the dissipation $\left[\left(u^{\prime}\right)^{3} / \mathrm{h}\right]$ and integral fluid time scale ( $\mathrm{h} / \mathrm{u}$ '). The authors were interested in determining the ability of these monodisperse spheres to track the flow using slip velocities, single point, and two point correlations. Each measurement was compared to "true gas" measurements made using $1 \mu \mathrm{~m}$ size fog particles (glycerin droplets). The results showed that larger particles (St > 1.4) lagged behind the gas flow at the centerline, and moved faster at the walls. The researchers also showed that smaller particles tend to congregate in low speed streaks. Drift velocities in the center plane where shown to be small for all the range of particles tested. Both two point and single point correlations were shown to decrease with increasing particle size (increasing Stokes number). Stokes numbers less than 1 showed very good correlations to the gas flow in turbulent channel flow.

Using the definition of the Stokes number, the findings of Lecuona et al. (2002), and Khalitov and Longmire (2003), it is assumed that particles with Stokes numbers less than 1 will accurately follow the flow. Based on values from Ferziger et al. (1999), Kelso et Al. (1996), the Stokes numbers were computed to range from 0.004-0.4 for olive oil drops with a mean diameter of $1 \mu \mathrm{~m}$. Particles of similar diameter, with less density would follow the streamlines with minimum deviation. Therefore, particles of nominal diameter of $1 \mu \mathrm{~m}$ were chosen as seed particles in this study.

### 2.1.8 Two Phase JICF Methodology

The primary objective of this research is to track the cross flow and its interaction with the liquid jet. Researchers have surmised that the body of the jet acts much like a cylinder in a cross flow due to marked density difference between the cross flow and the jet fluid. For high $q>6$, researchers have shown that a straight column of liquid is present for some distance, before droplets are stripped off the body of the jet by the cross flow. Also, the Reynolds number for the flow around a cylinder may be calculated using the diameter of the jet, similar to single phase JICF. For the flow around a cylinder, unsteady vortex shedding is onset at Reynolds numbers greater than 40. Both of these factors are influenced by the jet exit velocity and cross flow velocity. Using both of these parameters, the jet diameter and velocity are set at fixed values, while the cross flow velocity is variable.

Taking into account the momentum ratio, q , a jet diameter of 2 mm was used with a jet exit velocity of $3.25 \mathrm{~m} / \mathrm{s}$. Using the jet diameter, the Reynolds number for the flow around the jet was calculated and the cross flow velocity was varied. The various test parameters used in this two-phase JICF study are summarized in Table 2.

Table 2. 2 Select Experimental parameters for two phase JICF

| $\mathbf{U}_{\infty}$ <br> $(\mathbf{m} / \mathbf{s})$ | $\mathbf{U}_{\mathbf{j}}$ <br> $(\mathbf{m} / \mathbf{s})$ | $\mathbf{R e}_{\infty}$ | $\mathbf{R e}_{\mathbf{j}}$ | $\mathbf{q}$ <br> $(\mathbf{m o m e n t u m}$ <br> ratio) | Weber <br> $\mathbf{N u m b e r}$ | $\mathbf{R e}_{\text {cyl }}$ | Stokes <br> $\mathbf{N u m b e r}$ <br> $(\mathbf{S t})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7.28 | 3.25 | 2.03 E 5 | 5,752 | 172.80 | 1.72 | 890 | 0.004 |
| 11.50 | 3.25 | 3.21 E 5 | 5,752 | 69.25 | 4.30 | 1,405 | 0.006 |
| 15 | 3.25 | 4.19 E 5 | 5,752 | 40.70 | 7.32 | 1,833 | 0.008 |
| 22.07 | 3.25 | 6.17 E 5 | 5,752 | 18.80 | 15.85 | 2,700 | 0.231 |
| 30 | 3.25 | 8.38 E 5 | 5,752 | 10.18 | 29.29 | 3,667 | 0.481 |

For each case, the jet velocity was held constant while the cross flow velocity is varied. The momentum ratio (q) was set at values greater than 6 to ensure that a proper column of liquid was present before any instabilities were formed, or break up in the jet body began. At each cross flow velocity, the Reynolds number based on the
diameter of the test section $\left(\operatorname{Re}_{\infty}\right)$ is given along with the Reynolds number for the jet based on the jet diameter $\left(\mathrm{Re}_{\mathrm{j}}\right)$. Additionally, for each case, the Reynolds number based on the jet diameter $\left(\mathrm{Re}_{\mathrm{cyl}}\right)$ was greater than 40 , leading to the onset of vortex shedding in the wake of the jet. The Stokes number was calculated using the findings of Lecuona et al. (2002), and Khalitov and Longmire (2003). At every cross flow velocity, the Stokes number was less than 1, leading to proper flow tracking within the wake vortices using the $1 \mu \mathrm{~m}$ sized olive oil droplets. The olive oil seeding will be only used to validate the wind tunnel calibration that will follow. Due to oversaturation of the CCD camera from the large droplets of water, the Mie scattered image had to be filtered out to prevent from damaging the camera. Using the findings of Cessou et al. (2005), laser fluoresceine tagging was used to track the gas phase in this setup. Cessou et al. (2005) successfully showed that at 532 nm , Rhodamine 610 could be used to track the gas flow in a multiphase flow such as this.

For this study, Rhoadime 610 perchlorate was initially chosen. Rhodamine 610 percholorate is a mildly toxic fluoresceine powder, which when illuminated by an Nd-YAG laser, is excited to wavelengths ranging from $570-620 \mathrm{~nm}$. The powder is only dissolvable in either methanol or ethanol. When dissolved in ethanol at a molar concentration of $4.2 \mathrm{E}-4$, and excited by a laser of 532 nm , Rhodamine 610 fluoresces to a maximum wavelength of 596 nm (exciton.com). Ethanol was initially chosen for this case because of its ease of purchase and safety. However, due to the low vapor pressure of ethanol and methanol, both fluids could not be used in the high-speed cross flow, such as the one used in this study.

Kiton Red 620 is a powder, similar to Rhodamine 610, but is completely soluble in water. When excited by a 532 nm laser, Kiton Red 620 fluoresces in the range of 570-604 nm. To help raise the vapor pressure, 50 ml of Ethylene Glycol was added to the water to further prevent any evaporation that might occur before reaching the illumination region of the wind tunnel.

Since only the fluoresced light is of particular interest, all incoming green laser light into the camera must be filtered out. An OMEGA optical filter, which attenuated all wavelengths below 550 nm and passed all wavelengths above 550 nm , was used (Figure 2.12). The mixture of water and Kiton Red 620 was atomized in a TSI Model 9306 aerosol generator, which produced drops of less than $1 \mu \mathrm{~m}$ in diameter. The drops were injected through a 1 " hose 4 ' upstream of the liquid jet, to avoid any disturbances due to injection of the seeding. With this setup, the Mie scattered light from the body of the jet was filtered out and the fluoresced light from the seeding in the gas phase was tracked. Not only was the CCD camera safe from over saturation, but a clear distinction could now be made between the signals from the atomized particles and the signals from the jet and tracer particles in the gas flow, thereby reducing any errors that might arise due to interference between the signals from the two phases.


Figure 2.12 Transmission spectra for optical filter
(courtesy of TSI.com)

## CHAPTER 3 COMPUTATIONAL RESULTS

### 3.1 Computational Results

FLUENT's Volume Of Fluid (VOF) solver was used to model a two phase time dependent 2-d JICF. The VOF solver uses standard continuity and momentum equations to model the motion of the two phases as they move through the domain.

$$
\begin{equation*}
\frac{\partial}{\partial t} \rho u_{j}+\frac{\partial}{\partial x_{i}} \rho u_{i} u_{j}=-\frac{\partial P}{\partial x_{j}}+\frac{\partial}{\partial x_{i}} \mu\left(\frac{\partial u_{i}}{\partial x_{j}}+\frac{\partial u_{j}}{\partial x_{i}}\right)+\rho g_{j}+F_{j} \tag{eq.6}
\end{equation*}
$$

The complexity arises when the two fluid phases come into contact. This is where the VOF solver is unique. Properties such as the density ( $\rho$ ), and viscosity ( $\mu$ ) must be known apriori before the momentum equations can be solved. Each cell is assigned a volume fraction value $(\alpha)$ for the magnitude of the phase which is present within each cell. The interface tracking between the two phases is accomplished by solving a continuity equation for each phase.

$$
\begin{equation*}
\frac{\partial \alpha}{\partial t}+u_{i} \frac{\partial \alpha}{\partial x_{i}}=0 \tag{eq.7}
\end{equation*}
$$

The volume fraction value within each cell is used to calculate the density ( $\rho$ ), and viscosity ( $\mu$ ) of the fluid mixture within that cell. With knowledge of the fluid properties in a cell, the momentum equations may be solved.

$$
\begin{align*}
& \rho=\alpha_{2} \rho_{2}+\left(1-\alpha_{2}\right) \rho_{1}  \tag{eq.8}\\
& \mu=\alpha_{2} \mu_{2}+\left(1-\alpha_{2}\right) \mu_{1} \tag{eq.9}
\end{align*}
$$

Further complexity arises when reconstructing the shape of the interface between the two fluids. To achieve this FLUENT gives the user a couple options. For this particular study the geometric reconstruction scheme was used, due to its simplicity. The geometric reconstruction scheme utilizes a piecewise linear interpolation of the boundary within each cell. Using the volume fraction and the volume fraction derivatives within a cell, the scheme determines the position of the linear interface relative to the center of each partially filled cell. Next the solver calculated the amount of advecting fluid through each face using the linear interface representation and information of the normal and tangential velocities on the face. Finally the volume fraction in each cell is calculated through the balance of fluxes calculated in the previous step. For this type of boundary reconstruction scheme, a time dependent solution had to be chosen.

To validate the findings, results from a two phase time dependent liquid free jet simulation were compared to published theory. Initially, however, a flow domain was constructed using GAMBIT for both the free jet and 2-d JICF simulations. For the free jet an axisymetric domain was constructed with the jet inlet at the left of the domain, and outflow conditions at the outer boundaries (figure 3.1). The outflow condition was shown to give more accurate results which converged to a final solution. For the 2-d JICF the left boundary was a specified velocity, with the top and
far right boundaries being an outflow boundary condition. The bottom boundary was specified as a wall.


Axis of Revolution

Figure 3.1. Computational domain for free jet


Figure 3.2. Computational domain for 2-d JICF

The meshing scheme using was a standard square mesh with smaller grids near the jet exit and immediately downstream of the exit. The free jet domain was shown to be grid independent, and time independent by showing that the initial break
up location for each case was independent of time step and grid size. The solution showed grid independence with 57,000 cells.


Figure 3.3. Break up locations of a free jet for various grid sizes.

For the 2-d JICF the domain was shown to be grid independent by comparing the equivalent diameter for each case. The equivalent diameter is specified as a ratio between the droplet mean diameter, and jet diameter. The results became grid independent with 56,800 cells.


Figure 3.4. Convergence of equivalent diameter with grid size for a 2-d JICF.

To validate the results from the VOF solver, the results of the free jet were compared to theoretical results from a Rayleigh instability analysis and compared with the droplet diameter from the VOF solution. The droplet sizes were determined by measuring the size of the first droplet to break off the liquid column. Lord Rayleigh found that the largest disturbance wavelength that leads to break up was $\lambda=9.016 a$, where $\lambda$ is the wavelength of disturbance, and (a) is the radius of the jet. If we assume that the entire volume of fluid of a single drop consists of the entire volume of one wavelength of instability then we can equate the two and solve for the droplet diameter.

Equation the two volumes, $\frac{\pi d^{3}}{6}=\pi a^{2} \lambda$, and solving for $\frac{d}{2 a}$, we find that the initial droplet diameter normalized by the jet diameter is 1.89 . Comparing the solution from FLUENT's VOF solver of 1.42 , it is found that the numerical simulation is $25 \%$ different than the theoretical solution of Lord Rayleigh. Thus, the following results are purely qualitative and only show general trends resulting from variations in the momentum ratio q .

Initially, a q value of 20 was used, where the cross stream velocity is $U_{\infty}=1$ and the jet velocity is $\mathrm{U}_{\mathrm{j}}=0.5$.


Figure 3.5. Volume of fluid solution for $\mathrm{q}=20$.

Figure 3.5 shows the jet exiting from its outlet, and reacting with the cross flow. The red color indicates that the cell has a liquid volume ratio of 1 , and the dark blue indicates a liquid volume ratio of 0 . The plot shows that the jet is bent by the momentum of the cross flow and the shear forces break up the column of liquid. The break up location of the jet was found by analyzing the point at which the liquid column breaks up into individual droplets. This break up location was shown to be dependent on the momentum ratio q , as indicated by table 3.1.

Table 3.1 Break up locations with varying momentum ratios.

|  | $\mathrm{q}=20$ <br> $\left(\mathrm{U}_{\infty}=1, \mathrm{U}_{\mathrm{j}}=.5\right)$ | $\mathrm{q}=81.3$ <br> $\left(\mathrm{U}_{\infty}=.5, \mathrm{U}_{\mathrm{j}}=.5\right)$ | $\mathrm{q}=3252$ <br> $\left(\mathrm{U}_{\infty}=.5, \mathrm{U}_{\mathrm{j}}=1\right)$ |
| :---: | :---: | :---: | :---: |
| Break up <br> location <br> (X/d) From jet | 2.86 | 2 | 6.48 |
| Break up <br> Height <br> (Y/d) | 12.28 | 14 | 34.33 |

Table 3.1 shows that as the momentum ratios are increased, the break up location moves further in the x direction as well as the y direction. Simply put, the greater the momentum of the cross flow, the further the jet bends in the direction of the cross flow. Also, as the momentum ratio increases, the jet momentum increases pushing the jet further in the $y$-direction before shear forces from the cross flow break up the jet into individual droplets. When comparing the y break up location with the
finding of Fuller et al. (1997), moderate agreement is seen. Fuller et al. (1997) showed a break up location of $\mathrm{Y} / \mathrm{d}=10.4$, at $\mathrm{q}=20$. The VOF solution gives a value of $\mathrm{Y} / \mathrm{d}=12.28$. Any agreement that may be seen at lower momentum ratios becomes very poor at higher momentum ratios. For example, at $\mathrm{q}=81.3$, the VOF solution gives a Y/d break up location of 14, while the findings of Fuller et al. (1997) showed a break up location of $\mathrm{Y} / \mathrm{d}=31$ at the same momentum ratio. Due to the purely qualitative nature of this study, these differences are acceptable, but show some promise for the future of the VOF solver for two phase jet break up study.

At a q value of 81.3 the jet shows the least amount of bend in the direction of the cross flow (figure 3.6).


Figure 3.6. Volume of fluid solution for $\mathrm{q}=81.3$

These initial computational results show qualitatively the general trends in the interaction between the cross flow momentum and jet momentum. These results will hopefully closely mirror the results of the experimental findings, on a qualitative level. In the future, comparisons will be made between the computational model, and the experimental findings.

## CHAPTER 4

## EXPERIMENTAL RESULTS

### 4.1 Experimental Results

### 4.1.1 Liquid Jet Analysis

To ensure that the break up of the liquid jet is entirely due to the aerodynamic forces introduced, the stability of the jet without a cross flow was studied. In figure 2.5 , a schematic of the injector design can be found. The injector was designed in such a way to limit the amount of turbulence due to the change in cross section from a 6 mm exit to a 2 mm exit diameter.


Figure 4.1 Images of 2 mm water jet exit

Figure 4.1 shows a smooth column boundary of liquid with little to no instability in the boundary due to exit turbulence from the injector. The importance of this observation is to emphasize that any instabilities that might be found in subsequent cases is entirely due to the interaction between the liquid jet and the cross flow. The design of the injector is adequate in producing an un-disturbed water jet for this study.

### 4.1.2 Stability Analysis

The break up of a liquid jet in cross flow is greatly influenced by disturbances that grow along the upstream side of the jet. As Aalburg et al. (2004) illustrated, there are distinct disturbances of measurable wavelength, which can be found on the upstream side of the jet. These disturbances grow in amplitude and eventually lead to the break up of the liquid column. After the initial break up of the liquid column, large ligaments of fluid are separated and undergo a secondary aerodynamic break up mechanism breaking the ligaments up into smaller droplets (figure 4.2).


Figure 4.2 Illustration of the break up process of a two phase JICF (courtesy of Fuller et al. 1997)

There are four main classifications of the break up of a liquid jet, enhanced capillary break up, bag break up, multimode break up, and shear break up, at various critical Weber numbers. Capillary break up has characteristics similar to the break up of a free jet in still air, where disturbances form along the jet column leading to droplet separation. Bag break up is described by its presence of large ligaments, or "bags" of fluid separated from the break up point at the end of the jet. This type of break up generally has the highest amplitude disturbances before ligament separation. Shear break up is characterized by extreme jet bending, with little to no ligament formation. In shear break up, droplets are sheared off the sides of the jet as well as the rear of the jet (surface break up). Multimode break up is a combination of both bag break up and shear break up. In this regime, large ligaments of fluid are found as well as small droplets, in the wake of the jet. Fuller et al. (1997) were one of the first researchers to propose a distinct break up regime for the two-phase JICF at various
critical Weber numbers of 14,35 , and 80 , for the onset of bag break, multimode break up, and shear break up, respectively.

Taking into account the critical Weber numbers of Fuller et al. (1997) and Aalburg et al. (2004), a study on the break up of the two-phase JICF at relatively low Weber numbers was conducted. Images of the jet break up can be found in figures 4.3 and 4.4 , with a $255 \mu$ s exposure time.


Figure 4.3 Visualization of the break up process of a water jet in cross flow: a) $q=$ $172, \mathrm{We}=1.72$, Column break up; b) $\mathrm{q}=69.25, \mathrm{We}=4.3$, Column break up; c) q $=40.7$, $\mathrm{We}=7.32$, Bag break up; d) $\mathrm{q}=18.8, \mathrm{We}=15.85$, Multimode break up.


Figure 4.4 Break up process for $\mathrm{q}=10, \mathrm{We}=29.29$, Multimode break up.

In figures 4.3 and 4.4, a montage of the break up processes for the various momentum ratios is found. The transition from a bag break up with large ligaments, to multimode break up with some ligaments and some droplet shearing is seen. Figure 4.3(c) shows a bag like break up mechanisms, while figure 4.3(d) shows the transition to a multimode break up. Figure 4.3(d) shows the onset of multi-mode break up at a Weber numbers of 15.85 . The onset of multimode break up according to Aalburg et al. (2004) does not occur until a critical Weber number of 30. However, this picture shows multimode break up at critical Weber number below 30.

At every momentum ratio, disturbances can be found on the upstream side of the jet in the X-Z plane. Most notable are the disturbances seen in figure 4.3 (c) and
(d). These disturbances grow in magnitude and lead to the fracturing of the liquid at the trough of the disturbance wave. Figure 4.4, shows very distinct disturbance waves on the upstream side of the jet. This type of multimode break up shows "bags" or liquid break off with small sheared droplets as well. The break up process appears to be much more violent in nature. The frequencies of these waves were measured similar the methods of Aalburg et al. (2004). Using a magnification scale, the distance between the centers of each "node" of the wavelength was measured as a function of the Weber number (figure 4.5), using a dial gage caliper. Due to the penetration of the low Weber number jets out of the FOV of the CCD camera, the disturbance characteristics in the jets corresponding to the Weber number range of 10-40 could only be measured.


Figure 4.5 Disturbance wavelengths as a function of Weber number.

For each Weber number, 100 images were collected using the PIV CCD camera, where, on average, only $20 \%$ of the images had clear measurable wavelengths. Each reported wavelength has an estimated uncertainty of only $10 \%$ ( $95 \%$ confidence), with most of the uncertainty as a result of the deviation in measured values. The measured wavelengths decreased as the Weber number increased. This is a well-known trend for liquid jets injected into subsonic cross flows. The measured wavelengths were compared with the experimental curve fit of Aalburg et al. (2004). Good agreement is seen between the two results with a maximum deviation of about $25 \%$. This result is reasonable considering that the published uncertainties of Aalburg et al. (2004) were on the order of $\pm 25 \%$.

Along with the disturbance wavelengths, the break up locations were documented and compared with previous results (Fuller et al. 1997, Aalburg et al. 2004). For this study, the vertical break up location (penetration into the stream), $\mathrm{Z}_{\mathrm{b}}$, as well as the streamwise break up location, $\mathrm{X}_{\mathbf{b}}$, was measured using similar methods as the disturbance measurements (figure 4.6 and 4.7). Specifically, the streamwise break up location was defined as the distance from the center of the injector to the middle of the first disconnect in the liquid column. The break up height was measured as the distance from the wall to the middle of the first disconnect in the liquid column.


Figure 4.6 Non-dimensional break up location, $\mathrm{Z}_{\mathrm{b}}$, as a function of Weber number.


Figure 4.7 Non-dimensional break up location, $X_{b}$, as a function of Weber number.

Figures 4.6 and 4.7 show the non-dimensional break up locations for each Weber number tested. Each figure is plotted along with the published experimental curve fits of Fuller et al. (1997) and Aalburg et al. (2004). All primary break up locations are reported with a maximum of $10 \%$ uncertainty, and show excellent agreement with published results. The penetration of the jet decreased as the Weber number was increased. An increase in the Weber number implies an increase in the cross flow velocity, and therefore, an increase in the drag exerted on the jet. The increased drag on the jet results in a significant bending in the cross flow direction, and a decreased penetration. The streamwise break up location is shown to be independent of the Weber number and constant at a value of about 7.9 jet diameters for the present range of momentum ratios. The reasoning for this was first proposed by Fuller et al. (1997) who stated that the aerodynamic force, which accelerates the liquid, also reduces the time required for the column to break up affectively canceling both factors yielding a constant downstream break up location.

Using the same methodology as before, the trajectory of the jet was measured using a magnification scale at various downstream locations. Following a similar derivation first proposed by Fuller et al. (1997), the trajectory equation can be rearranged to solve for the drag coefficient $\left(\mathrm{C}_{\mathrm{d}}\right)$ on the jet at various momentum flux ratios.

$$
\begin{equation*}
\frac{x}{d}=\frac{C_{d}}{\pi}\left(\frac{\rho_{\infty} U_{\infty}^{2}}{\rho_{j} U_{j}^{2}}\right)\left(\frac{z^{2}}{d^{2}}\right) \tag{eq.10}
\end{equation*}
$$

Rearranging this equation to solve for $\mathrm{C}_{\mathrm{d}}$, it was found that the drag coefficient on the jet was $1.6,2.22$, and 2.05 , at momentum flux ratios of $40,18.8$, and 10 , respectively. Comparing the drag coefficient for a liquid jet with the drag coefficient on a solid cylinder, within the range of $\mathrm{Re}_{\text {cyl }}$ tested, similarities are seen. The drag on a solid cylinder in this Reynolds number range is constant at a value of 1.2 , whereas the current findings show drag coefficients of very comparable magnitudes. For this reason, a liquid jet in cross flow can be assumed to act similar to a solid cylinder in cross flow in the near field.

While disturbances are in fact present in the X-Z plane, disturbances are also seen in the X-Y plane of the jet for the three lowest momentum ratios. The threedimensional nature of the instability has been commented on by Aalburg et al. (2004), and various other researchers.


Figure 4.8 View of disturbances in the body of the jet in the $x-y$ plane at: a) $q=$ 40.7, $\mathrm{We}=7.32$, multimode break up; b) $\mathrm{q}=18.8$, $\mathrm{We}=15.85$, shear break up; c) $\mathrm{q}=10, \quad \mathrm{We}=29.29$, shear break up.

From Figure 4.8, it is observed that the disturbances seen in the $\mathrm{X}-\mathrm{Z}$ plane are also present in the $\mathrm{X}-\mathrm{Y}$ plane. The higher momentum ratio images could not be analyzed in this plane due to the minimal bending of the jet in the downstream direction. The three-dimensional nature of the disturbance may shed some light on the influence of the wake on the break up of the liquid column. Aalburg et al. (2004) attributed the disturbance in the x-z plane to Rayleigh Taylor instabilities, which arise due to the shearing of a less dense fluid against a more dense fluid. This shearing occurs along the body of the jet, while in the X-Z plane the shearing occurs on the undisturbed portion of the spray very near the exit point of the jet. This column of
liquid may act like a cylinder in cross flow resulting in the shedding of vortices downstream of the jet. The periodic shedding of vortices would result in a pressure distribution along the circumference of the jet, which might lead to the formation of disturbances seen in figure 4.5. As the location of the flow separation changes, the resulting force direction would change, thus resulting in a change in the jet break up location.


Figure 4.9 Transient nature of the break off point for $\mathrm{q}=40.7$

Figure 4.9 shows the change in the location of the break off point for $q=40.7$, from the top of the jet surface. Throughout the course of the break up process, the jet appears to "wave" in a sinusoidal nature along the $y$-axis. As discussed, this transient nature in the $\mathrm{X}-\mathrm{Y}$ plane may be attributed to a transient variation in the pressure distribution along the circumference of the jet.

In this section, the break-up characteristics have been described quantitatively and qualitatively. Taking into account all of the results from this study, and the published results of Fuller et al. (1997 \& 1998), and Aalburg et al. (2004 \& 2005), a spray characteristic matrix has been created. The matrix contains the ranges of the Weber numbers and momentum ratios from this study. The spray matrix is designed to allow a designer the ability to know what sort of spray break up could be expected with known non-dimensional Weber number and momentum ratio, at $\mathrm{Oh}<0.1$ (Appendix A table A23).

### 4.1.3 Spray Characteristics

The structure of the jet as it is atomized by the high speed cross flow is inherently three-dimensional, as figures 4.4 and 4.8 show. By placing the high-speed camera under the jet, a more detailed view of the jet break up process is revealed. Due to the increased penetration of the jet in the Z direction for high momentum values, images could only be taken for $\mathrm{q}=10,18.8$, and 40.7.


Figure 4.10 View of the jet spray for $\mathrm{q}=10, \mathrm{We}=29.29$.


Figure 4.11 View of the jet spray for $\mathrm{q}=18.8$, $\mathrm{We}=15.85$.


Figure 4.12 View of the jet spray for $\mathrm{q}=40.7, \mathrm{We}=7.32$.
Comparing all three images shows that the break up process seen in figure 4.12 is completely different from those seen in figures 4.10 and 4.11 . For $q=40.7$, large "ligaments" of liquid break off the jet and "explode" outward spreading in a linear fashion. The ligaments are stretched in the direction of the cross flow. This was first observed by Fuller etl al. (1997). For $q=10$, and 18.8, the images show the liquid being "sheared" off the sides of the jet spreading the droplets outward in a linear fashion as well. The width of the spray for $\mathrm{q}=18.8$, seems to be wider with a less dense spray core, when compared to $\mathrm{q}=10$.

To further understand how the jet spreads at various downstream locations, measurements were made of the spray core for $\mathrm{q}=10$, and 18.8. A scaled image was used to determine the magnification of the image which was in turn used to determine the actual sizes in 20 consecutive images. The measurement averages were used with a maximum standard deviation of only $6 \%$ of the averages.


Figure 4.13 Non-dimensional spray width at various downstream locations.

Figure 4.13 shows that for both momentum fluxes, the width of the jet was comparable at 5 diameters downstream of the center of the jet. This result is in agreement with those of Fuller et al. (1997) and Aalburg et al. (2004) who found that
independent of the momentum ratio and Weber number, the downstream break up location was constant at 8 diameters downstream of the jet. At downstream locations of 12 and 17.5 diameters, the width of the spray seems to grow linearly, however it is dependent on the momentum flux value. For the higher momentum flux, the spray becomes wider than that for the lower momentum flux. This is confirmed when looking at figures 4.10 and 4.11. However, for both cases it seems that the jet is "flattened" out by the cross flow, causing the jet to spread linearly in the Y-direction. It would make sense then that at higher cross flow values (lower q), the jet would spread more in the transverse direction. Figure 4.13, however, shows the opposite trend.

The discrepancy is due to the method of measurement. The purely qualitative nature of simply measuring the spray core is the cause of this error. In reality, the spray extends much further outward into the dark regions of the images used for this analysis. The size of the droplets does not allow for a large amount of light to be reflected from these drops preventing them from showing up on the images. At the lower momentum flux, more droplets are being sheared from the sides of the jet, at smaller Sauter Mean Diameters (SMD), which would give the impression that the spray width is in fact smaller than the width found in the higher momentum ratio image.

The findings of Madabhushi (2003), both experimentally and computationally, showed that the droplets along the width of the spray extended nearly 60 diameters in each direction. The findings, however, did show that a well-defined spray core did
exist within 10 diameters in each direction. The light is reflected readily from this region, thus allowing it to show up in the images used for this analysis. For this reason, the measurements made are purely qualitative, and should only help define the various trends seen in the interaction between the cross flow and the jet.

Using the trends seen in the results, a fairly good approximation of the bending process of the jet may be determined. Inspection of figures 4.10, and 4.11, shows the cross flow momentum "flattening" the upstream side of the jet causing it to expand outward in the $y$-direction.


Figure 4.14 Display of change in the cross section of the jet at various downstream locations.

As previous researchers have shown, the drag on the jet is very similar to that of a solid cylinder of equivalent diameter. This drag bends the jet in the downstream direction causing the cross section of the jet to change from a circle to an ellipsoidal
shape, before the break off point. Coupled with the lower pressure along the sides of the jet the "stretching" in the transverse direction becomes more pronounced. Whether or not this "stretching" process is steady or unsteady is yet to be determined, however, any unsteadiness may significantly contribute to the surface waves seen in figure 4.4.

### 4.1.4 PIV Cross Sectional Velocity Map



Figure 4.15 Wind tunnel velocity validation using PIV.

Figure 4.15 shows that the PIV data from the mean field in the cross section very closely resembles the data given from the previous calibration in figure 2.4. The maximum difference between calibration and measured data using the PIV is only $5 \%$. The validation not only shows that the calibration used is accurate, but it also indicates that the methodology used for the PIV is correct as well. In addition to validating the cross sectional velocities, the PIV mapped the velocity profile across the cross diameter of the test section (figure 4.16).


Figure 4.16 Wind tunnel velocity in the cross section of the wind tunnel using PIV.

Figure 4.16 shows a very even velocity profile along the centerline of the wind tunnel. At higher wind tunnel frequency (cross sectional velocity) the profile
becomes somewhat erratic, but well within acceptable limits for this study. This result is important in showing that any disturbance in the jet is primarily due to the interaction of the two fluid streams.

### 4.1.5 Axial PIV Results for JICF

Using the mixture of laser fluorescent powder and water for cross flow tagging, the interaction between the gaseous high speed cross flow and water jet can be investigated further. It was shown in section 4.1.4 that the cross flow of air was uniform and somewhat stable, with the proper output velocity as a function of indicated velocity. The initial test plane for the PIV system was aligned with the axial plane of the water jet (Figure 4.17).


Figure 4.17 PIV measurement plane for all axial locations.

Measurements in the $\mathrm{X}-\mathrm{Z}$ plane were made at various spanwise locations ranging from $\mathrm{Y} / \mathrm{d}=0,2$, and 4 . All images were collected using the methodology explained previously, and post processed with no interpolation. By not performing any interpolation of the data, no false information is shown. However, there appears to be holes in the velocity field due to the highly three-dimensional nature of the flow field. Due to the dissipation of flow seeding, at least 100 successive images were needed to get an average flow field.

Instantaneous resulting images were lacking in data density. Each set of successive 100 images was repeated under the exact some conditions to get a sense of the variance in the velocity field from image set to image set. The variance was found to range from $4 \%-6 \%$ throughout the entire flow field. This is more than appropriate for this study, and from this point forward each average velocity field is assumed to be "fully imaged" with no significant variation occurring with the inclusion of more image sets.

For the first momentum ratio of $\mathrm{q}=172$, the jet has a very little bend due to the low speed cross flow (figure 4.3a). The imaging plane is in the $\mathrm{X}-\mathrm{Z}$ plane at a spanwise location of $\mathrm{Y} / \mathrm{d}=0$. With very little dissipation of the seeding particles, a full velocity field was obtained showing the low speed cross flow moving around the body of the liquid jet issuing downward. All vector fields for each momentum ratio have the same color scaling to show any variations in velocity magnitude.


Figure 4.18 PIV vector field for $\mathrm{q}=172$ at $\mathrm{Y} / \mathrm{d}=0$.

Figure 4.18 shows a vector field with a high density of seeding particles near the central region of the image. The vectors at the interaction point between the jet and the cross flow show a very straight directionality with no seeding particles showing up in the body of the water jet. At the rear boundary of the jet there appears to be a slight acceleration of the cross flow with a high velocity magnitude with is then decelerated to the initial cross flow velocity. It appears that the cross flow is in fact moving around the body of the jet and being slightly accelerated by the jet boundary, as shown in figure 4.14.

To further validate this assumption, measurements were taken at spanwise locations of $\mathrm{Y} / \mathrm{d}=2$, and 4 .


Figure 4.19 PIV vector field for $\mathrm{q}=172$ at $\mathrm{Y} / \mathrm{d}=2$.

Figure 4.19 shows that the vectors are very straight along the upstream boundary of the jet, with some cross flow velocity vectors in the jet body. Due to the averaging of the velocity field, some of the vectors within the boundaries of the jet are shown to be a combination of the cross flow velocity in the X direction and the jet velocity in the $Z$ direction. In fact, instantaneous images show that these vectors are along the direction of the cross flow.


Figure 4.20 PIV vector field for $\mathrm{q}=172$ at $\mathrm{Y} / \mathrm{d}=4$.

Figure 4.20 shows a much better vector map at a larger spanwise location of 4 diameters from the center of the jet. Almost all information on the water jet is lost by the cross flow wrapping around the boundary of the jet. At 4 diameters from the jet boundary the seeding particles have moved around the column, and show up as velocity vectors equal in magnitude to the cross flow velocity. No appreciable acceleration is noticed in the vector field, however, it very well could be contained somewhere between the spanwise locations of 2 and 4 diameters. The complexity arises when analyzing the flow data in the exact boundary between the two flow regimes. Data is either lost, not present, or the actual droplets used for seeding coalesce with the water jet. The best indication of any acceleration may be seen in the $\mathrm{X}-\mathrm{Y}$ plane, which will be shown later on.

For the second momentum ratio of 69.25 , similar PIV velocity fields were obtained. The results show the jet bending more in the downstream direction.


Figure 4.21 PIV vector field for $\mathrm{q}=69$ at $\mathrm{Y} / \mathrm{d}=0$.

For this momentum ratio, the jet shows further bending with the cross flow moving around the body of the jet. At the downstream boundary of the jet, along the upper boundary, there appears to be a distinct lack of cross flow vectors. This region shows lost information not only along the boundary, but also at several downstream locations. The source of this error could be from the cross flow moving in and out of the laser light sheet, causing the information to be lost or removed as erroneous data. This observation further supports the idea that the cross flow is in fact moving around the jet and not being pushed downward in the axial direction of the jet. Also, the
presence of downstream locations showing a somewhat periodic loss of information could indicate the presence of some instabilities in the cross flow due to vortex shedding or separation of the cross flow. Again, more information is required and will be obtained when the plane of the laser light sheet is moved into the $\mathrm{X}-\mathrm{Y}$ plane. Again, the plane of measurements was moved to a spanwise location of 2 diameters to see if any differences are seen.


Figure 4.22 PIV vector field for $\mathrm{q}=69$ at $\mathrm{Y} / \mathrm{d}=2$.

Figure 4.22 immediately shows that any lost data at the downstream boundary of the jet is recovered at 2 diameters in the spanwise direction. This further supports the idea that at the very central region, downstream of the jet, there appears to be some instability due to the cross flow moving rapidly around the body of the jet.

For $\mathrm{q}=40$ (figure 4.23), many similar trends, such as those in previous momentum ratios, are observed.


Figure 4.23 PIV vector field for $\mathrm{q}=40$ at $\mathrm{Y} / \mathrm{d}=0$.


Figure 4.24 PIV vector field for $\mathrm{q}=40$ at $\mathrm{Y} / \mathrm{d}=2$.

Figures 4.23 , and 4.24 each show a liquid jet bending in the downstream direction with straight velocity vectors along the upstream boundary of the jet. With the measurement plane at the center of the jet $(\mathrm{Y} / \mathrm{d}=0)$, again there appears to be a distinct loss of flow information in the downstream side of the jet with some periodicity. When the plane is moved to 2 diameters, the information is regained and the velocity plots show very straight velocity vectors with no periodicity. Even at a higher cross flow velocity, the flow appears to continue to move around the body of the jet resulting in lost information at the central downstream location of the flow field.

For $\mathrm{q}=18.8$, the jet bends in the downstream direction with straight cross flow velocity vectors passing around the body of the jet.


Figure 4.25 PIV vector field for $\mathrm{q}=18.8$ at $\mathrm{Y} / \mathrm{d}=0$.

Similar to the cases of previous momentum ratios, there appears to be a highly turbulent structure in the downstream wake of the jet. This conclusion is reached by observing the velocity vectors at the rear of the jet which show a very random directionality. The droplets from the jet begin mixing and accelerating as they move downstream. By observed the differences in the length and direction of the vectors it is seen that the sheared droplets in the wake of the jet accelerate as they move downstream as well as change direction. When comparing this cross sectional slice with one from a spanwise location of 2 diameters it is observed that any turbulent structures present in the central slice are now removed due to the steady nature of the flow wrapping around the jet.


Figure 4.26 PIV vector field for $\mathrm{q}=18.8$ at $\mathrm{Y} / \mathrm{d}=2$.

Figure 4.26 shows a distinct instability wave along the upstream boundary of the jet with straight cross flow velocity vectors. On the downstream side of the jet the flow appears to recover and regain its flow directionality.

At the highest cross flow velocity, lowest momentum ratio; $q=10$, much of the downstream information on the cross flow is lost in high rate of droplet shear occurring along the rear of the jet. The velocity magnitudes indicate that droplets are being shearing off the sides of the jet and accelerating as they move downstream.


Figure 4.27 PIV vector field for $\mathrm{q}=10$ at $\mathrm{Y} / \mathrm{d}=0$.
There still appears to be somewhat of a periodic loss of information on the downstream side of the jet. A close inspection of these vectors shows that the directionality is highly random. This could be due to eddy formation in the wake of the jet. Further analysis needs to be done in the X-Y plane to determine if these eddys are present.


Figure 4.28 PIV vector field for $\mathrm{q}=10$ at $\mathrm{Y} / \mathrm{d}=2$.

At 2 diameters, in the spanwise direction, the cross flow remains straight with some periodicity in the downstream wake. Figure 4.28 was averaged over 200 images producing a low number of velocity vectors in the upstream side of the JICF. This was primarily due to seeding dissipation, and evaporation at a high speed cross flow velocity of $30 \mathrm{~m} / \mathrm{s}$. Also, much of the seeding gets moved around the body of the jet and is subsequently lost in the violent shearing of droplets along the sides and the rear of the jet. In summary, the X-Z plane gives plenty of information on the mechanism of the jet break up. The cross flow vectors are straight along the upstream boundary of the jet indicating a mechanism whereby, the air is moved around the body of the jet possibly contributing to the instability leading to jet break up. As the vectors pass around the jet and meet in the central downstream side, periodic loss of flow information is observed in the wake. This loss of information could indicate an
eddy structure rotating and "pushing out" any seed particles due to centrifugal force present on these particles.

Lecuona et. Al (2002) came to a similar conclusion showing that strong vortices resulted in a significant depletion of particle concentrations 1 second after the onset of vorticity. These "holes" on the data may be markers of strong vorticity in the flow, which may aid in the mixing of sheared jet droplets and seeding particles. This result indicates the origin of the disturbances may not be the Rayleigh-Taylor instability. As explained previously, these instability waves directly affect the break up of the jet. An understanding of the instability mechanism is needed to better control the atomization by the gaseous cross flow. The next step is to take velocity field measurements in the $\mathrm{X}-\mathrm{Y}$ plane at a single Z location $(\mathrm{Z} / \mathrm{d}=10)$ to see if any support may be given to these primary findings.

### 4.1.6 Spanwise JICF Results

Axial measurements in the $\mathrm{X}-\mathrm{Z}$ plane showed the cross flow and its interaction with the water jet boundary. The PIV vector fields indicated that the air did not follow the curvature of the jet, but simply passed around the body of the jet with some lost information in the very near field downstream of the jet. To better understand the interaction between the cross flow and the jet boundary, PIV measurements were taken in the $\mathrm{X}-\mathrm{Y}$ plane at a non-dimensional distance of 10 diameters from the wall. This location was chosen to allow for measurements to be made outside of any boundary layer that may exist at the wall of the test section.

Also, inside the boundary layer, the three- dimensional nature of the flow resulted in many seeding particles moving through the thickness of the light sheet, which flooded the vector field with erroneous data. With this in mind, measurements were limited to within 10 diameters from the wall due to the lack of flow seeding further from the wall.

While measuring the velocity fields of the free stream only, it was noticed that the wind tunnel had fallen out of calibration. For this reason, the momentum ratios were adjusted to reflect the change in free stream velocity for the spanwise measurements. Instead of momentum ratios of $q=69$ and 40 with free stream velocities of 11.5 and $15 \mathrm{~m} / \mathrm{s}$, respectively, the momentum ratios were changed to reflect the new free stream velocities (Table 4.2)

Table 4. 2 Adjusted momentum ratio's for re-calibrated free stream velocities.

| $\mathbf{U}_{\text {©old }}$ <br> $(\mathbf{m} / \mathbf{s})$ | $\mathbf{U}_{\text {©new }}$ <br> $(\mathbf{m} / \mathbf{s})$ | $\mathbf{q}_{\text {old }}$ <br> (momentum <br> ratio) | $\mathbf{q}_{\text {new }}$ <br> (momentum <br> ratio) | Weber <br> Number <br> (new) |
| :---: | :---: | :---: | :---: | :---: |
| 11.50 | 10.50 | 69.25 | 77.89 | 3.58 |
| 15 | 14 | 40.70 | 43.81 | 6.37 |

Spanwise measurements in the X-Y plane were limited to these two momentum ratios due to liquid droplet congregation on the walls of the test section. In order for the PIV system to track the seeding, a dark background must be present. At higher cross flow velocities, the liquid jet was bent more severely depositing large amounts of liquid droplets on the surface of the wind tunnel. The deposition of sheared jet droplets resulted in spurious vectors showing up in the background of the image, preventing any measurements of accurate velocity fields to be obtained. For this reason, only two momentum ratios allowed for deposition free measurements, and these will be the main focus of this section.

At both momentum ratios, repeatability and image independence studies were conducted. Both sets of results showed great repeatability to within $3 \%$ deviation from day to day, while all vector fields were shown to be image capture independent after 200 images to within $3 \%$ deviation as well. Low seeding in the flow field prohibited any instantaneous flow fields from being captured. Each instantaneous image only provided a few good vectors, making it necessary to average multiple consecutive images to obtain an entire flow field. To ensure that all image fields were completely converged, 300 images were collected and average velocity fields were calculated.

For the first momentum ratio of 77.89 , the curvature of the jet is very similar to that seen in figures 4.18 and 4.19 from the previous section. This allowed for measurements to be made with little to no deposition of either seeding particles or liquid droplets from the jet. The direction of the free stream vectors are in the
streamwise X direction and should help to picture the proper orientation of the flow field. In essence these measurements are made as a cross sectional "slice" of the X-Y plane.


Figure 4.29 PIV vector field for $\mathrm{q}=77.89$ at $\mathrm{Z} / \mathrm{d}=10$.

Figure 4.29 shows a vector map of the free stream flow as it interacts with the liquid jet. To aid in the image, an approximate location of the jet outlet is provided. Any free stream vectors within the downstream width of the jet are "blocked out" by the liquid column as it is bent downstream. The free stream vectors seem to be relatively oriented in the downstream direction with very small changes in velocity
magnitude. Due to interference form the injector, no vectors were collected in the very near field of the jet. It should be noted that this is an average field, and any periodicity or instability would not show up in this figure. As stated previously, limitations due to seeding density did not allow for any analysis of instantaneous vector fields which would have yielded much more useful information.

For $\mathrm{q}=43.81$, similar results were obtained. The vector field is very straight, with a change in the free stream magnitude. For the lower momentum ratio, the jet spreads more in the spanwise direction, further limiting any downstream observations that may be made (as seen in section 4.1.3).


Figure 4.30 PIV vector field for $\mathrm{q}=43.81$ at $\mathrm{Z} / \mathrm{d}=10$.

Both velocity vector fields show a distinct orientation to the cross flow downstream. Any motion through the thickness of the light sheet would result in erroneous vectors that would show up as very low velocities. These vector fields did not show this tendency, therefore it can be surmised that most the flow is oriented in the downstream direction. This further supports the idea that no free stream air is following the jet column as it is bent downstream. The air is simply moving around the body of the jet and interacting with the liquid boundary.

To better understand the nature of this interaction, several rakes were placed in the near field of the jet at various spanwise locations of $\mathrm{Y} / \mathrm{d}$ from the side of the jet. The velocity magnitudes were non-dimensionalized by the mean velocity of the free stream air. Downstream X/d locations were taken from the center of the jet with negative $\mathrm{X} / \mathrm{d}$ values being the upstream locations and positive $\mathrm{X} / \mathrm{d}$ locations being downstream.


Figure 4.31 Near field velocity profiles at $\mathrm{Z} / \mathrm{d}=10$.

Figure 4.31 sheds more light into the mechanisms of the interactions between the jet and the cross flow. Both momentum ratios show about a $20 \%$ reduction in
velocity magnitude 2 diameters from the side of the jet. When comparing the two momentum ratios it is observed that the lower momentum ratio (higher cross flow velocity) has a more significant reduction in velocity magnitude than the higher momentum ratio, at the same spanwise location. The width of the defect for the higher q seems to be larger, while the magnitude of the defect for $\mathrm{q}=44$ is larger.

At 4 diameters, both momentum ratios show a small recovery to values closer to the free stream velocity, while still showing some remnants of the jet boundary effects. Both spanwise locations show a near full recovery towards the free stream velocity around 3 diameters downstream of the jet. Due to the geometry of the setup, no wake deficit measurements could be made at the rear of the jet column. The side velocity profiles, however, provide more than enough information to infer that there is a significant velocity defect at the rear of the jet. Any effects that may be observed in the near field of the jet are obviously felt through the entire flow field.


Figure 4.32 Proximal velocity profiles at $\mathrm{Z} / \mathrm{d}=10$.

Figure 4.32 shows the velocity profiles of the boundary layer velocities along the side of the jet. Measurements could only be taken up to $\mathrm{Y} / \mathrm{d}=2$, but it is clearly seen that both momentum ratios also experience a velocity defect near the sides of the jet. The lower momentum value has a much more intense velocity defect than the higher momentum ratio. This is in good agreement to the findings seen in Figure 4.31.

The explanation of this velocity defect sheds some insight into the break up mechanism of the two-phase JICF. The observed velocity defect is due to a region of
intense shear at the boundary of the liquid jet and the cross flow. This intense shear is only magnified as the free stream velocity is increased, thus resulting in a larger velocity defect for lower values of $q$. This shear results in the removal of droplets from the jet surface, and the "stretching" of the liquid column in the spanwise direction along the sides of the jet. Coupled with the extremely high drag on the front of the jet, the jet expands in the spanwise direction, and begins to break apart.

The stripped droplets from the side of the jet are carried off by the cross flow following its streamlines and being carried to the rear of the jet. This explains the increased deposition of jet liquid droplets along the side walls of the test section (Figures $4.5 \mathrm{a}, \mathrm{b}$, and c ). The droplets that are sheared from the sides of the jet are very small which allows them to be "dragged" through the free stream at a much higher velocity than the larger droplets. This is complimentary to the findings of Fuller et Al. (1998) who were able to show that along the sides of the jet there exist droplets moving at much higher velocities than those near the center of the jet. Also, they were able to show that the Sauter Mean Diameter (SMD) of these droplets was much smaller than those in the central region as well.

Thus, the overall break up mechanism can be attributed to the high shear forces along the sides of the jet, as well as the intense drag on the front of the jet due to its shape. As the cross flow comes into contact with the jet it imparts a high drag force on the front of the jet, which has a much higher density than the cross flow. The air then passes around the jet losing nearly $20 \%$ of free stream magnitude 2 diameters away from the jet boundary, resulting in an intense shear region along the
sides of the jet. In the regime corresponding to periodic vortex shedding, this shear coupled with the pressure distribution could result in the formation of the column waves seen earlier.

Due to the geometry of the setup, and lack of seed density, the presence of the wake vortices cannot be validated directly. However, the axial velocity measurements indicate the presence of a "wake" region at the rear of the jet. Also, the PIV images displaying a periodic loss of information support the presence of periodically shed vortices from the separation of the shear layer on the jet surface. Therefore, these images provide indirect evidence of the presence of wake structures that significantly affect the jet break up; in this regard, the wake structures play a similar role to those in a single-phase JCIF that contribute to mixing.

## CHAPTER 5 CONCLUSIONS AND RECOMMENDATIONS

### 5.1 Conclusions

The break up mechanisms of a liquid jet in a high speed cross flow of air were studied for various momentum ratios. The three-dimensional flow patterns were visualized using high-speed camera images and PIV measurements in different planes. Based on the results, the following conclusions are made:

1. Lower momentum ratios increased jet bending in the downstream direction; disturbance waves were present in the jet for all the momentum ratios studied.
2. Reasonable agreement was obtained between the present results involving the onset of multimode break up, disturbance wavelengths, and the break up locations and results from past studies; however, the critical Weber number criterion provided by Aalburg et al (2004) appears to be limited. Multimode break up was observed at a Weber number of 15.85 , well short of the critical Weber number of 30 specified by Aalburg et al (2004). A comprehensive table was developed highlighting the different types of
break up and regimes encountered in two-phase as a function of the Weber number and the momentum ratio.
3. The PIV measurements indicate that the cross flow wraps around the jet, similar to the flow around a solid cylinder. The measurements highlight the presence of a wake in the rear of the jet and indirectly indicate the presence of periodically shed vortices.
4. The wake structures appear to influence the jet break up significantly. The high shear on the sides of the jet results in the stripping of drops from the jet surface; the shear layer separation from the jet sides could trigger the column waves observed on the jet. It appears that the Rayleigh-Taylor instability is not a leading reason for the jet instability for the momentum ratios between 10 and 172 .
5. The present method of using an optical filter and fluorescent seeding droplets for PIV measurements in a two-phase flow provides an avenue to make velocity measurements in different regions of the two-phase JCIF.
6. FLUENT'S Volume of Fluid (VOF) solver package showed great promise for the computational study of a two phase JICF.

### 5.2 Recommendations

Some of the recommendations to improve future research on this subject are:

1. Construction of the injector and wind tunnel setup in such a way that no interference results in the near field of the jet exit. This would allow for measurements to be made at the top of the test section preventing any interference from the bent liquid column as well.
2. Improvement in the injection of the seeding particles. The current setup produces seeding only in the near wall region. A global seeding system should be designed to seed the entire test section to allow for the capture of instantaneous images.
3. Using a higher speed wind tunnel, study of the critical Weber number for the onset of shear break up.
4. Utilization of a three-dimensional setup for the PIV system to obtain multi plane measurements simultaneously.

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## APPENDIX A

Table A 1 Wind tunnel calibration using pitot probe. ..... 118
Table A 2 Rotameter flow meter calibration check. ..... 119
Table A 3 Viscosity measurements of jet fluid ..... 119
Table A 4 Jet width measurements for $q=18.8$ ..... 120
Table A 5 Jet width measurements for $\mathrm{q}=10$. ..... 121
Table A 6 Test section velocity check with PIV ..... 122
Table A 7 Cross sectional velocity profile for 30 Hz . ..... 123
Table A 8 Cross sectional velocity profile for 40 Hz ..... 125
Table A 9 Cross sectional velocity profile for 45 Hz ..... 127
Table A 10 Cross sectional velocity profile for 50 Hz ..... 129
Table A 11 Cross sectional velocity profile for 60 Hz ..... 131
Table A 12 Wind tunnel calibration re-check with pitot probe. ..... 133
Table A 13 Image variance of PIV measurements for $q=78$ ..... 134
Table A 14 Image variance of PIV measurements for $q=44$. ..... 135
Table A 15 Repeatability of PIV images for $q=78$ ..... 136
Table A 16 Repeatability of PIV images for $q=44$. ..... 136
Table A 17 Side velocity profile for $\mathrm{q}=78$, at $\mathrm{Y} / \mathrm{d}=2$. ..... 137
Table A 18 Side velocity profile for $\mathrm{q}=78$, at $\mathrm{Y} / \mathrm{d}=4$. ..... 139
Table A 19 Side velocity profile for $\mathrm{q}=44$, at $\mathrm{Y} / \mathrm{d}=2$. ..... 141
Table A 20 Side velocity profile for $\mathrm{q}=44$, at $\mathrm{Y} / \mathrm{d}=4$ ..... 143
Table A 21 Proximal velocity profile for $\mathrm{q}=78$. ..... 145
Table A 22 Proximal velocity profile for $\mathrm{q}=44$ ..... 147
Table A 23 Spray characteristic break up matrix ..... 150
Table A 24 Wavelength and break up locations for $\mathrm{q}=10$. ..... 152
Table A 25 Wavelength and break up locations for $q=18.8$ ..... 152
Table A 26 Wavelength and break up locations for $q=40$. ..... 153

Table A 1 Wind tunnel calibration using pitot probe.

| Controller Freq | Pos | $\begin{gathered} \text { Delta P } \\ (\mathrm{mmH} 20) \end{gathered}$ | $\begin{gathered} \text { Delta P (in } \\ \mathrm{H} 20) \end{gathered}$ | $\begin{gathered} \hline \text { Delta P } \\ (\mathrm{Pa}) \end{gathered}$ | V ( $\mathrm{m} / \mathrm{s}$ ) | Q (m3/s) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 1 | 1.3 | 0.0512 | 12.758 | 4.646 | 0.816 |
|  | 2 | 1.3 | 0.0512 | 12.758 | 4.646 | 0.816 |
|  | 3 | 1.3 | 0.0512 | 12.758 | 4.646 | 0.816 |
|  | avg | 1.3 | 0.0512 | 12.758 | 4.646 | 0.816 |
|  | stdev | 0 | 0.0000 | 0.000 | 0.000 | 0.000 |
| 15 | 1 | 2.8 | 0.1103 | 27.479 | 6.819 | 1.198 |
|  | 2 | 2.8 | 0.1103 | 27.479 | 6.819 | 1.198 |
|  | 3 | 2.8 | 0.1103 | 27.479 | 6.819 | 1.198 |
|  | avg | 2.8 | 0.1103 | 27.479 | 6.819 | 1.198 |
|  | stdev | 0 | 0.0000 | 0.000 | 0.000 | 0.000 |
| 20 | 1 | 5 | 0.1970 | 49.071 | 9.112 | 1.601 |
|  | 2 | 5 | 0.1970 | 49.071 | 9.112 | 1.601 |
|  | 3 | 5 | 0.1970 | 49.071 | 9.112 | 1.601 |
|  | avg | 5 | 0.1970 | 49.071 | 9.112 | 1.601 |
|  | stdev | 0 | 0.0000 | 0.000 | 0.000 | 0.000 |
| 25 | 1 | 8 | 0.3152 | 78.513 | 11.526 | 2.025 |
|  | 2 | 8.1 | 0.3191 | 79.494 | 11.598 | 2.038 |
|  | 3 | 8.1 | 0.3191 | 79.494 | 11.598 | 2.038 |
|  | avg | 8.07 | 0.3178 | 79.167 | 11.574 | 2.034 |
|  | stdev | 0.06 | 0.0023 | 0.567 | 0.041 | 0.007 |
| 30 | 1 | 12.2 | 0.4807 | 119.732 | 14.233 | 2.501 |
|  | 2 | 12.2 | 0.4807 | 119.732 | 14.233 | 2.501 |
|  | 3 | 12.1 | 0.4767 | 118.751 | 14.175 | 2.491 |
|  | avg | 12.17 | 0.4794 | 119.405 | 14.214 | 2.497 |
|  | stdev | 0 | 0.0000 | 0.000 | 0.000 | 0.000 |
| 35 | 1 | 17.2 | 0.6777 | 168.803 | 16.900 | 2.969 |
|  | 2 | 17.2 | 0.6777 | 168.803 | 16.900 | 2.969 |
|  | 3 | 17.2 | 0.6777 | 168.803 | 16.900 | 2.969 |
|  | avg | 17.2 | 0.6777 | 168.803 | 16.900 | 2.969 |
|  | stdev | 0 | 0.0000 | 0.000 | 0.000 | 0.000 |
| 40 | 1 | 22.8 | 0.8983 | 223.762 | 19.458 | 7.226 |
|  | 2 | 22.8 | 0.8983 | 223.762 | 19.458 | 7.226 |
|  | 3 | 22.8 | 0.8983 | 223.762 | 19.458 | 7.226 |
|  | avg | 22.8 | 0.8983 | 223.762 | 19.458 | 7.226 |
|  | stdev | 0 | 0.0000 | 0.000 | 0.000 | 0.000 |
| 50 | 1 | 37.5 | 1.4775 | 368.029 | 24.954 | 9.268 |
|  | 2 | 37.5 | 1.4775 | 368.029 | 24.954 | 9.268 |
|  | 3 | 37.5 | 1.4775 | 368.029 | 24.954 | 9.268 |
|  | avg | 37.5 | 1.4775 | 368.029 | 24.954 | 9.268 |
| 60 | 1 | 55.3 | 2.1788 | 542.720 | 30.304 | 11.254 |
|  | 2 | 55.2 | 2.1749 | 541.738 | 30.276 | 11.244 |
|  | 3 | 55.2 | 2.1749 | 541.738 | 30.276 | 11.244 |
|  | avg | 55.23 | 2.1762 | 542.066 | 30.285 | 11.247 |

```
stdev }\begin{array}{llllll}{0}&{0.0000}&{0.000}&{0.000}&{0.000}
```

Table A 2 Rotameter flow meter calibration check.

| Trial \# | Rotameter Flow Rate <br> $(\mathrm{lpm})$ | Actual Flow Rate (lpm) |
| :---: | :---: | :---: |
| 1 | 0.6 | 0.626 |
| 2 | 0.6 | 0.624 |
| 3 | 0.6 | 0.623 |
|  |  |  |
| 1 | 0.4 | 0.426 |
| 2 | 0.4 | 0.415 |
| 3 | 0.4 | 0.428 |
|  |  |  |
| 1 | 0.8 | 0.792 |
| 2 | 0.8 | 0.788 |
| 3 | 0.8 | 0.791 |
|  |  |  |
| 1 | 0.5 | 0.524 |
| 2 | 0.5 | 0.526 |
| 3 | 0.5 | 0.53 |
|  |  |  |
| 1 | 0.7 | 0.713 |
| 2 | 0.7 | 0.707 |
| 3 |  | 0.72 |

Table A 3 Viscosity measurements of jet fluid.

| Trial | Time $(\mathrm{s})$ | Kinematic <br> Viscosity <br> $(\mathrm{cSt})$ | Kinematic <br> Viscosity <br> $(\mathrm{m} 2 / \mathrm{s})$ | Dynamic <br> Viscosity <br> $(\mathrm{m} 2 / \mathrm{s})$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 77.33 | 1.16 | $1.16 \mathrm{E}-06$ | $1.16 \mathrm{E}-03$ |
| 2 | 74.04 | 1.11 | $1.11 \mathrm{E}-06$ | $1.11 \mathrm{E}-03$ |
| 3 | 77.36 | 1.16 | $1.16 \mathrm{E}-06$ | $1.16 \mathrm{E}-03$ |
| 4 | 75.78 | 1.14 | $1.14 \mathrm{E}-06$ | $1.14 \mathrm{E}-03$ |
| 5 | 75.73 | 1.14 | $1.14 \mathrm{E}-06$ | $1.14 \mathrm{E}-03$ |
| 6 | 75.30 | 1.13 | $1.13 \mathrm{E}-06$ | $1.13 \mathrm{E}-03$ |
| 7 | 76.74 | 1.15 | $1.15 \mathrm{E}-06$ | $1.15 \mathrm{E}-03$ |
| 8 | 74.85 | 1.12 | $1.12 \mathrm{E}-06$ | $1.12 \mathrm{E}-03$ |
| 9 | 73.84 | 1.11 | $1.11 \mathrm{E}-06$ | $1.11 \mathrm{E}-03$ |
| 10 | 75.12 | 1.13 | $1.13 \mathrm{E}-06$ | $1.13 \mathrm{E}-03$ |
|  |  |  |  |  |
| avg | 75.61 | 1.13 | $1.13 \mathrm{E}-06$ | $1.13 \mathrm{E}-03$ |
| stdev | 1.2406 | 0.0186 | $1.86 \mathrm{E}-08$ | $1.86 \mathrm{E}-05$ |

Table A 4 Jet width measurements for $\mathrm{q}=18.8$

| Xpaper (in) | Xactual (cm) | Xactual (mm) | X/d | Wpaper (in) | Wactual (cm) | Wactual (mm) | W/d |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.222 | 1.040 | 10.403 | 5.201 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.216 | 1.012 | 10.122 | 5.061 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.234 | 1.097 | 10.965 | 5.483 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.224 | 1.050 | 10.497 | 5.248 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.23 | 1.078 | 10.778 | 5.389 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.22 | 1.031 | 10.309 | 5.155 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.219 | 1.026 | 10.262 | 5.131 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.234 | 1.097 | 10.965 | 5.483 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.27 | 1.265 | 12.652 | 6.326 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.2 | 0.937 | 9.372 | 4.686 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.2 | 0.937 | 9.372 | 4.686 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.222 | 1.040 | 10.403 | 5.201 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.213 | 0.998 | 9.981 | 4.991 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.232 | 1.087 | 10.872 | 5.436 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.208 | 0.975 | 9.747 | 4.873 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.223 | 1.045 | 10.450 | 5.225 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.226 | 1.059 | 10.590 | 5.295 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.231 | 1.082 | 10.825 | 5.412 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.229 | 1.073 | 10.731 | 5.366 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.236 | 1.106 | 11.059 | 5.530 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.343 | 1.607 | 16.073 | 8.037 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.329 | 1.542 | 15.417 | 7.709 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.345 | 1.617 | 16.167 | 8.083 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.328 | 1.537 | 15.370 | 7.685 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.343 | 1.607 | 16.073 | 8.037 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.339 | 1.589 | 15.886 | 7.943 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.330 | 1.546 | 15.464 | 7.732 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.311 | 1.457 | 14.574 | 7.287 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.388 | 1.818 | 18.182 | 9.091 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.343 | 1.607 | 16.073 | 8.037 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.289 | 1.354 | 13.543 | 6.771 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.310 | 1.453 | 14.527 | 7.263 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.350 | 1.640 | 16.401 | 8.201 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.320 | 1.500 | 14.995 | 7.498 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.342 | 1.603 | 16.026 | 8.013 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.348 | 1.631 | 16.307 | 8.154 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.351 | 1.645 | 16.448 | 8.224 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.344 | 1.612 | 16.120 | 8.060 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.359 | 1.682 | 16.823 | 8.411 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.340 | 1.593 | 15.933 | 7.966 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.444 | 2.081 | 20.806 | 10.403 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.450 | 2.109 | 21.087 | 10.544 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.442 | 2.071 | 20.712 | 10.356 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.46 | 2.156 | 21.556 | 10.778 |


| 0.750 | 3.515 | 35.145 | 17.573 | 0.462 | 2.165 | 21.649 | 10.825 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.453 | 2.123 | 21.228 | 10.614 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.441 | 2.067 | 20.665 | 10.333 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.430 | 2.015 | 20.150 | 10.075 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.484 | 2.268 | 22.680 | 11.340 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.458 | 2.146 | 21.462 | 10.731 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.416 | 1.949 | 19.494 | 9.747 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.409 | 1.917 | 19.166 | 9.583 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.452 | 2.118 | 21.181 | 10.590 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.440 | 2.062 | 20.619 | 10.309 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.460 | 2.156 | 21.556 | 10.778 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.483 | 2.263 | 22.634 | 11.317 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.442 | 2.071 | 20.712 | 10.356 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.428 | 2.006 | 20.056 | 10.028 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.453 | 2.123 | 21.228 | 10.614 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.484 | 2.268 | 22.680 | 11.340 |

Table A 5 Jet width measurements for $\mathrm{q}=10$.

| Xpaper <br> $($ in $)$ | Xactual <br> $(\mathrm{cm})$ | Xactual <br> $(\mathrm{mm})$ | X/d | Wpaper <br> $($ in $)$ | Wactual <br> $(\mathrm{cm})$ | Wactual <br> $(\mathrm{mm})$ | W/d |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.228 | 1.068 | 10.684 | 5.342 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.23 | 1.078 | 10.778 | 5.389 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.244 | 1.143 | 11.434 | 5.717 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.246 | 1.153 | 11.528 | 5.764 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.23 | 1.078 | 10.778 | 5.389 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.226 | 1.059 | 10.590 | 5.295 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.233 | 1.092 | 10.918 | 5.459 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.223 | 1.045 | 10.450 | 5.225 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.221 | 1.036 | 10.356 | 5.178 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.226 | 1.059 | 10.590 | 5.295 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.222 | 1.040 | 10.403 | 5.201 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.238 | 1.115 | 11.153 | 5.576 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.227 | 1.064 | 10.637 | 5.319 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.22 | 1.031 | 10.309 | 5.155 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.225 | 1.054 | 10.544 | 5.272 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.227 | 1.064 | 10.637 | 5.319 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.218 | 1.022 | 10.216 | 5.108 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.237 | 1.111 | 11.106 | 5.553 |
| 0.25 | 1.172 | 11.715 | 5.858 | 0.21 | 0.984 | 9.841 | 4.920 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.313 | 1.467 | 14.667 | 7.334 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.315 | 1.476 | 14.761 | 7.381 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.316 | 1.481 | 14.808 | 7.404 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.270 | 1.265 | 12.652 | 6.326 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.272 | 1.275 | 12.746 | 6.373 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.275 | 1.289 | 12.887 | 6.443 |


| 0.500 | 2.343 | 23.430 | 11.715 | 0.288 | 1.350 | 13.496 | 6.748 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.298 | 1.396 | 13.964 | 6.982 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.275 | 1.289 | 12.887 | 6.443 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.305 | 1.429 | 14.292 | 7.146 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.300 | 1.406 | 14.058 | 7.029 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.275 | 1.289 | 12.887 | 6.443 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.280 | 1.312 | 13.121 | 6.560 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.270 | 1.265 | 12.652 | 6.326 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.276 | 1.293 | 12.933 | 6.467 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.309 | 1.448 | 14.480 | 7.240 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.272 | 1.275 | 12.746 | 6.373 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.278 | 1.303 | 13.027 | 6.514 |
| 0.500 | 2.343 | 23.430 | 11.715 | 0.288 | 1.350 | 13.496 | 6.748 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.356 | 1.668 | 16.682 | 8.341 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.345 | 1.617 | 16.167 | 8.083 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.358 | 1.678 | 16.776 | 8.388 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.36 | 1.687 | 16.870 | 8.435 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.345 | 1.617 | 16.167 | 8.083 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.365 | 1.710 | 17.104 | 8.552 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.360 | 1.687 | 16.870 | 8.435 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.359 | 1.682 | 16.823 | 8.411 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.360 | 1.687 | 16.870 | 8.435 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.368 | 1.724 | 17.245 | 8.622 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.355 | 1.664 | 16.635 | 8.318 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.365 | 1.710 | 17.104 | 8.552 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.340 | 1.593 | 15.933 | 7.966 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.359 | 1.682 | 16.823 | 8.411 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.330 | 1.546 | 15.464 | 7.732 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.343 | 1.607 | 16.073 | 8.037 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.358 | 1.678 | 16.776 | 8.388 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.365 | 1.710 | 17.104 | 8.552 |
| 0.750 | 3.515 | 35.145 | 17.573 | 0.368 | 1.724 | 17.245 | 8.622 |

Table A 6 Test section velocity check with PIV.

| Freq $(\mathrm{Hz})$ | Mean Velocity PIV (m/s) | Mean Velocity Calib. (m/s) | Percent Difference |
| :---: | :---: | :---: | :---: |
| 30.6 | 14.13 | 15.01 | 5.86 |
| 40 | 19.23 | 19.62 | 1.99 |
| 45 | 21.42 | 22.07 | 2.96 |
| 50 | 24.18 | 24.53 | 1.41 |
| 60 | 29.83 | 29.43 | 1.36 |

Table A 7 Cross sectional velocity profile for 30 Hz .

| 30HZ | $\begin{gathered} \mathrm{Z} \\ (\mathrm{~mm}) \end{gathered}$ | $\begin{gathered} \mathrm{U} / \mathrm{s}) \\ (\mathrm{m} / \mathrm{s} \end{gathered}$ | $\begin{gathered} \mathrm{V} \\ (\mathrm{~m} / \mathrm{s}) \end{gathered}$ | Vel. Mag (m/s) |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} X \\ (\mathrm{~mm}) \end{gathered}$ |  |  |  |  |
| 64.262 |  | 14.733 | 0.714 |  |
|  | 27.812 | 14.733 | 0.714 | 14.752 |
| 64.262 | 27.454 | 14.554 | 0.539 | 14.567 |
| 64.262 | 27.097 | 14.298 | 0.341 | 14.304 |
|  |  | - | - |  |
| 64.262 | 26.739 | 14.167 | 0.216 | 14.168 |
| 64.262 | 26.381 | 14.020 | 0.250 | 14.023 |
|  |  | - | - |  |
| 64.262 | 26.024 | 13.877 | 0.277 | 13.880 |
|  |  | - | - |  |
| 64.262 | 25.666 | 13.762 | 0.297 | 13.765 |
|  |  | 13856 | 234 |  |
| 64.262 | 25.308 | 13.856 | 0.234 | 13.859 |
| 64.262 | 24.951 | $\stackrel{-}{13.985}$ | ${ }_{0}^{-171}$ | 13.987 |
|  |  | , | - |  |
| 64.262 | 24.593 | 14.054 | 0.100 | 14.056 |
|  |  | - |  |  |
| 64.262 | 24.235 | 14.206 | 0.126 | 14.212 |
| 64.262 | 23.878 | 14.385 | 0.413 | 14.398 |
|  |  | - |  |  |
| 64.262 | 23.520 | 14.427 | 0.536 | 14.444 |
| 64.262 | 23.162 | 14.012 | 0.561 | 14.031 |
|  |  | - |  |  |
| 64.262 | 22.805 | 13.509 | 0.597 | 13.532 |
|  |  |  |  |  |
| 64.262 | 22.447 | 13.290 | 0.562 | 13.313 |
| 64.262 | 22.089 | 13.470 | 0.246 | 13.486 |
|  |  | - | - |  |
| 64.262 | 21.732 | 13.705 | 0.130 | 13.712 |
| 64.262 | 21.374 | 13.817 | 0.280 | 13820 |
| 64.262 | 21.016 | 13.995 | 0.236 | 13.998 |
|  |  | - | - |  |
| 64.262 | 20.659 | 14.190 | 0.207 | 14.192 |
|  | 20.301 | 14.319 | 0.117 | 14.320 |
| 64.262 |  |  |  |  |
| 64.262 | 19.943 | 14.370 | 0.012 | 14.371 |
| 64.262 | 19.586 | - | 0.136 | 14.416 |

14.415

| 62 |  |  | 0.244 | 14.440 |
| :---: | :---: | :---: | :---: | :---: |
| 64.262 | 18.870 | 14.319 | 0.378 | 14.326 |
|  |  |  |  |  |
| 64.262 | 18.513 | 14.184 | 0.546 | 14.197 |
|  |  |  |  |  |
| 64.262 | 18.155 | 14.103 | 0.555 | 14.116 |
|  |  |  |  |  |
| 64.262 | 17.797 | 14.011 | 0.478 | 14.022 |
| 64.262 17.797 14.01 0.478 |  |  |  |  |
| 64.262 | 17.440 | 13.913 | 0.410 | 13.922 |
| 04.262 17.440 13.913 0.410 |  |  |  |  |
| 64.262 | 17.082 | 13.827 | 0.252 | 13.836 |
|  |  | - | - |  |
| 64.262 | 16.725 | 13.822 | 0.064 | 13.833 |
|  |  | - | - |  |
| 64.262 | 16.367 | 13.846 | 0.389 | 13.856 |
|  |  | - | - |  |
| 64.262 | 16.009 | 13.833 | 0.545 | 13.845 |
|  |  | - | - |  |
| 64.262 | 15.652 | 13.975 | 0.499 | 13.985 |
|  |  | - | - |  |
| 64.262 | 15.294 | 14.121 | 0.466 | 14.130 |
|  |  | - | - |  |
| 64.262 | 14.936 | 14.234 | 0.299 | 14.240 |
|  |  | - | - |  |
| 64.262 | 14.579 | 14.322 | 0.091 | 14.327 |
|  |  | - |  |  |
| 64.262 | 14.221 | 14.409 | 0.095 | 14.413 |
|  |  | - |  |  |
| 64.262 | 13.863 | 14.446 | 0.206 | 14.451 |
|  |  | - | - |  |
| 64.262 | 13.506 | 14.507 | 0.062 | 14.516 |
|  |  | - | - |  |
| 64.262 | 13.148 | 14.589 | 0.346 | 14.603 |
|  |  | - | - |  |
| 64.262 | 12.790 | 14.590 | 0.438 | 14.603 |
|  |  | - | - |  |
| 64.262 | 12.433 | 14.585 | 0.286 | 14.594 |
|  |  | - | - |  |
| 64.262 | 12.075 | 14.570 | 0.118 | 14.574 |
|  |  | - | - |  |
| 64.262 | 11.717 | 14.623 | 0.087 | 14.625 |
|  |  | - |  |  |
| 64.262 | 11.360 | 14.747 | 0.020 | 14.748 |
|  |  | - |  |  |
| 64.262 | 11.002 | 14.880 | 0.144 | 14.882 |
|  |  | - |  |  |
| 64.262 | 10.644 | 14.915 | 0.083 | 14.916 |
|  |  | - | - |  |
| 64.262 | 10.287 | 14.825 | 0.043 | 14.827 |

Table A 8 Cross sectional velocity profile for 40 Hz .

| 40HZ | $\begin{gathered} \mathrm{Z} \\ (\mathrm{~mm}) \end{gathered}$ | $\begin{gathered} \mathrm{U} / \mathrm{m}) \\ (\mathrm{m}) \end{gathered}$ | $\begin{gathered} \mathrm{V} \\ (\mathrm{~m} / \mathrm{s}) \end{gathered}$ | Vel. Mag (m/s) |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} X \\ (\mathrm{~mm}) \end{gathered}$ |  |  |  |  |
| 65.180 | 28.631 | 18.955 | 0.385 | 18.991 |
|  |  |  | - |  |
| 65.180 | 28.425 | 19.049 | 0.586 | 19.092 |
|  |  | - | - |  |
| 65.180 | 28.219 | 19.148 | 0.790 | 19.199 |
|  | 28.014 | 19.215 | 0.776 | 19.312 |
| 65.180 |  | 9.215 | 0.776 |  |
| 65.180 | 27.808 | 19.314 | 0.593 | 19.502 |
|  |  | - | - |  |
| 65.180 | 27.603 | 19.403 | 0.428 | 19.673 |
|  |  | 10.327 | 0.375 |  |
| 65.180 | 27.397 | 19.327 | 0.375 | 19.534 |
| 65.180 | 27.192 | 19.238 | 0.342 | 19.371 |
|  |  | - | - |  |
| 65.180 | 26.986 | 19.193 | 0.316 | 19.285 |
|  |  | - | - |  |
| 65.180 | 26.780 | 19.208 | 0.389 | 19.279 |
|  |  | - | - |  |
| 65.180 | 26.575 | 19.221 | 0.459 | 19.273 |
|  |  | - | - |  |
| 65.180 | 26.369 | 19.179 | 0.477 | 19.232 |
|  |  | - | - |  |
| 65.180 | 26.164 | 19.129 | 0.481 | 19.190 |
|  |  |  | 5 |  |
| 65.180 | 25.958 | 19.081 | 0.519 | 19.146 |
|  |  | 0 | 01 |  |
| 65.180 | 25.753 | 18.996 | 0.619 | 19.061 |
|  |  |  | - |  |
| 65.180 | 25.547 | 18.910 | 0.718 | 18.975 |
|  |  | - | - |  |
| 65.180 | 25.341 | 18.886 | 0.741 | 18.951 |
| 65.180 | 25.136 | 18.902 | 0.713 | 18.967 |
|  |  | - | - |  |
| 65.180 | 24.930 | 18.910 | 0.684 | 18.975 |
|  |  |  | . |  |
| 65.180 | 24.725 | 18.925 | 0.616 | 19.020 |
|  |  |  | 5 |  |
| 65.180 | 24.519 | 18.940 | 0.536 | 19.068 |


| 65.180 | 24.313 | 18.956 | 0.526 | 19.086 |
| :---: | :---: | :---: | :---: | :---: |
| 65.180 | 24.108 | 18.979 | 0.612 | 19.070 |
|  |  |  |  |  |
| 65.180 | 23.902 | 19.002 | 0.694 | 19.054 |
|  |  | - |  |  |
| 65.180 | 23.697 | 19.059 | 0.684 | 19.102 |
|  |  |  |  |  |
| 65.180 | 23.491 | 19.139 | 0.660 | 19.175 |
|  |  | - 10 | - |  |
| 65.180 | 23.286 | 19.179 | 0.639 | 19.209 |
| 65.180 | 23.080 | 19.091 | 0.594 | 19.120 |
|  |  |  | - |  |
| 65.180 | 22.874 | 19.002 | 0.550 | 19.032 |
|  |  |  |  |  |
| 65.180 | 22.669 | 18.965 | 0.532 | 18.994 |
|  |  | - | - |  |
| 65.180 | 22.463 | 18.942 | 0.525 | 18.971 |
| 65.180 | 22.258 | 18.918 | 0.516 | 18.946 |
|  |  | - | - |  |
| 65.180 | 22.052 | 18.868 | 0.453 | 18.895 |
|  | 21.847 | 18.814 | 0.388 | 18.842 |
| 65.180 |  | - | - |  |
| 65.180 | 21.641 | 18.799 | 0.365 | 18.828 |
|  |  | - | - |  |
| 65.180 | 21.435 | 18.828 | 0.386 | 18.856 |
|  |  | - | - |  |
| 65.180 | 21.230 | 18.857 | 0.408 | 18.884 |
|  |  |  |  |  |
| 65.180 | 21.024 | 18.836 | 0.444 | 18.863 |
|  |  | - | - |  |
| 65.180 | 20.819 | 18.811 | 0.492 | 18.841 |
|  |  | - | - |  |
| 65.180 | 20.613 | 18.793 | 0.533 | 18.822 |
|  |  | - | - |  |
| 65.180 | 20.408 | 18.787 | 0.557 | 18.817 |
|  |  | - | - |  |
| 65.180 | 20.202 | 18.782 | 0.581 | 18.811 |
| 65.180 | 19.996 | 18.773 | 0.618 | 18.804 |
|  |  | 18.773 | 0.618 |  |
| 65.180 | 19.791 | 18.759 | 0.654 | 18.795 |
|  |  | - | - |  |
| 65.180 | 19.585 | 18.742 | 0.684 | 18.783 |
| 65.180 | 19.380 | 18.740 | 0.676 | 18.776 |
| 65.180 | 19.174 | 18.741 | 0.666 | 18.772 |
|  |  | - | - |  |
| 65.180 | 18.969 | 18.713 | 0.640 | 18.742 |


| 65.180 | 18.763 | 18.597 | 0.567 | 18.624 |
| :---: | :---: | :---: | :---: | :---: |
| 65.180 | 18.557 | 18.496 | 0.499 | 18.521 |
|  |  | - | - |  |
| 65.180 | 18.352 | 18.596 | 0.511 | 18.625 |
| 65.180 | 18.146 | 18.714 | 0.528 | 18.746 |
|  |  | - | - |  |
| 65.180 | 17.941 | 18.823 | 0.491 | 18.855 |
| 65.180 | 17.735 | 18.995 | 0.372 | 19.029 |
|  |  | - | - |  |
| 65.180 | 17.530 | 19.167 | 0.252 | 19.204 |
| 65.180 | 17.324 | 19.134 | 0.233 | 19.164 |
|  |  | - | - |  |
| 65.180 | 17.118 | 19.008 | 0.280 | 19.030 |
| 65.180 | 16.913 | 18.914 | 0.324 | 18.930 |
|  |  | - | - |  |
| 65.180 | 16.707 | 18.981 | 0.294 | 18.999 |
|  |  | - | - |  |
| 65.180 | 16.502 | 19.059 | 0.257 | 19.080 |
| 65.180 | 16.296 | 19.046 | 0.283 | 19.067 |
| 65.180 | 16.091 | 18.984 | 0.354 | 19.003 |
| 65.180 | 15.885 | 18.922 | 0.421 | 18.940 |
| 65.180 | 15.679 | 19.021 | 0.459 | 19.043 |

Table A 9 Cross sectional velocity profile for 45 Hz .

| 45 HZ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| X <br> $(\mathrm{mm})$ | Z <br> $(\mathrm{mm})$ | $\mathrm{U} / \mathrm{s})$ <br> $(\mathrm{m})$ | V <br> $(\mathrm{m} / \mathrm{s})$ | Vel. Mag <br> $(\mathrm{m} / \mathrm{s})$ |
| 66.007 | 28.753 | 21.487 | 0.451 | 21.500 |
|  |  | - | - |  |
| 66.007 | 28.410 | 21.518 | 0.468 | 21.531 |
|  |  | - | - |  |
| 66.007 | 28.067 | 21.548 | 0.483 | 21.562 |
|  |  | - | - |  |
| 66.007 | 27.723 | 21.577 | 0.500 | 21.593 |
|  |  | - | - |  |
| 66.007 | 27.380 | 21.583 | 0.511 | 21.599 |
|  |  | - | - |  |
| 66.007 | 27.037 | 21.597 | 0.521 | 21.613 |
| 66.007 | 26.694 | 21.603 | 0.532 | 21.620 |


| 66.007 | 26.350 | 21.599 | 0.536 | 21.617 |
| :---: | :---: | :---: | :---: | :---: |
|  |  | - | - |  |
| 66.007 | 26.007 | 21.595 | 0.542 | 21.613 |
|  |  | - | - |  |
| 66.007 | 25.664 | 21.591 | 0.545 | 21.609 |
|  |  | - | - |  |
| 66.007 | 25.321 | 21.577 | 0.560 | 21.597 |
|  |  | - |  |  |
| 66.007 | 24.977 | 21.551 | 0.576 | 21.572 |
|  |  | - | - |  |
| 66.007 | 24.634 | 21.535 | 0.593 | 21.558 |
|  |  | - | - |  |
| 66.007 | 24.291 | 21.539 | 0.596 | 21.561 |
|  |  | - | - |  |
| 66.007 | 23.948 | 21.547 | 0.594 | 21.567 |
|  |  | - | - |  |
| 66.007 | 23.605 | 21.558 | 0.591 | 21.577 |
|  |  | - | - |  |
| 66.007 | 23.261 | 21.548 | 0.585 | 21.565 |
|  |  | - | - |  |
| 66.007 | 22.918 | 21.524 | 0.575 | 21.542 |
|  |  | - | - |  |
| 66.007 | 22.575 | 21.499 | 0.566 | 21.517 |
|  |  | - | - |  |
| 66.007 | 22.232 | 21.479 | 0.558 | 21.496 |
|  |  | - | - |  |
| 66.007 | 21.888 | 21.466 | 0.551 | 21.482 |
|  |  | - | - |  |
| 66.007 | 21.545 | 21.456 | 0.546 | 21.471 |
|  |  | - | - |  |
| 66.007 | 21.202 | 21.439 | 0.536 | 21.454 |
|  |  | - | - |  |
| 66.007 | 20.859 | 21.421 | 0.524 | 21.435 |
|  |  | - | - |  |
| 66.007 | 20.515 | 21.402 | 0.510 | 21.416 |
| 66.007 | 20.172 | 21.382 | 0.494 | 21.396 |
|  |  | - | - |  |
| 66.007 | 19.829 | 21.358 | 0.468 | 21.370 |
|  |  | - | - |  |
| 66.007 | 19.486 | 21.336 | 0.440 | 21.347 |
|  |  | - | - |  |
| 66.007 | 19.142 | 21.319 | 0.413 | 21.329 |
|  |  | - | - |  |
| 66.007 | 18.799 | 21.338 | 0.380 | 21.348 |
|  |  | - | - |  |
| 66.007 | 18.456 | 21.356 | 0.348 | 21.365 |
|  |  | - | - |  |
| 66.007 | 18.113 | 21.374 | 0.318 | 21.383 |
|  |  | - | - |  |
| 66.007 | 17.770 | 21.368 | 0.328 | 21.377 |
|  |  | - | - |  |
| 66.007 | 17.426 | 21.368 | 0.341 | 21.379 |


|  |  | - | - |  |
| :---: | :---: | :---: | :---: | :---: |
| 66.007 | 17.083 | 21.361 | 0.351 | 21.373 |
| 66.007 | 16.740 | 21.329 | 0.339 | 21.341 |
|  |  | - | - |  |
| 66.007 | 16.397 | 21.289 | 0.325 | 21.300 |
|  |  | - | - |  |
| 66.007 | 16.053 | 21.255 | 0.312 | 21.266 |
|  |  | - | - |  |
| 66.007 | 15.710 | 21.234 | 0.320 | 21.244 |
|  |  | - | - |  |
| 66.007 | 15.367 | 21.216 | 0.332 | 21.227 |
|  |  | - | - |  |
| 66.007 | 15.024 | 21.196 | 0.344 | 21.208 |
|  |  | - | - |  |
| 66.007 | 14.680 | 21.185 | 0.352 | 21.198 |
| 66.007 | 14.337 | 21.172 | 0.357 | 21.185 |
| 66.007 | 13.994 | 21.164 | 0.363 | 21.178 |
| 66.007 | 13.651 | 21.170 | 0.359 | 21.184 |
|  |  | - | - |  |
| 66.007 | 13.307 | 21.184 | 0.351 | 21.197 |
| 66.007 | 12.964 | 21.198 | 0.341 | 21.211 |
| 66.007 | 12.621 | 21.193 | 0.329 | 21.205 |
| 66.007 | 12.278 | 21.171 | 0.314 | 21.183 |
| 66.007 | 11.934 | 21.151 | 0.300 | 21.163 |

Table A 10 Cross sectional velocity profile for 50 Hz .

| 50HZ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \mathrm{X} \\ (\mathrm{~mm}) \end{gathered}$ | $\begin{gathered} \mathrm{Z} \\ (\mathrm{~mm}) \end{gathered}$ | $\begin{gathered} \mathrm{U} \\ (\mathrm{~m} / \mathrm{s}) \end{gathered}$ | $\begin{gathered} \mathrm{V} \\ (\mathrm{~m} / \mathrm{s}) \end{gathered}$ | Vel. Mag (m/s) |
| - |  |  |  |  |
| 68.048 | 27.293 | 24.364 | 0.134 | 24.370 |
|  |  | - | - |  |
| 68.048 | 26.965 | 24.717 | 0.187 | 24.724 |
|  |  | - | - |  |
| 68.048 | 26.636 | 25.063 | 0.508 | 25.072 |
|  |  | - | - |  |
| 68.048 | 26.308 | 25.199 | 0.756 | 25.212 |
|  |  | - | - |  |
| 68.048 | 25.979 | 25.236 | 0.963 | 25.257 |
| 68.048 | 25.651 | 25.273 | 1.169 | 25.302 |


| 68.048 | 25.323 | 2 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: |
|  |  | - | - |  |
| 68.048 | 24.994 | 25.116 | 1.788 | 25.187 |
|  |  | - | - |  |
| 68.048 | 24.666 | 24.922 | 2.130 | 25.019 |
|  |  | - | - |  |
| 68.048 | 24.338 | 24.764 | 2.349 | 24.878 |
|  |  | - | - |  |
| 68.048 | 24.009 | 24.466 | 2.046 | 24.556 |
|  |  | - | - |  |
| 68.048 | 23.681 | 24.158 | 1.755 | 24.226 |
|  |  | - | - |  |
| 68.048 | 23.352 | 23.866 | 1.441 | 23.912 |
|  |  | - | - |  |
| 68.048 | 23.024 | 23.902 | 1.303 | 23.940 |
|  |  | - | - |  |
| 68.048 | 22.696 | 23.999 | 1.177 | 24.030 |
|  |  | - | - |  |
| 68.048 | 22.367 | 24.091 | 1.051 | 24.115 |
|  |  | - | - |  |
| 68.048 | 22.039 | 24.031 | 1.038 | 24.055 |
|  |  | - | - |  |
| 68.048 | 21.711 | 24.034 | 0.999 | 24.055 |
|  |  | - | - |  |
| 68.048 | 21.382 | 24.036 | 0.960 | 24.056 |
|  |  | - | - |  |
| 68.048 | 21.054 | 23.948 | 0.931 | 23.967 |
|  |  | - | - |  |
| 68.048 | 20.725 | 23.795 | 0.744 | 23.809 |
|  |  | - | - |  |
| 68.048 | 20.397 | 23.642 | 0.556 | 23.651 |
|  |  | - | - |  |
| 68.048 | 20.069 | 23.558 | 0.408 | 23.563 |
|  |  | - | - |  |
| 68.048 | 19.740 | 23.592 | 0.363 | 23.595 |
|  |  | - | - |  |
| 68.048 | 19.412 | 23.626 | 0.329 | 23.629 |
| 68.048 | 19.083 | 23.658 | 0.273 | 23.660 |
|  |  | - | - |  |
| 68.048 | 18.755 | 23.516 | 0.525 | 23.526 |
|  |  | - | - |  |
| 68.048 | 18.427 | 23.286 | 0.771 | 23.302 |
|  |  | - | - |  |
| 68.048 | 18.098 | 23.066 | 1.021 | 23.090 |
|  |  | - | - |  |
| 68.048 | 17.770 | 23.179 | 1.190 | 23.210 |
|  |  | - | - |  |
| 68.048 | 17.442 | 23.384 | 1.293 | 23.420 |
|  |  | - | - |  |
| 68.048 | 17.113 | 23.588 | 1.395 | 23.630 |
|  |  | - | - |  |
| 68.048 | 16.785 | 23.739 | 1.494 | 23.787 |


| 68.048 | 16.456 |  |  | 23.996 |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 23.940 | 1.613 |  |
|  |  |  |  |  |
| 68.048 | 16.128 | 24.141 | 1.732 | 24.204 |
|  |  | - | - |  |
| 68.048 | 15.800 | 24.294 | 1.820 | 24.362 |
|  |  | - | - |  |
| 68.048 | 15.471 | 24.382 | 1.924 | 24.459 |
|  |  | - | - |  |
| 68.048 | 15.143 | 24.471 | 2.039 | 24.556 |
|  |  | - | - |  |
| 68.048 | 14.814 | 24.560 | 2.130 | 24.652 |
|  |  | - | - |  |
| 68.048 | 14.486 | 24.619 | 2.153 | 24.713 |
|  |  | - | - |  |
| 68.048 | 14.158 | 24.651 | 2.143 | 24.744 |
|  |  | - | - |  |
| 68.048 | 13.829 | 24.687 | 2.138 | 24.780 |
|  |  | - | - |  |
| 68.048 | 13.501 | 24.633 | 1.957 | 24.714 |
|  |  | - | - |  |
| 68.048 | 13.173 | 24.508 | 1.638 | 24.568 |
| 68.048 | 12.844 | 24.383 | 1.319 | 24.422 |
|  |  | - | - |  |
| 68.048 | 12.516 | 24.208 | 1.047 | 24.233 |
|  |  | - | - |  |
| 68.048 | 12.187 | 24.104 | 1.025 | 24.128 |
|  |  | - | - |  |
| 68.048 | 11.859 | 23.999 | 1.003 | 24.023 |
|  |  | - | - |  |
| 68.048 | 11.531 | 23.892 | 0.893 | 23.911 |

Table A 11 Cross sectional velocity profile for 60 Hz .

| 60HZ | $\begin{gathered} \mathrm{Z} \\ (\mathrm{~mm}) \end{gathered}$ | $\begin{gathered} \mathrm{U} \\ (\mathrm{~m} / \mathrm{s}) \end{gathered}$ | $\begin{gathered} \mathrm{V} \\ (\mathrm{~m} / \mathrm{s}) \end{gathered}$ | Vel. Mag$(\mathrm{m} / \mathrm{s})$ |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \mathrm{X} \\ (\mathrm{~mm}) \end{gathered}$ |  |  |  |  |
| 66.177 |  | - | - |  |
|  | 28.113 | 29.328 | 0.737 | 29.337 |
|  |  | - | - |  |
| 66.177 | 27.799 | 29.465 | 0.864 | 29.479 |
|  |  | - | - |  |
| 66.177 | 27.484 | 29.646 | 1.055 | 29.667 |
|  |  | - | - |  |
| 66.177 | 27.170 | 29.810 | 1.221 | 29.837 |
|  |  | - | - |  |
| 66.177 | 26.855 | 29.780 | 1.210 | 29.807 |
|  |  | - | - |  |
| 66.177 | 26.540 | 29.640 | 1.052 | 29.660 |
|  |  | - | - |  |
| 66.177 | 26.226 | 29.499 | 0.895 | 29.514 |


| 66.177 | 25.911 | 29.401 | 0.805 | 29.413 |
| :---: | :---: | :---: | :---: | :---: |
|  |  | - | - |  |
| 66.177 | 25.596 | 29.283 | 0.591 | 29.291 |
|  |  | - | - |  |
| 66.177 | 25.282 | 29.167 | 0.374 | 29.172 |
|  |  | - | - |  |
| 66.177 | 24.967 | 29.048 | 0.162 | 29.048 |
|  |  | - | - |  |
| 66.177 | 24.653 | 29.032 | 0.116 | 29.032 |
|  |  | - | - |  |
| 66.177 | 24.338 | 29.009 | 0.084 | 29.009 |
|  |  | - | - |  |
| 66.177 | 24.023 | 28.986 | 0.052 | 28.986 |
|  |  | - | - |  |
| 66.177 | 23.709 | 29.017 | 0.054 | 29.017 |
|  |  | - | - |  |
| 66.177 | 23.394 | 28.949 | 0.045 | 28.949 |
|  |  | - | - |  |
| 66.177 | 23.079 | 28.881 | 0.036 | 28.881 |
|  |  | - | - |  |
| 66.177 | 22.765 | 28.858 | 0.027 | 28.858 |
|  |  | - |  |  |
| 66.177 | 22.450 | 28.654 | 0.065 | 28.654 |
|  |  | - |  |  |
| 66.177 | 22.135 | 28.439 | 0.107 | 28.440 |
|  |  | - |  |  |
| 66.177 | 21.821 | 28.230 | 0.178 | 28.232 |
|  |  |  |  |  |
| 66.177 | 21.506 | 28.383 | 0.370 | 28.388 |
|  |  | - |  |  |
| 66.177 | 21.192 | 28.645 | 0.689 | 28.658 |
|  |  | - |  |  |
| 66.177 | 20.877 | 28.908 | 1.008 | 28.928 |
|  |  | - |  |  |
| 66.177 | 20.562 | 29.062 | 1.082 | 29.083 |
| 66.177 | 20.248 | 29.066 | 0.847 | 29.081 |
|  |  | - |  |  |
| 66.177 | 19.933 | 29.092 | 0.597 | 29.101 |
|  |  | - |  |  |
| 66.177 | 19.618 | 29.059 | 0.386 | 29.062 |
|  |  | - |  |  |
| 66.177 | 19.304 | 28.739 | 0.355 | 28.741 |
|  |  | - |  |  |
| 66.177 | 18.989 | 28.388 | 0.315 | 28.390 |
|  |  | - |  |  |
| 66.177 | 18.674 | 28.039 | 0.276 | 28.040 |
|  |  | - |  |  |
| 66.177 | 18.360 | 27.960 | 0.288 | 27.962 |
|  |  | - |  |  |
| 66.177 | 18.045 | 28.053 | 0.408 | 28.057 |
|  |  | - |  |  |
| 66.177 | 17.731 | 28.147 | 0.527 | 28.152 |


| 66.177 | 17.416 | 28.247 | 0.557 | 28.253 |
| :---: | :---: | :---: | :---: | :---: |
|  |  | - |  |  |
| 66.177 | 17.101 | 28.325 | 0.428 | 28.330 |
| 66.177 | 16.787 | 28.411 | 0.294 | 28.414 |
|  |  | - |  |  |
| 66.177 | 16.472 | 28.491 | 0.163 | 28.492 |
| 66.177 | 16.157 | $-\quad-$ | - |  |
|  |  | - | - | 28.570 |
| 66.177 | 15.843 | 28.747 | 0.010 | 28.749 |
| 66.177 | 15.528 | - | - | - |
|  |  | - | - |  |
| 66.177 | 15.214 | 28.903 | 0.137 | 28.905 |
|  |  | - | - |  |
| 66.177 | 14.899 | 28.884 | 0.014 | 28.886 |
|  |  | - |  |  |
| 66.177 | 14.584 | 28.882 | 0.126 | 28.884 |
| 66.177 | 14.270 | 28.807 | 0.193 | 28.807 |
|  |  | - |  |  |
| 66.177 | 13.955 | 28.956 | 0.016 | 28.957 |
| 66.177 | 13.640 | 28.981 | 0.137 | 28.983 |
| 66.177 | 13.326 | 29.032 | 0.295 | 29.034 |
| 66.177 | 13.011 | 29.252 | 0.568 | 29.261 |
| 66.177 | 12.696 | 29.550 | 1.044 | 29.577 |

Table A 12 Wind tunnel calibration re-check with pitot probe.

| Frequency <br> $(\mathrm{Hz})$ | DeltaP <br> (in H20) | Vpitot <br> $(\mathrm{m} / \mathrm{s})$ | Vcalib <br> $(\mathrm{m} / \mathrm{s})$ |
| :---: | :---: | :---: | :---: |
| 23.5 | 0.27 | 10.56 | 11.5 |
| 23.5 | 0.27 | 10.56 | 11.5 |
| 23.5 | 0.27 | 10.56 | 11.5 |
| 23.5 | 0.27 | 10.56 | 11.5 |
| avg | 0.27 | 10.56 | 11.5 |
| stdev | 0 | 0 | 0 |
| 30.6 | 0.49 | 14.24 | 15 |
| 30.6 | 0.48 | 14.09 | 15 |
| 30.6 | 0.49 | 14.24 | 15 |
| 30.6 | 0.48 | 14.09 | 15 |
| avg | 0.49 | 14.17 | 15 |
| stdev | 0.0058 | 0.0866 | 0 |

Table A 13 Image variance of PIV measurements for $\mathrm{q}=78$.

| Images | $X(\mathrm{~mm})$ | $Y(\mathrm{~mm})$ | Vel. Mag <br> $(\mathrm{m} / \mathrm{s})$ | U <br> $(\mathrm{m} / \mathrm{s})$ | $\mathrm{V}(\mathrm{m} / \mathrm{s})$ | \% Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 149.415 | 192.541 | 11.737 | 0.643 | 11.695 |  |
| 100 | 149.415 | 192.541 | 10.469 | 0.332 | 10.425 | 12.110 |
| 150 | 149.415 | 192.541 | 10.532 | 0.272 | 10.481 | 0.598 |
| 200 | 149.415 | 192.541 | 10.630 | 0.204 | 10.567 | 0.924 |
| 250 | 149.415 | 192.541 | 10.598 | 0.137 | 10.534 | -0.309 |
| 300 | 149.415 | 192.541 | 10.491 | 0.120 | 10.430 | -1.019 |
|  |  |  | 10.743 | 0.284 | 10.688 | -2.383 |
|  |  |  | 0.491 | 0.193 | 0.496 | 5.491 |


| Images | $X(\mathrm{~mm})$ | $Y(\mathrm{~mm})$ | Vel. Mag <br> $(\mathrm{m} / \mathrm{s})$ | U <br> $(\mathrm{m} / \mathrm{s})$ | $\mathrm{V}(\mathrm{m} / \mathrm{s})$ | \% Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 152.064 | 180.178 | 11.856 | 0.096 | 11.782 |  |
| 100 | 152.064 | 180.178 | 10.885 | 0.003 | 10.722 | -8.924 |
| 150 | 152.064 | 180.178 | 10.851 | 0.110 | 10.682 | -0.313 |
| 200 | 152.064 | 180.178 | 10.975 | 0.278 | 10.801 | 1.128 |
| 250 | 152.064 | 180.178 | 11.047 | 0.063 | 10.864 | 0.656 |
| 300 | 152.064 | 180.178 | 10.953 | 0.022 | 10.785 | -0.858 |
|  |  |  | 11.095 | 0.095 | 10.939 | -1.662 |
|  |  |  | 0.380 | 0.099 | 0.418 | 4.134 |


| Images | $X(\mathrm{~mm})$ | $Y(\mathrm{~mm})$ | Vel. Mag <br> $(\mathrm{m} / \mathrm{s})$ | U <br> $(\mathrm{m} / \mathrm{s})$ | $\mathrm{V}(\mathrm{m} / \mathrm{s})$ | \% Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 149.268 | 160.309 | 10.805 | 0.922 | 10.691 |  |
| 100 | 149.268 | 160.309 | 10.447 | 0.121 | 10.299 | -3.422 |
| 150 | 149.268 | 160.309 | 10.340 | 0.291 | 10.171 | -1.041 |
| 200 | 149.268 | 160.309 | 10.458 | 0.322 | 10.304 | 1.130 |
| 250 | 149.268 | 160.309 | 10.294 | 0.328 | 10.135 | -1.589 |
| 300 | 149.268 | 160.309 | 10.439 | 0.285 | 10.277 | 1.389 |
|  |  |  | 10.464 | 0.378 | 10.313 | -0.707 |
|  |  |  | 0.180 | 0.277 | 0.198 | 2.002 |


| Field |  |
| :---: | :---: |
| Average <br> Velocity <br> $(\mathrm{m} / \mathrm{s})$ | Deviation |
| 10.628 | 0.283 |

Table A 14 Image variance of PIV measurements for $\mathrm{q}=44$.

| Images | $X(\mathrm{~mm})$ | $Y(\mathrm{~mm})$ | Vel. Mag <br> $(\mathrm{m} / \mathrm{s})$ | $\mathrm{U}(\mathrm{m} / \mathrm{s})$ | $\mathrm{V}(\mathrm{m} / \mathrm{s})$ | \% Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 149.415 | 192.541 | 15.284 | 0.748 | 15.146 |  |
|  |  |  |  |  |  | - |
| 100 | 149.415 | 192.541 | 13.688 | 0.784 | 13.481 | 11.664 |
| 150 | 149.415 | 192.541 | 13.993 | 0.663 | 13.798 | 2.178 |
| 200 | 149.415 | 192.541 | 13.635 | 0.255 | 13.445 | -2.624 |
| 250 | 149.415 | 192.541 | 13.622 | 0.262 | 13.433 | -0.090 |
| 300 | 149.415 | 192.541 | 13.549 | 0.305 | 13.362 | -0.542 |
|  |  |  | 13.962 | 0.503 | 13.778 | -2.549 |
|  |  |  | 0.666 | 0.254 | 0.688 | 5.374 |


|  |  |  | Vel. Mag |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Images | $X(\mathrm{~mm})$ | $Y(\mathrm{~mm})$ | $(\mathrm{m} / \mathrm{s})$ | $\mathrm{U} / \mathrm{s})$ | $V(\mathrm{~m} / \mathrm{s})$ | \% Diff. |
| 50 | 152.064 | 180.178 | 13.456 | 0.185 | 13.315 |  |
| 100 | 152.064 | 180.178 | 13.264 | 0.276 | 13.116 | -1.445 |
| 150 | 152.064 | 180.178 | 13.841 | 0.368 | 13.687 | 4.168 |
| 200 | 152.064 | 180.178 | 13.798 | 0.350 | 13.647 | -0.308 |
| 250 | 152.064 | 180.178 | 13.805 | 0.096 | 13.644 | 0.047 |
| 300 | 152.064 | 180.178 | 13.904 | 0.141 | 13.748 | 0.713 |
|  |  |  | 13.678 | 0.236 | 13.526 | 0.635 |
|  |  |  | 0.257 | 0.112 | 0.252 | 2.124 |


| Images | $X(\mathrm{~mm})$ | $Y(\mathrm{~mm})$ | Vel. Mag <br> $(\mathrm{m} / \mathrm{s})$ | $\mathrm{U}(\mathrm{m} / \mathrm{s})$ | $V(\mathrm{~m} / \mathrm{s})$ | \% Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 149.268 | 160.309 | 15.860 | 0.860 | 15.723 |  |
| 100 | 149.268 | 160.309 | 15.475 | 0.077 | 15.285 | -2.486 |
| 150 | 149.268 | 160.309 | 14.900 | 0.284 | 14.716 | -3.860 |
| 200 | 149.268 | 160.309 | 14.566 | 0.183 | 14.375 | -2.297 |
| 250 | 149.268 | 160.309 | 14.524 | 0.237 | 14.354 | -0.286 |
| 300 | 149.268 | 160.309 | 14.260 | 0.002 | 14.037 | -1.853 |
|  |  |  | 14.931 | 0.274 | 14.748 | -2.156 |
|  |  |  | 0.618 | 0.305 | 0.639 | 1.287 |


| Field |  |
| :---: | :---: |
| Average |  |
| Velocity |  |
| $(\mathrm{m} / \mathrm{s})$ | Deviation |
| 13.904 | $(\mathrm{~m} / \mathrm{s})$ |

Table A 15 Repeatability of PIV images for $q=78$.
Trial 1


Trial 2

|  | Images | X | Y | $\begin{aligned} & \text { Vel. Mag } \\ & (\mathrm{m} / \mathrm{s}) \end{aligned}$ | $\mathrm{U}(\mathrm{m} / \mathrm{s})$ | $\begin{gathered} \mathrm{V} \\ (\mathrm{~m} / \mathrm{s}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 300 | 149.415 | 192.541 | 10.825 | 0.586 | 10.346 |
|  | 300 | 152.064 | 180.178 | 10.690 | 0.100 | 10.542 |
|  | 300 | 149.268 | 160.309 | 11.261 | 0.201 | 11.090 |
| avg. |  |  |  | 10.925 |  |  |
|  | Difference $2.723$ |  |  |  |  |  |

Table A 16 Repeatability of PIV images for $q=44$.
Trial1

| Images | $X$ | $Y$ | Vel. Mag <br> $(\mathrm{m} / \mathrm{s})$ | $\mathrm{U}(\mathrm{m} / \mathrm{s})$ | $\mathrm{V}(\mathrm{m} / \mathrm{s})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 300 | 149.415 | 192.541 | 13.549 | 0.305 | 13.362 |
| 300 | 152.064 | 180.178 | 13.904 | 0.141 | 13.748 |
| 300 | 149.268 | 160.309 | 14.260 | 0.002 | 14.037 |
|  |  |  | 13.904 |  |  |

Trial2

|  | Images | X | Y | $\begin{gathered} \hline \text { Vel. Mag } \\ (\mathrm{m} / \mathrm{s}) \end{gathered}$ | $\mathrm{U}(\mathrm{m} / \mathrm{s})$ | V (m/s) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 300 | 149.415 | 192.541 | 13.500 | 0.595 | 13.056 |
|  | 300 | 152.064 | 180.178 | 13.260 | 0.699 | 12.984 |
|  | 300 | 149.268 | 160.309 | 13.817 | 0.694 | 13.461 |
| avg. |  |  |  | 13.526 |  |  |
|  | Difference |  |  |  |  |  |
|  | -2.724 |  |  |  |  |  |

Table A 17 Side velocity profile for $\mathrm{q}=78$, at $\mathrm{Y} / \mathrm{d}=2$.

| X (mm) | Y (mm) | X/d | Y/d | Vel. Mag. $(\mathrm{m} / \mathrm{s})$ | Defect |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 153.0946 | 195.0428 | 2 | -1.771 | 9.849 | 0.929 |
| 153.0946 | 194.8823 | 2 | -1.691 | 9.853 | 0.929 |
| 153.0946 | 194.7217 | 2 | -1.611 | 9.848 | 0.929 |
| 153.0946 | 194.5611 | 2 | -1.531 | 9.769 | 0.922 |
| 153.0946 | 194.4006 | 2 | -1.450 | 9.690 | 0.914 |
| 153.0946 | 194.24 | 2 | -1.370 | 9.610 | 0.907 |
| 153.0946 | 194.0795 | 2 | -1.290 | 9.531 | 0.899 |
| 153.0946 | 193.9189 | 2 | -1.209 | 9.451 | 0.892 |
| 153.0946 | 193.7584 | 2 | -1.129 | 9.372 | 0.884 |
| 153.0946 | 193.5978 | 2 | -1.049 | 9.342 | 0.881 |
| 153.0946 | 193.4372 | 2 | -0.969 | 9.341 | 0.881 |
| 153.0946 | 193.2767 | 2 | -0.888 | 9.341 | 0.881 |
| 153.0946 | 193.1161 | 2 | -0.808 | 9.341 | 0.881 |
| 153.0946 | 192.9556 | 2 | -0.728 | 9.341 | 0.881 |
| 153.0946 | 192.795 | 2 | -0.647 | 9.341 | 0.881 |
| 153.0946 | 192.6344 | 2 | -0.567 | 9.345 | 0.882 |
| 153.0946 | 192.4739 | 2 | -0.487 | 9.371 | 0.884 |
| 153.0946 | 192.3133 | 2 | -0.407 | 9.398 | 0.887 |
| 153.0946 | 192.1528 | 2 | -0.326 | 9.424 | 0.889 |
| 153.0946 | 191.9922 | 2 | -0.246 | 9.451 | 0.892 |
| 153.0946 | 191.8316 | 2 | -0.166 | 9.454 | 0.892 |
| 153.0946 | 191.6711 | 2 | -0.086 | 9.454 | 0.892 |
| 153.0946 | 191.5105 | 2 | -0.005 | 9.454 | 0.892 |
| 153.0946 | 191.35 | 2 | 0.075 | 9.454 | 0.892 |
| 153.0946 | 191.1894 | 2 | 0.155 | 9.454 | 0.892 |
| 153.0946 | 191.0289 | 2 | 0.236 | 9.454 | 0.892 |
| 153.0946 | 190.8683 | 2 | 0.316 | 9.456 | 0.892 |
| 153.0946 | 190.7077 | 2 | 0.396 | 9.463 | 0.893 |
| 153.0946 | 190.5472 | 2 | 0.476 | 9.470 | 0.893 |
| 153.0946 | 190.3866 | 2 | 0.557 | 9.477 | 0.894 |
| 153.0946 | 190.2261 | 2 | 0.637 | 9.484 | 0.895 |
| 153.0946 | 190.0655 | 2 | 0.717 | 9.491 | 0.895 |
| 153.0946 | 189.9049 | 2 | 0.798 | 9.498 | 0.896 |
| 153.0946 | 189.7444 | 2 | 0.878 | 9.508 | 0.897 |
| 153.0946 | 189.5838 | 2 | 0.958 | 9.518 | 0.898 |
| 153.0946 | 189.4233 | 2 | 1.038 | 9.528 | 0.899 |
| 153.0946 | 189.2627 | 2 | 1.119 | 9.537 | 0.900 |
| 153.0946 | 189.1022 | 2 | 1.199 | 9.545 | 0.900 |
| 153.0946 | 188.9416 | 2 | 1.279 | 9.552 | 0.901 |
| 153.0946 | 188.781 | 2 | 1.359 | 9.559 | 0.902 |
| 153.0946 | 188.6205 | 2 | 1.440 | 9.566 | 0.902 |
| 153.0946 | 188.4599 | 2 | 1.520 | 9.573 | 0.903 |
| 153.0946 | 188.2994 | 2 | 1.600 | 9.580 | 0.904 |


| 153.0946 | 188.1388 | 2 | 1.681 | 9.603 | 0.906 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 153.0946 | 187.9782 | 2 | 1.761 | 9.701 | 0.915 |
| 153.0946 | 187.8177 | 2 | 1.841 | 9.799 | 0.924 |
| 153.0946 | 187.6571 | 2 | 1.921 | 9.897 | 0.934 |
| 153.0946 | 187.4966 | 2 | 2.002 | 9.994 | 0.943 |
| 153.0946 | 187.336 | 2 | 2.082 | 10.092 | 0.952 |
| 153.0946 | 187.1755 | 2 | 2.162 | 10.190 | 0.961 |
| 153.0946 | 187.0149 | 2 | 2.243 | 10.205 | 0.963 |
| 153.0946 | 186.8543 | 2 | 2.323 | 10.185 | 0.961 |
| 153.0946 | 186.6938 | 2 | 2.403 | 10.165 | 0.959 |
| 153.0946 | 186.5332 | 2 | 2.483 | 10.146 | 0.957 |
| 153.0946 | 186.3727 | 2 | 2.564 | 10.177 | 0.960 |
| 153.0946 | 186.2121 | 2 | 2.644 | 10.275 | 0.969 |
| 153.0946 | 186.0515 | 2 | 2.724 | 10.373 | 0.979 |
| 153.0946 | 185.891 | 2 | 2.805 | 10.470 | 0.988 |
| 153.0946 | 185.7304 | 2 | 2.885 | 10.568 | 0.997 |
| 153.0946 | 185.5699 | 2 | 2.965 | 10.666 | 1.006 |
| 153.0946 | 185.4093 | 2 | 3.045 | 10.764 | 1.015 |
| 153.0946 | 185.2488 | 2 | 3.126 | 10.777 | 1.017 |
| 153.0946 | 185.0882 | 2 | 3.206 | 10.787 | 1.018 |
| 153.0946 | 184.9276 | 2 | 3.286 | 10.798 | 1.019 |
| 153.0946 | 184.7671 | 2 | 3.366 | 10.808 | 1.020 |
| 153.0946 | 184.6065 | 2 | 3.447 | 10.818 | 1.021 |
| 153.0946 | 184.446 | 2 | 3.527 | 10.828 | 1.021 |
| 153.0946 | 184.2854 | 2 | 3.607 | 10.834 | 1.022 |
| 153.0946 | 184.1248 | 2 | 3.688 | 10.835 | 1.022 |
| 153.0946 | 183.9643 | 2 | 3.768 | 10.836 | 1.022 |
| 153.0946 | 183.8037 | 2 | 3.848 | 10.838 | 1.022 |
| 153.0946 | 183.6432 | 2 | 3.928 | 10.841 | 1.023 |
| 153.0946 | 183.4826 | 2 | 4.009 | 10.851 | 1.024 |
| 153.0946 | 183.3221 | 2 | 4.089 | 10.861 | 1.025 |
| 153.0946 | 183.1615 | 2 | 4.169 | 10.871 | 1.026 |
| 153.0946 | 183.0009 | 2 | 4.250 | 10.881 | 1.027 |
| 153.0946 | 182.8404 | 2 | 4.330 | 10.891 | 1.027 |
| 153.0946 | 182.6798 | 2 | 4.410 | 10.902 | 1.028 |
| 153.0946 | 182.5193 | 2 | 4.490 | 10.882 | 1.027 |
| 153.0946 | 182.3587 | 2 | 4.571 | 10.852 | 1.024 |
| 153.0946 | 182.1981 | 2 | 4.651 | 10.823 | 1.021 |
| 153.0946 | 182.0376 | 2 | 4.731 | 10.793 | 1.018 |
| 153.0946 | 181.877 | 2 | 4.811 | 10.763 | 1.015 |
| 153.0946 | 181.7165 | 2 | 4.892 | 10.733 | 1.013 |
| 153.0946 | 181.5559 | 2 | 4.972 | 10.713 | 1.011 |
| 153.0946 | 181.3954 | 2 | 5.052 | 10.722 | 1.012 |
| 152 |  |  |  |  |  |

Table A 18 Side velocity profile for $\mathrm{q}=78$, at $\mathrm{Y} / \mathrm{d}=4$.

| X (mm) | Y (mm) | X/d | Y/d | Vel. Mag. (m/s) | Defect |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 148.9736 | 195.0428 | 4 | -1.771 | 10.694 | 1.009 |
| 148.9736 | 194.8882 | 4 | -1.694 | 10.692 | 1.009 |
| 148.9736 | 194.7336 | 4 | -1.617 | 10.689 | 1.008 |
| 148.9736 | 194.579 | 4 | -1.539 | 10.686 | 1.008 |
| 148.9736 | 194.4244 | 4 | -1.462 | 10.684 | 1.008 |
| 148.9736 | 194.2698 | 4 | -1.385 | 10.681 | 1.008 |
| 148.9736 | 194.1151 | 4 | -1.308 | 10.679 | 1.007 |
| 148.9736 | 193.9605 | 4 | -1.230 | 10.677 | 1.007 |
| 148.9736 | 193.8059 | 4 | -1.153 | 10.679 | 1.007 |
| 148.9736 | 193.6513 | 4 | -1.076 | 10.681 | 1.008 |
| 148.9736 | 193.4967 | 4 | -0.998 | 10.685 | 1.008 |
| 148.9736 | 193.3421 | 4 | -0.921 | 10.678 | 1.007 |
| 148.9736 | 193.1875 | 4 | -0.844 | 10.639 | 1.004 |
| 148.9736 | 193.0329 | 4 | -0.766 | 10.600 | 1.000 |
| 148.9736 | 192.8783 | 4 | -0.689 | 10.560 | 0.996 |
| 148.9736 | 192.7236 | 4 | -0.612 | 10.521 | 0.993 |
| 148.9736 | 192.569 | 4 | -0.535 | 10.482 | 0.989 |
| 148.9736 | 192.4144 | 4 | -0.457 | 10.443 | 0.985 |
| 148.9736 | 192.2598 | 4 | -0.380 | 10.403 | 0.981 |
| 148.9736 | 192.1052 | 4 | -0.303 | 10.364 | 0.978 |
| 148.9736 | 191.9506 | 4 | -0.225 | 10.325 | 0.974 |
| 148.9736 | 191.796 | 4 | -0.148 | 10.286 | 0.970 |
| 148.9736 | 191.6414 | 4 | -0.071 | 10.247 | 0.967 |
| 148.9736 | 191.4867 | 4 | 0.007 | 10.207 | 0.963 |
| 148.9736 | 191.3321 | 4 | 0.084 | 10.168 | 0.959 |
| 148.9736 | 191.1775 | 4 | 0.161 | 10.149 | 0.957 |
| 148.9736 | 191.0229 | 4 | 0.239 | 10.152 | 0.958 |
| 148.9736 | 190.8683 | 4 | 0.316 | 10.164 | 0.959 |
| 148.9736 | 190.7137 | 4 | 0.393 | 10.186 | 0.961 |
| 148.9736 | 190.5591 | 4 | 0.470 | 10.218 | 0.964 |
| 148.9736 | 190.4045 | 4 | 0.548 | 10.267 | 0.969 |
| 148.9736 | 190.2499 | 4 | 0.625 | 10.316 | 0.973 |
| 148.9736 | 190.0952 | 4 | 0.702 | 10.366 | 0.978 |
| 148.9736 | 189.9406 | 4 | 0.780 | 10.415 | 0.983 |
| 148.9736 | 189.786 | 4 | 0.857 | 10.464 | 0.987 |
| 148.9736 | 189.6314 | 4 | 0.934 | 10.514 | 0.992 |
| 148.9736 | 189.4768 | 4 | 1.012 | 10.563 | 0.997 |
| 148.9736 | 189.3222 | 4 | 1.089 | 10.612 | 1.001 |
| 148.9736 | 189.1676 | 4 | 1.166 | 10.662 | 1.006 |
| 148.9736 | 189.013 | 4 | 1.244 | 10.711 | 1.010 |
| 148.9736 | 188.8583 | 4 | 1.321 | 10.761 | 1.015 |
| 148.9736 | 188.7037 | 4 | 1.398 | 10.810 | 1.020 |
| 148.9736 | 188.5491 | 4 | 1.475 | 10.859 | 1.024 |
| 148.9736 | 188.3945 | 4 | 1.553 | 10.893 | 1.028 |


| 148.9736 | 188.2399 | 4 | 1.630 | 10.915 | 1.030 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 148.9736 | 188.0853 | 4 | 1.707 | 10.936 | 1.032 |
| 148.9736 | 187.9307 | 4 | 1.785 | 10.958 | 1.034 |
| 148.9736 | 187.7761 | 4 | 1.862 | 10.969 | 1.035 |
| 148.9736 | 187.6215 | 4 | 1.939 | 10.967 | 1.035 |
| 148.9736 | 187.4668 | 4 | 2.017 | 10.966 | 1.035 |
| 148.9736 | 187.3122 | 4 | 2.094 | 10.965 | 1.034 |
| 148.9736 | 187.1576 | 4 | 2.171 | 10.964 | 1.034 |
| 148.9736 | 187.003 | 4 | 2.248 | 10.962 | 1.034 |
| 148.9736 | 186.8484 | 4 | 2.326 | 10.961 | 1.034 |
| 148.9736 | 186.6938 | 4 | 2.403 | 10.960 | 1.034 |
| 148.9736 | 186.5392 | 4 | 2.480 | 10.959 | 1.034 |
| 148.9736 | 186.3846 | 4 | 2.558 | 10.957 | 1.034 |
| 148.9736 | 186.2299 | 4 | 2.635 | 10.956 | 1.034 |
| 148.9736 | 186.0753 | 4 | 2.712 | 10.955 | 1.033 |
| 148.9736 | 185.9207 | 4 | 2.790 | 10.954 | 1.033 |
| 148.9736 | 185.7661 | 4 | 2.867 | 10.952 | 1.033 |
| 148.9736 | 185.6115 | 4 | 2.944 | 10.967 | 1.035 |
| 148.9736 | 185.4569 | 4 | 3.022 | 10.989 | 1.037 |
| 148.9736 | 185.3023 | 4 | 3.099 | 10.984 | 1.036 |
| 148.9736 | 185.1477 | 4 | 3.176 | 10.966 | 1.035 |
| 148.9736 | 184.9931 | 4 | 3.253 | 10.964 | 1.034 |
| 148.9736 | 184.8384 | 4 | 3.331 | 10.972 | 1.035 |
| 148.9736 | 184.6838 | 4 | 3.408 | 10.980 | 1.036 |
| 148.9736 | 184.5292 | 4 | 3.485 | 10.988 | 1.037 |
| 148.9736 | 184.3746 | 4 | 3.563 | 10.995 | 1.037 |
| 148.9736 | 184.22 | 4 | 3.640 | 11.003 | 1.038 |
| 148.9736 | 184.0654 | 4 | 3.717 | 11.011 | 1.039 |
| 148.9736 | 183.9108 | 4 | 3.795 | 11.019 | 1.040 |
| 148.9736 | 183.7562 | 4 | 3.872 | 11.027 | 1.040 |
| 148.9736 | 183.6015 | 4 | 3.949 | 11.035 | 1.041 |
| 148.9736 | 183.4469 | 4 | 4.027 | 11.043 | 1.042 |
| 148.9736 | 183.2923 | 4 | 4.104 | 11.050 | 1.042 |
| 148.9736 | 183.1377 | 4 | 4.181 | 11.058 | 1.043 |
| 148.9736 | 182.9831 | 4 | 4.258 | 11.066 | 1.044 |
| 148.9736 | 182.8285 | 4 | 4.336 | 11.053 | 1.043 |
| 148.9736 | 182.6739 | 4 | 4.413 | 11.035 | 1.041 |
| 148.9736 | 182.5193 | 4 | 4.490 | 11.030 | 1.041 |
| 148.9736 | 182.3647 | 4 | 4.568 | 11.028 | 1.040 |
| 148.9736 | 182.21 | 4 | 4.645 | 11.038 | 1.041 |
| 148.9736 | 182.0554 | 4 | 4.722 | 11.052 | 1.043 |
| 148.9736 | 181.9008 | 4 | 4.800 | 11.066 | 1.044 |
| 148.9736 | 181.7462 | 4 | 4.877 | 11.080 | 1.045 |
| 148.9736 | 181.5916 | 4 | 4.954 | 11.093 | 1.047 |
| 148.9736 | 181.437 | 4 | 5.032 | 11.107 | 1.048 |

Table A 19 Side velocity profile for $\mathrm{q}=44$, at $\mathrm{Y} / \mathrm{d}=2$.

| X (mm) | Y (mm) | X/d | Y/d | Vel. Mag. $(\mathrm{m} / \mathrm{s})$ | Defect |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 152.9626 | 195.0053 | 2 | -1.748 | 13.121 | 0.944 |
| 152.9626 | 194.8506 | 2 | -1.670 | 13.088 | 0.942 |
| 152.9626 | 194.6959 | 2 | -1.593 | 13.047 | 0.939 |
| 152.9626 | 194.5412 | 2 | -1.516 | 12.981 | 0.934 |
| 152.9626 | 194.3866 | 2 | -1.438 | 12.916 | 0.929 |
| 152.9626 | 194.2319 | 2 | -1.361 | 12.851 | 0.925 |
| 152.9626 | 194.0772 | 2 | -1.284 | 12.786 | 0.920 |
| 152.9626 | 193.9225 | 2 | -1.206 | 12.721 | 0.915 |
| 152.9626 | 193.7678 | 2 | -1.129 | 12.655 | 0.910 |
| 152.9626 | 193.6132 | 2 | -1.052 | 12.590 | 0.906 |
| 152.9626 | 193.4585 | 2 | -0.974 | 12.460 | 0.896 |
| 152.9626 | 193.3038 | 2 | -0.897 | 12.302 | 0.885 |
| 152.9626 | 193.1491 | 2 | -0.820 | 12.145 | 0.874 |
| 152.9626 | 192.9945 | 2 | -0.742 | 12.070 | 0.868 |
| 152.9626 | 192.8398 | 2 | -0.665 | 12.005 | 0.864 |
| 152.9626 | 192.6851 | 2 | -0.588 | 11.940 | 0.859 |
| 152.9626 | 192.5304 | 2 | -0.510 | 11.875 | 0.854 |
| 152.9626 | 192.3757 | 2 | -0.433 | 11.810 | 0.850 |
| 152.9626 | 192.2211 | 2 | -0.356 | 11.744 | 0.845 |
| 152.9626 | 192.0664 | 2 | -0.278 | 11.679 | 0.840 |
| 152.9626 | 191.9117 | 2 | -0.201 | 11.651 | 0.838 |
| 152.9626 | 191.757 | 2 | -0.124 | 11.686 | 0.841 |
| 152.9626 | 191.6023 | 2 | -0.046 | 11.721 | 0.843 |
| 152.9626 | 191.4477 | 2 | 0.031 | 11.756 | 0.846 |
| 152.9626 | 191.293 | 2 | 0.109 | 11.791 | 0.848 |
| 152.9626 | 191.1383 | 2 | 0.186 | 11.826 | 0.851 |
| 152.9626 | 190.9836 | 2 | 0.263 | 11.861 | 0.853 |
| 152.9626 | 190.8289 | 2 | 0.341 | 11.895 | 0.856 |
| 152.9626 | 190.6743 | 2 | 0.418 | 11.934 | 0.859 |
| 152.9626 | 190.5196 | 2 | 0.495 | 11.974 | 0.861 |
| 152.9626 | 190.3649 | 2 | 0.573 | 12.013 | 0.864 |
| 152.9626 | 190.2102 | 2 | 0.650 | 12.048 | 0.867 |
| 152.9626 | 190.0555 | 2 | 0.727 | 12.083 | 0.869 |
| 152.9626 | 189.9009 | 2 | 0.805 | 12.118 | 0.872 |
| 152.9626 | 189.7462 | 2 | 0.882 | 12.153 | 0.874 |
| 152.9626 | 189.5915 | 2 | 0.959 | 12.188 | 0.877 |
| 152.9626 | 189.4368 | 2 | 1.037 | 12.223 | 0.879 |
| 152.9626 | 189.2821 | 2 | 1.114 | 12.257 | 0.882 |
| 152.9626 | 189.1275 | 2 | 1.191 | 12.315 | 0.886 |
| 152.9626 | 188.9728 | 2 | 1.269 | 12.397 | 0.892 |
| 152.9626 | 188.8181 | 2 | 1.346 | 12.479 | 0.898 |


| 152.9626 | 188.6634 | 2 | 1.423 | 12.560 | 0.904 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 152.9626 | 188.5088 | 2 | 1.501 | 12.642 | 0.909 |
| 152.9626 | 188.3541 | 2 | 1.578 | 12.723 | 0.915 |
| 152.9626 | 188.1994 | 2 | 1.655 | 12.805 | 0.921 |
| 152.9626 | 188.0447 | 2 | 1.733 | 12.886 | 0.927 |
| 152.9626 | 187.89 | 2 | 1.810 | 12.995 | 0.935 |
| 152.9626 | 187.7354 | 2 | 1.887 | 13.105 | 0.943 |
| 152.9626 | 187.5807 | 2 | 1.965 | 13.211 | 0.950 |
| 152.9626 | 187.426 | 2 | 2.042 | 13.293 | 0.956 |
| 152.9626 | 187.2713 | 2 | 2.119 | 13.374 | 0.962 |
| 152.9626 | 187.1166 | 2 | 2.197 | 13.456 | 0.968 |
| 152.9626 | 186.962 | 2 | 2.274 | 13.537 | 0.974 |
| 152.9626 | 186.8073 | 2 | 2.351 | 13.619 | 0.980 |
| 152.9626 | 186.6526 | 2 | 2.429 | 13.700 | 0.986 |
| 152.9626 | 186.4979 | 2 | 2.506 | 13.782 | 0.991 |
| 152.9626 | 186.3432 | 2 | 2.583 | 13.831 | 0.995 |
| 152.9626 | 186.1886 | 2 | 2.661 | 13.860 | 0.997 |
| 152.9626 | 186.0339 | 2 | 2.738 | 13.890 | 0.999 |
| 152.9626 | 185.8792 | 2 | 2.815 | 13.920 | 1.001 |
| 152.9626 | 185.7245 | 2 | 2.893 | 13.949 | 1.004 |
| 152.9626 | 185.5698 | 2 | 2.970 | 13.979 | 1.006 |
| 152.9626 | 185.4152 | 2 | 3.047 | 14.008 | 1.008 |
| 152.9626 | 185.2605 | 2 | 3.125 | 14.040 | 1.010 |
| 152.9626 | 185.1058 | 2 | 3.202 | 14.095 | 1.014 |
| 152.9626 | 184.9511 | 2 | 3.279 | 14.149 | 1.018 |
| 152.9626 | 184.7964 | 2 | 3.357 | 14.197 | 1.021 |
| 152.9626 | 184.6418 | 2 | 3.434 | 14.227 | 1.023 |
| 152.9626 | 184.4871 | 2 | 3.511 | 14.256 | 1.026 |
| 152.9626 | 184.3324 | 2 | 3.589 | 14.286 | 1.028 |
| 152.9626 | 184.1777 | 2 | 3.666 | 14.315 | 1.030 |
| 152.9626 | 184.0231 | 2 | 3.743 | 14.345 | 1.032 |
| 152.9626 | 183.8684 | 2 | 3.821 | 14.374 | 1.034 |
| 152.9626 | 183.7137 | 2 | 3.898 | 14.404 | 1.036 |
| 152.9626 | 183.559 | 2 | 3.975 | 14.377 | 1.034 |
| 152.9626 | 183.4043 | 2 | 4.053 | 14.330 | 1.031 |
| 152.9626 | 183.2497 | 2 | 4.130 | 14.284 | 1.028 |
| 152.9626 | 183.095 | 2 | 4.208 | 14.238 | 1.024 |
| 152.9626 | 182.9403 | 2 | 4.285 | 14.191 | 1.021 |
| 152.9626 | 182.7856 | 2 | 4.362 | 14.145 | 1.018 |
| 152.9626 | 182.6309 | 2 | 4.440 | 14.098 | 1.014 |
| 152.9626 | 182.4763 | 2 | 4.517 | 14.052 | 1.011 |
| 152.9626 | 182.3216 | 2 | 4.594 | 14.004 | 1.007 |
| 152.9626 | 182.1669 | 2 | 4.672 | 13.956 | 1.004 |
| 152.9626 | 182.0122 | 2 | 4.749 | 13.909 | 1.001 |
| 152.9626 | 181.8575 | 2 | 4.826 | 13.863 | 0.997 |
| 152.9626 | 181.7029 | 2 | 4.904 | 13.816 | 0.994 |
| 152.9626 | 181.5482 | 2 | 4.981 | 13.770 | 0.991 |
| 152.9626 | 181.3935 | 2 | 5.058 | 13.723 | 0.987 |
|  |  |  |  |  |  |

Table A 20 Side velocity profile for $\mathrm{q}=44$, at $\mathrm{Y} / \mathrm{d}=4$.

| X (mm) | Y (mm) | X/d | Y/d | Vel. Mag. $(\mathrm{m} / \mathrm{s})$ | Defect |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 149.0289 | 195.0053 | 4 | -1.748 | 13.344 | 0.960 |
| 149.0289 | 194.8421 | 4 | -1.666 | 13.298 | 0.957 |
| 149.0289 | 194.6789 | 4 | -1.584 | 13.276 | 0.955 |
| 149.0289 | 194.5157 | 4 | -1.503 | 13.304 | 0.957 |
| 149.0289 | 194.3525 | 4 | -1.421 | 13.331 | 0.959 |
| 149.0289 | 194.1893 | 4 | -1.340 | 13.358 | 0.961 |
| 149.0289 | 194.0261 | 4 | -1.258 | 13.385 | 0.963 |
| 149.0289 | 193.8629 | 4 | -1.176 | 13.412 | 0.965 |
| 149.0289 | 193.6997 | 4 | -1.095 | 13.438 | 0.967 |
| 149.0289 | 193.5365 | 4 | -1.013 | 13.465 | 0.969 |
| 149.0289 | 193.3733 | 4 | -0.932 | 13.492 | 0.971 |
| 149.0289 | 193.2102 | 4 | -0.850 | 13.518 | 0.973 |
| 149.0289 | 193.047 | 4 | -0.768 | 13.545 | 0.974 |
| 149.0289 | 192.8838 | 4 | -0.687 | 13.572 | 0.976 |
| 149.0289 | 192.7206 | 4 | -0.605 | 13.598 | 0.978 |
| 149.0289 | 192.5574 | 4 | -0.524 | 13.625 | 0.980 |
| 149.0289 | 192.3942 | 4 | -0.442 | 13.652 | 0.982 |
| 149.0289 | 192.231 | 4 | -0.360 | 13.679 | 0.984 |
| 149.0289 | 192.0678 | 4 | -0.279 | 13.707 | 0.986 |
| 149.0289 | 191.9046 | 4 | -0.197 | 13.741 | 0.989 |
| 149.0289 | 191.7414 | 4 | -0.116 | 13.784 | 0.992 |
| 149.0289 | 191.5782 | 4 | -0.034 | 13.827 | 0.995 |
| 149.0289 | 191.415 | 4 | 0.047 | 13.879 | 0.998 |
| 149.0289 | 191.2518 | 4 | 0.129 | 13.933 | 1.002 |
| 149.0289 | 191.0886 | 4 | 0.211 | 13.988 | 1.006 |
| 149.0289 | 190.9254 | 4 | 0.292 | 14.042 | 1.010 |
| 149.0289 | 190.7622 | 4 | 0.374 | 14.097 | 1.014 |
| 149.0289 | 190.5991 | 4 | 0.455 | 14.151 | 1.018 |
| 149.0289 | 190.4359 | 4 | 0.537 | 14.205 | 1.022 |
| 149.0289 | 190.2727 | 4 | 0.619 | 14.260 | 1.026 |
| 149.0289 | 190.1095 | 4 | 0.700 | 14.314 | 1.030 |
| 149.0289 | 189.9463 | 4 | 0.782 | 14.369 | 1.034 |
| 149.0289 | 189.7831 | 4 | 0.863 | 14.423 | 1.038 |
| 149.0289 | 189.6199 | 4 | 0.945 | 14.476 | 1.041 |
| 149.0289 | 189.4567 | 4 | 1.027 | 14.520 | 1.045 |
| 149.0289 | 189.2935 | 4 | 1.108 | 14.563 | 1.048 |
| 149.0289 | 189.1303 | 4 | 1.190 | 14.599 | 1.050 |
| 149.0289 | 188.9671 | 4 | 1.271 | 14.628 | 1.052 |
| 149.0289 | 188.8039 | 4 | 1.353 | 14.657 | 1.054 |
| 149.0289 | 188.6407 | 4 | 1.435 | 14.664 | 1.055 |
| 149.0289 | 188.4775 | 4 | 1.516 | 14.666 | 1.055 |
| 149.0289 | 188.3143 | 4 | 1.598 | 14.668 | 1.055 |
| 149.0289 | 188.1511 | 4 | 1.679 | 14.670 | 1.055 |
| 149.0289 | 187.988 | 4 | 1.761 | 14.671 | 1.055 |


| 149.0289 | 187.8248 | 4 | 1.843 | 14.673 | 1.056 |
| :--- | :---: | :--- | :--- | :--- | :--- |
| 149.0289 | 187.6616 | 4 | 1.924 | 14.675 | 1.056 |
| 149.0289 | 187.4984 | 4 | 2.006 | 14.677 | 1.056 |
| 149.0289 | 187.3352 | 4 | 2.087 | 14.679 | 1.056 |
| 149.0289 | 187.172 | 4 | 2.169 | 14.681 | 1.056 |
| 149.0289 | 187.0088 | 4 | 2.251 | 14.682 | 1.056 |
| 149.0289 | 186.8456 | 4 | 2.332 | 14.688 | 1.057 |
| 149.0289 | 186.6824 | 4 | 2.414 | 14.717 | 1.059 |
| 149.0289 | 186.5192 | 4 | 2.495 | 14.746 | 1.061 |
| 149.0289 | 186.356 | 4 | 2.577 | 14.758 | 1.062 |
| 149.0289 | 186.1928 | 4 | 2.659 | 14.753 | 1.061 |
| 149.0289 | 186.0296 | 4 | 2.740 | 14.749 | 1.061 |
| 149.0289 | 185.8664 | 4 | 2.822 | 14.736 | 1.060 |
| 149.0289 | 185.7032 | 4 | 2.903 | 14.722 | 1.059 |
| 149.0289 | 185.54 | 4 | 2.985 | 14.708 | 1.058 |
| 149.0289 | 185.3769 | 4 | 3.067 | 14.695 | 1.057 |
| 149.0289 | 185.2137 | 4 | 3.148 | 14.681 | 1.056 |
| 149.0289 | 185.0505 | 4 | 3.230 | 14.667 | 1.055 |
| 149.0289 | 184.8873 | 4 | 3.311 | 14.653 | 1.054 |
| 149.0289 | 184.7241 | 4 | 3.393 | 14.639 | 1.053 |
| 149.0289 | 184.5609 | 4 | 3.475 | 14.626 | 1.052 |
| 149.0289 | 184.3977 | 4 | 3.556 | 14.612 | 1.051 |
| 149.0289 | 184.2345 | 4 | 3.638 | 14.598 | 1.050 |
| 149.0289 | 184.0713 | 4 | 3.719 | 14.586 | 1.049 |
| 149.0289 | 183.9081 | 4 | 3.801 | 14.582 | 1.049 |
| 149.0289 | 183.7449 | 4 | 3.883 | 14.577 | 1.049 |
| 149.0289 | 183.5817 | 4 | 3.964 | 14.559 | 1.047 |
| 149.0289 | 183.4185 | 4 | 4.046 | 14.531 | 1.045 |
| 149.0289 | 183.2553 | 4 | 4.127 | 14.503 | 1.043 |
| 149.0289 | 183.0921 | 4 | 4.209 | 14.493 | 1.043 |
| 149.0289 | 182.9289 | 4 | 4.291 | 14.485 | 1.042 |
| 149.0289 | 182.7657 | 4 | 4.372 | 14.476 | 1.041 |
| 149.0289 | 182.6026 | 4 | 4.454 | 14.467 | 1.041 |
| 149.0289 | 182.4394 | 4 | 4.535 | 14.459 | 1.040 |
| 149.0289 | 182.2762 | 4 | 4.617 | 14.450 | 1.040 |
| 149.0289 | 182.113 | 4 | 4.699 | 14.442 | 1.039 |
| 149.0289 | 181.9498 | 4 | 4.780 | 14.433 | 1.038 |
| 149.0289 | 181.7866 | 4 | 4.862 | 14.424 | 1.038 |
| 149.0289 | 181.6234 | 4 | 4.943 | 14.416 | 1.037 |
| 149.0289 | 181.4602 | 4 | 5.025 | 14.407 | 1.036 |
|  |  |  |  |  |  |

Table A 21 Proximal velocity profile for $\mathrm{q}=78$.

| X (mm) | Y (mm) | X/d | Vel. Mag. (m/s) | Defect |
| :---: | :---: | :---: | :---: | :---: |
| 153.0946 | 191.5105 | 1.953 | 9.454 | 0.892 |
| 153.0113 | 191.5105 | 1.994 | 9.575 | 0.903 |
| 152.9281 | 191.5105 | 2.036 | 9.697 | 0.915 |
| 152.8448 | 191.5105 | 2.078 | 9.818 | 0.926 |
| 152.7616 | 191.5105 | 2.119 | 9.939 | 0.938 |
| 152.6783 | 191.5105 | 2.161 | 10.061 | 0.949 |
| 152.5951 | 191.5105 | 2.202 | 10.176 | 0.960 |
| 152.5118 | 191.5105 | 2.244 | 10.283 | 0.970 |
| 152.4285 | 191.5105 | 2.286 | 10.391 | 0.980 |
| 152.3453 | 191.5105 | 2.327 | 10.498 | 0.990 |
| 152.262 | 191.5105 | 2.369 | 10.606 | 1.001 |
| 152.1788 | 191.5105 | 2.411 | 10.713 | 1.011 |
| 152.0955 | 191.5105 | 2.452 | 10.820 | 1.021 |
| 152.0123 | 191.5105 | 2.494 | 10.869 | 1.025 |
| 151.929 | 191.5105 | 2.535 | 10.859 | 1.024 |
| 151.8458 | 191.5105 | 2.577 | 10.849 | 1.024 |
| 151.7625 | 191.5105 | 2.619 | 10.840 | 1.023 |
| 151.6793 | 191.5105 | 2.660 | 10.830 | 1.022 |
| 151.596 | 191.5105 | 2.702 | 10.820 | 1.021 |
| 151.5128 | 191.5105 | 2.744 | 10.811 | 1.020 |
| 151.4295 | 191.5105 | 2.785 | 10.791 | 1.018 |
| 151.3463 | 191.5105 | 2.827 | 10.764 | 1.015 |
| 151.263 | 191.5105 | 2.868 | 10.737 | 1.013 |
| 151.1798 | 191.5105 | 2.910 | 10.710 | 1.010 |
| 151.0965 | 191.5105 | 2.952 | 10.683 | 1.008 |
| 151.0133 | 191.5105 | 2.993 | 10.655 | 1.005 |
| 150.93 | 191.5105 | 3.035 | 10.628 | 1.003 |
| 150.8468 | 191.5105 | 3.077 | 10.601 | 1.000 |
| 150.7635 | 191.5105 | 3.118 | 10.574 | 0.998 |
| 150.6802 | 191.5105 | 3.160 | 10.547 | 0.995 |
| 150.597 | 191.5105 | 3.202 | 10.520 | 0.992 |
| 150.5137 | 191.5105 | 3.243 | 10.493 | 0.990 |
| 150.4305 | 191.5105 | 3.285 | 10.465 | 0.987 |
| 150.3472 | 191.5105 | 3.326 | 10.438 | 0.985 |
| 150.264 | 191.5105 | 3.368 | 10.411 | 0.982 |
| 150.1807 | 191.5105 | 3.410 | 10.384 | 0.980 |
| 150.0975 | 191.5105 | 3.451 | 10.357 | 0.977 |
| 150.0142 | 191.5105 | 3.493 | 10.330 | 0.975 |
| 149.931 | 191.5105 | 3.535 | 10.303 | 0.972 |
| 149.8477 | 191.5105 | 3.576 | 10.280 | 0.970 |
| 149.7645 | 191.5105 | 3.618 | 10.270 | 0.969 |
| 149.6812 | 191.5105 | 3.659 | 10.260 | 0.968 |
| 149.598 | 191.5105 | 3.701 | 10.251 | 0.967 |
| 149.5147 | 191.5105 | 3.743 | 10.241 | 0.966 |
| 149.4315 | 191.5105 | 3.784 | 10.231 | 0.965 |


| 149.3482 | 191.5105 | 3.826 | 10.222 | 0.964 |
| :---: | :---: | :---: | :---: | :---: |
| 149.265 | 191.5105 | 3.868 | 10.215 | 0.964 |
| 149.1817 | 191.5105 | 3.909 | 10.214 | 0.964 |
| 149.0985 | 191.5105 | 3.951 | 10.214 | 0.964 |
| 149.0152 | 191.5105 | 3.992 | 10.214 | 0.964 |
| 148.9319 | 191.5105 | 4.034 | 10.213 | 0.964 |
| 148.8487 | 191.5105 | 4.076 | 10.213 | 0.963 |
| 148.7654 | 191.5105 | 4.117 | 10.213 | 0.963 |
| 148.6822 | 191.5105 | 4.159 | 10.220 | 0.964 |
| 148.5989 | 191.5105 | 4.201 | 10.243 | 0.966 |
| 148.5157 | 191.5105 | 4.242 | 10.266 | 0.968 |
| 148.4324 | 191.5105 | 4.284 | 10.289 | 0.971 |
| 148.3492 | 191.5105 | 4.325 | 10.312 | 0.973 |
| 148.2659 | 191.5105 | 4.367 | 10.334 | 0.975 |
| 148.1827 | 191.5105 | 4.409 | 10.357 | 0.977 |
| 148.0994 | 191.5105 | 4.450 | 10.380 | 0.979 |
| 148.0162 | 191.5105 | 4.492 | 10.403 | 0.981 |
| 147.9329 | 191.5105 | 4.534 | 10.426 | 0.984 |
| 147.8497 | 191.5105 | 4.575 | 10.448 | 0.986 |
| 147.7664 | 191.5105 | 4.617 | 10.471 | 0.988 |
| 147.6832 | 191.5105 | 4.658 | 10.494 | 0.990 |
| 147.5999 | 191.5105 | 4.700 | 10.517 | 0.992 |
| 147.5167 | 191.5105 | 4.742 | 10.540 | 0.994 |
| 147.4334 | 191.5105 | 4.783 | 10.563 | 0.996 |
| 147.3501 | 191.5105 | 4.825 | 10.585 | 0.999 |
| 147.2669 | 191.5105 | 4.867 | 10.608 | 1.001 |
| 147.1836 | 191.5105 | 4.908 | 10.631 | 1.003 |
| 147.1004 | 191.5105 | 4.950 | 10.653 | 1.005 |
| 147.0171 | 191.5105 | 4.991 | 10.653 | 1.005 |
| 146.9339 | 191.5105 | 5.033 | 10.652 | 1.005 |
| 146.8506 | 191.5105 | 5.075 | 10.652 | 1.005 |
| 146.7674 | 191.5105 | 5.116 | 10.652 | 1.005 |
| 146.6841 | 191.5105 | 5.158 | 10.651 | 1.005 |
| 146.6009 | 191.5105 | 5.200 | 10.651 | 1.005 |
| 146.5176 | 191.5105 | 5.241 | 10.650 | 1.005 |
| 146.4344 | 191.5105 | 5.283 | 10.649 | 1.005 |
| 146.3511 | 191.5105 | 5.324 | 10.647 | 1.004 |
| 146.2679 | 191.5105 | 5.366 | 10.645 | 1.004 |
| 146.1846 | 191.5105 | 5.408 | 10.644 | 1.004 |
| 146.1014 | 191.5105 | 5.449 | 10.642 | 1.004 |
| 146.0181 | 191.505 | 5.491 | 10.640 | 1.004 |
| 145.9349 | 191.5105 | 5.533 | 10.636 | 1.003 |
| 145.8516 | 191.5105 | 5.574 | 10.618 | 1.002 |
| 145.7684 | 191.5105 | 5.616 | 10.599 | 1.000 |
| 145.6851 | 191.5105 | 5.657 | 10.580 | 0.998 |
| 145.6018 | 191.5105 | 5.699 | 10.561 | 0.996 |
| 145.5186 | 191.5105 | 5.741 | 10.542 | 0.995 |
| 145.4353 | 191.5105 | 5.782 | 10.524 | 0.993 |
| 145.3521 | 191.5105 | 5.824 | 10.505 | 0.991 |
|  |  |  |  |  |


| 145.2688 | 191.5105 | 5.866 | 10.486 | 0.989 |
| :--- | :--- | :--- | :--- | :--- |
| 145.1856 | 191.5105 | 5.907 | 10.467 | 0.987 |
| 145.1023 | 191.5105 | 5.949 | 10.449 | 0.986 |
| 145.0191 | 191.5105 | 5.990 | 10.430 | 0.984 |
| 144.9358 | 191.5105 | 6.032 | 10.411 | 0.982 |
| 144.8526 | 191.5105 | 6.074 | 10.392 | 0.980 |

Table A 22 Proximal velocity profile for $\mathrm{q}=44$.

| X | Y | $\mathrm{X} / \mathrm{d}$ | Vel. Mag. (m/s) | Defect |
| :---: | :---: | :---: | :---: | :---: |
| 153.103 | 191.4931 | 1.948 | 11.604 | 0.829 |
| 153.0193 | 191.4931 | 1.990 | 11.688 | 0.835 |
| 152.9356 | 191.4931 | 2.032 | 11.773 | 0.841 |
| 152.8519 | 191.4931 | 2.074 | 11.857 | 0.847 |
| 152.7681 | 191.4931 | 2.116 | 11.942 | 0.853 |
| 152.6844 | 191.4931 | 2.158 | 12.027 | 0.859 |
| 152.6007 | 191.4931 | 2.200 | 12.111 | 0.865 |
| 152.517 | 191.4931 | 2.242 | 12.196 | 0.871 |
| 152.4332 | 191.4931 | 2.283 | 12.280 | 0.877 |
| 152.3495 | 191.4931 | 2.325 | 12.365 | 0.883 |
| 152.2658 | 191.4931 | 2.367 | 12.450 | 0.889 |
| 152.1821 | 191.4931 | 2.409 | 12.534 | 0.895 |
| 152.0983 | 191.4931 | 2.451 | 12.619 | 0.901 |
| 152.0146 | 191.4931 | 2.493 | 12.703 | 0.907 |
| 151.9309 | 191.4931 | 2.535 | 12.788 | 0.913 |
| 151.8472 | 191.4931 | 2.576 | 12.873 | 0.919 |
| 151.7634 | 191.4931 | 2.618 | 12.955 | 0.925 |
| 151.6797 | 191.4931 | 2.660 | 13.037 | 0.931 |
| 151.596 | 191.4931 | 2.702 | 13.119 | 0.937 |
| 151.5123 | 191.4931 | 2.744 | 13.201 | 0.943 |
| 151.4285 | 191.4931 | 2.786 | 13.283 | 0.949 |
| 151.3448 | 191.4931 | 2.828 | 13.352 | 0.954 |
| 151.2611 | 191.4931 | 2.869 | 13.375 | 0.955 |
| 151.1774 | 191.4931 | 2.911 | 13.398 | 0.957 |
| 151.0936 | 191.4931 | 2.953 | 13.420 | 0.959 |
| 151.0099 | 191.4931 | 2.995 | 13.443 | 0.960 |
| 150.9262 | 191.4931 | 3.037 | 13.465 | 0.962 |
| 150.8425 | 191.4931 | 3.079 | 13.485 | 0.963 |
| 150.7587 | 191.4931 | 3.121 | 13.502 | 0.964 |
| 150.675 | 191.4931 | 3.162 | 13.519 | 0.966 |
| 150.5913 | 191.4931 | 3.204 | 13.535 | 0.967 |
| 150.5076 | 191.4931 | 3.246 | 13.552 | 0.968 |
| 150.4238 | 191.4931 | 3.288 | 13.569 | 0.969 |
| 150.3401 | 191.4931 | 3.330 | 13.586 | 0.970 |
| 150.2564 | 191.4931 | 3.372 | 13.603 | 0.972 |
| 10 |  |  |  |  |


| 150.1727 | 191.4931 | 3.414 | 13.620 | 0.973 |
| :---: | :---: | :---: | :---: | :---: |
| 150.0889 | 191.4931 | 3.456 | 13.636 | 0.974 |
| 150.0052 | 191.4931 | 3.497 | 13.653 | 0.975 |
| 149.9215 | 191.4931 | 3.539 | 13.670 | 0.976 |
| 149.8377 | 191.4931 | 3.581 | 13.687 | 0.978 |
| 149.754 | 191.4931 | 3.623 | 13.704 | 0.979 |
| 149.6703 | 191.4931 | 3.665 | 13.721 | 0.980 |
| 149.5866 | 191.4931 | 3.707 | 13.738 | 0.981 |
| 149.5028 | 191.4931 | 3.749 | 13.754 | 0.982 |
| 149.4191 | 191.4931 | 3.790 | 13.771 | 0.984 |
| 149.3354 | 191.4931 | 3.832 | 13.788 | 0.985 |
| 149.2517 | 191.4931 | 3.874 | 13.805 | 0.986 |
| 149.1679 | 191.4931 | 3.916 | 13.822 | 0.987 |
| 149.0842 | 191.4931 | 3.958 | 13.839 | 0.988 |
| 149.0005 | 191.4931 | 4.000 | 13.861 | 0.990 |
| 148.9168 | 191.4931 | 4.042 | 13.883 | 0.992 |
| 148.833 | 191.4931 | 4.083 | 13.906 | 0.993 |
| 148.7493 | 191.4931 | 4.125 | 13.928 | 0.995 |
| 148.6656 | 191.4931 | 4.167 | 13.951 | 0.996 |
| 148.5819 | 191.4931 | 4.209 | 13.967 | 0.998 |
| 148.4981 | 191.4931 | 4.251 | 13.960 | 0.997 |
| 148.4144 | 191.4931 | 4.293 | 13.952 | 0.997 |
| 148.3307 | 191.4931 | 4.335 | 13.944 | 0.996 |
| 148.247 | 191.4931 | 4.377 | 13.936 | 0.995 |
| 148.1632 | 191.4931 | 4.418 | 13.928 | 0.995 |
| 148.0795 | 191.4931 | 4.460 | 13.937 | 0.996 |
| 147.9958 | 191.4931 | 4.502 | 13.962 | 0.997 |
| 147.9121 | 191.4931 | 4.544 | 13.987 | 0.999 |
| 147.8283 | 191.4931 | 4.586 | 14.011 | 1.001 |
| 147.7446 | 191.4931 | 4.628 | 14.036 | 1.003 |
| 147.6609 | 191.4931 | 4.670 | 14.061 | 1.004 |
| 147.5772 | 191.4931 | 4.711 | 14.085 | 1.006 |
| 147.4934 | 191.4931 | 4.753 | 14.110 | 1.008 |
| 147.4097 | 191.4931 | 4.795 | 14.135 | 1.010 |
| 147.326 | 191.4931 | 4.837 | 14.160 | 1.011 |
| 147.2423 | 191.4931 | 4.879 | 14.184 | 1.013 |
| 147.1585 | 191.4931 | 4.921 | 14.209 | 1.015 |
| 147.0748 | 191.4931 | 4.963 | 14.234 | 1.017 |
| 146.9911 | 191.4931 | 5.004 | 14.258 | 1.018 |
| 146.9074 | 191.4931 | 5.046 | 14.283 | 1.020 |
| 146.8236 | 191.4931 | 5.088 | 14.308 | 1.022 |
| 146.7399 | 191.4931 | 5.130 | 14.333 | 1.024 |
| 146.6562 | 191.4931 | 5.172 | 14.357 | 1.026 |
| 146.5725 | 191.4931 | 5.214 | 14.382 | 1.027 |
| 146.4887 | 191.4931 | 5.256 | 14.407 | 1.029 |


| 146.405 | 191.4931 | 5.297 | 14.432 | 1.031 |
| :---: | :---: | :---: | :---: | :---: |
| 146.3213 | 191.4931 | 5.339 | 14.456 | 1.033 |
| 146.2376 | 191.4931 | 5.381 | 14.453 | 1.032 |
| 146.1538 | 191.4931 | 5.423 | 14.445 | 1.032 |
| 146.0701 | 191.4931 | 5.465 | 14.437 | 1.031 |
| 145.9864 | 191.4931 | 5.507 | 14.429 | 1.031 |
| 145.9026 | 191.4931 | 5.549 | 14.421 | 1.030 |
| 145.8189 | 191.4931 | 5.591 | 14.418 | 1.030 |
| 145.7352 | 191.4931 | 5.632 | 14.433 | 1.031 |
| 145.6515 | 191.4931 | 5.674 | 14.449 | 1.032 |
| 145.5677 | 191.4931 | 5.716 | 14.465 | 1.033 |
| 145.484 | 191.4931 | 5.758 | 14.481 | 1.034 |
| 145.4003 | 191.4931 | 5.800 | 14.496 | 1.035 |
| 145.3166 | 191.4931 | 5.842 | 14.512 | 1.037 |
| 145.2328 | 191.4931 | 5.884 | 14.526 | 1.038 |
| 145.1491 | 191.4931 | 5.925 | 14.541 | 1.039 |
| 145.0654 | 191.4931 | 5.967 | 14.556 | 1.040 |
| 144.9817 | 191.4931 | 6.009 | 14.571 | 1.041 |
| 144.8979 | 191.4931 | 6.051 | 14.586 | 1.042 |
| 144.8142 | 191.4931 | 6.093 | 14.600 | 1.043 |

Table A 23 Spray characteristic break up matrix

| $\begin{gathered} \hline \text { For small } \\ \text { Oh } \end{gathered}$ | $172 \geq \mathrm{q} \geq 70$ | $70>q \geq 40$ | $40>q \geq 20$ | $20>q \geq 15$ | $15>q \geq 10$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $30 \geq \mathrm{We} \geq 25$ | - Nondimensional disturbance wavelength $0.8 \leq \lambda / \mathrm{d}<0.74 *$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Combined surface/column break up with multimode break up characteristics ** -Nondimensional break up height $33 \leq Z / \mathrm{d} \leq 53^{* *}$ | - Nondimensional disturbance wavelength $0.8 \leq \lambda / \mathrm{d}<0.74^{*}$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Column break up with multimode break up characteristics ** <br> -Nondimensional break up height $24.3 \leq \mathrm{Z} / \mathrm{d}<33^{* *}$ <br> -Droplet sizes ranging from 40$125 \mu \mathrm{~m} 300$ diameters downstream*** | - Nondimensional disturbance wavelength $0.8 \leq \lambda / \mathrm{d}<0.74 *$ <br> -Downstream break up occurs <br> at $X / d=8^{*}$ <br> -Column break up with multimode break up characteristics ** <br> -Nondimensional break up height $16.8 \leq \mathrm{Z} / \mathrm{d}<24.3^{* *}$ | - Nondimensional disturbance wavelength $0.8 \leq \lambda / \mathrm{d}<0.74^{*}$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Column break up with multimode break up characteristics ** <br> -Nondimensional break up height $14.5 \leq \mathrm{Z} / \mathrm{d}<16.8^{* *}$ | -Significant drag on the jet with bending <br> -Multimode break up mechanism <br> -High shear along sides of the jet with droplet stripping <br> -Significant droplet deposition along wall lining <br> - Nondimensional disturbance wavelength $0.8 \leq \lambda / \mathrm{d}<0.74^{*}$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Nondimensional break up height $11.7 \leq \mathrm{Z} / \mathrm{d}<14.5^{* *}$ |
| $25>$ We $\geq 14$ | - Nondimensional disturbance wavelength $1 \leq \lambda / \mathrm{d}<0.8^{*}$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Column break up regime with bag break up mechanism** <br> -Nondimensional break up height $33 \leq Z / \mathrm{d} \leq 53^{* *}$ | - Nondimensional disturbance wavelength $1 \leq \lambda / d<0.8^{*}$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Column break up regime with bag break up mechanism** <br> -Nondimensional break up height $24.3 \leq \mathrm{Z} / \mathrm{d}<33^{* *}$ | - Nondimensional disturbance wavelength $1 \leq \lambda / \mathrm{d}<0.8^{*}$ <br> -Downstream break up occurs at $X / d=8^{*}$ <br> -Column break up regime with bag break up mechanism** -Nondimensional break up height $16.8 \leq \mathrm{Z} / \mathrm{d}<24.3^{* *}$ | -Significant drag on the jet with bending <br> -Mostly bag break up with some multimode break up -High shear along sides of the jet with droplet stripping <br> -Increased droplet deposition on wall lining - Nondimensional disturbance wavelength $1 \leq \lambda / \mathrm{d}<0.8^{*}$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Nondimensional break up height $14.5 \leq Z / d<16.8^{* *}$ | - Nondimensional disturbance wavelength $1 \leq \lambda / d<0.8^{*}$ <br> -Downstream break up occurs at $X / d=8^{*}$ <br> -Significant drag on the jet with bending <br> -Column break up regime with bag break up mechanism** <br> -Nondimensional break up height $11.7 \leq \mathrm{Z} / \mathrm{d}<14.5^{* *}$ -Increasing surface break up |


| $14>\mathrm{We} \geq 7$ | -Nondimensional disturbance wavelength $1.4 \leq \lambda / \mathrm{d}<1^{*}$ -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Enhanced capillary break up regime, with some bag break up near $\mathrm{We}=14^{* *}$ <br> -Nondimensional break up height $33 \leq Z / \mathrm{d} \leq 53^{* *}$ | -Nondimensional disturbance wavelength $1.4 \leq \lambda / \mathrm{d}<1^{*}$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Enhanced capillary break up regime, with some bag break up near $\mathrm{We}=14^{* *}$ <br> -Nondimensional break up height $24.3 \leq \mathrm{Z} / \mathrm{d}<33^{* *}$ | -Increased drag on jet results in significant bending <br> -Column break up with bag break up mechanism and large <br> ligaments <br> -Nondimensional disturbance wavelength $1.4 \leq \lambda / \mathrm{d}<1^{*}$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Nondimensional break up height $16.8 \leq \mathrm{Z} / \mathrm{d}<24.3^{* *}$ | -Nondimensional disturbance wavelength $1.4 \leq \lambda / \mathrm{d}<1^{*}$ <br> -Downstream break up occurs at $X / d=8^{*}$ <br> -Enhanced capillary break up regime, with some bag break up near $\mathrm{We}=14^{* *}$ -Nondimensional break up height $14.5 \leq \mathrm{Z} / \mathrm{d}<16.8^{* *}$ | -Nondimensional disturbance wavelength $1.4 \leq \lambda / \mathrm{d}<1^{*}$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Enhanced capillary break up regime, with some bag break up near $\mathrm{We}=14^{* *}$ -Nondimensional break up height $11.7 \leq \mathrm{Z} / \mathrm{d}<14.5^{* *}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $7>\mathrm{We} \geq 4$ | -Nondimensional disturbance wavelength $1.4<\lambda / \mathrm{d} \leq 1.8^{*}$ -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Enhanced capillary break up regime** <br> -Nondimensional break up height $33 \leq$ Z/d $\leq 53^{* *}$ | -Slight bending of the jet with penetration $\mathrm{Z} / \mathrm{d}<250$ <br> -Column break up mechanism <br> -Nondimensional disturbance wavelength $1.4<\lambda / \mathrm{d} \leq 1.8^{*}$ <br> -Significant velocity defect along the side of the jet <br> -Downstream break up occurs at $X / d=8^{*}$ | -Nondimensional disturbance wavelength $1.4<\lambda / \mathrm{d} \leq 1.8^{*}$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Enhanced capillary break up regime** | -Nondimensional disturbance wavelength $1.4<\lambda / \mathrm{d} \leq 1.8^{*}$ <br> -Downstream break up occurs at $\mathrm{X} / \mathrm{d}=8^{*}$ <br> -Enhanced capillary break up regime** | -Nondimensional disturbance wavelength $1.4<\lambda / \mathrm{d} \leq 1.8^{*}$ <br> -Downstream break up occurs at $X / d=8^{*}$ <br> -Enhanced capillary break up regime** |
| $4>\mathrm{We} \geq 1$ | ```-Very little jet bending with penetration \(\mathrm{Z} / \mathrm{d}>250\) -column break up mechanism with very large wavelength disturbances -No apparent thinning of the liquid column before break up* -Enhanced capillary break up regime** -Nondimensional break up height \(33 \leq Z / \mathrm{d} \leq 53^{* *}\)``` |  |  |  |  |

Table A 24 Wavelength and break up locations for $q=10$.

| We | q | $\lambda$ (in) | Xb (in) | $\mathrm{Zb}(\mathrm{in})$ | $\lambda / \mathrm{d}$ | $\mathrm{Xb} / \mathrm{d}$ | $\mathrm{Zb} / \mathrm{d}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 29.29 | 10 |  | 1.082 | 1.388 |  | 6.9 | 8.82 |
| 29.29 | 10 | 0.145 |  |  | 0.92 |  |  |
| 29.29 | 10 | 0.228 | 1.198 | 1.625 | 1.4 | 7.6 | 10.3 |
| 29.29 | 10 | 0.13 | 1.211 | 1.726 | 0.825 | 7.7 | 11 |
| 29.29 | 10 | 0.165 | 1.25 | 1.837 | 1.04 | 7.9 | 11.66 |
| 29.29 | 10 | 0.135 | 1.398 | 1.742 | 0.86 | 8.8 | 11.06 |
| 29.29 | 10 | 0.139 | 1.36 | 1.767 | 0.883 | 8.6 | 11.22 |
| 29.29 | 10 | 0.13 | 1.219 | 1.706 | 0.82 | 7.74 | 10.83 |
| 29.29 | 10 | 0.14 | 1.322 | 1.7 | 0.889 | 8.39 | 10.8 |
| 29.29 | 10 | 0.157 | 1.201 | 1.638 | 0.99 | 7.6 | 10.4 |
| 29.29 | 10 | 0.153 | 1.257 | 1.72 | 0.97 | 7.98 | 10.92 |
| 29.29 | 10 | 0.136 | 1.215 | 1.75 | 0.86 | 7.72 | 11.11 |
|  |  |  |  |  | 0.950636 | 7.90273 | 10.7382 |
|  |  |  |  |  | 0.164448 | 0.53145 | 0.73643 |
|  |  |  |  |  | Precision | 0.089844 | 0.29035 |
|  |  |  |  | Uncert. | 0.090737 | 0.29063 | 0.40254 |

Table A 25 Wavelength and break up locations for $\mathrm{q}=18.8$.

| We | q | $\lambda($ in $)$ | $\mathrm{Xb}(\mathrm{in})$ | $\mathrm{Zb}(\mathrm{in})$ | $\lambda / \mathrm{d}$ | $\mathrm{Xb} / \mathrm{d}$ | $\mathrm{Zb} / \mathrm{d}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15.85 | 18.8 | 0.194 | 1.2 | 2.218 | 1.23 | 7.62 | 14.08 |
| 15.85 | 18.8 |  | 1.35 | 2.242 |  | 8.5 | 14.23 |
| 15.85 | 18.8 | 0.219 | 1.24 | 2.245 | 1.4 | 7.9 | 14.3 |
| 15.85 | 18.8 | 0.163 | 1.245 | 2.266 | 1.04 | 7.9 | 14.4 |
| 15.85 | 18.8 | 0.18 | 1.259 | 2.294 | 1.14 | 8 | 14.57 |
| 15.85 | 18.8 | 0.169 | 1.255 | 2.263 | 1.07 | 7.97 | 14.37 |
| 15.85 | 18.8 | 0.168 | 1.3 | 2.244 | 1.07 | 8.25 | 14.25 |
| 15.85 | 18.8 | 0.229 | 1.214 | 2.24 | 1.45 | 7.71 | 14.22 |
| 15.85 | 18.8 | 0.2 | 1.248 | 2.186 | 1.27 | 7.92 | 13.88 |
| 15.85 | 18.8 | 0.168 | 1.245 | 2.309 | 1.07 | 7.91 | 14.66 |
| 15.85 | 18.8 |  | 1.251 | 2.304 |  | 7.94 | 14.63 |
| 15.85 | 18.8 | 0.159 | 1.265 | 2.308 | 1 | 8.03 | 14.65 |
| 15.85 | 18.8 | 0.168 | 1.1 | 2.3 | 1.07 | 7 | 14.6 |
| 15.85 | 18.8 | 0.232 | 1.278 | 2.269 | 1.47 | 8.11 | 14.4 |
|  |  |  |  |  | 1.19 | 7.91143 | 14.3743 |
|  |  |  |  |  | 0.169706 | 0.33777 | 0.23372 |
|  |  |  |  | Precision | 0.087986 | 0.15987 | 0.11063 |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |

Table A 26 Wavelength and break up locations for $q=40$.

|  | We | q | $\lambda$ (in) | Xb (in) | Zb (in) | $\lambda / \mathrm{d}$ | Xb/d | Zb/d |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 7.32 | 40 | 0.3 | 1.286 | 4.2 | 1.9 | 8.16 | 26.7 |
|  | 7.32 | 40 |  | 1.227 | 3.57 |  | 7.8 | 22.7 |
|  | 7.32 | 40 |  | 1.29 | 4.2 |  | 8.19 | 26.6 |
|  | 7.32 | 40 | 0.251 | 1.287 | 4.244 | 1.6 | 8.17 | 26.9 |
|  | 7.32 | 40 | 0.258 |  |  | 1.6 |  |  |
|  | 7.32 | 40 | 0.304 | 1.184 | 3.58 | 1.9 | 7.52 | 22.73 |
|  | 7.32 | 40 | 0.2574 | 1.316 | 3.89 | 1.74 | 8.4 | 24.7 |
|  | 7.32 | 40 | 0.247 | 1.257 | 3.975 | 1.57 | 7.98 | 25.24 |
|  | 7.32 | 40 |  | 1.278 | 4.16 |  | 8.1 | 26.4 |
|  | 7.32 | 40 | 0.31 | 1.296 | 3.83 | 1.96 | 8.22 | 24.3 |
|  | 7.32 | 40 |  | 1.284 | 3.892 |  | 8.15 | 24.7 |
|  | 7.32 | 40 | 0.28 | 1.17 | 3.92 | 1.78 | 7.43 | 24.89 |
|  | 7.32 | 40 |  | 1.348 | 3.765 |  | 8.5 | 23.9 |
|  | 7.32 | 40 |  | 1.31 | 3.785 |  | 8.3 | 24.03 |
|  | 7.32 | 40 | 0.244 | 1.281 | 4.157 | 1.54 | 8.13 | 26.3 |
|  | 7.32 | 40 | 0.216 |  |  | 1.37 |  |  |
|  | 7.32 | 40 | 0.242 |  |  | 1.54 |  |  |
|  | 7.32 | 40 | 0.219 |  |  | 1.39 |  |  |
|  | 7.32 | 40 | 0.223 | 1.213 | 3.879 | 1.42 | 7.7 | 24.6 |
|  | 7.32 | 40 | 0.214 | 1.149 | 3.916 | 1.36 | 7.3 | 24.87 |
|  | 7.32 | 40 | 0.204 | 1.268 | 3.897 | 1.3 | 8.05 | 24.7 |
|  | 7.32 | 40 |  | 1.114 | 3.859 |  | 7.07 | 24.5 |
| avg. |  |  |  |  |  | 1.598 | 7.95389 | 24.9311 |
| stdev |  |  |  |  |  | 0.214915 | 0.39803 | 1.24794 |
|  |  |  |  |  | Precision | 0.097719 | 0.16324 | 0.51181 |
|  |  |  |  |  | Uncert. | 0.098541 | 0.16373 | 0.51196 |

## APPENDIX B

Figure B1 Calibration plot of Actual Flow Rate vs. Indicated Flow Rate................ 155


Figure B1 Calibration plot of Actual Flow Rate vs. Indicated Flow Rate

## NOMENCLATURE

| d | $=$ Diameter of water jet |
| :---: | :---: |
| $\mathrm{d}_{\mathrm{p}}$ | $=$ Diameter of seed particle |
| $\mathrm{d}_{\mathrm{t}}$ | $=$ Diameter of test section |
| $f$ | $=$ Frequency of instability wave |
| F | $=$ Total body forces |
| Oh | $=$ Liquid Ohnesorge number $\left[\mu_{\mathrm{j}} /\left(\rho_{\mathrm{j}} \mathrm{d}_{\mathrm{j}} \sigma\right)^{0.5}\right]$ |
| P | $=$ Fluid pressure |
| $q$ | $=$ Ratio of cross flow momentum to jet momentum |
| $\mathrm{Re}_{\infty}$ | $=$ Reynolds number for the cross flow ( $\left.\mathrm{U}_{\infty} \mathrm{d}_{t} / v_{\infty}\right)$ |
| $\mathrm{Re}_{\mathrm{j}}$ | $=$ Reynolds number for the water jet ( $\left.\mathrm{U}_{\mathrm{j}} \mathrm{d} / \mathrm{v}_{\mathrm{j}}\right)$ |
| $\mathrm{Re}_{\text {cyl }}$ | $=$ Reynolds number for a solid cylinder of jet diameter ( $\mathrm{U}_{\infty} \mathrm{d} / \mathrm{v}_{\infty}$ ) |
| Str | $=$ Strouhal Number |
| St | $=$ Stokes Number |
| $U_{\infty}$ | $=$ Mean Velocity of cross flow |
| $\mathrm{U}_{\mathrm{j}}$ | $=$ Injectant Velocity |
| We | $=$ Weber Number |
| X | $=$ Streamwise coordinate |
| Y | $=$ Spanwise coordinate |
| Z | $=$ Vertical coordinate from wall |
| $\alpha$ | $=$ Volulme fraction of fluid |

$\varepsilon \quad=$ Density Ratio of Continuum to Seeding Particle
$\lambda_{\mathrm{s}} \quad=$ Wavelength of instability
$v_{\infty} \quad=$ Kinematic Viscosity of air
$v_{\mathrm{j}} \quad=$ Kinematic Viscosity of water
$\omega \quad=$ Rotational Frequency of Vortex
$\rho_{\infty} \quad=$ Cross flow air density
$\rho_{j} \quad=$ Density of Water from Injector
$\sigma \quad=$ Surface Tension of Water

